Algorithms Exercise #1

a. Environment

I. OS: Windows 11

II. Compiler: GNU GCC Compiler

III. IDE: Code::Blocks 20.03

b. Results

I. Methods:

i. Main function:

(1) Using *ifstream* and *ofstream* to input and output txt.file.

```
93      //read in txt
94      ifstream in;
95      ofstream out;
96      in.open("input.txt");
97      out.open("output.txt");
98      if(out.fail()){
99          cout<<"Error opening output\n";
100         exit(1);
101     }
102     if(in.fail()){
103         cout<<"Error opening input\n";
104         exit(1);
105     }
106     int yt_num;
107     in>>yt_num;
```

(2) Using while loop to handle each tableau, and perform certain operation based on ‘choice’. Using *getline* and *istringstream* to read in a whole line of input. The inserted numbers are stored in ‘insert_key’ vector.

```
109     while(yt_num!=0){
110         int choice;
111         in>>choice;
112         //cout<<"choice"<<choice<<"\n";
113
114         if(choice==1){
115             vector<vector<int>> yt;
116             vector<int> insert_key;
117             int insert_num;
118             string l;
119             in.get();
120             getline(in,l);
121             istringstream i(l);
122             while(i>>insert_num){
123                 insert_key.push_back(insert_num);
124             }
125             int insert_size=insert_key.size();
126             out<<"Insert ";
127             for(int i=0;i<insert_size;i++){
128                 out<<insert_key[i]<<" ";
129             }
130             out<<"\n";
```

(3) Store the tableau index in ‘vector<vector<int>> yt’, if the read in index is ‘x’, we store it as INF, which is define as INT_MAX.

```
131             //store tableau data
132             string line;
133             while(getline(in,line)){
134                 stringstream iss(line);
135                 vector<int> row;
136                 string c;
137
138                 if(line.empty()){
139                     break;
140                 }
141                 while(iss>>c){
142                     if(c=="x"){row.push_back(INF);}
143                     else if(isdigit(c[0])){
144                         row.push_back(stoi(c));
145                     }
146                 }
147                 yt.push_back(row);
148             }
```

ii. Insert:

(1) First, set a swap function for exchanging two indices. We will use it later.

```
10  void swap(int &a, int &b)
11  {
12      int temp = a;
13      a = b;
14      b = temp;
15  }
```

(2) Then we insert the inserted number aka. ‘key’ in the last position of tableau (yt [m-1][n-1]), and perform the INSERT function, which reconstruct the tableau that make each index be in the correct position.

```
43  void initial(vector<vector<int>>&yt,vector<int>&insert_key,int m,int n){
44      for(int key:insert_key){
45          if(yt[m-1][n-1]!=INF){
46              cout<<"Cannot insert!\n";
47          }
48          else{
49              yt[m-1][n-1]=key;
50              INSERT(yt,m-1,n-1);
51          }
52      }
53  }
```

(3) In INSERT function, we use recursive concept. We move the bottom-right corner’s index upwards and leftwards until it is in the correct position. We handle the first row and column separately, and the base case is when we reach the top-left corner.

```
16  void INSERT(vector<vector<int>>&yt,int i,int j){
17      if(i==0 && j==0){
18          return;
19      }
20      if(i==0){       //first row
21          if(yt[i][j]<yt[i][j-1]){
22              swap(yt[i][j],yt[i][j-1]);
23              INSERT(yt,i,j-1);
24          }
25          return;
26      }
27      if(j==0){       //first column
28          if(yt[i][j]<yt[i-1][j]){
29              swap(yt[i][j],yt[i-1][j]);
30              INSERT(yt,i-1,j);
31          }
32          return;
33      }
34      if(yt[i][j]<yt[i-1][j]){        //up
35          swap(yt[i][j],yt[i-1][j]);
36          INSERT(yt,i-1,j);
37      }
38      if(yt[i][j]<yt[i][j-1]){     //left
39          swap(yt[i][j],yt[i][j-1]);
40          INSERT(yt,i,j-1);
41      }
42  }
```

iii. Extract-min:

(1) We know that the min in the tableau is the top-left corner index, we assigned it to ‘min’ and set its position value to INF. Then use fix function to reconstruct the tableau.

```
void EXTRACT_MIN(vector<vector<int>>&yt,ofstream& out){
    int min=yt[0][0];
    yt[0][0]=INF;
    fix(yt,0,0);
    out<<"Extract-min "<<min<<"\n";
}
```

(2) We consider (i, j) as the root node, and find the right and bottom nodes of it. Then we compare its right and bottom node, swap the root node with the smaller node. The function starts from (0, 0) node which value is INF, and implement the fix function recursively until its right and bottom nodes are both INF.

```
void fix(vector<vector<int>>&yt,int i,int j){
    int m=yt.size();
    int n=yt[0].size();
    // get the bottom and right num of cur
    int bottom,right;
    if(i+1<m){bottom=yt[i+1][j];}
    else{bottom=INF;}
    if(j+1<n){right=yt[i][j+1];}
    else{right=INF;}
    if (bottom==INF && right==INF) {
        return;
    }
    if(bottom<right){ //down
        swap(yt[i][j],yt[i+1][j]);
        fix(yt,i+1,j);
    }
    else{ //right
        swap(yt[i][j],yt[i][j+1]);
        fix(yt,i,j+1);
    }

}
```

iv. Output: Using output function to output the result in the txt.file.

```
void output(vector<vector<int>>&yt,int m,int n,ofstream& out){
    for(int i=0;i<m;i++){
        for(int j=0;j<n;j++){
            if(yt[i][j]==INF){out<<"x ";}
            else{out<<yt[i][j]<<" ";}
        }
        out<<"\n";
    }
    out<<"\n";
}
```

II. Running time analysis:

- m is the number of rows, n is the number of columns.

i. Insert:

(1) 'INSERT' function: Time Complexity is O(m+n), which is the worst case that it needs to go upwards m times and leftwards n times to its correct position.

(2) 'initial' function: Assume there are k inserted number (key), then it called k times INSERT function. Time Complexity is **O (k* (m+n))**.

ii. Extract-min:

(1) 'EXTRACT-MIN' function called fix function. We divided the m*n problem into (m-1)*n or m*(n-1) subproblem. The worst case is the index at the top-left corner moves downwards m times and rightwards n times, so the time complexity is **O(m+n)**.

iii. Output: Time Complexity is O(m*n).