

1	(i)	State $f(x) \leq 10$	B1	1 [Any equiv but must be or imply \leq]
	(ii)	Attempt correct process for composition of functions Obtain 6 or correct expression for $ff(x)$ Obtain - 71	M1 A1 A1	[whether algebraic or numerical] 3
2		Either Obtain $x = 0$ Form linear equation with signs of $6x$ and x different State $6x - 1 = -x + 1$ Obtain $\frac{2}{7}$ and no other non-zero value	B1 M1 A1 A1	[ignoring errors in working] [ignoring other sign errors] [or correct equiv with or without brackets] 4 [or exact equiv]
		Or Obtain $36x^2 - 12x + 1 = x^2 - 2x + 1$ Attempt to solve quadratic equation Obtain $\frac{2}{7}$ and no other non-zero value Obtain 0	B1 M1 A1 B1	[for equiv] [as far as factorisation or subn into formula] [or exact equiv] (4) [ignoring errors in working]
	(i)	Attempt solution involving (natural) logarithm Obtain $-0.017t = \ln \frac{25}{180}$ Obtain 116	M1 A1 A1	[or equiv] 3 [or greater accuracy rounding to 116]
	(ii)	Differentiate to obtain $k e^{0.017t}$ Obtain correct $-3.06 e^{0.017t}$ Obtain 1.2	M1 A1 A1	[any constant k different from 180; solution must involve differentiation] [or unsimplified equiv: accept + or -] 3 [or greater accuracy: accept + or - answer]
4	(a)	State or imply $\int \pi y^2 dx$ Integrate to obtain $k \ln x$ Obtain $4\pi \ln x$ or $4 \ln x$ Obtain $4\pi \ln 5$	B1 M1 A1 A1	[any constant k , involving π or not; or equiv such as $k \ln 4x$] [or equiv] 4 [or similarly simplified equiv]

	(b)	Attempt calculation involving attempts at y values Attempt $\frac{1}{3} \times 1(x_0 + 4x_1 + 2x_2 + 4x_3 + x_4)$ Obtain $\frac{1}{3}(\sqrt{2} + 4\sqrt{5} + 2\sqrt{10} + 4\sqrt{17} + \sqrt{26})$ Obtain 12.758	M1 M1 A1 A1	[with each of 1, 4, 2 present at least once as coefficients] [with attempts at five y values] [or exact equiv or decimal equivs] 4 [or greater accuracy]
	(i)	Obtain $R = \sqrt{13}$, or 3.6 or 3.61 or greater accuracy Attempt recognisable process for finding α Obtain $\alpha = 33.7$	B1 M1 A1	[allow sine/cosine muddles] 3 [or greater accuracy]
5	(ii)	Attempt to find at least one value of $\theta + \alpha$ Obtain value rounding to 76 or 104 Subtract their α from at least one value Obtain one value rounding to 42 or 43, or to 70 Obtain other value 42.4 or 70.2	*M1 A1 M1 A1 A1	[following their R] [dependent on *M1] 5 [or greater accuracy; no other answers between 0 and 360; ignore answers outside 0 to 360]
	(a)	Attempt use of product rule Obtain $\ln x + 1$ Equate attempt at first derivative to zero and obtain value involving e Obtain e^{-1}	*M1 A1 M1 A1	[or unsimplified equiv] [dependent on *M1] 4 [or exact equiv]
6	(b)	Attempt use of quotient rule Obtain $\frac{(4x + c)1 - 4(4x + c)}{(4x + c)^2}$ Show that first derivative cannot be zero	M1 A1 A1	[or equiv using product rule or ...] [or equiv] 3 [AG; derivative must be correct]
	(i)	State $2 \cos^2 x = 1$	B1	1
7	(ii)	Attempt to express left hand side in terms of $\cos x$ Identify $\frac{1}{\cos x}$ as $\sec x$	M1 M1	[using expression of form $a \cos^2 x + b$] [maybe implied]

		Confirm result	A1	3 [AG; necessary detail required]												
	(iii)	Use identity $\sec^2 x = 1 + \tan^2 x$	B1													
		Attempt solution of quadratic equation in $\tan x$	M1	[or equiv]												
		Obtain $2 \tan^2 x + 3 \tan x - 9 = 0$ and hence $\tan x = -3, \frac{1}{2}$	A1													
		Obtain at least two of 0.983, 4.12, 1.89, 5.03 (or of $0.313\pi, 1.31\pi, 0.602\pi, 1.60\pi$)	A1	[allow answers with only 2 s.f.; allow greater accuracy; allow $0.983 + \pi, 1.89 + \pi$ allow degrees: 56, 236, 108, 288]												
		Obtain all four solutions	A1	5 [now with at least 3 s.f.; must be radians; no other solutions in the range $0 - 2\pi$; ignore solutions outside range $0 - 2\pi$]												
8	(i)	Attempt relevant calculations with 5.2 and 5.3	M1													
		Obtain correct values	A1	<table border="1"> <thead> <tr> <th></th> <th>y_1</th> <th>y_2</th> <th>$2.1 - y_2$</th> </tr> </thead> <tbody> <tr> <td>5.2</td> <td>2.83</td> <td>2.87</td> <td>-0.04</td> </tr> <tr> <td>5.3</td> <td>2.89</td> <td>2.88</td> <td>0.006</td> </tr> </tbody> </table>		y_1	y_2	$2.1 - y_2$	5.2	2.83	2.87	-0.04	5.3	2.89	2.88	0.006
	y_1	y_2	$2.1 - y_2$													
5.2	2.83	2.87	-0.04													
5.3	2.89	2.88	0.006													
		Conclude appropriately	A1	3 [AG; comparing y values or noting sign change in difference in y values or equiv]												
	(ii)	Equate expressions and attempt rearrangement to $x =$	M1													
		Obtain $x = \frac{5}{4} \ln(3x + 8)$	A1	2 [AG; necessary detail required]												
	(iii)	Obtain correct first iterate	B1													
		Carry out correct process to find at least two iterates in all	M1													
		Obtain 5.29	A1	3 [must be exactly 2 decimal places; 5.2 \rightarrow 5.2687 \rightarrow 5.2832 \rightarrow 5.2863 \rightarrow 5.2869, 5.25 \rightarrow 5.2793 \rightarrow 5.2855 \rightarrow 5.2868 \rightarrow 5.2870, 5.3 \rightarrow 5.2898 \rightarrow 5.2877 \rightarrow 5.2872 \rightarrow 5.2871]												
	(iv)	Obtain integral of form $k(3x + 8)^{\frac{1}{3}}$	M1													
		Obtain integral of form $k e^{\frac{1}{3}x}$	M1													

		Obtain $\frac{1}{4}(3x + 8)^{\frac{4}{3}} - 5e^{\frac{1}{3}x}$	A1	[or equiv]
		Apply limits 0 and their answer to (iii)	M1	[applied to difference of two integrals]
		Obtain 3.78	A1	5 [or greater accuracy]
9	(i)	Indicate stretch and (at least one) translation	M1	[... in general terms]
		State translation by 7 units in negative x direction	A1	[or equiv; using correct terminology]
		State stretch in x direction with factor $1/m$	A1	[must follow the translation by 7; or equiv; using correct terminology]
		Indicate translation by 4 units in negative y direction	B1	4 [or equiv; at any stage; the two translations may be combined]
	(ii)	Refer to each y value being image of unique x value	B1	[or equiv]
		Attempt correct process for finding inverse	M1	
		Obtain expression involving $(x + 4)^2$ or $(y + 4)^2$	M1	
		Obtain $\frac{(x + 4)^2 - 7}{m}$	A1	4 [or equiv]
	(iii)	Refer to fact that curves are reflections of each other in line $y = x$	B1	[or equiv]
		Attempt arrangement of either $f(x) = x$ or $f^{-1}(x) = x$	M1	
		Apply discriminant to resulting quadratic equation	M1	
		Obtain $(m - 2)(m - 14) < 0$	A1	[or equiv]
		Obtain $2 < m < 14$	A1	5