

## 4722 Core Mathematics 2

		Mark	Total	
1	<p>area of sector = <math>\frac{1}{2} \times 11^2 \times 0.7</math>  <math>= 42.35</math></p> <p>area of triangle = <math>\frac{1}{2} \times 11^2 \times \sin 0.7 = 38.98</math>  hence area of segment = <math>42.35 - 38.98</math>  <math>= 3.37</math></p>	<p>M1  A1  M1  A1</p>	4	<p>Attempt sector area  Obtain 42.35, or un  Attempt triangle ar  subtract from atten  Obtain 3.37, or bett</p>
2	<p>area <math>\approx \frac{1}{2} \times 2 \times \{2 + 2(\sqrt{12} + \sqrt{28}) + \sqrt{52}\}</math></p> <p><math>\approx 26.7</math></p>	<p>M1  M1  M1  A1</p>	4	<p>Attempt y-values at  Correct trapezium m  find area between x  Correct h (soi) for t  Obtain 26.7 or bette</p>
3	<p>(i) <math>\log_a 6</math></p> <p>(ii) <math>2\log_0 x - 3\log_0 y = \log_0 x^2 - \log_0 y^3</math>  <math>= \log_{10} \frac{x^2}{y^3}</math></p>	<p>B1  M1*  M1dep*  A1</p>	3	<p>State <math>\log_a 6</math> cwo  Use <math>b \log a = \log a^b</math>  Use <math>\log a - \log b =</math>  Obtain <math>\log_{10} \frac{x^2}{y^3}</math></p>
4	<p>(i) <math>\frac{BD}{\sin 62} = \frac{16}{\sin 50}</math>  <math>BD = 18.4 \text{ cm}</math></p> <p>(ii) <math>18.4^2 = 10^2 + 20^2 - 2 \times 10 \times 20 \times \cos \theta</math>  <math>\cos \theta = 0.3998</math>  <math>\theta = 66.4^\circ</math></p>	<p>M1  A1  M1  M1  A1</p>	2	<p>Attempt to use cor  Obtain 18.4 cm  Attempt to use cor  Attempt to rearrang  (from <math>a^2 = b^2 + c</math>  Obtain <math>66.4^\circ</math></p>
5	<p><math>\int 12x^{\frac{1}{2}} dx = 8x^{\frac{3}{2}}</math></p>	<p>M1</p>		<p>Attempt to integrat</p>

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6	<p>(i) <math>u_1 = 7</math> <math>u_2 = 9, u_3 = 11</math></p> <p>(ii) Arithmetic Progression</p> <p>(iii) <math>\frac{1}{2} N (14 + (N - 1) \times 2) = 2200</math> <math>N^2 + 6N - 2200 = 0</math> <math>(N - 44)(N + 50) = 0</math> hence <math>N = 44</math></p>	<p>B1 B1  B1 M1 A1 M1 A1</p> <p>2  1  5</p>	<p>Correct <math>u_1</math> Correct <math>u_2</math> and <math>u_3</math>  Any mention of a Correct interpreta Attempt sum of A Correct (unsimpli Attempt to solve Obtain <math>N = 44</math> on</p>	8
7	<p>(i) Some of the area is below the x-axis</p> <p>(ii)</p> $\left[ \frac{1}{3}x^3 - \frac{3}{2}x^2 \right]_0^3 = \left( 9 - \frac{27}{2} \right) - (0 - 0)$ $= -4\frac{1}{2}$ $\left[ \frac{1}{3}x^3 - \frac{3}{2}x^2 \right]_3^5 = \left( \frac{125}{3} - \frac{75}{2} \right) - \left( 9 - \frac{27}{2} \right)$ $= 8\frac{2}{3}$ <p>Hence total area is <math>13\frac{1}{6}</math></p>	<p>B1  M1 A1 M1 A1 M1 A1 A1</p> <p>1      7</p>	<p>Refer to area / cu area' ... Attempt integrati Obtain <math>\frac{1}{3}x^3 - \frac{3}{2}x^2</math> Use limits 3 (and Obtain <math>(-4)\frac{1}{2}</math> Use limits 5 and 3 Obtain <math>8\frac{2}{3}</math> (allow Obtain total area  SR: if no longer f [0, 3] and [3, 5]</p>	8
8	<p>(i) <math>u_4 = 10 \times 0.8^3</math> <math>= 5.12</math></p> <p>(ii) <math>S_{20} = \frac{10(1 - 0.8^{20})}{1 - 0.8}</math> <math>= 49.4</math></p> <p>(iii) <math>\frac{10}{1 - 0.8} - \frac{10(1 - 0.8^N)}{(1 - 0.8)} &lt; 0.01</math></p>	<p>M1 A1  M1 A1 M1 A1</p> <p>2  2</p>	<p>Attempt <math>u_4</math> using Obtain 5.12 aef  Attempt use of co Obtain 49.4 Attempt <math>S_x</math> using Obtain <math>S_x = 50</math>, o</p>	

		Mark	Total
9	<p>(i) <math>(90^\circ, 2), (-90^\circ, -2)</math></p> <p>(ii) (a) <math>180 - \alpha</math> (b) <math>-\alpha</math> or <math>\alpha - 180</math></p> <p>(iii) <math>2\sin x = 2 - 3\cos^2 x</math>  <math>2\sin x = 2 - 3(1 - \sin^2 x)</math>  <math>3\sin^2 x - 2\sin x - 1 = 0</math>  <math>(3\sin x + 1)(\sin x - 1) = 0</math>  <math>\sin x = -1/3, \sin x = 1</math>  <math>x = -19.5^\circ, -161^\circ, 90^\circ</math></p>	<p>B1 B1</p> <p>B1 B1</p> <p>M1 A1 M1 A1 A1✓ A1</p>	<p>2</p> <p>1 1    6</p> <p>State at least 2 correct answers State all 4 correct answers (radians is B1 B0) State <math>180 - \alpha</math> State <math>-\alpha</math> or <math>\alpha - 180</math> (radians or unsimplified)  Attempt use of cosine rule Obtain <math>3\sin^2 x - 2\sin x - 1 = 0</math> Attempt to solve quadratic Obtain <math>x = -19.5^\circ</math> Obtain second correct answer for their <math>x</math> Obtain <math>90^\circ</math> (radians or degrees)  SR: answer only (if correct)</p>
<b>10</b>			
10	<p>(i) <math>(2x + 5)^4 = (2x)^4 + 4(2x)^3 \cdot 5 + 6(2x)^2 \cdot 5^2 + 4(2x) \cdot 5^3 + 5^4</math>  <math>= 16x^4 + 160x^3 + 600x^2 + 1000x + 625</math></p> <p>(ii) <math>(2x + 5)^4 - (2x - 5)^4 = 320x^3 + 2000x</math></p> <p>(iii) <math>9^4 - (-1)^4 = 6560</math> and <math>7360 - 800 = 6560</math> <b>A.G.</b>  <math>320x^3 - 1680x + 800 = 0</math>  <math>4x^3 - 21x + 10 = 0</math>  <math>(x - 2)(4x^2 + 8x - 5) = 0</math>  <math>(x - 2)(2x - 1)(2x + 5) = 0</math>  Hence <math>x = 1/2, x = -5/2</math></p>	<p>M1* M1* A1dep* A1</p> <p>M1 A1</p> <p>B1 M1 A1✓ A1 M1 A1</p>	<p>4</p> <p>2</p> <p>6</p> <p>Attempt expansion of <math>(2x + 5)^4</math> (at least 4 terms) Attempt coefficients Obtain two correct terms Obtain a fully correct expansion  Identify relevant terms change of sign Obtain <math>320x^3 + 2000x</math>  Confirm root, at <math>x = 1/2</math> Attempt complete factorisation Obtain quotient of <math>4x^2 + 8x - 5</math> and their coeff of <math>x^3</math> Obtain <math>(4x^2 + 8x - 5)</math> Attempt to solve quadratic Obtain <math>x = 1/2, x = -5/2</math>  SR: answer only (if correct)</p>