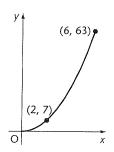
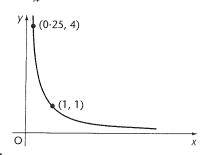


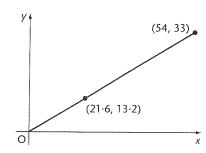
**f)** 
$$y = \frac{7x^2}{4}$$



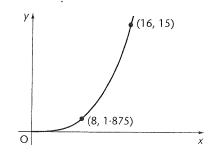
**g)** 
$$y = \frac{1}{x}$$



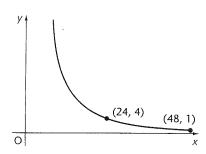
**h)** 
$$y = \frac{11x}{18}$$



$$i) \quad y = \frac{15x^3}{4096}$$



**j)** 
$$y = \frac{2304}{x^2}$$



#### Exercise 3.5 (page 31)

- **1** a) (i)  $y \propto x^2$
- (ii)  $y = x^2$
- **b)** (i)  $y \propto x^2$ (iii) 128
- (ii)  $y = 2x^2$
- c) (i)  $y \propto x^2$
- (ii)  $y = \frac{1}{3}x^2$
- d) (i)  $y \propto x^2$
- (ii)  $y = 0.4x^2$
- (iii) 490
- e) (i)  $y \propto x^2$
- (ii)  $y = 1.2x^2$
- **f)** (i)  $y \propto \frac{1}{x^2}$
- (ii)  $y = \frac{225}{x^2}$
- (iii) 1
- **g)** (i)  $y \propto \frac{1}{x^2}$
- (ii)  $y = \frac{1250}{x^2}$
- **h)** (i)  $y \propto \frac{1}{x^2}$
- (iii) 0·2
- i) (i)  $y \propto \frac{1}{x^2}$
- (ii)  $y = \frac{800}{x^2}$
- **(i)**  $y \propto \frac{1}{x^2}$
- (ii)  $y = \frac{256}{r^2}$
- 2 a) Multiplied by 4
  - b) Multiplied by 2.25
- 3 a)  $h = \frac{5}{98}u^2$ 
  - **b)** 216 m (to the nearest whole number)
- 4  $1.52 \times 10^8 \,\mathrm{km}^2$

## **Revision exercise A1** (page 33)

- **1 a)**  $600 \times 80 = 48000, 48140$ 
  - $60 \div 4 = 15, 16.63$
  - $\frac{30^2}{0.5}$  = 1800, 1668.52
- 2 a)  $1.458 \times 10^4$ 
  - **b)**  $2.385 \times 10^{-1}$
- 3 a)  $x^2 + 8x + 7$ 
  - **b)**  $a^2 + 2a 15$
  - c)  $2y^2 2y 4$
  - **d)**  $2x^2 9x 5$
  - e)  $4a^2 3ab b^2$
- $2a^{5}$
- **b**) 5*a*
- $a^5$ c)
- **d)**  $24a^4b^4$
- **e)** 3*xz*
- **f)**  $4a^2c$

- 5 a) 3(a+2b-4c)
  - **b)** a(2+3b)
  - c) ab(a-3b)
  - 2xy(x 3)d)
  - 7ab(c+2a)e)

  - $3(3a^2+b^2-2c^2)$ f)
  - **g**) 5(pq - 2)
  - $2a(1-2a+3a^2)$
  - i) 50ac(2b-1)
- (x-7)(x+7)6 a)
  - b) (x-1)(x+1)
  - No factors c)
  - d) (x-y)(x+y)
  - e) (11-b)(11+b)
- 7 a) (x-9)(x-7)
- **b)** 2(x+3)(x-7)
- (x-2)(3x-2)c)
- d) (x+3)(2x-5)
- e) 3(x-4)(x+4)
- f) (2x+3)(x-7)
- g) 3(2x+1)(x-5)
- **h)** (5x-6)(x-3)
- i) (2x+1)(4x-5)
- j) (3x+2)(2x-5)
- 8 a)

- 9 a)  $x = \frac{-4}{3}$  or x = 3
  - **b)** x = 3.5 or x = -4
- c)  $x = \pm 8$
- **10 a)** 0.06 units
- **11** 25, 125, 625, 1, 0·2
  - (ii) xy = 50
  - (i)  $y \propto \frac{1}{x}$ (i)  $y \propto x$
- **(ii)** y = 2x
- c) (i)  $y \propto \frac{1}{x}$
- (ii) xy = 0.2
- **d**) (i)  $y \propto x^2$
- (ii)  $y = 0.025x^2$

#### 4 Indices

### Exercise 4.1 (page 38)

- 1 a)  $n^{\frac{1}{3}}$
- $n^{\frac{2}{5}}$ c)
- **d**)  $n^{\frac{1}{4}}$
- e)  $n^4$
- f)
- 2 a)
- **b)** 2
- c) 1
- d)
- 8 **e**)
- 3 a) 2
- **b**)  $\frac{1}{8}$
- c) 16
- **d**) 64
- **e**) 8

- 4 a)
- **b**) 3
- c)
- **d**)  $\frac{1}{81}$
- e)
- 5 a) 3
  - c)
- **b**) 81
- **d**) 3

b)

b)

d) 27

d)

**d)** 16

**d)** 64

**b)** 64

**b**) 6

**b)** 16

 $\frac{343}{3} = 114\frac{1}{3}$ 

- e)
- 6 a)
  - c) 1
  - e)
- 7 a) 4
- c) 1 e) 128
- 8 a) 12
- c)
- a) 125
- c) 100
- 9 10 a)
  - $\frac{16}{3} = 5\frac{1}{3}$
- c) **11 a)** 1000
- b)

d) 15

- c)  $113\frac{3}{4}$
- **d)** 0
- **12** a) 1.925414 = 1.9254 (to 5 s.f.)
  - **b)** 21.717639 = 21.718 (to 5 s.f.)
  - c) 1.045910 = 1.0459 (to 5 s.f.)
  - **d)** 0.003538869 = 0.0035389 (to 5 s.f.)
- **13 a)** 111.5664 = 111.57 (to 5 s.f.)
  - **b)** 0.02059629 = 0.020596 (to 5 s.f.)
  - c) 1.072135 = 1.0721 (to 5 s.f.)
  - **d)** 0.04058084 = 0.040581 (to 5 s.f.)
- **14 a)** 31
  - **b)** 1.009998068 = 1.0100 (to 5 s.f.)
  - 1.544857 = 1.5449 (to 5 s.f.) c)
  - d) 2.107773 = 2.1078 (to 5 s.f.)
- 15 a)
  - b) 6.760315 = 6.7603 (to 5 s.f.)
  - 1.276518 = 1.2765 (to 5 s.f.) c)
- **16** a) 106.1208 = 106.12 (to 5 s.f.)
  - **b)** 13.427845 = 13.428 (to 5 s.f.)
  - 25.30439 = 25.304 (to 5 s.f.) c)
- 17 a) 145
  - 7.483282 = 7.4833 (to 5 s.f.) b)
  - c) 1.422970 = 1.4230 (to 5 s.f.)
- **18 a)** 3.7711
  - **b)** 2.167981 = 2.1680 (to 5 s.f.)
  - c)
- 19 a) 3547.171 = 3547.2 (to 5 s.f.)
  - 4.732081 = 4.7321 (to 5 s.f.) 299.5320705 = 299.53 (to 5 s.f.) **c**)
- 20 a)
- **b)** 243
- $\frac{1}{5}$ c)
- **d**) 18
- **e)** 16  $\frac{36}{5} = 7\frac{1}{5}$
- f) 72

- 3 a) 25.7 cm c) 51.3 cm e)
- b) 25.9 cm **d)** 26.3 cm
- 25.8 cm f) 11.7 cm
- 43° 4 a)
- 100° b)
- 185° c) 148° e)
- 58° d) f) 57°
- 179° 159° i)
- **h)** 203° 62° j)
- **k**) 188° 5 a) 4.9 cm
- 257° I) **b)** 3.4 cm
- c) 4.8 cm e) 3.7 cm 13.4 cm g)
- d) 5.6 cm f) 2.5 cm h) 5.55 cm
- i) 4.62 cm
- **b)** 1.51 cm
- 6 a) 6.59 cm c) 1.81 m
- 7 Blue area =  $626 \,\mathrm{mm^2}$  (nearest mm<sup>2</sup>) Black length =  $167 \, \text{mm}$  (nearest mm)
- a)  $344 \,\mathrm{m}^2$  (nearest  $\mathrm{m}^2$ ) **b)** 77 m (nearest m)
- 186.7°, 62.6 cm<sup>2</sup>
- 10 208 cm

### Exercise 6.2 (page 54)

- 1 a)  $18 \, \text{cm}^3$ c)  $70 \,\mathrm{m}^3$
- **b)**  $54 \, \text{cm}^3$
- e)  $179 \, \text{cm}^3$
- **d)**  $50 \, \text{cm}^3$
- $2 a) 103 cm^3$
- $30\,\mathrm{cm}^3$ f) **b)**  $314 \, \text{cm}^3$
- c)  $51.5 \text{ cm}^3$
- d)  $154 \,\mathrm{cm}^3$
- e)  $1010 \, \text{cm}^3$
- f)  $181 \, {\rm cm}^{3}$
- 3 a)  $524 \,\mathrm{cm}^3$  $33.5 \,\mathrm{mm}^3$ c)
- **b)**  $998 \, \text{cm}^3$ **d)**  $113 \, \text{cm}^3$
- e)  $435 \, \text{cm}^3$
- f) 1988 mm<sup>3</sup> **b)**  $121 \, \text{cm}^3$

**b)** 3.1 cm

**b)**  $2310 \, \text{cm}^3$ 

b) 12.4 cm

- 4 a)  $6.57 \, \text{cm}^3$ 5 12 cm
- 6 a) 3.6cm
  - 6.2 cm c)
- 7 a)  $556 \,\mathrm{cm}^3$ 
  - c)  $4190 \, \text{cm}^3$
- a) 6.6 cm 8
- 9 117 ml

- 11 88 12 69
- 13 69 100 mm<sup>3</sup>
- 14 12 cm 15 3·17 cm
- 10 7.96 cm

# Upper and lower bounds

## Exercise 7.1 (page 60)

- **1** a) 61.2 seconds
  - c) 12.4 m
  - e) 185 mm
- g) 148·3 cm 2 a) 61 seconds
  - 12·38 m c)
  - 183 mm e) 148·1 cm
- b) 24.51 seconds
- **d)**  $1.747 \, \text{kg}$
- f) 12.738 kg
- **h)** 105.86 seconds
- **b)** 24.49 seconds
- **d)** 1.745 kg
- f) 12.736 kg
- **h)** 105.84 seconds

- 3 a) 704 g
  - 790 g c)

  - e) 0.16 second
  - **g)** 9000 m
- **4 a)** 702 g
- **c)** 770 g
- e) 0.14 second
- **g)** 8800 m
- 5 50.8 cm
- **6 a)** 29.20 seconds
- **b)** 1.06 seconds 7 UB = 26.5 cm, LB = 23.5 cm

**b)** 6.7 cm

76 m

d) 4.2 seconds

**b)**  $20.507175 \,\mathrm{m}^2$ 

**d)**  $40.1625 \,\mathrm{m}^2$ **b)**  $20.415675 \,\mathrm{m}^2$ 

d)  $38.8825 \,\mathrm{m}^2$ 

**b)** 12.74625 m

d) 11.707 275 m

**d)** 11.630375 m .

b)  $1.25 \,\mathrm{m/second}$ 

b) 1.28 m/second

**b)** 10.6 cm

b) 5.17 cm

**b)** 12.51025 m

**h)** 0.138 g

**b)** 6.5 cm

f) 74 m

**h)**  $0.136 \, \text{g}$ 

d)

f)

4.4 seconds

- 8 UB = 3 kg, LB = 2.8 kg
- 9 UB = 1 cm, LB = 0 cm
- **10 a)** UB = 13.8, LB = 13.6
  - **b)** UB = 3.6, LB = 3.4

#### Exercise 7.2 (page 62)

- 1 No
- **2** 75 mm
- 3 a)  $16.3625 \,\mathrm{m}^2$ 
  - c)  $56.910875 \,\mathrm{m}^2$
- 4 a) 15.5625 m<sup>2</sup>
- c)  $56.759175 \text{ m}^2$
- **5** a) 1141.7575 cm
- c) 146.625 km
- 6 a) 1131·2875 cm
- c) 138-425 km
- 7 a) 5.08 cm/second
- c)  $10.5 \,\mathrm{m/second}$
- 8 a) 5.61 cm/second
- c) 10.7 m/second 9 0.02288 kg/cm<sup>3</sup>
- 10 a) 11.7 cm
- c) 20.4 cm
- 11 a) 2.54 cm c) 3.66 m
- 12 UB = 844, LB = 830 people/square mile
- 13 UB =  $536.25 \,\text{cm}^2$ , LB =  $490.25 \,\text{cm}^2$
- 14 UB = 7.88 m/second, LB = 7.74 m/second
- **15** a) UB =  $87.95 \text{ cm}^3$ , LB =  $81.37 \text{ cm}^3$ 
  - **b)** UB = 1702 g, LB = 1566 g
- **16** UB = 84.5, LB = 20.2
- **17** UB = 0.405, LB = 0.384

## Revision exercise B1 (page 64)

- 1 a)  $n^{-1}$ 
  - $n^{\frac{7}{2}}$ c)
- 2 a)
- c)
- e) 4 2 g)
- i)  $1\frac{1}{2}$
- **3 a**) 625 c) 9
- e) 42 4 g)
- 32 h) 144

 $\frac{1}{25}$ 

b)  $m^3$ 

**b**) 1

d) 16

f)

- 80
- b) d) 8
- f) 500
- **h**)  $2\frac{1}{12}$

**STAG** 

- 4 a) 2.9242
  - **c)** 4096
- 5 a) 9 c) 3.9842
- 6 a)  $2^7$ 

  - **c)**  $7^{\frac{2}{3}}$
  - **e)**  $2^{6n+5}$

- 7 a)  $2^3 \times 5$ c)  $2^3 \times 17$ 8 a)  $3^2 \times 5^2$ b)  $2 \times 3^2 \times 5$ d)  $2^2 \times 3 \times 7^2$ 8 a)  $3^2 \times 5^2$ b)  $2 \times 5^{\frac{1}{3}}$ c)  $2^4 \times 7^{\frac{10}{3}}$ d)  $2^3 \times 3^{\frac{5}{2}}$ 9 a)  $a = \frac{2b 5c}{8}$ b) a = 2b
- **10 a)**  $p = \frac{q}{7}$
- 11 a) 8.51 cm
- **12 a)** 66⋅0°
- **13 a)** 6.21 cm
- **14** 7240 cm<sup>3</sup>
- **15** 136 m<sup>3</sup>
- **18 a)** UB of space 1000-5 mm
  - so UB of two units 1001 mm (or other valid explanation).
  - **b)** 1.5 mm

- 21 978·75 m
- 22 602 people/km<sup>2</sup>

## 8 Similarity and enlargement

#### Exercise 8.1 (page 68)

- - **c)** 25
  - **e)** 36

- $4 25 \text{ cm}^2$

**b)** 9

**d**) 16 **f)** 100

**b)** 64

**d**) 8

**f)** 512

**b)** 6

**d)** 10

- 8 360 cm<sup>2</sup>
- 9  $5.2 \,\mathrm{m}^2$

- **b)** 0.49842
- **d)** 0.00025674
- **b)** 1.6765
- **d)** 512
- **b)** 36
- **d**) 3<sup>6</sup>

- **b)**  $p = \frac{2}{2-t}$ 

  - **f)**  $p = \pm \sqrt{2b 4a}$
  - **b)**  $27.7 \, \text{cm}^2$
  - **b)** 144°
  - **b)** 4.84 cm

- 16 UB = 535 g, LB = 505 g
- **17 a)** 31·2 cm **b)** 8·2 cm
- UB of each unit 500.5 mm,
- 19 UB =  $101 \, \text{cm}^3$ , LB =  $94.2 \, \text{cm}^3$
- **20 a)** 7.38 m/second **b)** 7.35 m/second

- 1 a) 4
- **2 a)** 1000
  - **c)** 125
  - **e)** 27
- 3 a) 4
  - **c)** 8
- 5 a)  $72.5 \,\mathrm{cm}^2$
- **b)** 18·1 m<sup>2</sup>
- 6 1 litre
- 7 25.9 cl
- **10** 1:50

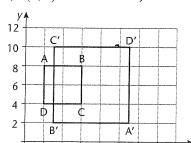
- **11** 1:1.59
- **12** 12.6 cm
- **13** 12.96 m<sup>2</sup>
- **14** 27:64:125
- **15** 12.5 cm
- **16 a)** 2 m
  - c)  $18750 \,\mathrm{cm}^3$
- **17** 2.48 m
- **18 a)** 3.6 m
- **b)** 5.76 litres

**b)**  $3 \, \text{m}^2$ 

- **19** a) 15
- **b)** 225
- c)  $4.52 \,\mathrm{m}^3$
- **20** 15·1 cm
- **21**  $0.0226\,\mathrm{m}^2$  or  $226\,\mathrm{cm}^2$
- **22** 3·30:2·08:3·78 or 1·59:1:1·82
- 23 77·44 cm<sup>2</sup>

## Exercise 8.2 (page 71)

- **1** a) (1, 8)
- **b**) -3



2 4 6 8 10 12 14 16 <sup>X</sup>

- 3 a) (0,3)
- **b)** ⁻2 **b)** ⁻0⋅5
- **4 a)** (2, 3)

# 9 Probability

# Exercise 9.1 (page 77)

- $\frac{1}{10} = \frac{1}{2}$
- 2 0.65
- $\frac{8}{52} = \frac{2}{13}$
- $4 \quad \frac{16}{100} = \frac{4}{25}$
- **5** 0·24
- $6 \frac{3}{6} = \frac{1}{2}; \frac{1}{4}$
- 8 0.56
- 9 0.85
- **10** 0.04 11 Don't add up to 1
- **12 a)** 0.75
- **b)** 0.175
- 13 a)  $\frac{1}{13}$ 13 a)  $\frac{1}{13}$ 14 a) 0.6, 0.4
- **b)**  $\frac{1}{169}$ **b)** 0.24
- 15  $\frac{1}{144}$
- 16  $\frac{1}{27}$
- 17 a)  $\frac{15}{23}$
- **b**)  $\frac{18}{23}$
- **b)** 0.65

STAGE

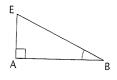
- 12 Yes.  $CE = 11.96 \,\text{m}$  and  $AC = 87.3 \,\text{m}$ Also AC =  $\sqrt{80^2 + 35^2} = 87.3 \,\mathrm{m}$
- 13 a) 11.0 cm
- **b)** 35.5°
- **14 a)** 10.9 m
- **b**) 68.9°
- c) 11.7 m

## Exercise 10.3 (page 95)

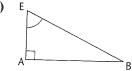
- 1 a) 10.63 units to 2 d.p.
  - **b)** 10.82 units to 2 d.p.
  - c) 15.33 units to 2 d.p.
  - **d)** 5.48 units to 2 d.p.
  - e) 12.37 units to 2 d.p.
- 2 6 or -6

## Exercise 10.4 (page 98)

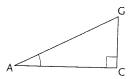
1 a)

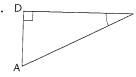


b)



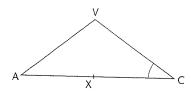
c)



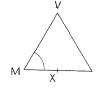


- **2** a) 32°
- **b**) 58°
- 26.6° c)
- d) 32·5°
- 3 a) 33·7°
- **b**) 36.5°

4 a)



b)

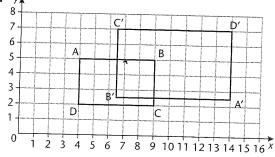


- **5** a) 65.4°
- **b)** 74.6°
- **6** 67·4°
- 7 a) 23·4°
- **b**) 49·3°
- **8** 62·1°
- 9 a) 11.6 cm
- **b)** 11.7 cm
- 10 a) 22.9 cm
  - **b)** (i) 12.6°
- (ii) 60·8°
- 11 35·3°; all cubes are similar

## Revision exercise C1 (page 100)

- 1 a)  $180 \, \text{cm}^2$
- **b)** 6 cm; 95 cm<sup>2</sup>
- c) 614·4 ml; 1200 ml
- 2 800 ml
- 3 7·42 cm

4 y4



A'(14, 2.5), B'(6.5, 2.5), C'(6.5, 7), D'(14, 7)

- **5 a)** (0, 4)
- **b**) -2
- **6** 0.85
- 7 0.13
- **8 a)** 0.09
- **b)** 0.42
- 0.25 a)
- **b)** 0.75
- c) 0.08
- **10 a)** 0.01
- **b)** 0.18
- **11** 0.57
- 12  $\frac{11}{60}$
- **13** a) 5.39 units
- **b)** 9.22 units
- 14 a) 56.8°
- **b**) 8.96 m
- 15 11·0 cm

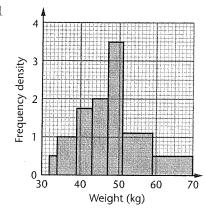
- **16 a)** 5.5 units
- c) 13 units
- **b)** 12.4 units
- 17 a) Angle BHC
- b) Angle AGB
- 18 a) Angle  $YBV = 51.1^{\circ}$ 
  - **b)** Angle CAD =  $35.0^{\circ}$
  - c) 12.8 m
- **19 a)** 149°
- b) 5.85 km
- c) 4.9°

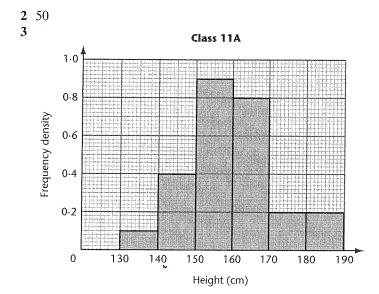
b) Only get people who are using the train at that time. These may not be representative of the population.

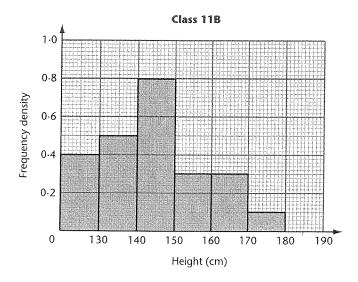
People may not want to take part as they are rushing home from work.

c) Likely to cover only people who read a lot. Not a random selection.

# Revision exercise D1 (page 149)







4	a)	<i>a</i> = 49°	(angle at the circumference
		<i>b</i> = 131°	= $\frac{1}{2}$ angle at the centre) (sum of angles on a straight line)

b) 
$$c = 120^{\circ}$$
 (opposite angles of a cyclic quadrilateral) (angles at centre and circumference)

$$e = 120^{\circ}$$
 (angles at centre and circumference)

$$f = 10^{\circ}$$
 (base angle of isosceles triangle)

d) Angle DAB = 
$$70^{\circ}$$
 (base angle of isosceles triangle)

Angle OAB = angle DAB - angle EAO  
= 
$$70^{\circ} - 40^{\circ} = 30^{\circ}$$

$$= 70^{\circ} - 40^{\circ} = 30^{\circ}$$
Therefore angle AOB = 120°

Therefore 
$$g = 60^{\circ}$$
 (angles at centre and circumference)

e) Angle at 
$$B = 70^{\circ}$$
 (base angle of isosceles triangle)

Therefore 
$$h = 70^{\circ}$$
 (angle between chord and tangent)

f) 
$$i = 55^{\circ}$$
 (base angle of isosceles triangle)

Therefore 
$$j = 70^{\circ}$$
 (angle sum of triangle)  
 $k = 55^{\circ}$  (angle between chord  
and tangent)

· 
$$l = 70^{\circ}$$
 (angle between chord and tangent)

g) Third angle of triangle = 
$$70^{\circ}$$

Therefore 
$$m = 70^{\circ}$$
 (base angle of isosceles triangle)

$$n = 40^{\circ}$$
 (angle sum of a triangle)

**h)** 
$$o = 25^{\circ}$$
 (angles in same segment)

Third angle of triangle = 
$$80^{\circ}$$

$$p = 75^{\circ}$$
 (angle sum of a triangle)

i) 
$$q = 62^{\circ}$$
 (angles at centre and circumference)

$$r = 28^{\circ}$$
 (base angles of isosceles triangle)  
 $s = 29^{\circ}$  (angle sum of a triangle)

**j**) 
$$t = 5.66 \,\text{cm}$$
 to 2 d.p. (Pythagoras)  $u = 38.9^{\circ}$  to 1 d.p. (trigonometry)

5 a) 
$$y = \frac{1}{2}x + 2$$
 or  $2y = x + 4$ 

**b)** 
$$y = \frac{-15}{8}x + 15 \text{ or } 15x + 8y = 120$$

c) 
$$y = \frac{5}{3}x - 1$$
 or  $3y = 5x - 3$ 

6 a) 
$$y = 3x + 2$$

**b)** 
$$y = -2x + 6$$
 or  $2x + y = 6$ 

c) 
$$y = \frac{1}{2}x + 5$$
 or  $2y = x + 10$ 

7 a) 
$$y = \frac{5}{2}x - 10$$
 or  $2y = 5x - 20$ 

**b)** 
$$y = \frac{2}{5}x + \frac{8}{5}$$
 or  $5y = 2x + 8$ 

c) 
$$3x + y = 9$$

8 AB: 
$$x + 3y = 14$$

BC: 
$$y = 2x - 7$$

AC: 
$$5x + y = 14$$

**9 a)** 
$$y = 7x - 34$$

**b)** 
$$2y = 5x - 20$$

c) 
$$5x + 4y = 6$$

c) 
$$5x + 4y = 6$$

**10 a)** 
$$x + 2y = 4$$

**b)** 
$$3x + 2y = 2$$

c) 
$$2y = 5x - 11$$
  
11 Yes – random sample of subscribers.