

1	$\frac{d}{dx}(xy) = x \frac{dy}{dx} + y$ $\frac{d}{dx}(y^2) = 2y \frac{dy}{dx}$	B1	s.o.i. e.g. $2x \frac{dy}{dx} + y$
	Substitute (1,2) into their differentiated equation and attempt to solve for $\frac{dy}{dx}$. [Allow subst of (2,1)] $\frac{dy}{dx} = -2$	B1	
		M1 dep at least 1 x B1	Or attempt to solve their diff equation for $\frac{dy}{dx}$ and then substitute (1,2)
		A1	4
2	(i) $1 + (-2)(-3x) + \frac{(-2)(-3)}{1.2}(-3x)^2 (+ \dots \text{ignore})$ $= 1 + 6x$ $\dots + 27x^2$	M1	State or imply; accept $-3x^2$ & $-9x^2$
		B1	Correct first 2 terms
		A1	3 Correct third term
	(ii) $(1 + 2x)^2(1 - 3x)^{-2}$ Attempt to expand $(1 + 2x)^2$ & select (at least) 2 relevant products and add 55 (Accept $55x^2$) <u>SR 1</u> For expansion of $(1 + 2x)^2$ with 1 error, A1✓ <u>SR 2</u> For expansion of $(1 + 2x)^2$ & > 1 error, A0 <u>Alternative Method</u> For correct method idea of long division 1 +10x +55x ²	M1	For changing into suitable form, seen/implied
		M1	
		A2✓	4 If (i) is $a + bx + cx^2$, f.t. $4(a + b) + c$
		M1	
		A1,A1,A1(4)	
3	(i) $\frac{A}{x} + \frac{B}{3-x}$ & c-u rule or $A(3-x) + Bx \equiv 3 - 2x$ $\frac{1}{x}$ $-\frac{1}{3-x}$	M1	Correct format + suitable method
		A1	seen in (i) or (ii)
		A1	3 ditto; $\frac{1}{x} - \frac{1}{3-x}$ scores 3 immediately
	(ii) $\int \frac{1}{x}(dx) = \ln x$ or $\ln x $ $\int \frac{1}{3-x}(dx) = -\ln(3-x)$ or $-\ln 3-x $ Correct method idea of substitution of limits $\ln 2 (+ \ln 1 - \ln 1) - \ln 2 = 0$ <u>Alternative Method</u> If ignoring PFs, $\ln x(3-x)$ immediately As before	B1	
		B1	Check sign carefully; do not allow $\ln(x-3)$
		M1	Dep on an attempt at integrating
		A1	4 Clearly seen; WWW AG
		B2	$\ln x(x-3) \rightarrow 0$
		M1,A1 (4)	
	(iii) Suitable statement or clear implication e.g. Equal amounts (of area) above and below (axis) or graph crosses axis or there's a root (Be lenient)	B1	1

4	(i) Working out $\mathbf{b} - \mathbf{a}$ or $\mathbf{a} - \mathbf{b}$ or $\mathbf{c} - \mathbf{a}$ or $\mathbf{a} - \mathbf{c}$	M1)	Irrespective of label
	$= \pm (-3\mathbf{i} - \mathbf{j} - \mathbf{k})$ or $\pm (-2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$	A1)	If not scored, these 1 st 3 marks can be
	Method for finding magnitude of <u>any</u> vector	M1)	awarded in part (ii)
	Method for finding scalar product of <u>any</u> 2 vectors	M1		
	Using $\cos \theta = \frac{\mathbf{a} \cdot \mathbf{b}}{ \mathbf{a} \mathbf{b} }$ AEF for <u>any</u> 2 vectors	M1		
	[Alternative cosine rule method] $ \overrightarrow{BC} = \sqrt{6}$	B1		
	Cosine rule used	M1		'Recognisable' form
	$45.3^\circ, 0.79(0), \frac{\pi}{3.97}$ (45.289378, 0.7904487)	A1	6	Do not accept supplement (134.7 etc)

(ii)	Use of $\frac{1}{2} \overrightarrow{AB} \overrightarrow{AC} \sin \theta$	M1		Accept $\left \frac{1}{2} \overrightarrow{AB} \times \overrightarrow{AC} \right $
	3.54 (3.5355) or $\frac{5\sqrt{2}}{2}$	A1	2	Accept from correct supp (134.7 etc)

5	(i) $\frac{dA}{dt}$ or kA^2 seen	M1		
	$\frac{dA}{dt} = kA^2$	A1	2	

(ii)	Separate variables + attempt to integrate	*M1		Accept if based on $\frac{dA}{dt} = kA^2$ or A^2
	$-\frac{1}{A} = kt + c$ or $-\frac{1}{kA} = t + c$ or $-\frac{1}{A} = t + c$	A1		
	Subst one of (0,0), (1,1000) or (2,2000) into eqn.	dep*M1		Equation must contain k and/or c
	Subst another of (0,0), (1,1000) or (2,2000) into eqn	dep*M1		This equation must contain k <u>and</u> c
	Substitute $A = 3000$ into eqn with k and c subst	dep*M1		
	$t = \frac{7}{3}$ ISW	A1	6	Accept 2.33, 2h 20 m

6	(i) Attempt to connect du and dx e.g. $\frac{du}{dx} = e^x$	M1		But not $du = dx$
	Use of $e^{2x} = (e^x)^2$ or $(u-1)^2$ s.o.i.	A1		
	Simplification to $\int \frac{u-1}{u} (du)$ WWW	A1	3	AG

(ii)	Change $\frac{u-1}{u}$ to $1 - \frac{1}{u}$ or use parts	M1		If parts, may be twice if $\int \ln x \, dx$ is involved
	$\int \frac{1}{u} du = \ln u$	A1		Seen anywhere in this part
	<u>Either</u> attempt to change limits <u>or</u> resubstitute	M1 (indep)		Expect new limits $e+1$ & 2
	Show as $e+1 - \ln(e+1) - \{2 \text{ or } (1+1)\} + \ln 2$	A1		
	WWW show final result as $e-1 - \ln\left(\frac{e+1}{2}\right)$	A1	5	AG

7	(i) Produce at least 2 of the 3 relevant eqns in λ and μ Solve the 2 eqns in λ & μ as far as $\lambda = \dots$ or $\mu = \dots$ 1 st solution: $\lambda = -2$ or $\mu = 3$ 2 nd solution: $\mu = 3$ or $\lambda = -2$ f.t. Substitute their λ and μ into 3 rd eqn and find 'a' Obtain $a = 2$ & clearly state that a cannot be 2	M1 M1 A1 A1√ M1 A1	e.g. $1 + 3\lambda = -8 + \mu$, $-2 + \lambda = 2 - 2\mu$ 6
	(ii) Subst their λ or μ (& poss a) into either line eqn Point of intersection is $-5\mathbf{i} - 4\mathbf{j}$ N.B. In this question, award marks irrespective of labelling of parts	M1 A1	2 Accept any format <u>No f.t. here</u>
8	(i) <u>Integration method</u> Attempt to change $\cos^2 6x$ into $f(\cos 12x)$ $\cos^2 6x = \frac{1}{2}(1 + \cos 12x)$ $\int = \frac{1}{2}x + \frac{1}{24}\sin 12x + c$ <u>Differentiation method</u> Differentiate RHS producing $\frac{1}{2} + \frac{1}{2}\cos 12x$ ---(E) Attempt to change $\cos 12x$ into $f(\cos 6x)$ Simplify (E) WWW to $\cos^2 6x$ + satis finish	M1 A1 A1 B1 M1 A1	with $\cos^2 6x$ as the subject of the formula AG Accept $\frac{1}{2}\left(x + \frac{1}{12}\sin 12x\right)$ Accept $\pm 2\cos^2 6x + \pm 1$ 3
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	(ii) Parts with $u = x$, $dv = \cos^2 6x$ $x\left(\frac{1}{2}x + \frac{1}{24}\sin 12x\right) - \int \left(\frac{1}{2}x + \frac{1}{24}\sin 12x\right)dx$ $\int \sin 12x dx = -\frac{1}{12}\cos 12x$ Correct use of limits to <u>whole</u> integral $\frac{\pi^2}{288} - \frac{\pi^2}{576} - \frac{1}{288} - \frac{1}{288}$ $\frac{\pi^2}{576} - \frac{1}{144}$ S.R. If final marks are A0 + A0, allow SR A1 for	*M1 A1 B1 dep*M1 A1 +A1	Correct expression only Clear indication somewhere in this part Accept () (-0) AE unsimp exp. Accept $12x24, \sin \pi$ here 6 Tolerate e.g. $\frac{2}{288}$ here 0.01/0.010/0.0101/0.0102/0.0101902

9	(i)	$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$	M1	Used, not just quoted
		$\frac{dx}{dt} = -4 \sin t$ or $\frac{dy}{dt} = 3 \cos t$	*B1	
		$\frac{dy}{dx} = -\frac{3 \cos t}{4 \sin t}$ or $\frac{3 \cos t}{-4 \sin t}$ ISW	dep*A1	3 Also $\frac{-3 \cos t}{4 \sin t}$ provided B0 not awarded
		SR: M1 for Cartesian eqn attempt + B1 for $\frac{d}{dx}(y^2) = 2y \frac{dy}{dx}$ + A1 as before (must be in terms of t)		
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	(ii)	$y - 3 \sin p = \left(\text{their } \frac{dy}{dx} \right) (x - 4 \cos p)$	M1	Accept p or t here
		or $y = \left(\text{their } \frac{dy}{dx} \right) x + c$ & subst cords to find c		Ditto
		$4y \sin p - 12 \sin^2 p = -3x \cos p + 12 \cos^2 p$	A1	Correct equation cleared of fractions
		or $c = \frac{12 \sin^2 p + 12 \cos^2 p}{4 \sin p}$		
		$3x \cos p + 4y \sin p = 12$ WWW	A1	3 AG Only p here. Mixture earlier \rightarrow A0
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	(iii)	Subst $x = 0$ and $y = 0$ separately in tangent eqn	M1	to find R & S
		Produce $\frac{3}{\sin p}$ and $\frac{4}{\cos p}$	A1	Accept $\frac{12}{4 \sin p}$ and/or $\frac{12}{3 \cos p}$
		Use $\Delta = \frac{1}{2} \left(\frac{3}{\sin p} \cdot \frac{4}{\cos p} \right) = \frac{12}{\sin 2p}$ WWW	A1	3 AG
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	(iv)	Least area = 12 $p = \frac{1}{4}\pi$ as final or only answer S.R. $45^\circ \rightarrow$ B1 ;	B1 B2	3 These B marks are independent. S.R. $[-12$ and e.g. $-\pi/4 \rightarrow$ B1]