Consecutive sums

Framing

Many numbers can be expressed as the sum of two or more consecutive integers.

For example,

$$15 = 7 + 8$$

and

$$10 = 1 + 2 + 3 + 4$$

Can you say which numbers can be expressed this way, which numbers cannot be expressed in this way, and prove your statements?