

Mark Scheme Sample Assessment Material

GCSE

GCSE in Mathematics Specification A Higher Tier

Paper 2: (Calculator)



General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Mark schemes will indicate within the table where, and which strands of QWC, are being assessed. The strands are as follows:

i) ensure that text is legible and that spelling, punctuation and grammar are accurate so that meaning is clear

Comprehension and meaning is clear by using correct notation and labelling conventions.

ii) select and use a form and style of writing appropriate to purpose and to complex subject matter

Reasoning, explanation or argument is correct and appropriately structured to convey mathematical reasoning.

iii) organise information clearly and coherently, using specialist vocabulary when appropriate.

The mathematical methods and processes used are coherently and clearly organised and the appropriate mathematical vocabulary used.

Guidance on the use of codes within this mark scheme

M1 - method mark

A1 - accuracy mark

B1 - working mark

C1 - communication mark

QWC - quality of written communication

oe - or equivalent

cao - correct answer only

ft - follow through

sc - special case

Specification A Paper 2 Higher Tier

		= 12 Roger 24 4 M1 $\frac{4}{5} \times 75$ Bethan 36 $\frac{4}{5} \times 75$			A1 Bethan 36	(Allow 3 marks for the correct numbers the wrong way round)	 l otal Tor Question: 4 marks	= 4.3 4 B2 for trial between 4.3 and 4.4 inclusive			NB trials where x has 1 d.p should be rounded or truncated to at least 2	18 at least 3.5F	or	.33	74	72	65	12	00	99	
	Working	12	$3 \times 12 = 36$	$2 \times 12 = 24$				f(x) = 0		4.10 48.42											
1MA0/2H	Question	-						2.													

1MA0/2H	1/2H				
One	Question	Working	Answer	Mark	Additional Guidance
e,		$25^2 - 7^2 = 576$ $\sqrt{576} = 24$	84 cm ²	4	M1 $25^2 - 7^2$ M1 $\sqrt{55^2 - 7^2}$
		$\frac{1}{2} \times 24 \times 7$			M1 (dep) $\frac{1}{2}$ ×'24'×7
					A1 cao ²
					Total for Question: 4 marks
4. H	(a)	(a) $18000 - 6475 = 11525$	£ 1152.50	4	M1 18000 — 6475 A1 11525
		100 - 100			M1 '11525' $\times \frac{20}{100}$
					A1 £1152.50
	(q)	12305 ' × 100 18000	12.8	2	M1 $\frac{2305}{18000} \times 100$
					A1 ft on '2305'
					Total for Question: 6 marks

															S
	Additional Guidance	B3 Fully correct	(BZ All entries correct, no key) (B1 correct corries inordered key or no key)	(b) correct entires arioraered, hely or no hely) OR	(B2 Three rows correct, key or no key)	(B1 Two rows correct, key or no key)		M1 finds median correctly for original data and adds 5	A1 cao OR	MT Redoes table (ft) with each value increased by 5 and attempts to	find median	A1 cao	C1 All the values have increased by 5 minutes so when you subtract the	5 minutes will cancel out.	Total for Question: 6 marks
	Mark	3						2					—		
	Answer	Correct stem	and lear					27 minutes					The same +	reason	
	Working	0:8	1: 0235/8	2. 0122233 3: 1345	4: 456		Key 416 means 46 minutes	Old median = 22	New median = 22 + 5						
1MA0/2H	Question	(a)						(q)					(c)		
1MA	On	5.													

1MA0/2H)/2H				
One	Question	Working	Answer	Mark	Additional Guidance
9.	(a)	1 gallon = 4.54 litres,	No	2	Response may convert into gallons, litres, or cm ³
Ⅱ		200 gallons = 908 litres			
OWC		$= 908000 \text{ cm}^3$			Calculations may be performed in different orders
≡ =		Vol of tank			
		$60^2 \times x \pi \times 180 =$			M1 Using formulae to find volume of tank
		2035752.04cm³			B1 Converts between litres and cubic centimetres
					M1 reads off graph for 11, 21, 41, 51 or 10 litres within tolerance (4.4 —
		908000< 1017876.02			4.6)
		G			AT Answer in cm ² , litres or gallons
		N C			C1 Decision and reason OWC: Decision should be stated: with
		Vol of tank			appropriate supporting statement
		$60^2 \times \pi \times 180 = 2035752.04$ cm ³			
		Half vol of tank			
		= 1017876.02 cm ³ = 1017-876_litres			
		000000000000000000000000000000000000000			
		1017.876 ÷ 4.54 = 224 gallons			
		224 > 200			
	(q)	"908000" cm ³ × 0.85 g/cm ³	771.8	3	M1 "908000" × 0.85
		= //1800 g			M1(dep) //1800÷1000 A1 770 — 772
			-,		Total for Question: 8 marks
7.		10 + 45 + 150 + 245 + 225 + 55	6.08 hours	4	M1 for mid interval values
		120			M1 for multiplying frequencies by mid-interval values
					M1 for adding (freq × mid-interval values) ÷ 120 A1 cao
	-1				Total for Question: 4 marks

			2 2 2 1 1
	Additional Guidance	C1 a clear and coherent explanation	M1 multiply through by 6 and cancels fractions M1 (dep)expand 3(x - 10) M1 (dep)collect terms on each side correctly A1 cao M1 collects terms over 6 M1 (dep) expand 3(x - 10) M1 (dep) multiply through by 6 and collect terms A1 cao
	Mark		4
	Answer	Clear and coherent explanation	£140
	Working	Fred pays $\frac{x}{3}$ and Jim pays $\frac{x-10}{2}$ Malcolm gets £170 for Fred and Jim, so Malcolm gets $\frac{x}{3} + \frac{x-10}{2} = 170$	Fred has $\frac{2x}{3}$ left, so solving for x using $\frac{x}{3} + \frac{x - 10}{2} = 170$ $2x + 3(x - 10) = 170 \times 6$ $5x = 1050$ OR $\frac{x}{3} + \frac{x - 10}{2} = \frac{2x + 3(x - 10)}{6}$ $\frac{x}{3} + \frac{x - 10}{2} = \frac{2x + 3(x - 10)}{6}$ $\frac{5x - 30}{5} = 170$ $\frac{5x - 30}{5} = 170$ $\frac{5x - 30}{5} = 170$
/2H	Question	(a)	(q)
1MA0/2H	One	ώ	

1MA0/2H				
Question	Working	Answer	Mark	Additional Guidance
9.	Makes a comparison of the	Correct	4	B1, B1, B1 for any 4 of the following done correctly
QWC	shape of the distribution by	comparisons		
≡ ,	drawing			Plots frequency polygon or produces table
	Makes a comparison of the			compares modes
Æ	modal classes(31-40, 11-20)			compares medians
	Makes a comparison of the			compares total sales
	class intervals that contain			
	the medians.(31-40, 21-30)			C1 for comments on shape of the distributions
	Works out an estimate of the			QWC: Decisions should be stated, and all comments should be clear
	total sales of each shop(2635,			and follow through from any working or diagrams
	3530)			
				Total for Ouestion: 4 marks

1MA0/2H	H				
Question	on	Working	Answer	Mark	Additional Guidance
10.	(a)	10. (a) $x^{3/2} \times x^{1/2}$	x ²	3	B1 $x^{3/2}$ seen B1 $x^{2/4}$ oe seen A1 cao
	(g)	(b) $x^2 - 1x + 2x - 2 = 18$ $x^2 + x - 20 = 0$ (x + 5)(x - 4)	4, -5	4	M1 Correct expansion B1 $x^2 + x - 20 = 0$ B1 $(x + 5)(x - 4)$ A1 cao
	(C)	(c) $x^2 + x - 6 = 0$ (x + 3)(x - 2) x = -3, x = 2	x = -3, y = 8 x = 2, y = 3	ro.	M1 Sets equations equal and rearranges B1 $x^2 + x - 6 = 0$ oe B1 $(x - 3)(x + 2)$ A2 Two correct pair of solutions A1 correct set of x values
					Total for Question: 12 marks

1MA0/2H	/2H				
Question	tion	Working	Answer	Mark	Additional Guidance
<u></u>	(a)		28	-	B1 27 – 29
	(Q)	68 – 42	26	2	M1 68 — 42
					A1 $26 - 30$ (need $\frac{1}{2}$ sq tolerance on each)
毘	(C)	15% of 80 = 12	Yes, with correct conclusion	2	M1 looks up 68 or 40 min on cumulative frequency A1 correct conclusion
		.1			Total for Question: 5 marks
12. QWC		$\sin 68^{\circ} = \frac{AC}{8.5}$	Reason	4	$M1 \sin 68^{\circ} = \frac{AC}{8.5}$
≡ ;		$AC = 8.5 \times \sin 68^{\circ} = 7.881$ 7.881 + 1 < 9	by calculation		M1 AC = 8.5 × sin 68° A1 7.88(1
빝					C1 8.88(1 + conclusion QWC: Decision should be stated, supported by clearly laid out working
					Note $\frac{AC}{\sin 68} = \frac{8.5}{\sin 90}$ does not get marks until in the form
					$AC = \frac{8.5}{\sin 90} \times \sin 68$
					Total for Question: 4 marks

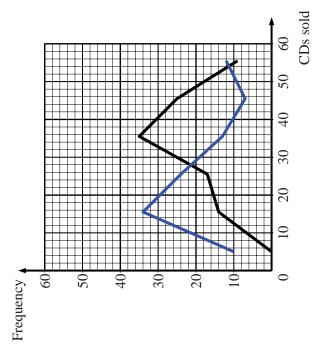
1MA0/2H				
Question	Working	Answer	Mark	Additional Guidance
13.	$T = k\sqrt{A}$; 40 = $k\sqrt{100}$	31.0	4	M1 $T = k\sqrt{A}$
	k = 4			M1 $40 = k\sqrt{100}$
	$T = 4\sqrt{A}$ $T = 4\sqrt{60}$			A1 $T=4\sqrt{A}$
				A1 for 30.98 or 31(.0)
				OR
				M2 for $\frac{T}{40} = \sqrt{\frac{60}{100}}$ oe
				M1 for $T=40 imes \sqrt{\frac{60}{100}}$ oe
				A1 for 30.98 or 31.0
				Total for Question: 4 marks

1MA0/2H Question	/2H tion	Working	Answer	Mark	Additional Guidance
14.	(q)	Eliminate y to get $2x + 3 = 4x + 2$, $x = 0.5$ $y = 4$	y = -0.5x + 4.25	Z.	M1 eliminate y M1 substitute the found value of x in one equation A1 both answers M1 an equation of the form $y = mx + c$ with either c correct or m correct or the correct gradient stated
		OR			OR
		y = 2x + 3 and $y = 4x + 2$ drawn correctly on graph paper Perpendicular drawn correctly through (0.5, 4) Intercept found Gradient found			B1 $y=2x+3$ drawn B1 $y=4x+2$ drawn M1 draws perpendicular though point of intersection M1 an equation of the form $y=mx+c$ with either c correct or m correct or the correct gradient stated A1 cao
					Total for Question: 5 marks
15.	(a)	(a) UB 8.35 × 3.65 = 30.4775	30.4775	2	M1 sight of 8.35 or 3.65 A1 30.4775
	(q)	LB 8.25 × 3.55 = 29.2875	30	2	M1 8.25 × 3.55 A1 30 (dep on 8.25 X 3.55 seen)
					Total for Question: 4 marks

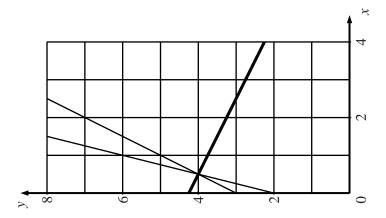
1MA0/2H	/2H				
Question	tion	Working	Answer	Mark	Additional Guidance
16.	(a)	Vol = $x \times (x - 2) \times 2 = 51$ Vol = $2x^2 - 4x - 51 = 0$	Derives given answer and condition	4	M1 Vol = $x \times (x - 2) \times 2$ M1 expands bracket correctly A1 (E1) sets equal to 51 B1 $x > 2$ as the lengths of the cuboid have to be positive.
	(q)	$x = \frac{-(-4)\pm\sqrt{(-4)^2 - 4\times2\times(-5)}}{2\times2}$ $x = \frac{4\pm\sqrt{424}}{4}$	6.15, -4.15 both to 3sf	м	M1 correct substitution (allow sign errors in a, b and c) into quadratic formula $ M1_{x} = \frac{4 \pm \sqrt{424}}{4} $ A1 6.14(7, -4.14(7)
	- 1				Total for Question: 7 marks
71.		Angle BAC = $180^{\circ} - 47^{\circ} - 58^{\circ}$ = 75° AC $\frac{AC}{\sin 47} = \frac{220}{\sin 75} (= \frac{AB}{\sin 58})$ $220 \sin 47$ AC = $\sin 75$ = 166.57 $\frac{1}{2} \times 220 \times 166.57 \times \sin 58$ Area= $\frac{1}{2} \times 220 \times 166.57 \times \sin 58$ = 15538	15500 m²	ъ	B1 for 75° $\frac{AC}{AC} = \frac{220}{\sin 75} (= \frac{AB}{\sin 58})$ M1 $AC = \frac{\sin 75}{\sin 75}$ M1 $\frac{1}{2} \times 220 \times "166.57" \times \sin 58$ A1 15500 m ²
					Total for Question: 5 marks

Mark Additional Guidance	360 720		B1 $(180 - 72) \div 2 = 54^{\circ}$	M1 for finding equal sides of isosceles triangle; $x = \frac{x}{\sin 54} = \frac{10}{\sin 72}$		M1 for finding area of isosceles triangle = $\frac{1}{2}x^2 \sin 72$	7	A1 for $34.40954801(ft)$ B1 for area of pentagon = $5 \times (ft) = 172.0477401(ft)$	B1 for area of dodecahedron = $12 \times (ft) = 2064.572881 \text{ cm}^2$							OR	B1 for $\frac{360}{2} = 72^{\circ}$	S	M1 for using right-angled trigonometry; h = 5 tan54°	A1 for 6.8819	M1 for finding area of isosceles triangle = $\frac{1}{2} \times 10 \times h$	A1 for 34.40954801(ft)	B1 for area of pentagon = $5 \times (ft) = 172.0477401(ft)$	B1 for area of dodecahedron = $12 \times (ft) = 2064.572881$ cm ²	
Answer	2065 cm ²																								
Working	Pentagon = 5 equal isos	triangles	$\frac{360}{1} = 72^{\circ}$	5 Base angles = $(180 - 72) \div 2$	= 54°	for finding equal sides of isosceles triangle;	$\frac{x}{x} = \frac{10}{x} = \frac{10}{x}$	sin 54 sin 72 8.506508084	area of isosceles triangle =	$\frac{1}{2}x^2 \sin 72$	= 34.40954801	area of pentagon	= 3 × 34.40934801 = 172 0477401	area of dodecahedron	104//40:2/1 × 21 -	OR	20 220 +45ir 25io	trigonometry; h = 5tan54°	= 6.8819	Area of isosceles triangle =	$\frac{1}{2} \times 10 \times h$	= 34.40954801	area of pentagon	= 5 × 34.40954801 = 172 0477401	
1MA0/2H Question	18.																								

	Additional Guidance			l isos triangle:							1 95.10565163)			
	Additio	OR	B1 for 108° (and base angles 36°)	B1 for base angles 72° (and 36°) M1 for finding equal sides of 3rd isos triangle:	$\frac{x}{\sin 72} = \frac{10}{\sin 36}$	A1 for x = 16.18033989	M1 for area = $\frac{1}{2}x^2 \sin 36$	7	M1 for area = $2(\frac{1}{2}10^2 \sin 108)$	1	A1 for one of (76.94208845 and 95.10565163)	B1 for area of dodecahedron	A1 for 2065 cm ² (oe)	
	Mark	6												
	Answer	2065 cm ²												
	Working	OR	Pentagon split into 3 isos	triangles, where 2 are equal. Area of 2 isos triangles	$= 2(\frac{1}{2}10^2 \sin 108)$	= 95.10565163	$\frac{1}{\sin 72} = \frac{1}{\sin 36}$	x = 16.18033989	$x^2 = 261.803399$	Area of 3rd isos triangle	$=\frac{1}{2}$ (261.803399)sin36	2	= 76.94208845	
/2H	Question	P.C.												
1MA0/2H	Que	18. (Cont)												



6



14.



October 2009

For more information on Edexcel and BTEC qualifications please visit our website: www.edexcel.org.uk

Edexcel Limited. Registered in England and Wales No. 4496750 Registered Office: One90 High Holborn, London WC1V 7BH. VAT Reg No 780 0898 07