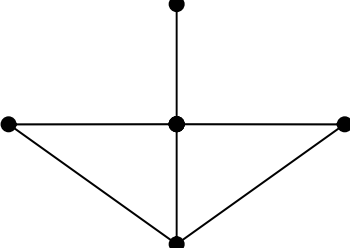
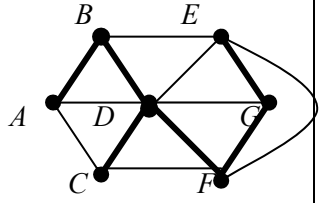


4736 Decision Mathematics 1

1	(i)	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	M1	<i>A</i> , <i>B</i> and <i>C</i> correct for first pass	
		614	416	1	198 (<i>A</i> =198)	A1	<i>D</i> = 198 on first pass	
		198	891	2	693 (<i>A</i> =693)	M1	sca at second <u>and</u> third passes	
		693	396	3	297	A1	Second and third passes correct	
	(ii)	0				B1	0	[1]
	(iii)	To make the algorithm terminate				B1	So that it does not get stuck in a loop	[1]
Total = 6								

2	(i)	eg 	M1	Graph need not be simple or planar	[2]
			A1	A graph with five vertices and at least three correct vertex orders A graph with five vertices of orders 1, 2, 2, 3, 4	
	(ii)	Semi-Eulerian It has <u>exactly</u> two odd nodes	M1	Unless their graph was not connected, in which case the answer is 'neither'	[2]
			A1	(Unless their graph was not connected, in which case follow this through)	
	(iii)	A tree with five vertices would only have four arcs, but this graph has six <u>Or</u> A tree must have at least two vertices of order 1	B2	Give B1 for an incomplete reason, eg 'too many arcs' or 'it has a cycle'	[2]
Total = 6					

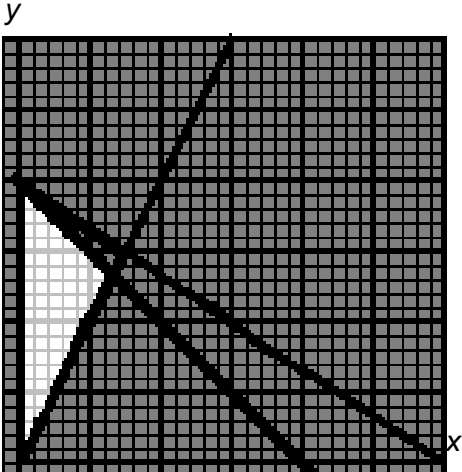
ANSWERED ON INSERT

3	(i)	<i>AB</i> = 9		M1	Not selecting <i>CF</i> (working seen on list)	[5]
		<i>DF</i> = 14		A1	Selecting correct arcs (working seen on list)	
		<i>BD</i> = 16		M1	A spanning tree drawn	
		<i>CD</i> = 18		A1	Correct (minimum) spanning tree drawn	
		<i>FG</i> = 20	Total weight = 100	B1	100 cao	
		<i>CF</i> = 22				
		<i>EG</i> = 23				
		<i>EF</i> = 26				
		<i>AC</i> = 27				
		<i>DE</i> = 28				
		<i>AD</i> = 29				
		<i>DG</i> = 34				
		<i>BE</i> = 37				

	(ii)	Delete EG from spanning tree $100 - 23 = 77$ Two shortest arcs from E are EG and EF $77 + 23 + 26 = 126$ Lower bound = 126	B1	Follow through from part (i) if possible Weight of MST on reduced network																													
			M1	Adding two shortest arcs to MST																													
			A1	126 cao	[3]																												
	(iii)	$A - B - D - F - G - E$ – stall Misses out vertex C	M1	$A - B - D - F - G - E$																													
			A1	<u>Cannot continue</u> because B , D and F have already been visited	[2]																												
	(iv)	$B - A - C - D - F - G - E - B$ Upper bound = 148	M1	Tour starts $B - A - C - D - F -$																													
			A1	Correct tour, starting and ending at B																													
			B1	148 cao	[3]																												
	(v)	<div><div>B<table><tr><td>2</td><td>9</td></tr><tr><td>9</td><td></td></tr></table></div><div>E<table><tr><td>6</td><td>46</td></tr><tr><td>46</td><td></td></tr></table></div></div> <div><div>A<table><tr><td>1</td><td>0</td></tr><tr><td></td><td></td></tr></table></div><div>D<table><tr><td>3</td><td>25</td></tr><tr><td>29</td><td>25</td></tr></table></div><div>G<table><tr><td>7</td><td>56</td></tr><tr><td></td><td>56</td></tr></table></div></div> <div><div>C<table><tr><td>4</td><td>27</td></tr><tr><td>27</td><td></td></tr></table></div><div>F<table><tr><td>5</td><td>39</td></tr><tr><td>39</td><td></td></tr></table></div></div> <p>Weight = 56 Route = $A - B - D - G$</p>	2	9	9		6	46	46		1	0			3	25	29	25	7	56		56	4	27	27		5	39	39		M1	(Accept correct working starting from G , if seen) At least three sets of temporary labels correct, with no extras	
2	9																																
9																																	
6	46																																
46																																	
1	0																																
3	25																																
29	25																																
7	56																																
	56																																
4	27																																
27																																	
5	39																																
39																																	
			A1	Temporary labels all correct, with no extras																													
			B1	Permanent labels correct																													
			B1	Order of labelling (correct or follow through their permanent labels)	[4]																												
			B1	56 cao																													
			B1	$A - B - D - G$ cao	[2]																												
	(vi)	A , B , C and G are odd $AB = 9$ $AC = 27$ $AG = 56$ $CG = \underline{42}$ $BG = \underline{47}$ $BC = \underline{34}$ 51 74 90 Repeat AB and CG ($C - F - G$) = 51 Weight = $300 + 51 = 351$	B1	Identifying or using A , B , C , G (seen)																													
			M1	At least one correct pairing seen or total seen (not just six weights)																													
			A1	All three totals correct, or explanation of how it is known that other pairings are too long																													
			B1	351 cao	[4]																												
Total =					23																												

ANSWERED ON INSERT

4	(i)	8	B1	cao	[1]
	(ii)	1 comparison and 1 swap	B1	1 and 1	[1]
	(iii)	76 65 21 13 88 62 67 28 34	B1	Correct list (complete)	[2]
		2 comparisons and 1 swap	B1	2 and 1	
(iv)		<div style="display: flex; justify-content: space-between;"> 76 65 21 13 88 62 67 28 34 C S </div> <div style="display: flex; justify-content: space-between;"> 88 76 65 21 13 62 67 28 34 1 0 </div> <div style="display: flex; justify-content: space-between;"> 88 76 65 62 21 13 67 28 34 4 4 </div> <div style="display: flex; justify-content: space-between;"> 88 76 65 62 21 13 67 28 34 3 2 </div> <div style="display: flex; justify-content: space-between;"> 88 76 67 65 62 21 13 28 34 5 4 </div> <div style="display: flex; justify-content: space-between;"> 88 76 67 65 62 28 21 13 34 3 2 </div> <div style="display: flex; justify-content: space-between;"> 88 76 67 65 62 34 28 21 13 4 3 </div>	M1	Underlined values correct in 3 rd and 4 th passes, values not underlined may be left blank	[3]
			M1	Similarly for 5 th and 6 th passes, follow through slips in previous passes	
			A1	Similarly for 7 th and 8 th passes, but cao (Dependent on both M marks)	
			M1	Reasonable attempt at Comp and Swap	
			A1	1 4 3 5 3 4 cao in figures	
			A1	0 4 2 4 2 3 cao in figures	

(vi)	 <p>Vertices of feasible region are $(0, 0)$, $(0, 4)$ and $(1\frac{1}{3}, 2\frac{2}{3})$</p> <p>$x = 0, y = 4 \Rightarrow P = 16$ $x = 1, y = 3 \Rightarrow P = 17$ $(x = 1\frac{1}{3}, y = 2\frac{2}{3} \Rightarrow P = 17\frac{1}{3})$</p> <p>Make 1 batch of plain cookies and 3 batches of chocolate chip cookies</p>	<p>M1 At least two of the lines $y = 2x$, $x + y = 4$ and $4x + 6y = 24$ drawn correctly</p> <p>A1 All three lines drawn correctly and graph has both scales and labels</p> <p>A1 Feasible region identified and correct</p> <p><u>Follow through</u> their feasible region if possible</p> <p>M1 At least two correct</p> <p>A1 <u>All</u> (three) correct (1 dp or better)</p> <p>M1 Or a line of constant profit <u>drawn</u> (or gradient discussed) and used correctly on <u>integer-valued</u> coordinates</p> <p>A1 For (1, 3) or 17 chosen (cao)</p> <p>B1 Interpretation: 1 batch of plain, 3 batches of chocolate chip (cao)</p>	<p>[3]</p> <p>[2]</p> <p>[3]</p>
Total =			
25			