

4722 Core Mathematics 2

1 (i) $\int (x^3 + 8x - 5) dx = \frac{1}{4}x^4 + 4x^2 - 5x + c$	M1 Attempt integration – increase in power for at least 2 terms
	A1 Obtain at least 2 correct terms
	A1 3 Obtain $\frac{1}{4}x^4 + 4x^2 - 5x + c$ (and no integral sign or dx)
(ii) $\int 12x^{\frac{1}{2}} dx = 8x^{\frac{3}{2}} + c$	B1 State or imply $\sqrt{x} = x^{\frac{1}{2}}$
	M1 Obtain $kx^{\frac{3}{2}}$
	A1 3 Obtain $8x^{\frac{3}{2}} + c$ (and no integral sign or dx) (only penalise lack of + c, or integral sign or dx once)
6	
2 (i) $140^\circ = 140 \times \frac{\pi}{180}$ $= \frac{7}{9}\pi$	M1 Attempt to convert 140° to radians
	A1 2 Obtain $\frac{7}{9}\pi$, or exact equiv
(ii) arc $AB = 7 \times \frac{7}{9}\pi$ $= 17.1$ chord $AB = 2 \times 7 \sin \frac{7}{18}\pi = 13.2$ hence perimeter = 30.3 cm	M1 Attempt arc length using $r\theta$ or equiv method
	A1✓ Obtain 17.1, $\frac{49}{9}\pi$ or unsimplified equiv
	M1 Attempt chord using trig. or cosine or sine rules
	A1 4 Obtain 30.3, or answer that rounds to this
6	
3 (i) $u_1 = 23^{1/3}$ $u_2 = 22^{2/3}$, $u_3 = 22$	B1 State $u_1 = 23^{1/3}$
	B1 2 State $u_2 = 22^{2/3}$ and $u_3 = 22$
(ii) $24 - \frac{2k}{3} = 0$ $k = 36$	M1 Equate u_k to 0
	A1 2 Obtain 36
(iii) $S_{20} = \frac{20}{2} \left(2 \times 23 \frac{1}{3} + 19 \times \frac{-2}{3} \right)$ $= 340$	M1 Attempt sum of AP with $n = 20$
	A1 Correct unsimplified S_{20}
	A1 3 Obtain 340
7	
4 $\int_{-2}^2 (x^4 + 3) dx = \left[\frac{1}{5}x^5 + 3x \right]_{-2}^2$	M1 Attempt integration – increase of power for at least 1 term
	A1 Obtain correct $\frac{1}{5}x^5 + 3x$
	M1 Use limits (any two of -2, 0, 2), correct order/subtraction
	A1 Obtain $24 \frac{4}{5}$
	B1 State or imply correct area of rectangle
	M1 Attempt correct method for shaded area
	A1 7 Obtain $51 \frac{1}{5}$ aef such as 51.2, $\frac{256}{5}$
OR	
Area = $19 - (x^4 + 3)$ $= 16 - x^4$	M1 Attempt subtraction, either order
	A1 Obtain $16 - x^4$ (not from $x^4 + 3 = 19$)
$\int_{-2}^2 (16 - x^4) dx = \left[16x - \frac{1}{5}x^5 \right]_{-2}^2$	M1 Attempt integration
	A1 Obtain $\pm \left(16x - \frac{1}{5}x^5 \right)$

$$= (32 - \frac{32}{5}) - (-32 - \frac{-32}{5})$$

$$= 51\frac{1}{5}$$

- M1 Use limits – correct order / subtraction
 A1 Obtain $\pm 51\frac{1}{5}$
 A1 Obtain $51\frac{1}{5}$ only, no wrong working

7

5 (i) $\frac{TA}{\sin 107} = \frac{50}{\sin 3}$
 $TA = 914 \text{ m}$

- M1 Attempt use of correct sine rule to find TA , or equiv
 A1 2 Obtain 914, or better

(ii) $TC = \sqrt{914^2 + 150^2 - 2 \times 914 \times 150 \times \cos 70}$
 $= 874 \text{ m}$

- M1 Attempt use of correct cosine rule, or equiv, to find TC
 A1✓ Correct unsimplified expression for TC , following their (i)
 A1 3 Obtain 874, or better

(iii) dist from $A = 914 \times \cos 70 = 313 \text{ m}$
 beyond C , hence 874 m is shortest dist
OR
 perp dist = $914 \times \sin 70 = 859 \text{ m}$

- M1 Attempt to locate point of closest approach
 A1 2 Convincing argument that the point is beyond C ,
 or obtain 859, or better
SR B1 for 874 stated with no method shown

7

6 (i) $S_{\infty} = \frac{20}{1-0.9}$
 $= 200$

- M1 Attempt use of $S_{\infty} = \frac{a}{1-r}$
 A1 2 Obtain 200

(ii) $S_{30} = \frac{20(1-0.9^{30})}{1-0.9}$
 $= 192$

- M1 Attempt use of correct sum formula for a GP, with $n = 30$
 A1 2 Obtain 192, or better

(iii) $20 \times 0.9^{p-1} < 0.4$
 $0.9^{p-1} < 0.02$
 $(p-1)\log 0.9 < \log 0.02$
 $p-1 > \frac{\log 0.02}{\log 0.9}$
 $p > 38.1$
 hence $p = 39$

- B1 Correct $20 \times 0.9^{p-1}$ seen or implied
 M1 Link to 0.4, rearrange to $0.9^k = c$ (or $>$, $<$), introduce
 logarithms, and drop power, or equiv correct method
 M1 Correct method for solving their (in)equation
 A1 4 State 39 (not inequality), no wrong working seen

8

7 (i) $6k^2a^2 = 24$
 $k^2a^2 = 4$
 $ak = 2$ **A.G.**

- M1* Obtain at least two of 6 , k^2 , a^2
 M1dep* Equate $6k^ma^n$ to 24
 A1 3 Show $ak = 2$ convincingly – no errors allowed

(ii) $4k^3a = 128$
 $4k^3(\frac{2}{k}) = 128$
 $k^2 = 16$
 $k = 4$, $a = \frac{1}{2}$

- B1 State or imply coeff of x is $4k^3a$
 M1 Equate to 128 and attempt to eliminate a or k
 A1 Obtain $k = 4$
 A1 4 Obtain $a = \frac{1}{2}$
SR B1 for $k = \pm 4$, $a = \pm \frac{1}{2}$

(iii) $4 \times 4 \times (\frac{1}{2})^3 = 2$

- M1 Attempt $4 \times k \times a^3$, following their a and k (allow if still in
 terms of a , k)
 A1 2 Obtain 2 (allow $2x^3$)

9

8 (a)(i) $\log_a xy = p + q$

B1 1 State $p + q$ cwo

(ii) $\log_a \left(\frac{a^2 x^3}{y} \right) = 2 + 3p - q$

M1 Use $\log a^b = b \log a$ correctly at least onceM1 Use $\log \frac{a}{b} = \log a - \log b$ correctlyA1 3 Obtain $2 + 3p - q$

(b)(i) $\log_{10} \frac{x^2 - 10}{x}$

B1 1 State $\log_{10} \frac{x^2 - 10}{x}$ (with or without base 10)

(ii) $\log_{10} \frac{x^2 - 10}{x} = \log_{10} 9$

B1 State or imply that $2 \log_{10} 3 = \log_{10} 3^2$

$\frac{x^2 - 10}{x} = 9$

M1 Attempt correct method to remove logs

$x^2 - 9x - 10 = 0$

A1 Obtain correct $x^2 - 9x - 10 = 0$ aef, no fractions

$(x - 10)(x + 1) = 0$

M1 Attempt to solve three term quadratic

$x = 10$

A1 5 Obtain $x = 10$ only**10**

9 (i) $f(1) = 1 - 1 - 3 + 3 = 0$ A.G.

B1 Confirm $f(1) = 0$, or division with no remainder shown, or matching coeffs with $R = 0$

$f(x) = (x - 1)(x^2 - 3)$

M1 Attempt complete division by $(x - 1)$, or equivA1 Obtain $x^2 + k$ A1 Obtain completely correct quotient (allow $x^2 + 0x - 3$)

$x^2 = 3$

M1 Attempt to solve $x^2 = 3$

$x = \pm \sqrt{3}$

A1 6 Obtain $x = \pm \sqrt{3}$ only

(ii) $\tan x = 1, \sqrt{3}, -\sqrt{3}$

B1✓ State or imply $\tan x = 1$ or $\tan x =$ at least one of their roots from (i)

$\tan x = \sqrt{3} \Rightarrow x = \pi/3, 4\pi/3$

M1 Attempt to solve $\tan x = k$ at least once

$\tan x = -\sqrt{3} \Rightarrow x = 2\pi/3, 5\pi/3$

A1 Obtain at least 2 of $\pi/3, 2\pi/3, 4\pi/3, 5\pi/3$ (allow degs/decimals)

$\tan x = 1 \Rightarrow x = \pi/4, 5\pi/4$

A1 Obtain all 4 of $\pi/3, 2\pi/3, 4\pi/3, 5\pi/3$ (exact radians only)B1 Obtain $\pi/4$ (allow degs / decimals)B1 6 Obtain $5\pi/4$ (exact radians only)

SR answer only is B1 per root, max of B4 if degs / decimals

12