- **11** a)  $x \le 18$
- **b)**  $x \le 5$
- c) x < 4
- **d)** x > 10
- **e)**  $x \le 14\frac{1}{2}$
- $\mathbf{f)} \quad x \ge -2$
- g)  $x > 1\frac{7}{10}$
- **12** a)  $\frac{1}{4}x + 8 + \frac{1}{2}x + 1 + x = 30$

which simplifies to  $\frac{7x}{4} = 21$ 

- **b)** x = 12; lengths are 7 cm, 11 cm and 12 cm.
- 13 a) (i) £(100-x) (ii)  $£_3^2(100-x)$ 

  - (iii) £[ $x + \frac{2}{3}(100 x)$ ] or £ $\left(\frac{x + 200}{3}\right)$
  - **b)**  $\frac{x + 200}{3} \le 80$
  - c)  $x \le 40$ ; the most she could have paid for the jeans is £40.

# 5 Percentage increase and decrease

# Exercise 5.1 (page 43)

- 1 a) 1.06
- **b)** 1.09
- c) 1·175
- **d)** 1.0125
- e) 1.04
- f) 1.18
- g) 1·125
- h) 1.056
- 2 a) 0.94
- **b)** 0.91
- c) 0.825
- **d)** 0.9875
- e) 0.96
- **f)** 0.82
- **g)** 0.875
- h) 0.944
- **3** a) £420
- **b)** £480
- c) £720
- a) £5040
- c) £8592
- **b)** £5904
- 5 a) £192
- c) £60
- **b)** £140

**b)** £630.80

- **6 a)** £699·20
- c) £281·20 7 £168
- 8 1107
- 9 68 000 m<sup>2</sup>
- 10 105·3 cm
- 11 £4.28
- **12** £789.60
- **13** £19·20
- 14 £810.75
- 15 £4·12
- 16 £622·50
- **17** £141
- **18** 79·2p (or 79p)

### Exercise 5.2 (page 45)

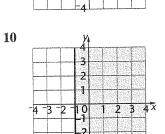
- 1 £53.75
- 2 75 tonnes
- 3 40

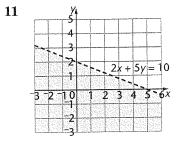
- 4 £50
- 5 £75.05
- 6 56500
- **7** £12500
- 8 £14200
- 9 1540
- **10** £8800
- **11** £27 000
- 12 2.48 million
- **13** £24000
- **14** £11 000
- **15** £480
- **16 a)** £87.87
- **b)** £14.99
- **17 a)** 79p
- **b)** £1.24

# 6 Linear inequalities

### Exercise 6.1 (page 50)

- 1 x > 2
- 2 y < -2
- 3 y < 2x
- **4**  $y \ge x + 2$
- $5 \ 3x + 4y > 12$
- 6  $y \le 2x 4$
- 7 y < 2x + 1
- **8**  $2x + 3y \le 12$





**STAGE** 

21 a)

	AB (£)	BB (£)
(i)	£5237·50	£5225
(ii)	£5460·09	£5460·13
(iii)	£5692·15	£5705-83

- b) She might only want to save for one year or to change to another bank after one year.
- **22** 5 years

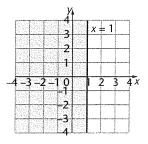
### Exercise 8.2 (page 72)

- 1 a)
- c)
- d)
- e)
- f)
- g)
- h)
- b)
- c)
- d)
- e)
- g)
- h)
- 3 a) £696·73
- **b)** £7982·44
- £3124·13 c)
- £39912·49
- 4 a) £168.79 c) £874·01
- £41.99 d) £4398·49
- 5 £19·26
- 6 £96
- £18575
- 8 £14.87
- **9** 2340 rabbits

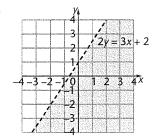
# Revision exercise B1 (page 74)

- 1 £17680
- 2 £55·25
- **3** 79p
- 4 £520
- **5** a)  $y \le 3$
- **b)** 3x + 4y > 12

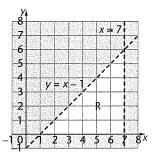
6 a)



b)

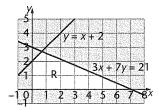


# 7



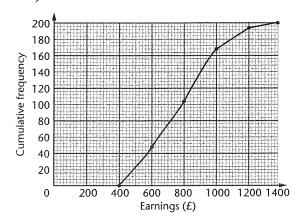
The region required is labelled R.

### 8



The region required is labelled R.

#### 9 a)

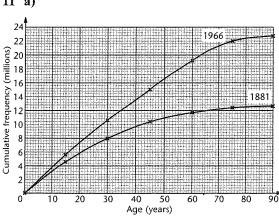


- **b)** (i) Median is £780
  - (ii) Interquartile range is £940 - £600 = £340
  - (iii) Number of employees earning more than £900 is 60

- b) (i) Median is 46
  - Interquartile range is 58 32 = 26(ii)
  - (iii) 170 118 = 52
  - (iv) 60% = 102

102 candidates got more than 42%

11 a)



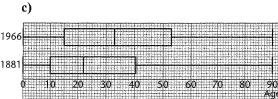
b) 1881: median 22, lower quartile 10, upper quartile 40.5

1966: median 33, lower quartile 15,

upper quartile 53

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8

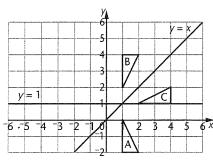


- d) The average age was much higher in 1966 and the ages were more spread out.
- 12 £540, £777.60
- **13** 1679 bacteria
- 14 a) £6083·26
- **b)** 9 years
- **15** 331 people
- 16 576 accidents

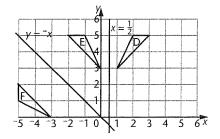
### Transformations

### Exercise 9.1 (page 78)

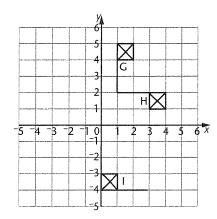
1 a), b)



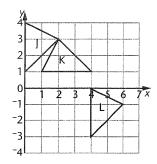
2 a), b)



3 a), b)

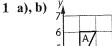


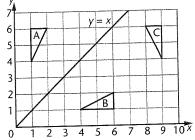
4 a), b)



- 5 Triangles C, F, G are reflections; triangles B,
  - D, E are rotations.
- a) Rotation through 90° clockwise about (2, 4)
  - **b)** Reflection in the line x = -1
  - c) Reflection in the line  $y = \bar{x}$
  - d) Rotation through 180° about (4, 2)
  - Rotation through 90° clockwise about (3, -1)
  - Reflection in the line  $y = -2\frac{1}{2}$

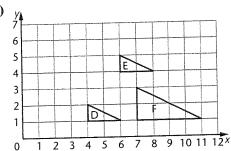
# Revision exercise C1 (page 121)





c) Reflection in the line x = 5

2 a), b)

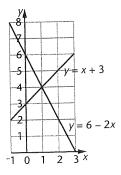


c) Enlargement, scale factor 2, centre (1, 1)

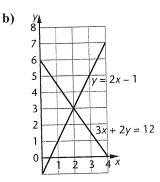
3 B 7 6 5 3 2 6 7 8 9 10 11 X 5 3

- 4 a) Translation through  $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ 
  - **b)** Reflection in the line x = -4.5
  - c) Rotation though 90° clockwise about (0, 2)
  - d) Rotation through 90° anticlockwise about (-3, -1)
  - e) Enlargement, scale factor  $\frac{1}{2}$ , centre (0, 2)
  - f) Reflection in the line  $y = \bar{x}$
  - g) Enlargement, scale factor -2, centre (0, 0)

5 a)



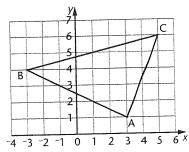
$$x = 1, y = 4$$



$$x = 2, y = 3$$

- **6 a)** x = 7, y = 8
- **b)** x = 2, y = 3
- c) x = 3, y = 1
- **d)** x = 5, y = 2
- e) x = -1, y = 2x = 1, y = 2
- **f)** x = -2, y = 3**h)**  $x = \frac{1}{2}, y = 2\frac{1}{2}$
- $x = \frac{1}{2}, y = -1$ i)
  - **b)** 0.000538 79000
- 635 100 c)
- **d)** 0.0704
- 8500000 e)
- **f)** 0.0050
- 86700000 g)
- h) 0.0010
- $7.6 \times 10^{3}$ a)
- **b)**  $8.99 \times 10$
- $6 \times 10^{4}$ c)  $5.6 \times 10^{-2}$ e)
- **d)**  $4.66 \times 10^2$
- $5.5 \times 10^{-3}$ g)
- $5.646 \times 10^5$ f)  $6.74 \times 10^4$
- $4.2 \times 10^{-5}$ i)
- h) j)  $2.4 \times 10^7$
- 6000 9 a)
- **b**) 500
- 0.007c)
- **d**) 450 **f)** 0.00287
- e) 0.00844700 g)
- **h**) 0.055
- 7230000i)
- 0.0000548 j)
- **10 a)**  $6 \times 10^8$ c)  $4 \times 10^{3}$
- **b)**  $6 \times 10^{5}$ **d)**  $3 \times 10^7$
- e)  $1.2 \times 10^{10}$
- $5 \times 10^{3}$ f)
- $6.3 \times 10^4$ g)
- **h)**  $7.7 \times 10^5$
- $3.6\times10^{-3}$ i)  $8.96 \times 10^{7}$ 11 a)
- **b)**  $7.82 \times 10^4$
- $3.17 \times 10^{3}$ c)
- **d)**  $7.97 \times 10^6$  $5.21 \times 10^{3}$ f)
- $5.96 \times 10^{10}$ e)  $6.65 \times 10^4$ g)
- h)  $7.85 \times 10^5$
- $3.90 \times 10^{-4}$ i) 2.5
- 12 a)
- b) -1
- 0 c)

13

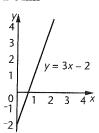


Gradient of AB = -0.5Gradient of BC = 0.25Gradient of AC = 2.5

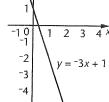
STAGE

8

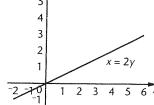
- 1.2 (km/minute)
- 2.6 km
- 15 a)



b)



c)



- d) 3 2
- 16 Check students' answers.

Lines should be of the form given below.

- **a)** y = 3x + k
- **b)** y = -3x + k
- c) x = 2y + k or
  - $y = \frac{1}{2}x + k$
- x = k

# 13 Similar figures

### **Exercise 13.1 (page 127)**

- 1 8cm
- 2 8cm
- 3 PQ = 4.2 cm, PR = 5.88 cm
- 4 PQ = 3.5 cm, QR = 6.02 cm
- 5 UV = 3.4 cm, UW = 4.4 cm
- 6 3 cm
- 7 42 m
- 8 x = 2.7 cm, y = 3 cm
- 9 42 m
- 10 a) Angle BAC = angle CDE

(alternate angles)

Angle ACB = angle DCE

(vertically opposite angles) Angle ABC = angle CED

(alternate angles)

Corresponding angles are equal so triangle

ABC is similar to triangle CDE.

- **b)** AC = 13.5 cm, BC = 27 cm
- 11 Angles are equal but the sides not proportional. (AR is smaller than AE but AB is the same in both.)
- 12 Sides are proportional but the angles not equal.
- 13 a) Angle A is common

Angle APQ = angle ABC

(corresponding angles)

Angle AQP = angle ACB

(corresponding angles)

(One of these can be substituted by 'angle

sum of triangle'.)

- **b)**  $6.27 \, \text{cm}$
- **14** a) Angle ADC = angle BAC (right angles) Angle DAB = angle DCA =  $90^{\circ}$  – angle

Angle DBA = angle DAC

(angle sum of triangle)

**b)** 1.8 cm

121

- 5 a) None Area c)
  - b) Length
  - e) None
- d) Volume f) Length
- 6 a) Nonsense c) Nonsense
- b) Area
- e) Nonsense
- d) Volume f) Area
- g) Volume i) Length
- 7 a) Cube (3)
- b) Square (2)

Volume

c) Square (2)

# Revision exercise D1 (page 159)

- 1 2.4 cm
- 2 No:  $\frac{6}{8} = 0.75$ ;  $\frac{3}{5} = 0.6$  or  $\frac{8}{5} = 1.6$ ;  $\frac{6}{3} = 2$
- 3 a) Angle BAC =  $85^{\circ}$ ; Angle QRP =  $40^{\circ}$ ; corresponding angles are equal so the triangles are similar.
  - **b)** 1.7
- 4 PR = 6.64 cm, QR = 6.24 cm
- 5 David takes longer but his times are more consistent.
- 6 10F median 15, range 21; 10G median 11, range 28; 10G students do the problem more quickly on average but with a wider spread of times. The interquartile range would eliminate extremes.
- 7 French adults drink more wine than English adults. Spread of amounts is similar but slightly wider in England.
- 8 Mean £161 400, range a maximum of £160 000. House prices are higher in the Southeast, with a wider spread of prices.
- 9 a) 35·1°
- **b)** 61.0°
- c) 59·7°
- d) 8.43 cm
- e) 7.55 cm
- f) 19.43 cm
- **10** 43.5 m
- 11 45.6°, 45.6°, 88.9° (to 3 s.f.)
- 12 4.6 m
- 13 a) West 4.83 km, North 1.29 km
  - **b)** 131.6°, 6.46 km
- **14** a) Area
- b) Length
- Volume c)
- **15 a)** 2 (square)
- **b)** 2 (square)
- **c)** 3 (cube)

### 17 Quadratics

### **Exercise 17.1 (page 164)**

- 1  $a^2 + 6a + 8$
- $a^2 + 6a + 5$
- 3  $x^2 + 7x + 6$
- $4x^2 + 11x + 18$
- $5 a^2 + 10a + 21$
- 6  $a^2 + 13a + 30$
- 7  $y^2 2y 15$
- 8  $x^2 3x 28$

- 9  $a^2 4a 12$
- 10  $p^2 + 3p 18$
- 11  $a^2 3a + 2$
- 12  $a^2 2a 15$
- 13  $x^2 + x 6$
- 14  $y^2 y 20$
- 15  $x^2 10x + 16$
- **16**  $a^2 11a + 18$ 18  $x^2 + 9x - 22$
- 17  $y^2 + 10y + 25$ 19  $x^2 - 2x + 1$
- **20**  $x^2 6x + 9$
- **21**  $y^2 + 4y + 4$
- 22  $y^2 4y + 4$ **24**  $a^2 + 12a + 36$
- 23  $a^2 12a + 36$ 25  $a^2 + 16a + 64$
- **26**  $x^2 9$ **28**  $a^2 - 64$
- 27  $x^2 25$ **29**  $a^2 - 81$
- 30  $a^2 + 40a + 400$
- 31  $y^2 1$
- 32  $a^2 36$
- 33 (x+5)(x+3),  $x^2 + 8x + 15$

### **Exercise 17.2 (page 168)**

- 1 (x+3)(x+2)
- 2 (x+5)(x+2)4 (x+3)(x+1)
- 3(x+5)(x+1)5(x+4)(x+2)
- 6 (x+5)(x+3)
- (x+4)(x+1)7 9 (x+1)(x+1)
- 8 (x+5)(x+4)10 (x+6)(x+1)
- 11 (x-6)(x-1)
- 12 (x-6)(x-3)
- 13 (x-2)(x-5)
- 14 (x-3)(x-4)**16** (a-1)(a-1)
- 15 (x-3)(x-1)17 (y-7)(y-2)
- **18** (b-6)(b-4)
- 19 (x-4)(x-2)**21** (a+6)(a+2)
- **20** (c-3)(c-1)22 (a+12)(a+3)**24** (x-9)(x-3)
- 23 (a-3)(a-3)25 (b-8)(b-4)
- **26** (b-5)(b-5)**28** (x + 12)(x + 2)
- 27 (x+3)(x+8)**29** (x-5)(x-4)
- 30 (x-7)(x-8)

### **Exercise 17.3 (page 169)**

- 1 (x-4)(x+2)
- 2 (x+3)(x-1)3(x-1)(x+5)4 (x+5)(x-2)
- 5 (x+2)(x-3)
- 6 (x-4)(x+3)
- 7 (x+6)(x-1)9 (x+3)(x-1)
- 8 (x+7)(x-2)10 (x-5)(x+3)
- 11 (x-6)(x+3)
- 12 (x-7)(x+4)
- 13 (x-10)(x+1)
- 14 (x-2)(x-15)
- 15 (x+7)(x+2)
- 16 (x-4)(x+8)
- 17 (y+11)(y-2)19 (x+4)(x-3)
- **18** (a + 12)(a 3)
- **21** (a-2)(a+10)
- **20** (x+5)(x-4)22 (y+3)(y+16)
- 23 (a-9)(a+3)
- **24** (a-8)(a+2)
- **25** (b+2)(b+10)
- **26** (b-12)(b-3)
- 27 (x+13)(x-2)
- 28 (x+10)(x-3)
- **29** (x-3)(x-6)
- 30 (x-8)(x+5)

# **Exercise 17.4 (page 170)**

- 1 (x+2)(x-2)
- 2 (x+1)(x-1)
- 3 (x+5)(x-5)5 (x+7)(x-7)
- 4 (x+6)(x-6)6 (x+9)(x-9)
- 7 (y+10)(y-10)9 (y+20)(y-20)
- 8 (m+12)(m-12)**10** (a+13)(a-13)
- **11** (y + 11)(y 11)
- 12 (b+15)(b-15)
- 13 (a+17)(a-17)
- **14** (p+q)(p-q)

TAGE

# Revision exercise E1 (page 191) 1 a) $x^2 + 12x + 27$

**b)**  $y^2 + y - 42$ 

 $a^2 - 16a + 64$ 

**d)**  $b^2 - 12b + 20$ 

e) 
$$p^2 + 7p - 30$$

 $a^2 - 81$ 

 $a^2 + 18a + 81$ (x-8)(x-2)

**h**) 
$$x^2 - 21x + 20$$

**2** a) 
$$(x+4)(x+1)$$

**b)** 
$$(x-2)(x-4)$$

**d)** 
$$(x+5)(x+3)$$

e) 
$$(x-7)(x+1)$$
  
i)  $(x-10)(x+7)$ 

**f)** 
$$(x+2)(x-5)$$

g) 
$$(x-6)(x-2)$$

2005

**h)** 
$$(x-5)(x+3)$$

3 a) 
$$(a+8)(a-8)$$

j) 
$$(x+12)(x+4)$$

(x+3)(x-3)

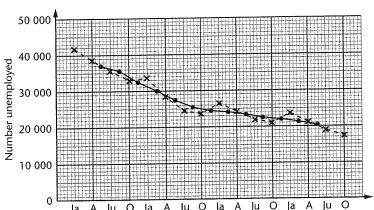
**k**) 
$$(x-9)(x+2)$$

(p+10)(p-10)

l) 
$$(x+10)(x-2)$$
  
d)  $(x+14)(x-14)$ 

3 a) 
$$(a+8)(a-8)$$

4 a), c)



2003

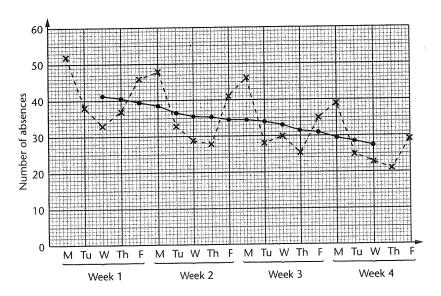
2002

b) Moving averages 37175, 35200, 32750, 30000, 27600, 25800, 24675, 24075, 23475, 22775, 22000, 21175, 20325

2004

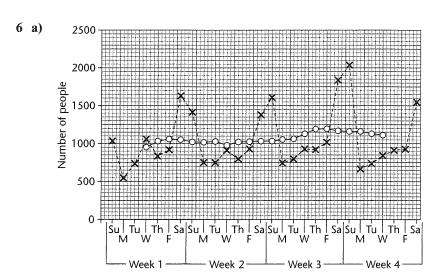
General trend downwards; quarter up to January always highest, then steadily lower

5 a), c)



- Moving averages 41·2, 40·4, 39·4, 38·6, 36·8, 35·8, 35·4, 34·4, 34·6, 34, 32·8, 31·4, 30·8, 29·4, 28.6, 27.4
- General trend downwards; Mondays always highest, followed by Friday

STAGE



- **b)** 964, 1017, 1045, 1048, 1022, 1017, 1020, 988, 1016, 1019, 1027, 1030, 1050, 1063, 1129, 1192, 1183, 1172, 1163, 1158, 1146, 1100
- The trend is fairly steady, with just a slight increase. The weekend numbers (Saturday and Sunday) are always higher than the weekday numbers (Monday to Friday).

7 a) 
$$x = 2 \text{ or } 4$$

**b)** 
$$x = -2 \text{ or } -3$$

c) 
$$x = 3 \text{ or } -1$$

**d)** 
$$x = 5 \text{ or } -2$$

**e)** 
$$x = 4 \text{ or } 1$$

f) 
$$x = -5 \text{ or } -2$$

**g)** 
$$x = 7 \text{ or } -2$$

**h)** 
$$x = -15$$
 or  $-2$ 

i) 
$$x = 5 \text{ or } 4$$

**j**) 
$$x = -3 \text{ or } -1$$

**k)** 
$$x = 12 \text{ or } -3$$

1) 
$$x = -9 \text{ or } 2$$

**8 a)** 
$$x = 0$$
 or  $-8$ 

**b)** 
$$x = 0 \text{ or } 5$$

**c)** 
$$x = \pm 8$$

**d)** 
$$x = \pm 10$$

**e)** 
$$x = 0 \text{ or } 10$$

**f)** 
$$x = 5 \text{ or } -1$$

**g**) 
$$x = -4$$
 or 2

**h)** 
$$x = 9 \text{ or } -1$$

**9 a)** 
$$a = \sqrt{x - by}$$

**b)** 
$$y = \frac{x}{1 - a}$$

c) 
$$b = \frac{cd}{a - x}$$
  
g)  $x = \frac{4y + 15}{3 + 3y}$ 

$$\mathbf{d)} \quad b = \frac{ac - cd}{a + d}$$

e) 
$$b = \sqrt[3]{A - 3c^2d}$$
 f)  $a = \frac{2A}{2b + \pi}$ 

i) 
$$y = \frac{-x}{8a+3}$$
 j)  $s = \sqrt{\frac{3t-P}{5}}$  k)  $u = \frac{fv}{v-f}$ 

$$\mathbf{k)} \quad u = \frac{fv}{v - f}$$

**b)** 
$$r = \sqrt[3]{\frac{3V}{2\pi}}$$

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