

- Look at this pattern:

$$1 = 1$$

$$1 + 2 = 3$$

$$1 + 2 + 4 = 7$$

$$1 + 2 + 4 + 8 = 15$$

Continue the pattern for three more lines.

What will the sum of the 10^{th} line, the 100^{th} line, the n^{th} line?

- Repeat this for

$$1 = 1$$

$$1 + 3 = 4$$

$$1 + 3 + 9 = 13$$

$$1 + 3 + 9 + 27 = 40$$

and for

$$1 = 1$$

$$1 + 4 = 5$$

$$1 + 4 + 16 = 21$$

$$1 + 4 + 16 + 64 = 85$$

- Write down a general pattern of this kind.

What would be the sum of the n^{th} row of this general pattern?

- Does your rule still work for these sequences?

$$1$$

$$1 + \frac{1}{2}$$

$$1 + \frac{1}{2} + \frac{1}{4}$$

$$1$$

$$1 + \frac{3}{2}$$

$$1 + \frac{3}{2} + \frac{9}{4}$$

- What happens if the pattern does not start with 1?

e.g. $8 + 16 + 32 + 64 \dots$

or $9 + 36 + 144 + 576 \dots$