

More sequences and series

Generalising and creating formulae

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5

7

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3

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7

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7

+

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Square numbers can be represented as the sum of consecutive odd numbers.

	Sequence	Square numbers
S_1	1	1
S_2	1 + 3	4
S_3	1 + 3 + 5	9
S_{25}	1 + 3 + ... + ?	?
S_{64}	1 + 3 + ... + ?	?
S_{95}	?	?

Have you a method for filling in the missing numbers quickly?

What is the sum of $1 + 3 + \dots + 149 + 151 + 153$?

Which square number has this value?

What is the value of $51 + 53 + 55 + \dots + 149 + 151 + 153$?

Which square numbers could help you find this value?

You could now explore square numbers as the sum of two consecutive triangle numbers.

More sequences and series: grid

Resource sheet
