

#useR #Rstudio
#hydrology #timeseries

Atelier numérique
Workshop

hydRologie avec R

hydRology with R

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Hydrologue



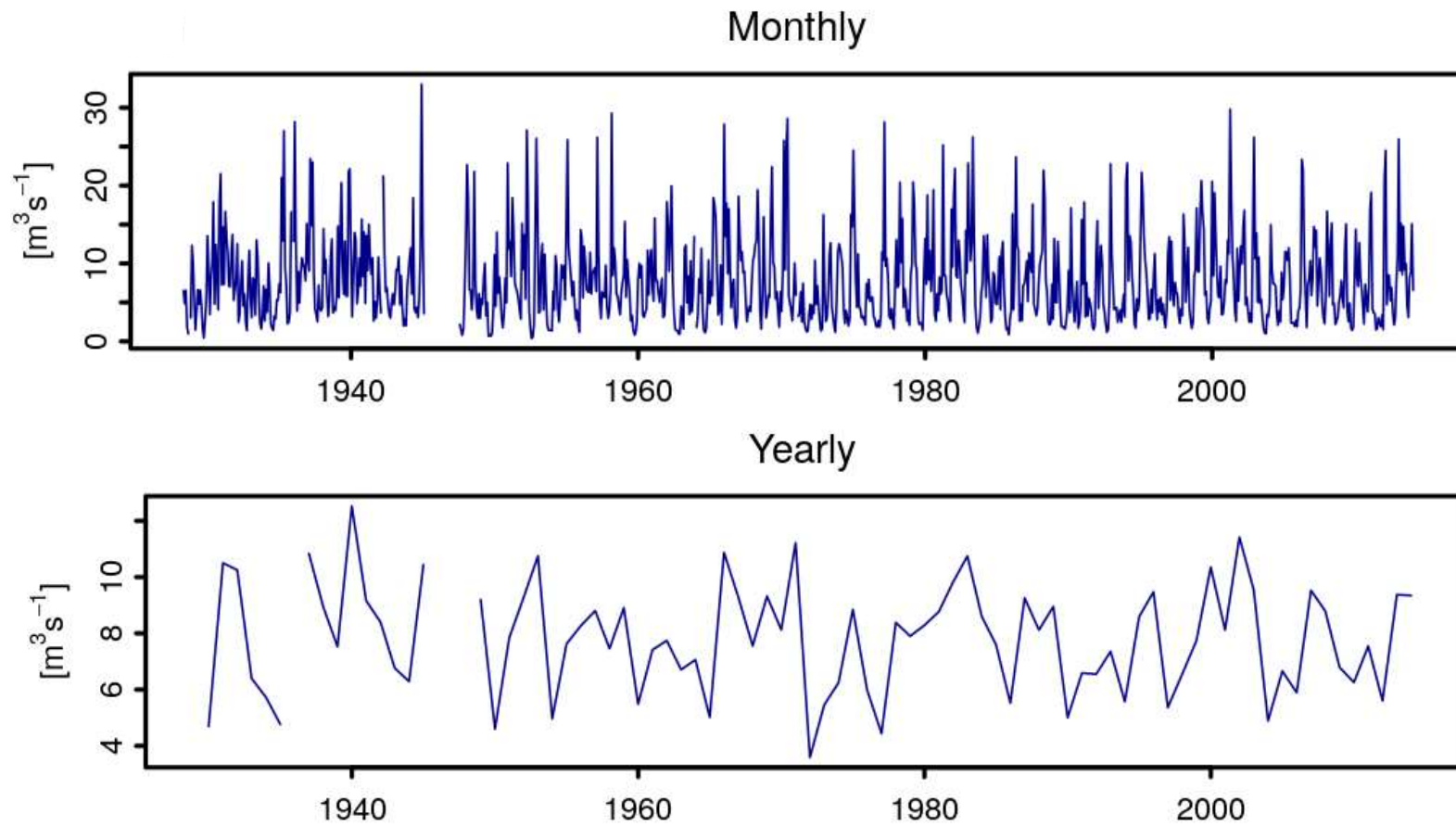
<https://github.com/hydrocodes>



1. Introduction aux séries temporelles hydrologiques



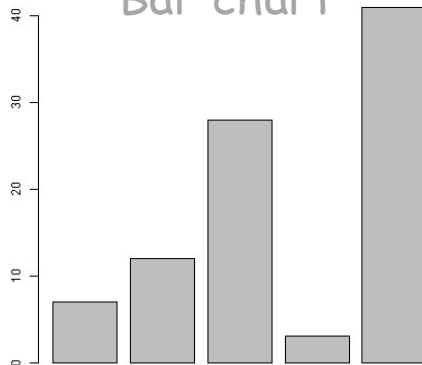
1.1 *¿Comment analyser une serie temporelle?*



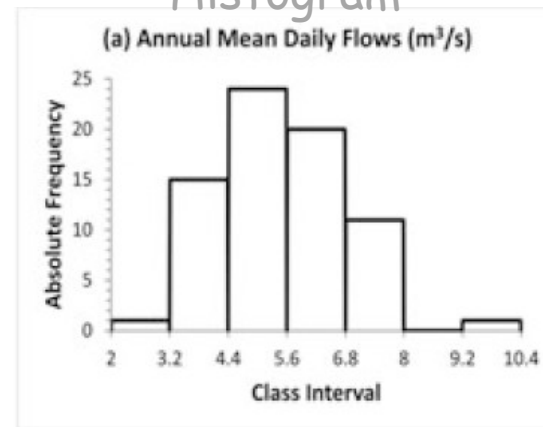
1.2 Analyse préliminaire de données hydrologiques

a. Types de représentations graphiques

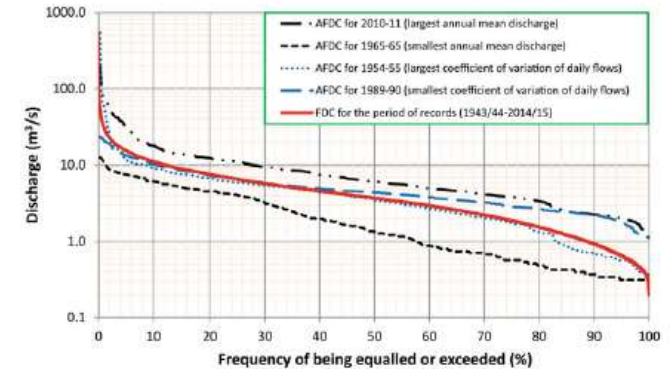
Diagramme à barres
Bar chart



Histogramme
Histogram



Courbe de durée
Duration curves



Parámetro de la población

Estadística de la muestra

1. Punto medio

Media aritmética

$$\mu = E(X) = \int_{-\infty}^{\infty} x f(x) dx$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

Mediana

x tal que $F(x) = 0.5$

Valor de la información en el 50o. percentil

Media geométrica

antilog $[E(\log x)]$

$$\left(\prod_{i=1}^n x_i \right)^{1/n}$$

Coefficiente de variación

$$CV = \frac{\sigma}{\mu}$$

$$CV = \frac{s}{\bar{x}}$$

2. Variabilidad

Varianza

$$\sigma^2 = E[(x - \mu)^2]$$

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

Desviación estándar

$$\sigma = \{E[(x - \mu)^2]\}^{1/2}$$

$$s = \left[\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 \right]^{1/2}$$

3. Simetría

Coefficiente de asimetría (oblicuidad)

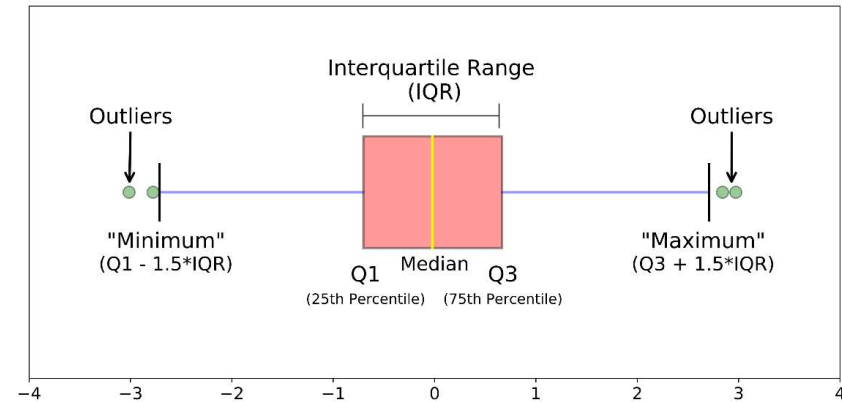
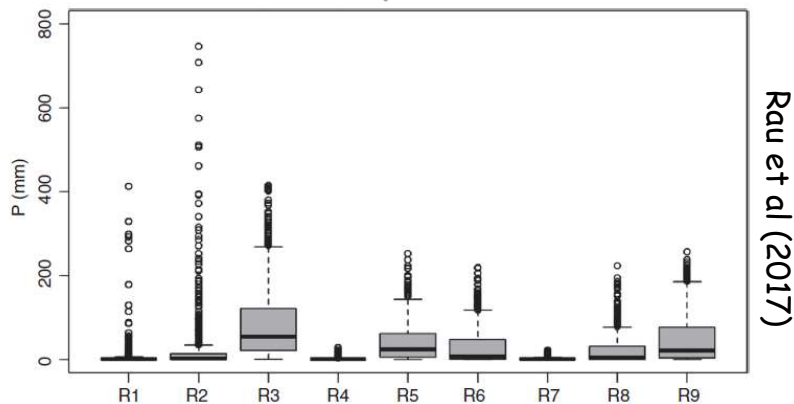
$$\gamma = \frac{E[(x - \mu)^3]}{\sigma^3}$$

$$C_s = \frac{n \sum_{i=1}^n (x_i - \bar{x})^3}{(n-1)(n-2)s^3}$$

b. Statistiques descriptifs

c. Méthodes exploratoires

Boîte à moustaches
Box plot



Naghetini (2017)

d. Association de données

Nuages de points
Scatter plot

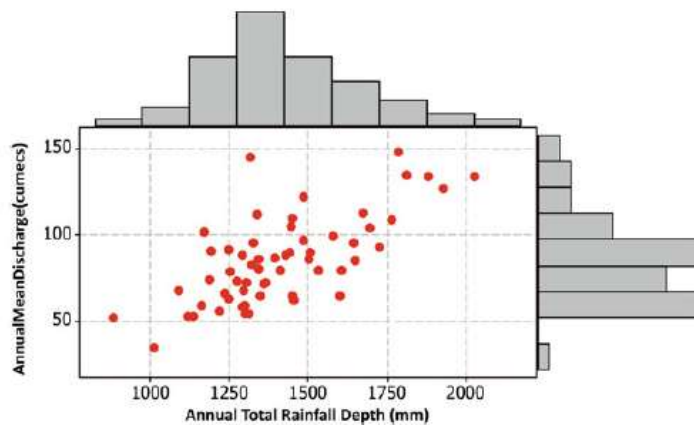
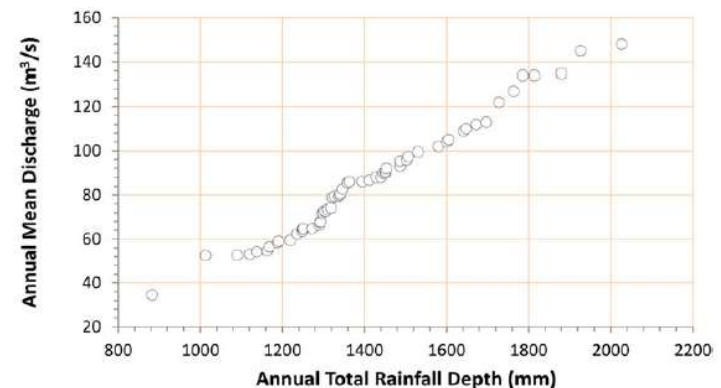


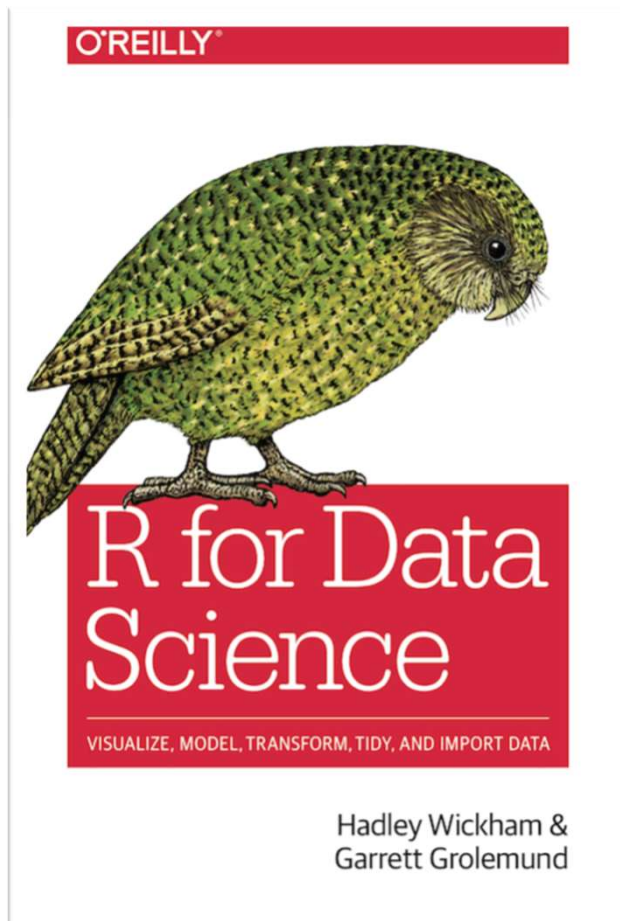
Diagramme Quantile-Quantile
Empirical Quantile-Quantile Diagram
Q-Q Plot





2. *Environnement R et Rstudio*

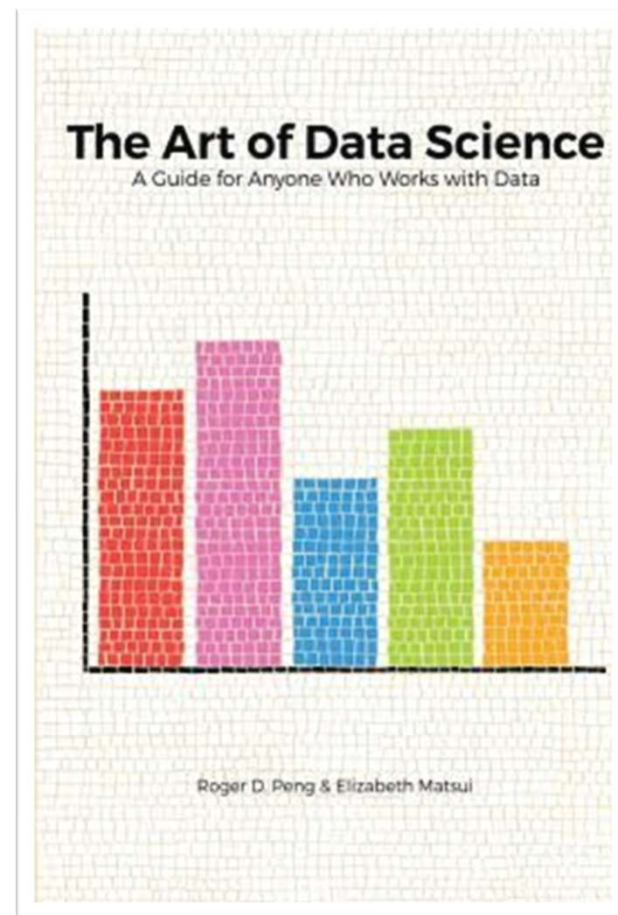




<https://r4ds.had.co.nz/>

<https://es.r4ds.hadley.nz/>

<https://github.com/jrnold/r4ds-exercise-solutions/blob/master/README.md>



<https://bookdown.org/rdpeng/artofdatascience/>

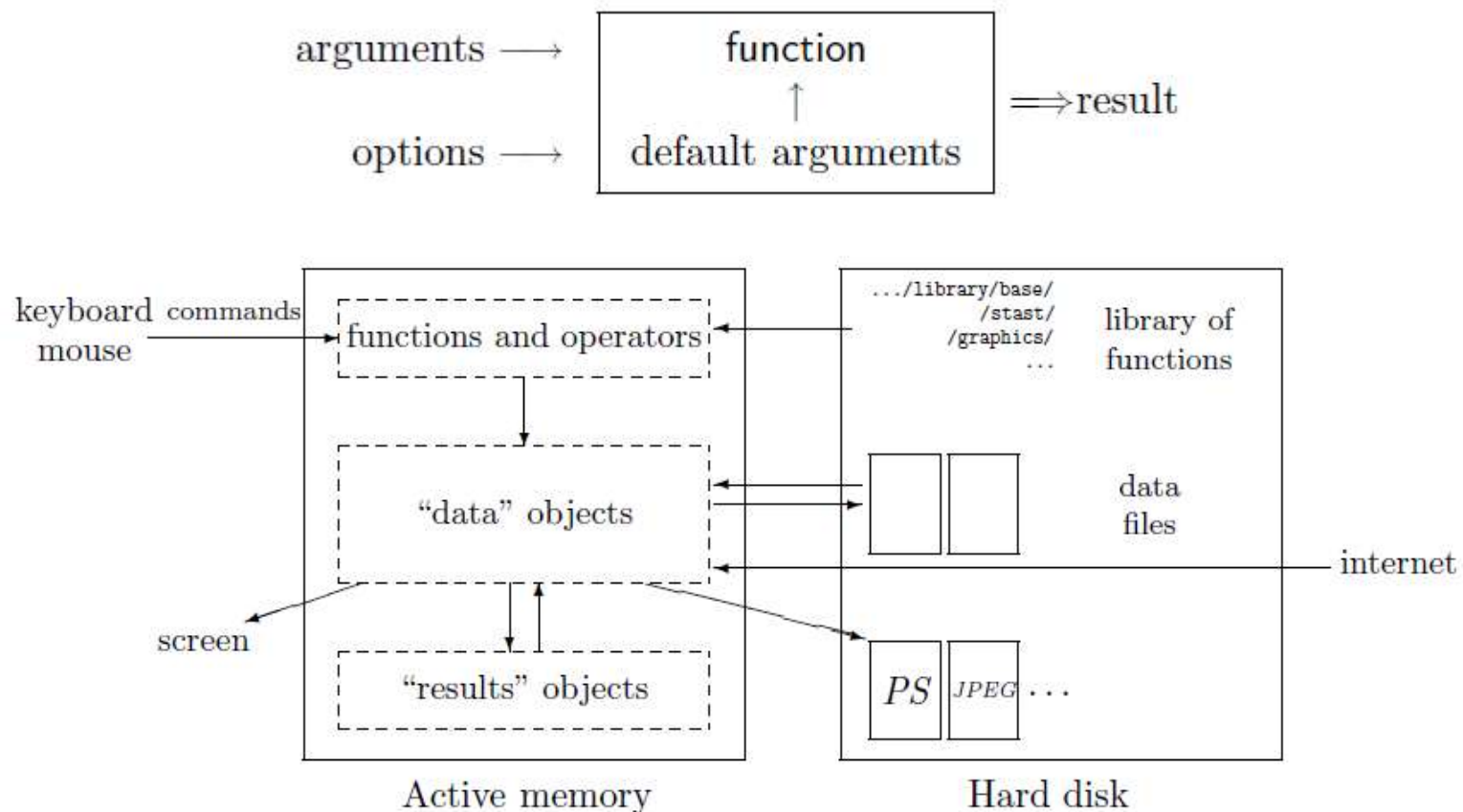
<https://github.com/waldronlab/The-Art-of-Data-Science/blob/master/README.md>

R-4.2.3 pour Windows (32/64 bit) - mars 2023

<https://cran.r-project.org/bin/windows/base/>



- ✓ Système pour l'analyse statistique et de graphiques (Ihaka y Gentleman, 1996).
- ✓ Langage interprété, ce n'est pas un langage compilé.
- ✓ Facile et intuitive, « ce n'est pas un langage de programmation » strictement.

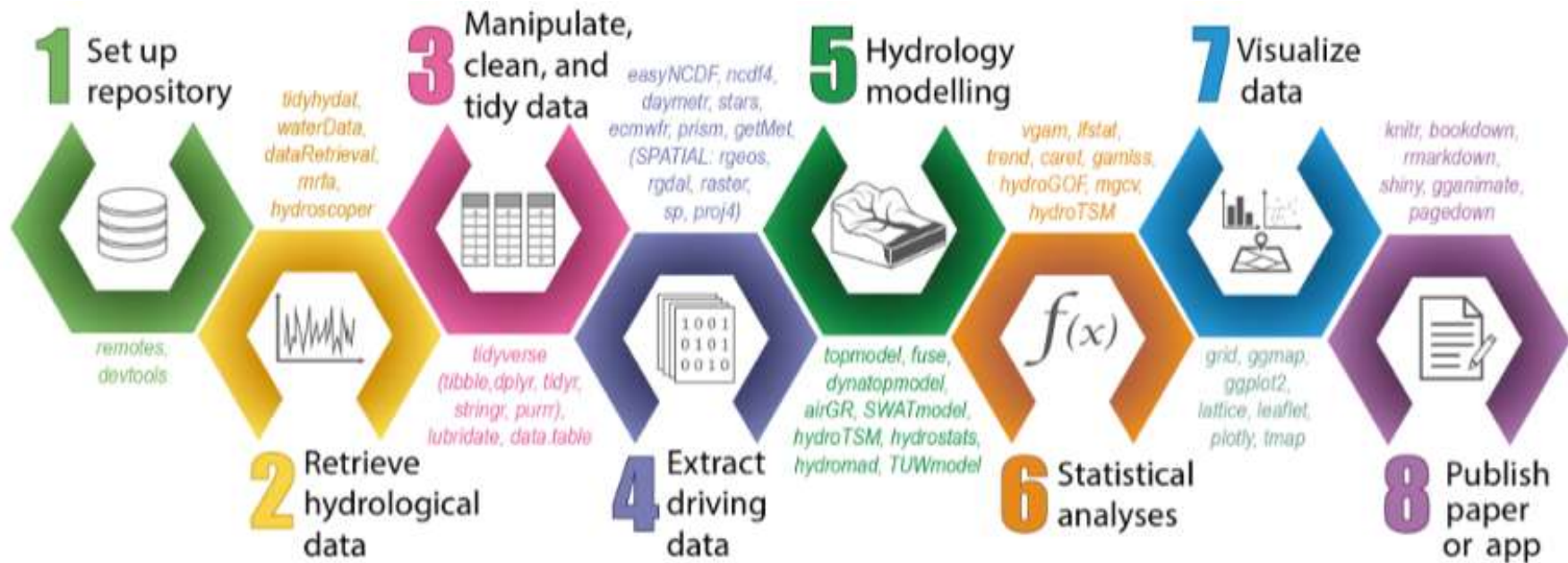


Paradis (2002)

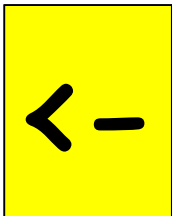
The Comprehensive R Archive Net-work (CRAN)

<https://cran.r-project.org>

Flux de travail typique en R en hydrologie

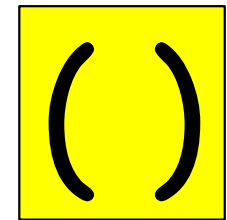


Slater et al (2019)



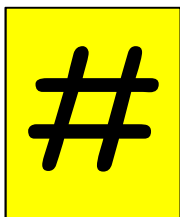
"Classes" d'objets basiques ou "atomic" en R:

- numeric (nombres réels)
- integer
- complex
- logical (True/False)



Types d'objets en R pour représenter les données

object	modes	several modes possible in the same object?	
vector	numeric, character, complex <i>or</i> logical	No	c()
factor	numeric <i>or</i> character	No	factor()
array	numeric, character, complex <i>or</i> logical	No	array()
matrix	numeric, character, complex <i>or</i> logical	No	matrix()
data frame	numeric, character, complex <i>or</i> logical	Yes	data.frame()
ts	numeric, character, complex <i>or</i> logical	No	ts()
list	numeric, character, complex, logical, function, expression, ...	Yes	list()



Conversion entre classes d'objets

Conversion to	Function	Rules
numeric	as.numeric	FALSE → 0 TRUE → 1 "1", "2", ... → 1, 2, ... "A", ... → NA
logical	as.logical	0 → FALSE other numbers → TRUE "FALSE", "F" → FALSE "TRUE", "T" → TRUE other characters → NA
character	as.character	1, 2, ... → "1", "2", ... FALSE → "FALSE" TRUE → "TRUE"

Fonctions de probabilité

Distribución/función	función
Gausse (normal)	rnorm(n, mean=0, sd=1)
exponencial	rexp(n, rate=1)
gamma	rgamma(n, shape, scale=1)
Poisson	rpois(n, lambda)
Weibull	rweibull(n, shape, scale=1)
Cauchy	rcauchy(n, location=0, scale=1)
beta	rbeta(n, shape1, shape2)
'Student' (t)	rt(n, df)
Fisher-Snedecor (F)	rf(n, df1, df2)
Pearson (χ^2)	rchisq(n, df)
binomial	rbinom(n, size, prob)
géométrica	rgeom(n, prob)
hypergéométrica	rhyper(nn, m, n, k)
logística	rlogis(n, location=0, scale=1)
lognormal	rlnorm(n, meanlog=0, sdlog=1)
binomial negativa	rnbinom(n, size, prob)
uniforme	runif(n, min=0, max=1)
Estadístico de Wilcoxon's	rwilcox(nn, m, n), rsignrank(nn, n)

Opérateurs en R

Arithmetic		Operators		Logical	
		Comparison			
+	addition	<	lesser than	! x	logical NOT
-	subtraction	>	greater than	x & y	logical AND
*	multiplication	<=	lesser than or equal to	x && y	id.
/	division	>=	greater than or equal to	x y	logical OR
^	power	==	equal	x y	id.
%%	modulo	!=	different	xor(x, y)	exclusive OR
%%/	integer division				

plot(x)	plot of the values of x (on the y -axis) ordered on the x -axis
plot(x, y)	bivariate plot of x (on the x -axis) and y (on the y -axis)
sunflowerplot(x, y)	id. but the points with similar coordinates are drawn as a flower which petal number represents the number of points
pie(x)	circular pie-chart
boxplot(x)	"box-and-whiskers" plot
stripchart(x)	plot of the values of x on a line (an alternative to boxplot() for small sample sizes)
coplot(x~y z)	bivariate plot of x and y for each value (or interval of values) of z
interaction.plot(f1, f2, y)	if $f1$ and $f2$ are factors, plots the means of y (on the y -axis) with respect to the values of $f1$ (on the x -axis) and of $f2$ (different curves); the option fun allows to choose the summary statistic of y (by default fun=mean)
matplot(x,y)	bivariate plot of the first column of x vs. the first one of y , the second one of x vs. the second one of y , etc.
dotchart(x)	if x is a data frame, plots a Cleveland dot plot (stacked plots line-by-line and column-by-column)
fourfoldplot(x)	visualizes, with quarters of circles, the association between two dichotomous variables for different populations (x must be an array with dim=c(2, 2, k), or a matrix with dim=c(2, 2) if $k = 1$)
assocplot(x)	Cohen-Friendly graph showing the deviations from independence of rows and columns in a two dimensional contingency table
mosaicplot(x)	'mosaic' graph of the residuals from a log-linear regression of a contingency table
pairs(x)	if x is a matrix or a data frame, draws all possible bivariate plots between the columns of x
plot.ts(x)	if x is an object of class "ts", plot of x with respect to time, x may be multivariate but the series must have the same frequency and dates
ts.plot(x)	id. but if x is multivariate the series may have different dates and must have the same frequency
hist(x)	histogram of the frequencies of x
barplot(x)	histogram of the values of x
qqnorm(x)	quantiles of x with respect to the values expected under a normal law
qqplot(x, y)	quantiles of y with respect to the quantiles of x
contour(x, y, z)	contour plot (data are interpolated to draw the curves), x and y must be vectors and z must be a matrix so that dim(z)=c(length(x), length(y)) (x and y may be omitted)
filled.contour(x, y, z)	id. but the areas between the contours are coloured, and a legend of the colours is drawn as well
image(x, y, z)	id. but the actual data are represented with colours
persp(x, y, z)	id. but in perspective
stars(x)	if x is a matrix or a data frame, draws a graph with segments or a star where each row of x is represented by a star and the columns are the lengths of the segments
symbols(x, y, ...)	draws, at the coordinates given by x and y , symbols (circles, squares, rectangles, stars, thermometres or "boxplots") which sizes, colours, etc. are specified by supplementary arguments
termplot(mod.obj)	plot of the (partial) effects of a regression model (mod.obj)

Tracer des graphiques

add=FALSE if TRUE superposes the plot on the previous one (if it exists)

axes=TRUE if FALSE does not draw the axes and the box

type="p" species the type of plot, "p": points, "l": lines, "b": points connected by lines, "o": id. but the lines are over the points, "h": vertical lines, "s": steps, the data are represented by the top of the vertical lines, "S": id. But the data are represented by the bottom of the vertical lines

xlim=, ylim= species the lower and upper limits of the axes, for example
with xlim=c(1, 10) or xlim=range(x)

xlab=, ylab= annotates the axes, must be variables of mode character

main= main title, must be a variable of mode character

sub= sub-title (written in a smaller font)

RStudio Desktop 2023

<https://rstudio.com/products/rstudio/download/#download>



Environnement de développement intégré pour le langage de programmation R

The screenshot shows the RStudio Desktop 2023 interface with several annotations in red boxes:

- Editeur des codes / Console des scripts:** Points to the source editor on the left where R code is being written.
- Espace d'objets et historique:** Points to the Environment pane on the right, which displays the objects in the current R session.
- Console R / Console des résultats:** Points to the Console pane at the bottom left, which shows the output of the R code.
- Figures et fichiers:** Points to the Plots pane on the bottom right, which displays a line graph of Discharge (m³/s) versus Hours.

The source editor contains the following R code:

```
1 library(devtools)
2 devtools::install_github ("hydrocodes/hydRopUrban")
3
4 library(hydRopUrban)
5 data <- read.table(file.choose(), header=TRUE)
6 output <- read.table(file.choose(), header=TRUE)
7 dt <- 0.05 # time interval for plotting in hr (e.g. 0.05 or 3-min)
8 D <- 1
9 rational(data,dt)
10 rationalm(data,dt)
11 rationalu(data,dt)
12
13 caquots(data, a=5, b=-0.6)
14 caquotp(data, a=5, b=-0.6)
15
16
```

The Environment pane shows the following objects:

- myplot: List of 14
- r: Formal class RasterStack
- region: Formal class 'SpatialPolygonsDataFrame'
- res: List of 12
- data: num [1:406] 2573 4136 6612 5010 4208 ...
- dt: 0.05
- n: 3
- output: "D:/2_Courses/R_Hidrologia/Tutorial_files/urba..."
- Qm: num [1:432] 10.75 17.52 4.66 3.35 0.44 ...
- Qmd: Time-Series [1:432] from 1981 to 2017: 10.75 1...

The Console shows the following output:

```
** testing if installed package can be loaded from final location
*** arch - i386
*** arch - x64
** testing if installed package keeps a record of temporary installation path
* DONE (hydRopUrban)
> library(hydRopUrban)
> data <- read.table(file.choose(), header=TRUE)
> output <- read.table(file.choose(), header=TRUE)
> dt <- 0.05 # time interval for plotting in hr (e.g. 0.05 or 3-min)
> rationalu(data,dt)
[1] 0.01948328
[1] 0.02329645
[1] "qpeak = 0.041258 m3/s, volume = 83.839531 m3"
>
```

The Plots pane shows a line graph of Discharge (m³/s) versus Hours. The x-axis ranges from 0.0 to 1.5, and the y-axis ranges from 0.00 to 0.04. The graph shows a solid line and a dashed line, both peaking around 0.5 hours.

A. Commandes et codes dans l'environnement Rstudio

Exercice A.1

Dans la **console de résultats**, effectuer les opérations suivantes:

- 1) $3^2 - 5 * 9 * (25 - 18)$
- 2) Créer une série consécutive de 1 al 8.
- 3) Créer une série consécutive de 8 lettres en commençant par "a".
- 4) Attribuer l'opération $8 * 5^2$ à l'objet *value*.
- 5) Visualiser l'objet *value* crée.
- 6) Créer l'objet *p*, en stockant une séquence depuis 5 jusqu'à 15 de 2 en 2.
- 7) Visualiser *p*.
- 8) Stocker les valeurs suivantes de pluie annuelle (mm/an) de différents stations pluviométriques d'un bassin hydrographique: 200, 210.2, 490, 100.5, 150.1, 190, 310 y 200.2 dans l'objet *rain*.
- 9) Visualiser *rain*.
- 10) Obtenir le 5ème element de *rain*.
- 11) Stocker les valeurs suivantes d'Elevation (msnm) : 3200, 3500, 4500, 3050, 3100, 2800, 3800, 3500 dans l'objet *elev*.
- 12) Visualiser *elev*.

Réponses A.1

```
> 3^2-5*9*(25-18)
[1] -306
> 1:8
[1] 1 2 3 4 5 6 7 8
> letters[1:8]
[1] "a" "b" "c" "d" "e" "f" "g" "h"
> value<-8*5^2 #Attribuer une opération à l'objet value
> value #Visualiser l'objet "value"
[1] 200
> p<-seq(from=5, to=15, by=2) #sequence depuis 5 jusqu'à 15 de 2 en 2
> print (p)
> rain<-c(200, 210.2, 490, 100.5, 150.1, 190, 310, 200.2) #Emploi de la fonction c(combiner)
> rain #Visualiser l'objet "rain"
[1] 200 210.2 490 100.5 150.1 190 310 200.2
> rain[5] #Obtenir le 5eme element de l'objet rain
[1] 150.1
> elev<-c(3200, 3500, 4500, 3050, 3100, 2800, 3800, 3500) # Vecteur des elevations
> elev #Visualiser l'objet "elev"
[1] 3200 3500 4500 3050 3100 2800 3800 3500
```

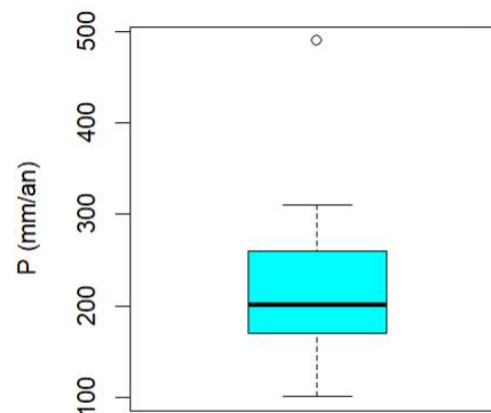
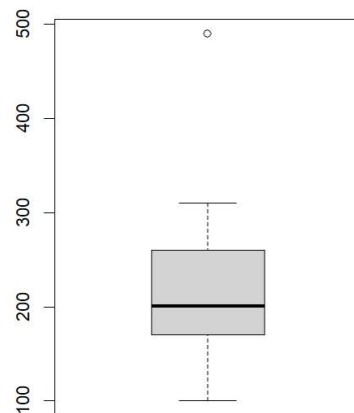
Exercice A.2

Dans la **console de résultats**, effectuer les opérations suivants:

- 1) Obtenir la moyenne, médiane, l'écart-type, variance de l'objet **rain** (de l'exercice A.1).
- 2) Visualiser un résumé des principaux statistiques.
- 3) Tracer une boîte à moustaches avec les valeurs de l'objet **rain** et interpréter.
- 4) Ajouter au dernier graphique une couleur de remplissage «cyan» avec une étiquette dans l'axe verticale "P (mm/an)"

Réponses A.2

```
> mean(rain)
[1] 231.375
> median(rain)
[1] 200.1
> sd(rain)
[1] 120.0709
> var(rain)
[1] 14417.03
> summary(rain)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  100.5  180.0   200.1   231.4   235.2   490.0
> boxplot(rain)
> boxplot(rain, ylab="P (mm/año)", col="cyan") #Boite à moustaches avec l'etiquette dans la verticale
```



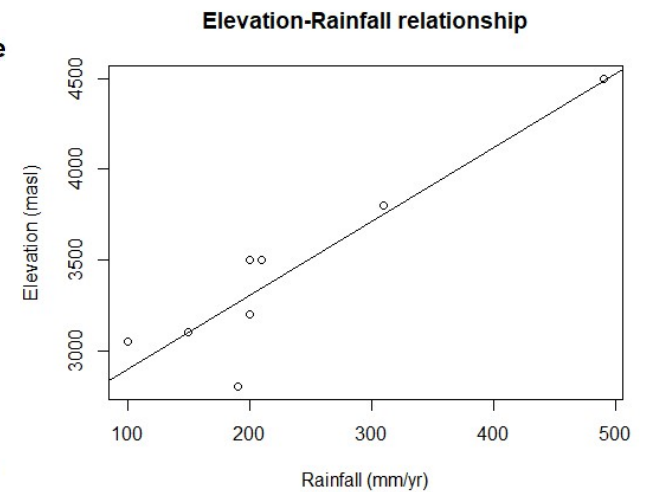
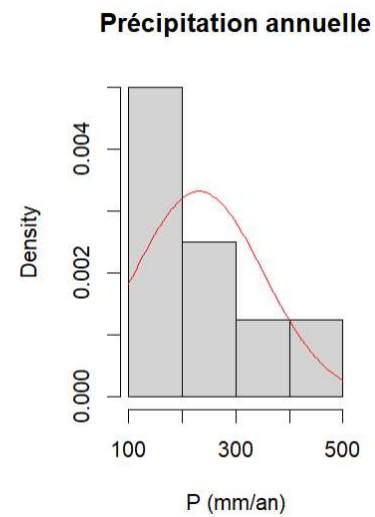
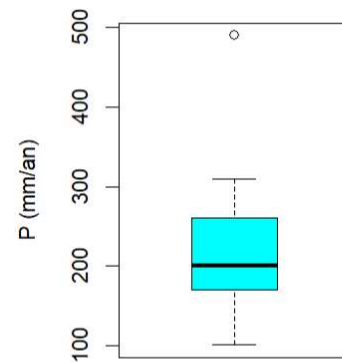
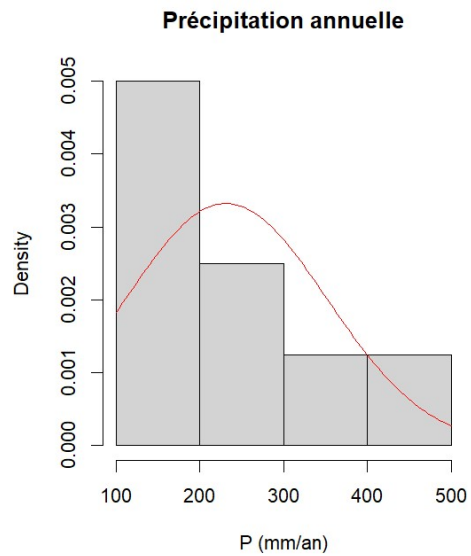
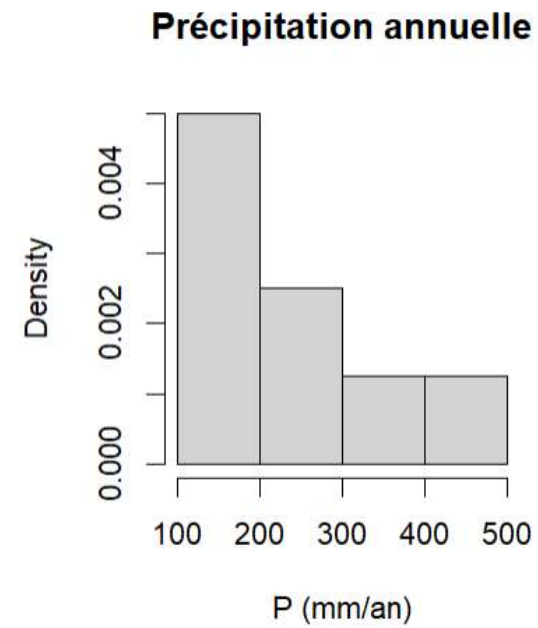
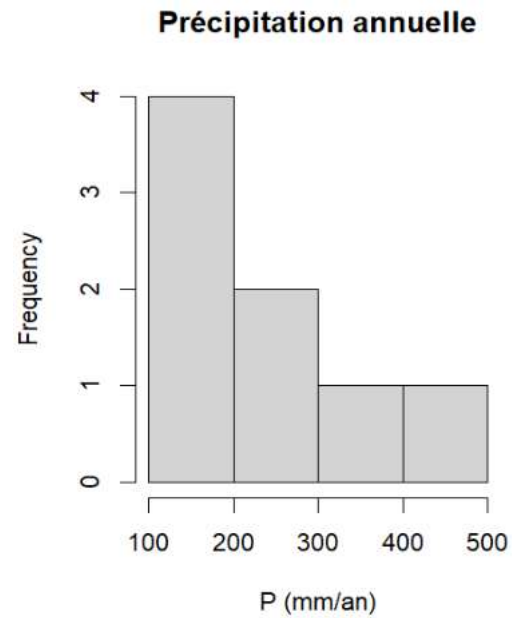
Exercices A.3

Dans la console de résultats, effectuer les opérations suivantes:

- 1) Tracer un histogramme de fréquences pour l'objet *rain*, utilisez la fréquence.
- 2) Tracer un histogramme de fréquences pour l'objet *rain*, utilisez la densité.
- 3) Ajoutez une courbe de distribution normale dans le graphique précédent avec une couleur rouge avec la moyenne et l'écart-type estimées précédemment.
- 4) Ajoutez dans un seul graphique (1 file x 2 colonnes), la boîte à moustache et l'histogramme.
- 5) Séparez les graphiques précédents.
- 6) Calculez la covariance entre la pluie et l'élévation.
- 7) Calculez le coefficient de corrélation entre la pluie et l'élévation.
- 8) Calculez l'équation de régression linéaire entre la pluie et l'élévation.
- 9) Tracer un nuage de points entre la pluie et l'élévation.
- 10) Ajoutez une ligne de tendance dans le graphique précédent.

Réponses A.3

```
> hist(rain, main="Précipitation annuelle", xlab="P (mm/an)", freq=F) # Histogramme, F(False) pour
n'est pas utiliser la fréquence
> curve(dnorm(x, mean(rain, na.rm = T), sd(rain, na.rm = T)), add = TRUE, col="red") # Ajouter une
courbe de distribution normale en rouge
> split.screen(c(1,2)) #Fonction pour créer une espace des figures, e.g. 2 figures dans 1 ligne et 2
colonnes
> screen(2) #Utiliser cette fonction pour préciser la position avant de tracer la figure
> close.screen(all=TRUE) # fonction pour retourner aux conditions initiales d'une figure par fenêtre
> cov(rain,elev) #covariance
[1] 58855.89
> cor(rain,elev) #coefficient de corrélation r
[1] 0.9182557
> lm(elev ~ rain) #équation de régression linéaire
Call:
lm(elev ~ rain)
Coefficients:
(Intercept)      rain
  2486.688      4.082
> plot(rain,elev,main="Elevation-Rainfall relationship",xlab="Rainfall (mm/yr)", ylab="Elevation
(masl)")
> abline(lm(elev~rain))
```



3. Analyse exploratoire et traitement de données



read.table(file, header = FALSE, sep = "", quote = "\"", dec = ".", row.names, col.names, as.is = FALSE, na.strings = "NA", colClasses = NA, nrows = -1, skip = 0, check.names = TRUE, fill = !blank.lines.skip, strip.white = FALSE, blank.lines.skip = TRUE, comment.char = "#")

read.csv(file, header = TRUE, sep = ",", quote="\"", dec=".", fill = TRUE, ...)

Lecture de fichiers, base de données

file	the name of the file (within "" or a variable of mode character), possibly with its path (the symbol \ is not allowed and must be replaced by /, even under Windows), or a remote access to a file of type URL (http://...)
header	a logical (FALSE or TRUE) indicating if the file contains the names of the variables on its first line
sep	the field separator used in the file, for instance <code>sep="\t"</code> if it is a tabulation
quote	the characters used to cite the variables of mode character
dec	the character used for the decimal point
row.names	a vector with the names of the lines which can be either a vector of mode character, or the number (or the name) of a variable of the file (by default: 1, 2, 3, ...)
col.names	a vector with the names of the variables (by default: V1, V2, V3, ...)
as.is	controls the conversion of character variables as factors (if FALSE) or keeps them as characters (TRUE); as.is can be a logical, numeric or character vector specifying the variables to be kept as character
na.strings	the value given to missing data (converted as NA)
colClasses	a vector of mode character giving the classes to attribute to the columns
nrows	the maximum number of lines to read (negative values are ignored)
skip	the number of lines to be skipped before reading the data
check.names	if TRUE, checks that the variable names are valid for R
fill	if TRUE and all lines do not have the same number of variables, "blanks" are added
strip.white	(conditional to sep) if TRUE, deletes extra spaces before and after the character variables
blank.lines.skip	if TRUE, ignores "blank" lines
comment.char	a character defining comments in the data file, the rest of the line after this character is ignored (to disable this argument, use <code>comment.char = ""</code>)

Configurer des Séries temporelles

`ts(data = NA, start = 1, end = numeric(0), frequency = 1, deltat = 1, ts.eps = getOption("ts.eps"), class, names)`

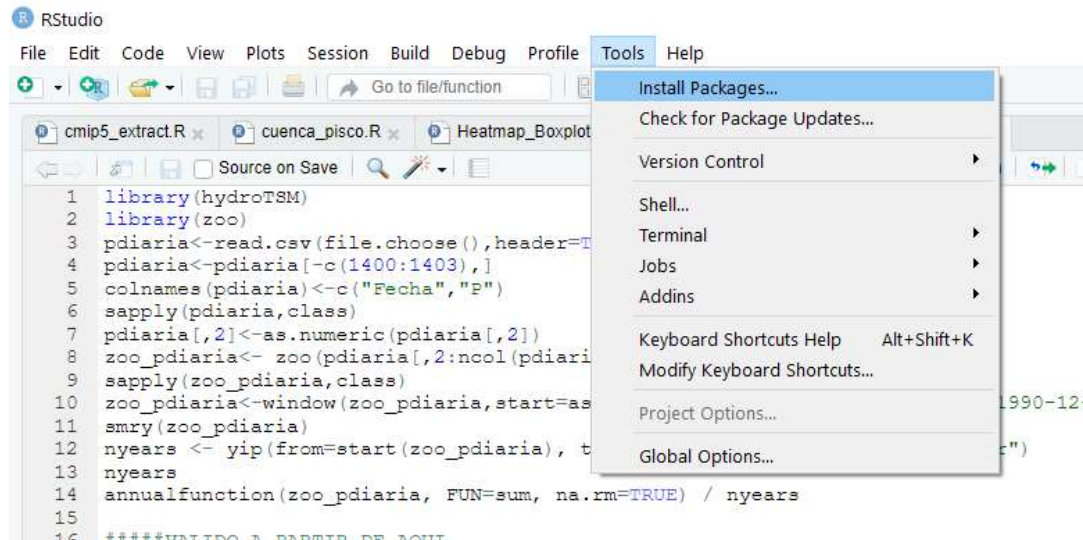
<code>data</code>	a vector or a matrix
<code>start</code>	the time of the rst observation, either a number, or a vector of two integers (see the examples below)
<code>end</code>	the time of the last observation specied in the same way than <code>start</code>
<code>frequency</code>	the number of observations per time unit
<code>deltat</code>	the fraction of the sampling period between successive observations (ex. 1/12 for monthly data); only one of frequency or <code>deltat</code> must be given
<code>ts.eps</code>	tolerance for the comparison of series. The frequencies are considered equal if their dierence is less than <code>ts.eps</code>
<code>class</code>	class to give to the object; the default is "ts" for a single series, and c("mts", "ts") for a multivariate series
<code>names</code>	a vector of mode character with the names of the individual series in the case of a multivariate series; by default the names of the columns of data, or Series 1, Series 2, . . .

Ex: `ts(donnees, start=c(1964, 1), end=c(2007, 12), frequency=12)`

B. Explorer dans les données de précipitations mensuelles stockées dans un fichier d'une station

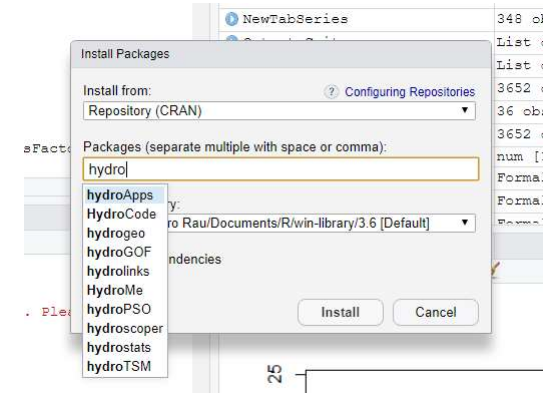
Utilisation des packages: lattice, zoo, hydroTSM

- Installer les packages avec: TOOLS - INSTALL PACKAGES: lattice, zoo, hydroTSM
- Télécharger le fichier "pmensual.txt"
https://github.com/hydrocodes/Series_hidro_R/blob/master/Tutorial_files/pmensual.txt
- Révision du fichier de type texte (generé depuis MS Excel)



The screenshot shows the RStudio interface. The 'Tools' menu is open, and 'Install Packages...' is selected. The background shows an R script with the following code:

```
1 library(hydroTSM)
2 library(zoo)
3 pdiaria<-read.csv(file.choose(),header=T)
4 pdiaria<-pdiaria[-c(1400:1403),]
5 colnames(pdiaria) <-c("Fecha", "P")
6 sapply(pdiaria,class)
7 pdiaria[,2]<-as.numeric(pdiaria[,2])
8 zoo_pdiaria<- zoo(pdiaria[,2:ncol(pdiaria)],
9 sapply(zoo_pdiaria,class)
10 zoo_pdiaria<-window(zoo_pdiaria,start=as.Date("1990-12-
11 smry(zoo_pdiaria)
12 nyears <- yip(from=start(zoo_pdiaria), to=end(zoo_pdiaria))
13 nyears
14 annualfunction(zoo_pdiaria, FUN=sum, na.rm=TRUE) / nyears
15
16 #####VALIDO A PARTIR DE AQUI
```



Exercice B

Dans la console de codes ou scripts, créer un code qui fait le suivant:

- 1) Lecture du fichier de précipitations mensuelles "pmensuelle.txt" stockés en format table avec 13 colonnes (année mois1 mois2 mois12) y 45 lignes (nom valeur1 valeur2 ...).
- 2) Tracer tout la série temporelle.
- 3) Ajouter une courbe de tendance du type lowess.
- 4) Tracer une carte de chaleur ou "heatmap"

Sauver le script avec le nom: Analyse_mensuelle.R

Réponses B

```
library("lattice") #Appeler le package lattice  
library("hydroTSM") # Appeler le package hydroTSM  
pmensual<-read.table(file.choose(), header = F, check.names = F) #lecture du fichier avec l'option fenêtre  
en saillie, chercher la route du fichier et sélectionner. « Header=F" dans le cas où l'entête ne contient pas  
de données sinon que de noms
```

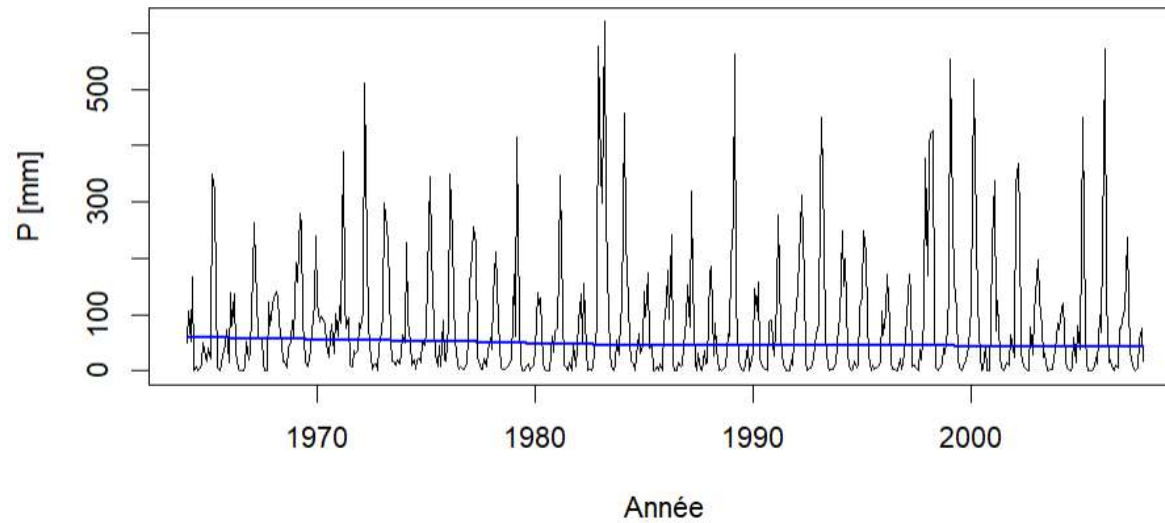
#Visualiser la serie temporelle

```
datos<-pmensual[2:45,2:13]  
datos_vector<-as.vector(t(datos)) #convertir en vecteur  
datos_ts<-ts(datos_vector, start=c(1964, 1), end=c(2007, 12), frequency=12)  
plot.ts(datos_ts, col="black", main=" Précipitation Mensuelle", ylab="P [mm]", xlab="Année")  
lines(lowess(time(datos_ts), datos_ts), col="blue", lwd=2) #ajouter la courbe de tendance
```

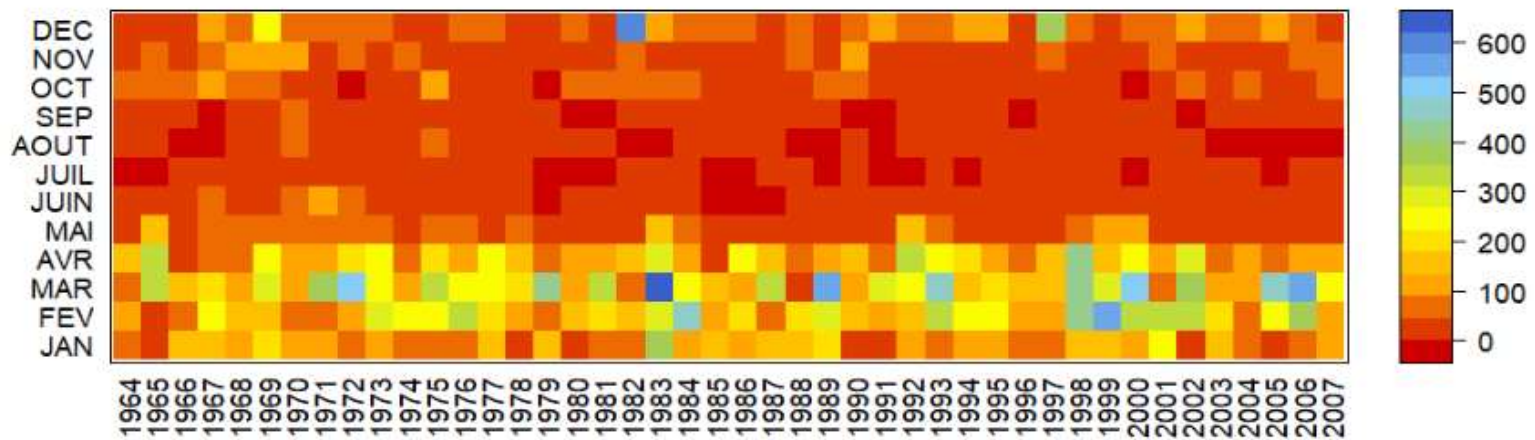
#Carte de chaleur ou HeatMap:

```
lluvia<-pmensual[2:45,2:13] #lecture de données de pluies sans etiquettes et mois (depuis 1964 à 2007)  
meses<-pmensual[1:1,2:13] #lecture de l'entête des mois dans la premiere ligne  
colnames(lluvia)<-unlist(meses) #desagregation des noms de mois et attribuer à la matrice  
rownames(lluvia)<-pmensual[2:45,1:1] #désagrégation des dates dans le lignes et attribuer à la matrice  
matrixplot(lluvia, ColorRamp="Precipitation", main="Précipitation Mensuelle 1964-2007 (mm/mois)")
```

Précipitation Mensuelle



Précipitation Mensuelle 1964-2007 (mm/mois)



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