

$$A_{s1} = \frac{\pi \cdot d_{bL}^2}{4} = \frac{3.141593 \cdot 25^2}{4} = 490.873852 \text{ mm}^2$$

$$A_s = n_b \cdot A_{s1} = 13 \cdot 490.873852 = 6381.360078 \text{ mm}^2$$

Reinforcement ratio

$$\rho_L = \frac{A_s}{A_f} = \frac{6381.360078}{262500} = 0.02430994$$

Design check: $0.005 \leq \rho_L = 0.02430994 \leq 0.04$. The check is satisfied! ✓

[§ 5.4.3.4.2 (8)]

Vertical web reinforcement

Bar diameter - $d_{bv} = 10 \text{ mm}$

Bar spacing - $s_v = 250 \text{ mm}$

Maximum bar spacing

[EN 1992-1-1, § 9.6.2 (3)]

$$s_{v,\max} = \min(3 \cdot b_{wo}; 400) = \min(3 \cdot 300; 400) = 400 \text{ mm}$$

$$\text{Single bar area} - A_{sv1} = \frac{\pi \cdot d_{bv}^2}{4} = \frac{3.141593 \cdot 10^2}{4} = 78.539816 \text{ mm}^2$$

$$\text{Reinforcement ratio} - \rho_v = \frac{2 \cdot A_{sv1}}{s_v \cdot b_{wo}} = \frac{2 \cdot 78.539816}{250 \cdot 300} = 0.002094395$$

Minimum reinforcement ratio - $\rho_{v,min} = 0.002$

[EN 1992-1-1, § 9.6.2 (1)]

Minimum reinforcement ratio for zones with compressive strain > 0.002

[§ 5.4.3.4.2 (11)]

$$\rho_{v,min} = 0.005$$

Horizontal web reinforcement

Bar diameter - $d_{bh} = 12 \text{ mm}$

Bar spacing - $s_h = 150 \text{ mm}$

Maximum bar spacing - $s_{h,\max} = 400 \text{ mm}$

[EN 1992-1-1, § 9.6.3 (2)]

$$\text{Single bar area} - A_{sh1} = \frac{\pi \cdot d_{bh}^2}{4} = \frac{3.141593 \cdot 12^2}{4} = 113.097336 \text{ mm}^2$$

$$\text{Reinforcement ratio} - \rho_h = \frac{2 \cdot A_{sh1}}{s_h \cdot b_{wo}} = \frac{2 \cdot 113.097336}{150 \cdot 300} = 0.005026548$$

Minimum reinforcement ratio

[EN 1992-1-1, § 9.6.3 (1)]

$$\rho_{h,min} = \max(0.25 \cdot \rho_v; 0.001) = \max(0.25 \cdot 0.002094395; 0.001) = 0.001$$

Transverse reinforcement in confined boundary elements

Characteristic yield strength - $f_{ywk} = 500 \text{ MPa}$

$$\text{Design yield strength} - f_{ywd} = \frac{f_{ywk}}{\gamma_s} = \frac{500}{1.15} = 434.782609 \text{ MPa}$$

Concrete cover to hoops - $c = 42 \text{ mm}$

Hoop diameter - $d_{bw} = 8 \text{ mm}$

Minimum diameter

[EN 1992-1-1, § 9.5.3 (1)]

$$d_{bw,min} = \max(6; 0.25 \cdot d_{bL}) = \max(6; 0.25 \cdot 25) = 6.25 \text{ mm}$$

Hoop diameter check:

$d_{bw} = 8 \geq d_{bw,min} = 6.25 \text{ mm}$. The check is satisfied! ✓

Critical region height

[§ 5.4.3.4.2 (1)]

$$h_{cr_} = \max\left(l_w; \frac{h_w}{6}\right) = \max\left(4000; \frac{19000}{6}\right) = 4000 \text{ mm}$$

Must not be greater than

$$h_{cr,max} = \min(2 \cdot l_w; h_s) = \min(2 \cdot 4000; 3820) = 3820 \text{ mm}, \text{ for number of storeys } n_s = 6 \leq 6$$

$$h_{cr} = \min(h_{cr_}; h_{cr,max}) = \min(4000; 3820) = 3820 \text{ mm}$$

Shear wall dimensions check

[§ 5.1.2 (1)]

$$\frac{l_w}{b_{wo}} = \frac{4000}{300} = 13.333333 \geq 4. \text{ The check is satisfied! ✓}$$

$$\text{Minimum thickness} - b_{w,min} = \max\left(150; \frac{h_s}{20}\right) = \max\left(150; \frac{3820}{20}\right) = 191 \text{ mm}$$

[§ 5.4.1.2.3 (1)]

$b_{wo} = 300 \text{ mm} \geq b_{w,min} = 191 \text{ mm}$. The check is satisfied! ✓

Confined boundary element length

[§ 5.4.3.4.2 (6)]

$$l_c = h_c - (d_{bw} + 2 \cdot c) = 875 - (8 + 2 \cdot 42) = 783 \text{ mm}$$

Minimum confined boundary element length

$$l_{c,min} = \max(0.15 \cdot l_w; 1.5 \cdot b_c) = \max(0.15 \cdot 4000; 1.5 \cdot 300) = 600 \text{ mm}$$

$l_c = 783 \text{ mm} \geq l_{c,min} = 600 \text{ mm}$. The check is satisfied! ✓

Minimum confined boundary element thickness

[§ 5.4.3.4.2 (10)]

For $l_c = 783 \text{ mm} \leq \max(2 \cdot b_c; 0.2 \cdot l_w) = \max(2 \cdot 300; 0.2 \cdot 4000) = 800 \text{ mm}$:

$$b_{c,min} = \max\left(\frac{h_s}{15}; 200\right) = \max\left(\frac{3820}{15}; 200\right) = 254.666667 \text{ mm}$$

$b_c = 300 \text{ mm} \geq b_{c,min} = 254.666667 \text{ mm}$. The check is satisfied! ✓

Check for normalized axial load

[§ 5.4.3.4.1 (2)]

$$\nu_d = \frac{N_{Ed}}{A_c \cdot f_{cd}} \cdot 10^3 = \frac{2254}{1200000 \cdot 16.666667} \cdot 10^3 = 0.1127$$

$\nu_d = 0.1127 \leq 0.4$. The check is satisfied! ✓

Design anchorage length

$\eta_1 = 1$ - when good conditions are provided

$\eta_2 = 1$ - for $d_{bL} = 25 \leq 32 \text{ mm}$

$$f_{ctd} = \frac{\alpha_{ct} \cdot f_{ctk,005}}{\gamma_c} = \frac{1 \cdot 1.795475}{1.5} = 1.196983 \text{ MPa}$$

$$f_{bd} = 2.25 \cdot \eta_1 \cdot \eta_2 \cdot f_{ctd} = 2.25 \cdot 1 \cdot 1 \cdot 1.196983 = 2.693212 \text{ MPa}$$

[EN 1992-1-1, § 8.4.2 (2)]

$$\sigma_{sd} = f_{yd} = 434.782609 \text{ MPa}$$

$$l_{b,rqd} = \frac{d_{bL}}{4} \cdot \frac{\sigma_{sd}}{f_{bd}} = \frac{25}{4} \cdot \frac{434.782609}{2.693212} = 1008.977825 \text{ mm}$$

[EN 1992-1-1, § 8.4.3 (2)]

$$\alpha_1 = 1, \alpha_2 = 1, \alpha_3 = 1, \alpha_5 = 1, \alpha_6 = 1.5$$

[EN 1992-1-1, Table 8.2]

$$l_{0_} = \alpha_1 \cdot \alpha_2 \cdot \alpha_3 \cdot \alpha_5 \cdot \alpha_6 \cdot l_{b,rqd} = 1 \cdot 1 \cdot 1 \cdot 1.5 \cdot 1008.977825 = 1513.466738 \text{ mm}$$

[EN 1992-1-1, § 8.7.3 (1)]

$$l_{0,min} = \max(0.3 \cdot \alpha_6 \cdot l_{b,rqd}; 15 \cdot d_{bL}; 200) = \max(0.3 \cdot 1.5 \cdot 1008.977825; 15 \cdot 25; 200) = 454.040021 \text{ mm}$$

$$l_0 = \text{round}(\max(l_{0_}; l_{0,min})) = \text{round}(\max(1513.466738; 454.040021)) = 1513 \text{ mm}$$

Confined core dimensions (between centerlines of hoops)

$$b_0 = b_c - (d_{bw} + 2 \cdot c) = 300 - (8 + 2 \cdot 42) = 208 \text{ mm}$$

$$h_0 = h_c - (d_{bw} + 2 \cdot c) = 875 - (8 + 2 \cdot 42) = 783 \text{ mm}$$

Maximum bar spacing

$$d_{b1} = \frac{h_c - 2 \cdot (d_{bw} + c) - d_{bL}}{n_{b1} - 1} = \frac{875 - 2 \cdot (8 + 42) - 25}{6 - 1} = 150 \text{ mm}$$

$$d_{b2} = \frac{b_c - 2 \cdot (d_{bw} + c) - d_{bL}}{n_{b2} - 1} = \frac{300 - 2 \cdot (8 + 42) - 25}{3 - 1} = 87.5 \text{ mm}$$

Maximum distance between consecutive longitudinal bars engaged by hoops

$$d_{h,max} = 200 \text{ mm}$$

[§ 5.4.3.4.2 (9)]

Distance between bars engaged by hoops

$$n_{h1} = \max\left(\text{floor}\left(\frac{d_{h,max}}{d_{b1}}\right); 1\right) = \max\left(\text{floor}\left(\frac{200}{150}\right); 1\right) = 1$$

$$n_{h2} = \max\left(\text{floor}\left(\frac{d_{h,max}}{d_{b2}}\right); 1\right) = \max\left(\text{floor}\left(\frac{200}{87.5}\right); 1\right) = 2$$

Distance between bars engaged by hoops

$$d_{h1} = n_{h1} \cdot d_{b1} = 1 \cdot 150 = 150$$

$$d_{h2} = n_{h2} \cdot d_{b2} = 2 \cdot 87.5 = 175$$

Distance between bars engaged by hoops

$$n_{h1} = \text{round}\left(\frac{(n_{h1} - 1) \cdot d_{b1}}{d_{h1}}\right) = \text{round}\left(\frac{(6 - 1) \cdot 150}{150}\right) = 5$$

$$n_{h2} = \text{round}\left(\frac{(n_{b2}-1) \cdot d_{b2}}{d_{h2}}\right) = \text{round}\left(\frac{(3-1) \cdot 87.5}{175}\right) = 1$$

Hoop spacing in the critical region

$$s_{cr} = \min\left(\frac{b_0}{2}; 8 \cdot d_{bl}; 175\right) = \min\left(\frac{208}{2}; 8 \cdot 25; 175\right) = 104 \text{ mm}$$

[§ 5.4.3.4.2 (9)]

Hoop spacing in lap zone

$$s_l = \min\left(100; \frac{b_c}{4}\right) = \min\left(100; \frac{300}{4}\right) = 75 \text{ mm}$$

[§ 5.6.3 (3), c)]

Hoop spacing outside lap zone

$$s = \min(b_c; 20 \cdot d_{bl}; 400) = \min(300; 20 \cdot 25; 400) = 300 \text{ mm}$$

[EN 1992-1-1, § 9.5.3 (3)]

Transverse reinforcement in the lap zone

Required area of one leg

$$A_{st} = s_l \cdot \frac{d_{bl}}{50} \cdot \frac{f_{yld}}{f_{ywd}} = 75 \cdot \frac{25}{50} \cdot \frac{434.782609}{434.782609} = 37.5 \text{ mm}^2$$

[§ 5.6.3 (4)]

Provided area of one leg

$$A_{sw1} = \frac{\pi \cdot d_{bw}^2}{4} = \frac{3.141593 \cdot 8^2}{4} = 50.265482 \text{ mm}^2$$

Design check: $A_{sw1} = 50.265482 \text{ mm}^2 \geq A_{st} = 37.5 \text{ mm}^2$. The check is satisfied! ✓

Check for bar diameters > 20 mm:

Number of legs in the outer 1/3 of lap zone

$$n_w = \text{round}\left(\frac{2 \cdot l_0}{3 \cdot s_l}\right) = \text{round}\left(\frac{2 \cdot 1513}{3 \cdot 75}\right) = 13$$

Total area of legs in the outer 1/3 of lap zone

$$\Sigma A_{sw} = A_{sw1} \cdot n_w = 50.265482 \cdot 13 = 653.451272$$

Design check: $\Sigma A_{sw} = 653.451272 \text{ mm}^2 \geq A_{s1} = 490.873852 \text{ mm}^2$

[EN 1992-1-1 § 8.7.4.1 (3)]

An additional hoop is required for compressed bars

at $4 \cdot d_{bl} = 4 \cdot 25 = 100 \text{ mm}$ from the end of the lap zone.

[EN 1992-1-1 § 8.7.4.2 (1)]

Detailing for local ductility in the critical region

Total length of confining links

$$\Sigma l_i = (n_{h1} + 1) \cdot b_0 + (n_{h2} + 1) \cdot h_0 = (5 + 1) \cdot 208 + (1 + 1) \cdot 783 = 2814$$

Mechanical volumetric ratio of confining hoops within the critical region

$$\omega_d = \frac{A_{sw1} \cdot \Sigma l_i}{b_0 \cdot h_0 \cdot s_{cr}} \cdot \frac{f_{ywd}}{f_{cd}} = \frac{50.265482 \cdot 2814}{208 \cdot 783 \cdot 104} \cdot \frac{434.782609}{16.666667} = 0.2178507$$

The minimum value is 0.08.

[§ 5.4.3.2.2 (8)]

Design check: $\omega_d = 0.2178507 \geq 0.08 = 0.08$. The check is satisfied! ✓

Sum of the squares of the distances between consecutive engaged bars

$$\Sigma b2_i = 2 \cdot (n_{h1} \cdot d_{h1}^2 + n_{h2} \cdot d_{h2}^2) = 2 \cdot (5 \cdot 150^2 + 1 \cdot 175^2) = 286250$$

Confinement effectiveness factors for bars and links

$$\alpha_n = 1 - \frac{\Sigma b2_i}{6 \cdot b_0 \cdot h_0} = 1 - \frac{286250}{6 \cdot 208 \cdot 783} = 0.7070664$$

$$\alpha_s = \left(1 - \frac{s_{cr}}{2 \cdot b_0}\right) \cdot \left(1 - \frac{s_{cr}}{2 \cdot h_0}\right) = \left(1 - \frac{104}{2 \cdot 208}\right) \cdot \left(1 - \frac{104}{2 \cdot 783}\right) = 0.7001916$$

$$\alpha = \alpha_n \cdot \alpha_s = 0.7070664 \cdot 0.7001916 = 0.495082$$

Analysis results

Fundamental period of first vibration mode - $T_1 = 0.6795 \text{ s}$

Upper limit period of constant spectral acceleration - $T_C = 0.4 \text{ s}$

Basic behavior factor value - $q_0 = 3$

Design bending moment - $M_{Ed} = 9591 \text{ kNm}$

Bending moment capacity - $M_{Rd} = 13268 \text{ kNm}$

(The above values refer to the section above the base)

Curvature ductility factor

$$\mu_{\Phi} = 2 \cdot q_0 \cdot \frac{M_{Ed}}{M_{Rd}} - 1 = 2 \cdot 3 \cdot \frac{9591}{13268} - 1 = 3.337202 \text{ - for } T_1 \geq T_C$$

[§ 5.2.3.4 (3)]

For steel class B, ductility factor is increased by 50% - $\mu_{\Phi} = 5.005803$

[§ 5.2.3.4 (4)]

$$\text{Design value of steel yield strain} - \varepsilon_{sy,d} = \frac{f_{yd}}{E_s} = \frac{434.782609}{200000} = 0.002173913$$

Mechanical ratio of vertical web reinforcement

$$\omega_v = \rho_v \cdot \frac{f_{yd}}{f_{cd}} = 0.002094395 \cdot \frac{434.782609}{16.666667} = 0.05463639$$

Design check: $a\omega_d \geq a\omega_{d,\min} = 30 \cdot \mu_{\Phi} \cdot (v_d + \omega_v) \cdot \varepsilon_{sy,d} \cdot b_c / b_0 - 0.035$ [§ 5.4.3.4.2 (4)]

$$a\omega_d = \alpha \cdot \omega_d = 0.495082 \cdot 0.2178507 = 0.1078539$$

$$a\omega_{d,\min} = 30 \cdot \mu_{\Phi} \cdot (v_d + \omega_v) \cdot \varepsilon_{sy,d} \cdot \frac{b_c}{b_0} - 0.035 = 30 \cdot 5.005803 \cdot (0.1127 + 0.05463639) \cdot 0.002173913 \cdot \frac{300}{208} - 0.035 = 0.04379262$$

The required curvature ductility is provided: $a\omega_d = 0.1078539 \geq a\omega_{d,\min} = 0.04379262 . \checkmark$

Ultimate strain of confined concrete

$$\varepsilon_{cu2,c} = 0.0035 + 0.1 \cdot a\omega_d = 0.0035 + 0.1 \cdot 0.1078539 = 0.01428539$$

Neutral axis depth at ultimate curvature

$$x_u = (v_d + \omega_v) \cdot l_w \cdot \frac{b_c}{b_0} = (0.1127 + 0.05463639) \cdot 4000 \cdot \frac{300}{208} = 965.402273 \text{ mm}$$

Confined boundary element length

$$l_{c,req} = x_u \cdot \left(1 - \frac{\varepsilon_{cu2}}{\varepsilon_{cu2,c}}\right) = 965.402273 \cdot \left(1 - \frac{0.0035}{0.01428539}\right) = 728.873416 \text{ mm}$$

Design check: $l_c = 783 \text{ mm} \geq l_{c,req} = 728.873416 \text{ mm}$. The check is satisfied! \checkmark

NOTE: All references are according to EN 1998-1, unless noted otherwise.

@hydrostructai.com