QT-Opt: Scalable Deep Reinforcement Learning for Vision-Based Robotic Manipulation

arXiv:1806.10293, Kalashnikov et al, 2018.

Sumamrized by Hyecheol (Jerry) Jang

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RL Paper Study, Jun. 29. 2020



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 - Reinforcement Learning
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 - Deep Learning
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 Provide ability to make decision in long-term, using previous experiences in complex and robust scenarios
- Combining two techniques
 - Able to learn policy continuously from their experience
 - No need for manual engineering, use data they collects



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 - Hardness of object (Soft or Hard)
 - Surface Characteristics (Slippery, Sticky, . . .)
 - Color Variation
 - Shape Variation
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- Noise of sensors
 - ⇒ Still hard to handle though we have sufficiently large training set
 - ⇒ Collecting those training set is expensive (real experiments)



- Focused on learning narrow, individual tasks
 - hitting a ball
 - opening door
 - throwing objects
 - ...



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 - \Rightarrow Use **Grasping** to achieve *generalization*



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 - ⇒ Use Grasping to achieve generalization
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 - **1** Observe the scene (*Normally, using a depth camera*)
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 - Different with how humans and animals behave
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 - ⇒ Where this researches start!!

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Use Reinforcement Learning with Deep Neural Network to perform pre-grasp manipulation, response to dynamic disturbances, and learn grasping in a generic framework that makes minimal assumptions about the task

Goal: Constraint/Condition + Literature Review



- Closed-loop condition (With feedback, Morrison, et al.)
 - For the other papers work on closed-loop grasping, they deals with servoing problems.
 - This paper focuses on making generalized RL algorithm
 - In practice, it makes Kalashnikov et al.'s method (this method) to autonomously acquire complicated grasping strategy

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- Self-supervised learning task
 - Compare to prevoius work(by Zeng et al.), Kalashnikov et al. utilize more general action space
 - Actions consist of end-effector Cartesian motion and gripper opening/closing

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- **Self-supervised** learning task
 - Compare to prevoius work(by Zeng et al.), Kalashnikov et al. utilize more general action space
 - Actions consist of end-effector Cartesian motion and gripper opening/closing
- Observation comes from a single RGB camera over the sholder
 - Many current grasping system utilizes depth sensing
 - Using wrist-mounted cameras

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 - partially observed formulation (POMDP) is more general.
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 - However, assuming current observation contains all necessary information for this task, it is sufficient to use MDP.
- MDP have a general and powerful formalism for decision making problems.
 - However, it is hard to train
- For each step of MDP:
 - **1** Observes Image from robot's camera (see Fig. 1)
 - 2 choose a gripper command, Reward:
 - failed grasp: reward of 0
 - successful grasp: reward of 1
 Defined success when the robot holds the object above a certain height



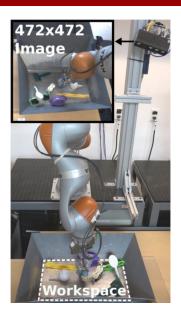


Figure 1: Configuration of robot cell, with a sample observation image on top-right box

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- Using scalable off-policy algorithm based on Q-learning
 - actor-critic algorithm are popular for handling continuous actions
 - However, Kalashnikov et al. found scalable and more stable ways to train only Q-function
- Large Dataset and Network (See Fig. 2)
 - Kalashnikov et al. devised distributed training system (with 7 robots)
 - Asynchronously update target values, collect on-policy data, reloads off-policy data from previous experiences, and train network on both data stream.

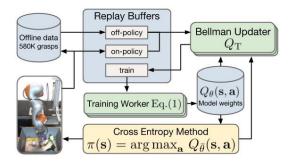


Figure 2: Distributed Reinforcement Learning infrastructure for QT-Opt.

Optional: On-policy vs Off-policy Poole et al.



• On-policy Learning learns the value of the policy being carried out by the agent, including the exploration steps.

e.g. SARSA(State-Action-Reward-State-Action) (See Fig. 3)

Optional: On-policy vs Off-policy Poole et al.



- On-policy Learning learns the value of the policy being carried out by the agent, including the exploration steps.
 - e.g. SARSA(State-Action-Reward-State-Action) (See Fig. 3)
- Off-policy Learning learns the value of the optimal policy independently of the agent's action
 - e.g. Q-Learning (See Fig. 4)

Optional: On-policy vs Off-policy Poole et al.



```
controller SARSA(S,A,γ,α)
inputs:
       S is a set of states
       A is a set of actions
       y the discount
       \alpha is the step size
internal state:
                                                                               controller Q-learning(S,A,y,a)
       real array OS.AI
                                                                               2:
                                                                                          Inputs
       previous state s
                                                                               3:
                                                                                                  S is a set of states
       previous action a
                                                                                                  A is a set of actions
begin
                                                                               5:
                                                                                                  y the discount
       initialize O/S.A/ arbitrarily
                                                                               6.
                                                                                                  \alpha is the step size
                                                                               7:
                                                                                          Local
       observe current state s
                                                                                                  real array O/S.A1
                                                                               8:
       select action a using a policy based on O
                                                                                                  previous state s
                                                                               9:
       repeat forever:
                                                                               10:
                                                                                                   previous action a
              carry out an action a
                                                                                           initialize Q/S,A/ arbitrarily
                                                                               11:
              observe reward rand state s'
                                                                               12.
                                                                                           observe current state s
              select action a'using a policy based on O
                                                                               13.
                                                                                           repeat
              Q[s,a] \leftarrow Q[s,a] + \alpha(r + \gamma Q[s',a'] - Q[s,a])
                                                                                                   select and carry out an action a
                                                                               14
               5-5'
                                                                               15:
                                                                                                   observe reward r and state s'
                                                                                                   Q[s,a] \leftarrow Q[s,a] + \alpha(r + \gamma \max_{a'} Q[s',a'] - Q[s,a])
               a = a'
                                                                               16:
                                                                               17:
                                                                                                   5 -5'
       end-repeat
                                                                               18
                                                                                           until termination
end
```

Figure 3: SARSA Algorithm

Figure 4: Q-Learning Algorithm

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QT-Opt



- Continuous action version of Q-Learning
 - For scalable learning and optimized for stability
 - To handle large amount of off-policy image data for complex tasks

QT-Opt: Revisit Q-Learning



- state: $s \in \mathcal{S}$ (Image Observations)
- action: $a \in A$ (Robot Arm Motions and Gripper commands)
- at each time step t
 - Choose an action
 - 2 transition to new state
 - **3** receive reward $\gamma(s_t, a_t)$

QT-Opt: Revisit Q-Learning



• Need to solve for Optimal Q-function: Minimize Bellman Error

$$\mathcal{E}(\theta) = \mathbb{E}_{(\mathsf{s},\mathsf{a},\mathsf{s}') \sim p(\mathsf{s},\mathsf{a},\mathsf{s}')}[\mathcal{D}(\mathcal{Q}_{\theta}(\mathsf{s},\mathsf{a}),\mathcal{Q}_{\mathcal{T}}(\mathsf{s},\mathsf{a},\mathsf{s}'))]$$

Where $Q_T(s, a, s') = r(s, a) + \gamma V(s')$ (target value)

- D: divergence metric (squared difference for Q-Learning)
- Expectation is taken under the distribution over all previously observed transition



- Use two target network to improve stability
 - Maintaining two lagged version of the parameter vector $heta, ar{ heta}_1, ar{ heta}_2$
 - $\bar{\theta_1}$: exponential moving averaged version of θ , averaging constant: 0.9999
 - $ar{ heta_2}$: lagged version of $ar{ heta_1}$, lagged by 6000 gradient steps



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- Compute target value by $V(s') = \min_{i=1,2} \mathcal{Q}_{\bar{\theta_i}}(s', arg \max_{a'} \mathcal{Q}_{\bar{\theta_1}}(s', a'))$



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- After collects samples from environment interaction, then perform off-policy training on all samples collected
 - Problem: Large-scale learning (Technically Difficult)
 - Solution: Use Parallel Asynchronous version (which leads ability to scale up the process)

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 - using a second network that "amortize" the maximization
 - constraining the Q-function to be convex in a, so that makes the function to easily find maximum analytically
- problem of previous solutions
 - Unstable: problematic for large-scale RL tasks where running hyperparameter sweeps is very expensive
 - Action-convex value functions are poor fit for complex manipulation tasks



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- the Bellman equation is evaluated with stocastic optimization
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 - easy to parallelize
 - moderately robust to local optima



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 - each training workers compute gradient that sent to parameter server asynchronously



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 - each training workers compute gradient that sent to parameter server asynchronously
 - Empirically, it requires up to 15M gradient steps to train effective Q-function due to complexity of the task and the size of dataset and model



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Environment Settings: Overview



- Policy
 - locate object
 - position for grasping (pre-grasping manipulation, if needed)
 - pick up (regrasping, if needed)
 - Pull up the object
 - signal thermination

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 - pick up (regrasping, if needed)
 - Pull up the object
 - signal thermination
- Reward
 - only indicates whether or not an object was successfully picked up
- End-to-End approach of grasping!!
 - no prior knowledge about object, physics, or motion planning
 - model itself autonomously extract the knowledges from data

Environment Settings: MDP for grapsing



- state observation $s \in S$ includes:
 - robot's current camera observation (RGB image, res: 472×472) from over-the-sholder single-lens camera
 - current status of gripper (binary)
 - vertical position of the gripper relative to the floor

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 - current status of gripper (binary)
 - vertical position of the gripper relative to the floor
- action $a = (t, r, g_{open}, g_{close}, e) \in A$ includes:
 - vector in Cartesian space $t \in \mathbb{R}^3$ (desired change in the gripper position)
 - change in azimuthal angle via sine-cosine encoding, $r \in \mathbb{R}^2$
 - binary gripper open and close command, g_{open}, g_{close}
 - termination command, e

Environment Settings: Reward Function



- 1: if gripper carries the object up above certain height at the end of the episode
- 0: otherwise

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- penalty (-0.05): for all time steps prior to termination
 - emits termination action
 - exceed the maximum number of time steps(20)

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- 0: otherwise
- penalty (-0.05): for all time steps prior to termination
 - emits termination action
 - exceed the maximum number of time steps(20)
- delayed and sparse reward function is challenging, but more practical for automated self-supervision

Environment Settings: Q-function



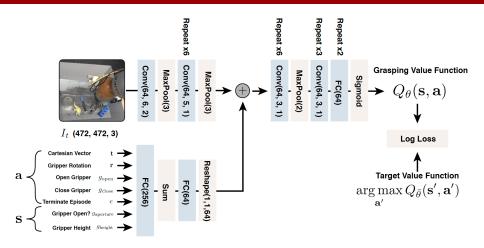


Figure 5: Neural Network Architecture for Q-Fuction. It has total of 1.2M parameters. The image is processed with convolution filters, and the other inputs are processed by fully connected layer, then concatenated with the image

Environment Settings: Data Collection



- Need to collect data on sufficiently large and diverse set of objects
- Use multiple robots and multiple experiments to collect such data
 - Took four months, 800 Robot hrs
 - Collected during multiple separated experiments, and each experiment reused the data from the previous one

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 - Success Rate: Around 15-30%
 - Switching to QT-Opt once it reach 50% of success rate

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 - Switching to QT-Opt once it reach 50% of success rate
- Other Conditions
 - Using seven LBR IIWA robots
 - with 4-10 objects per robots
 - objects were replaced every 4 hours during business hours
 - Use different objects during test



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