

## 1 Opgave 1

- True, pick  $m = n^2 + 1$
- True, pick  $n = 0$
- True, pick  $x = 3, y = 1$ .
- False
- True
- True
- False

## 2 Opgave 2

- 1,2,5,6
- 2,4,5,6,7
- 1,3,4,6,7,8
- 3,4,5,6,7
- 2,3,4,5,7,8
- 1,4
- 2,3,4,5,6,7,8
- 1,2,3,4,5,6

## 3 Opgave 3

b)

$$(p \rightarrow q) \vee (\neg p \rightarrow q) \equiv (\neg p \vee q) \vee (p \vee q) \equiv (\neg p \vee p) \vee (q \vee q) \equiv \mathbf{T} \vee q \equiv \mathbf{T}$$

## 4 Opgave 4

Use floor division and modulo operator

- $1 \mid 66 \mid 1 \mid 66$
- $-2 \mid 21 \mid -2 \mid 21$
- $-5 \mid 2 \mid -5 \mid 2$
- $11 \mid 8 \mid 11 \mid 8$

## 5 Opgave 5

a)

$$a_2 = 6 \cdot 3 - 9 \cdot 1 = 9$$

$$a_3 = 6 \cdot 9 - 9 \cdot 3 = 54 - 27 = 27$$

$$a_4 = 6 \cdot 27 - 9 \cdot 9 = 81$$

b)

$$n = 0, a_0 = 3^0 = 1$$

$$n = 1, a_1 = 3^1 = 3$$

So the basis steps are correct.

c)

We now assume that  $a_j = 3^j$  for any  $j \leq k$

d)

Now we have to show that  $a_{k+1} = 3^{k+1}$ .

By using the formula, we can write:

$$a_{k+1} = 6a_k - 9 \cdot a_{k-1}$$

$$= 6 \cdot 3^k - 9 \cdot 3^{k-1} = 2 \cdot 3 \cdot 3^k - 3^2 \cdot 3^{k-1} = 3^{k+1}(2 - 1) = 3^{k+1}$$

## 6 Opgave 6

Let  $A = \{1, 2\}$ ,  $B = \{2, 3\}$ .

$$A \cap B = \{2\}$$

$$A + B = \{1, 2, 2, 3\}$$

$$A + B - (A \cap B) = \{1, 2, 2, 3\} - \{2\} = \{1, 2, 3\}$$