

4211 Homework 9

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1

(a)

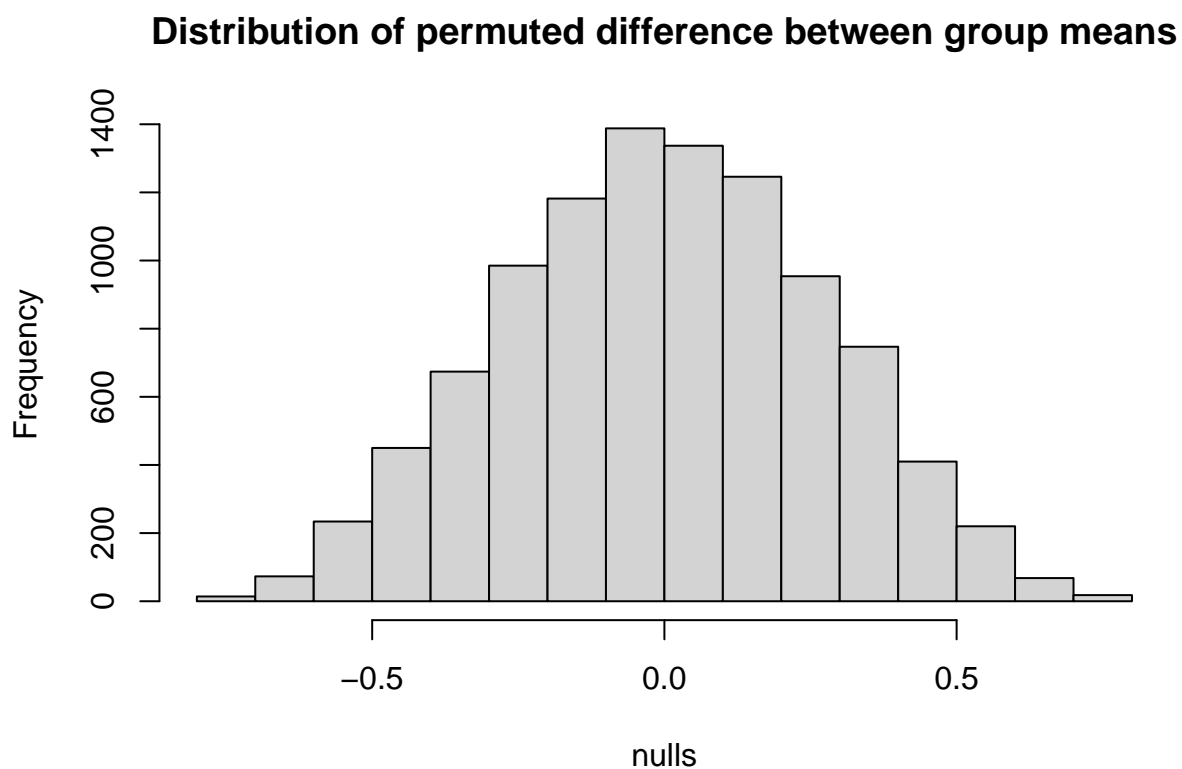
```
x = data.frame(
  msce = c(8.27,8.20,8.25,8.14,9.00,8.10,7.20,8.32,7.70,8.50,9.48,8.65,8.16,8.83,7.76,8.63),
  eth = c(rep(0,9), rep(1,7))
)

permtest = function(x,y){
  xstar = sample(x)
  return(mean(y[xstar==1])-mean(y[xstar==0]))
}

set.seed(488103)
observeddiff = mean(x$msce[x$eth==1]-x$msce[x$eth==0])

## Warning in x$msce[x$eth == 1] - x$msce[x$eth == 0]: longer object length is not
## a multiple of shorter object length

nulls = replicate(10000, permtest(x$eth, x$msce))
hist(nulls, main = "Distribution of permuted difference between group means")
```



(b)

```
mean(abs(nulls)>abs(observeddiff))
```

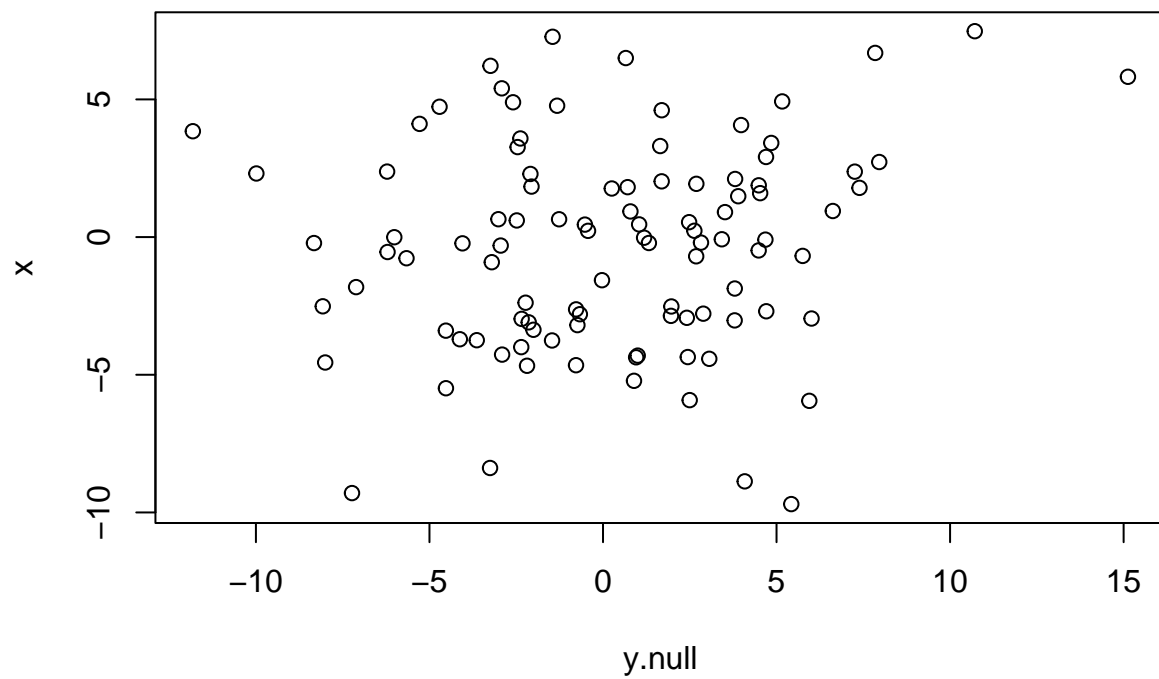
```
## [1] 0.0442
```

The difference is significant at the level $\alpha = 0.05$.

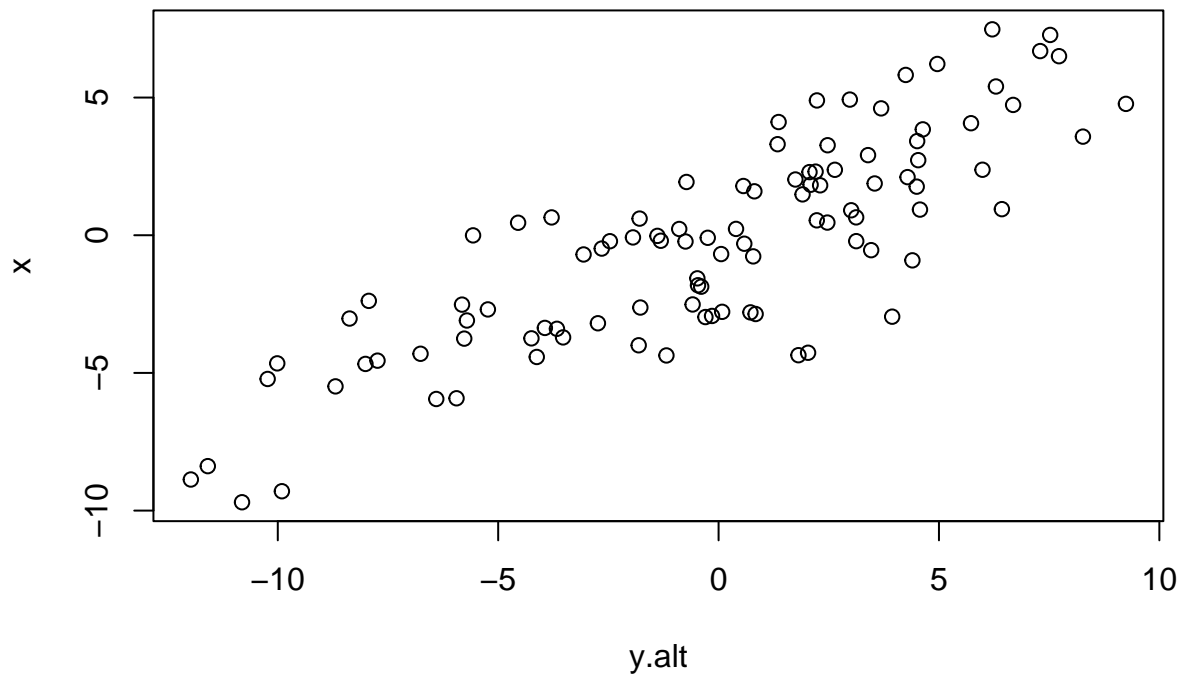
2

(a)

```
set.seed(4211)
x=rnorm(100,0,4)
y.null=rnorm(100,0,5) # null hypothesis
y.alt=x+rnorm(100,0,3) # alternative hypothesis
## from a location model with normal errors
plot(y.null, x)
```



```
plot(y.alt, x)
```



```
cor.test(x, y.null)
```

```
##
## Pearson's product-moment correlation
##
## data:  x and y.null
## t = 1.5235, df = 98, p-value = 0.1309
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.04567892  0.33841165
## sample estimates:
##      cor
## 0.1521039
```

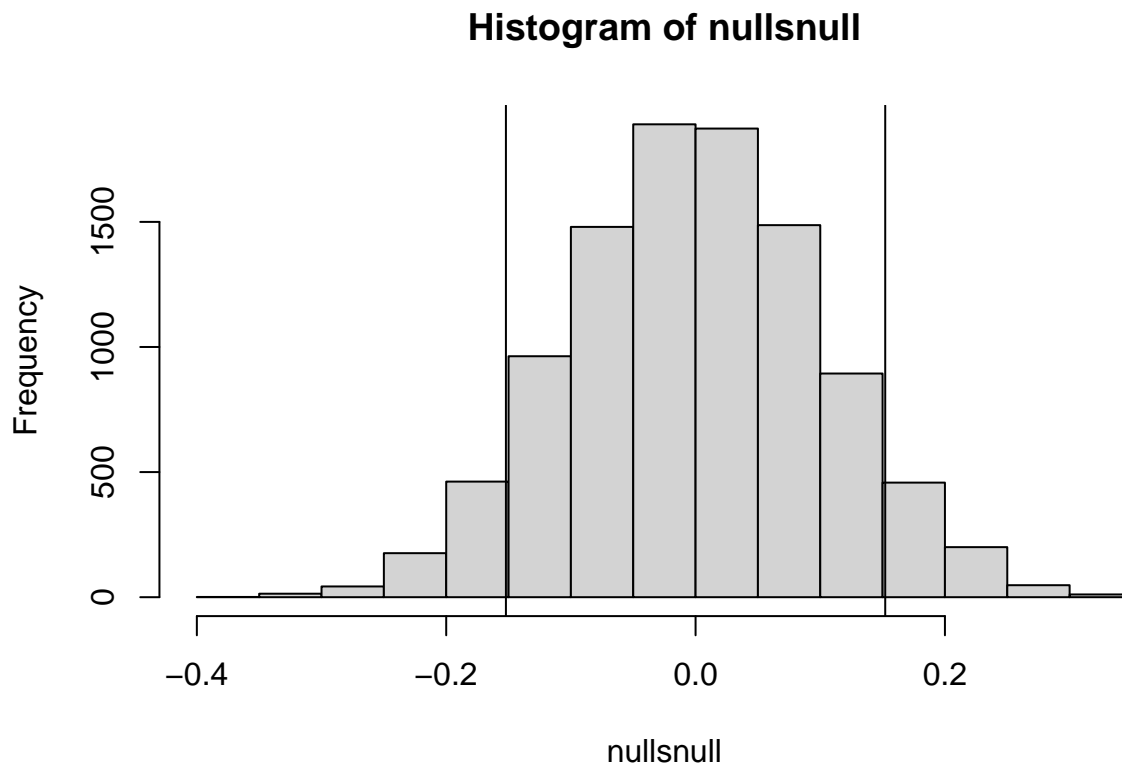
```
cor.test(x, y.alt)
```

```
##
## Pearson's product-moment correlation
##
## data:  x and y.alt
## t = 14.757, df = 98, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
##  0.7576060 0.8828581
```

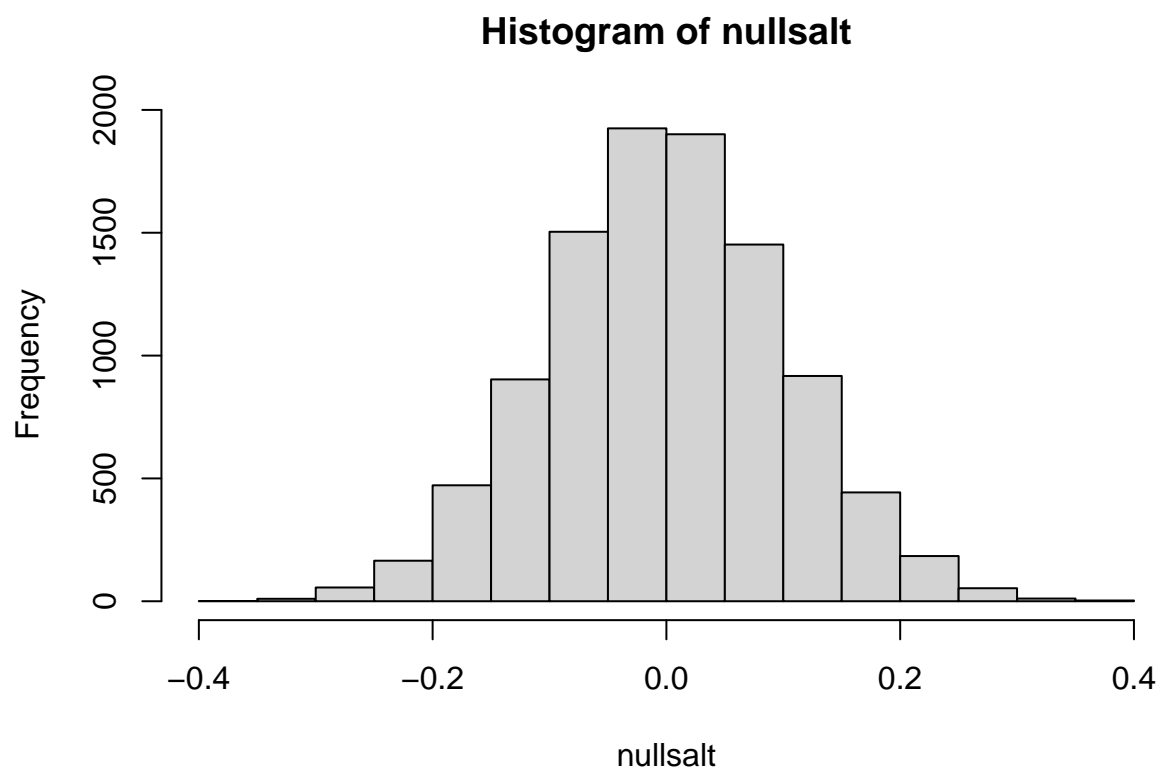
```
## sample estimates:  
##      cor  
## 0.8304473
```

(b)

```
permtest = function(x,y){  
  xstar = sample(x)  
  return(cor(xstar, y))  
}  
  
set.seed(488103)  
observedcornull = cor(x, y.null)  
observedcoralt = cor(x, y.alt)  
nullsnull = replicate(10000, permtest(x, y.null))  
nullsalt = replicate(10000, permtest(x, y.alt))  
hist(nullsnull)  
abline(v=observedcornull)  
abline(v=-observedcornull)
```



```
hist(nullsalt)
```



```
mean(abs(nullsnull)>abs(observedcornull))
```

```
## [1] 0.1362
```

```
mean(abs(nullsalt)>abs(observedcoralt))
```

```
## [1] 0
```

3

(a)

```
bootstrap = function(x,y){  
  index = sample(1:length(x), replace = TRUE)  
  xstar = x[index]  
  ystar = y[index]  
  return(cor(xstar, ystar))  
}  
  
set.seed(488103)  
bootnull = replicate(10000, bootstrap(x, y.null))  
bootalt = replicate(10000, bootstrap(x, y.alt))  
var(bootnull)
```

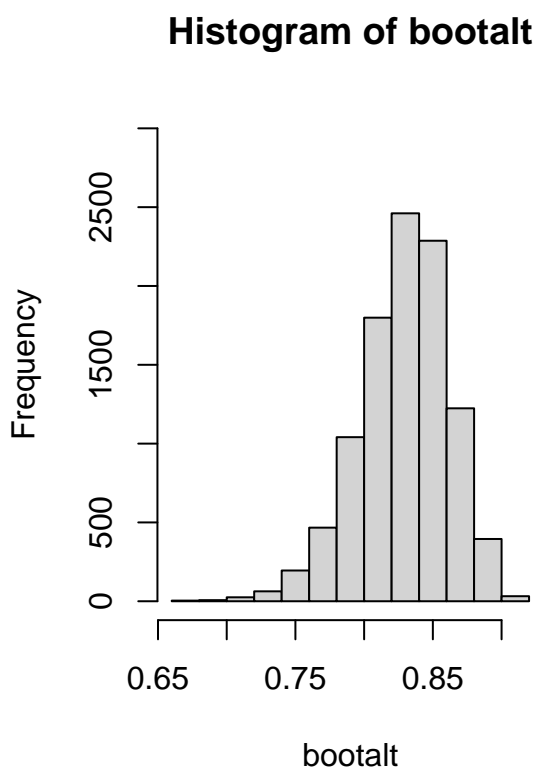
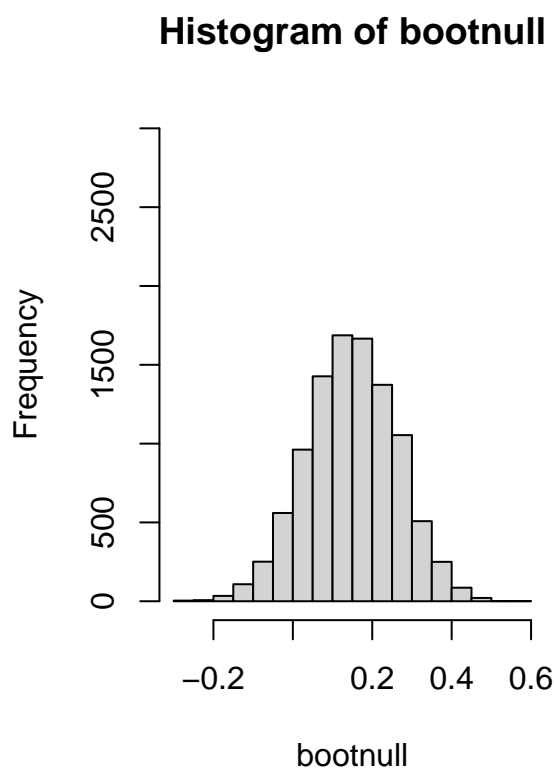
```
## [1] 0.01283102
```

```
var(bootalt)
```

```
## [1] 0.001072049
```

(b)

```
par(mfrow=c(1,2))  
hist(bootnull, ylim=c(0,3000))  
hist(bootalt, ylim=c(0,3000))
```



The distribution of correlation under the null hypothesis appears to be normally distributed about 1.5, while the distribution of correlation under the alternative hypothesis is skewed left, with a peak around 0.83.