

Stats for DS HW 5

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3.4.8

(a)

negative binomial

(b)

sample space = $\{5, 6, 7, \dots\}$

PMF = $f(x) = \text{choose}(x-1, 4)(0.05^5)(0.95^{(x-5)})$

(c)

```
1 - pnbinom(35, 5, 0.05)
```

```
## [1] 0.9519717
```

3.4.19

(a)

$$\text{Var}(X_1) = 2.6, \text{Var}(X_2) = 3.8$$

(b)

```
0.6*(dpois(0, 2.6))+0.4*(dpois(0,3.8))
```

```
## [1] 0.05351246
```

(c)

$$P(\text{by } X_2 \mid \text{no errors}) = P(\text{by } X_2 \text{ and no errors})/P(\text{no errors}) =$$

```
0.4*dpois(0,3.8)/(0.6*(dpois(0, 2.6))+0.4*(dpois(0,3.8)))
```

```
## [1] 0.1672192
```

3.5.1

(a)

```
1 - pexp(4, 1/6)
```

```
## [1] 0.5134171
```

(b)

variance = $1/36$

```
qexp(0.95, 1/6)
```

```
## [1] 17.97439
```

(c)

(i)

```
1 - pexp(5, 1/6)
```

```
## [1] 0.4345982
```

(ii)

6 years, because the exponential distribution is memoryless.

3.5.8

(a)

```
1 - pnorm(600, 500, 80)
```

```
## [1] 0.1056498
```

(b)

```
qnorm(0.99, 500, 80)
```

```
## [1] 686.1078
```

4.2.3

(a)

```
0.15+0.135+0.12+0.3
```

```
## [1] 0.705
```

```
0.12+0.135
```

```
## [1] 0.255
```

(b)

$f(x) = 0.42$ for $x=8$, 0.31 for $x=10$, 0.27 for $x=12$, 0 otherwise $f(y) = 0.48$ for $y=1.5$, 0.405 for $y=2$, 0.115 for $y=2.5$

(c)

```
(.135+.12)/(.135+.12+.15)
```

```
## [1] 0.6296296
```

4.2.8

(a)

Solving the double integral with bounds 0 to 1.5 and x to $3-x$ ($2e^{(-x-y)}$) $dydx$ results in $1-4e^{-3}$ or about 0.80

(b)

marginal pdf of y is $f(y) = (-2e^{(-y)}) * ((-2e^{(-y)}) - 1)$ for $y \geq 0$. marginal pdf of x is $f(x) = 2e^{(-2x)}$ for $x \geq 0$