```
**********plantilla**********

#include<bits/stdc++.h>
using namespace std;
#define all(v) (v).begin(),(v).end()
#define pb(x) push_back(x)

#define sqr(x) ((x)*(x))
#define mp(x,y) make_pair((x),(y))
#define fast_io() ios_base::sync_with_stdio(0);cin.tie(0);
#define fi first
#define se second
#define sz(v) ((int)v.size())
typedef pair<int,int> pii;
typedef vector<int> vi;
typedef long long ll;
typedef unsigned long long ull;
typedef long double ld;


int main(){
     //fast_io();

     return 0;
}
```

```
**************************BIG-INTEGER************************
import java.math.BigInteger;
import java.util.Scanner;
/**
 * Created by ADVANCE on 24/10/2015.
 */
public class dasd {
    public static void main(String[] args) {
        Scanner s=new Scanner (System.in);
        BigInteger num=s.nextBigInteger();
        BigInteger[] factoriales= new BigInteger[1040];
        BigInteger aux1=new BigInteger("1");
        factoriales[0]=aux1;
        for (int i=1;i<=520;i++){
            BigInteger _i= new BigInteger(Integer.toString(i));
            factoriales[i]=factoriales[i-1].multiply(_i);
        }
        for(int i=1;i<520;i++){
            int
res=num.compareTo((factoriales[2*i].divide((factoriales[i].multipl
y(factoriales[i+1])))));
            if(res==0){
                System.out.println(i+2);
            }
        }
        System.out.println(factoriales[5]);

    }
}
************************************************************
```

```
import java.math.BigInteger;
import java.util.Scanner;
import java.io.*;
import java.math.*;

/**
 * Created by ADVANCE on 24/10/2015.
 */
public class dasd {
    public static void main(String[] args) {
        Scanner s=new Scanner (System.in);
        BigInteger num1=s.nextBigInteger();
        BigInteger num2=s.nextBigInteger();
        BigInteger n=s.nextBigInteger();
        BigInteger[] fib= new BigInteger[21];
        fib[1]=num1;
        fib[2]=num2;
        for (int i=3;i<=20;i++){
            BigInteger _i= new BigInteger(Integer.toString(i));
            fib[i]=((fib[i-1].multiply(fib[i-1]))).add(fib[i-2]);
        }

        System.out.println(fib[n.intValue()]);
    }
}
```

```
**********************BIT**************************+++

const int INF=(1<<29);


struct FT{
      int BIT[100002];
      FT(){
            for(int i=0;i<100002;i++) BIT[i]=INF;
      }
      void update(int n,int val){
            while(n<=100002){
                  BIT[n]=min(val,BIT[n]);
                  n+=(n & -n);
            }
      }
      int query(int n){
            int mini=INF;
            while(n){
                  mini=min(mini,BIT[n]);
                  n-=(n & - n);
            }
            return mini;
      }
};

int main(){
      fast_io();
      int t;cin>>t;
      while(t>0){
            t--;
            FT BIT;
            int n;cin>>n;
            vector< pair<int,pii> > v;
            for(int i=0;i<n;i++){
                  int a,b,c;cin>>a>>b>>c;
                  v.pb( mp( a, mp( b,c ) ) );
            }
            sort(all(v));
            int cont=0;
            for(int i=0;i<sz(v);i++){
                  int mini=BIT.query(v[i].se.fi);
                  if(mini < v[i].se.se) cont++;
                  else BIT.update(v[i].se.fi,v[i].se.se);
            }
            cout<<(n-cont)<<endl;
      }


      return 0;
}
```

```
********************GEOMETRY*****************************

#define EPS 1e-8
#define PI acos(-1)
#define Vector Point

struct Point
{
    double x, y;
    Point(){}
    Point(double a, double b) { x = a; y = b; }
    double mod2() { return x*x + y*y; }
    double mod()  { return sqrt(x*x + y*y); }
    double arg()  { return atan2(y, x); }
    Point ort()   { return Point(-y, x); }
    Point unit()  { double k = mod(); return Point(x/k, y/k); }
};
Point operator +(const Point &a, const Point &b) { return
Point(a.x + b.x, a.y + b.y); }
Point operator -(const Point &a, const Point &b) { return
Point(a.x - b.x, a.y - b.y); }
Point operator /(const Point &a, double k) { return Point(a.x/k,
a.y/k); }
Point operator *(const Point &a, double k) { return Point(a.x*k,
a.y*k); }
bool operator ==(const Point &a, const Point &b){ return fabs(a.x
- b.x) < EPS && fabs(a.y - b.y) < EPS;}
bool operator !=(const Point &a, const Point &b){ return !(a==b);}
bool operator <(const Point &a, const Point &b){ if(a.x != b.x)
return a.x < b.x; return a.y < b.y;}
double dist(const Point &A, const Point &B)    { return hypot(A.x
- B.x, A.y - B.y); }
double cross(const Vector &A, const Vector &B) { return A.x * B.y
- A.y * B.x; }
double dot(const Vector &A, const Vector &B)   { return A.x * B.x
+ A.y * B.y; }
double area(const Point &A, const Point &B, const Point &C) {
return cross(B - A, C - A); }

double get_angle( Point A , Point P , Point B )
{
     double ang = (A-P).arg() - (B-P).arg();
     while(ang < 0) ang += 2*PI;
     while(ang > 2*PI) ang -= 2*PI;
     return min(ang, 2*PI-ang);
}
bool isInt(double k){ return abs(k - int(k + 0.5)) < 1e-5;}
/////
//responde si un punto esta en un poligono convexo incluyendo la
frontera
bool isIn( Point O , Point A , Point B , Point X )
{
```

```
     return abs( abs( area(O,A,B)) -( abs(area(O,A,X)) +
abs(area(A,B,X)) + abs(area(O,B,X)) ) ) < EPS ;
}
// transforma el angulo de atan2 al rango 0 - 2PI
double f( double a )
{
     if( a < 0 )a += 2*PI;
     return a;
}
////////////////////////////////////////////////////////////////
//////////////
// Heron triangulo y cuadrilatero ciclico
//http://en.wikipedia.org/wiki/Brahmagupta's_formula -----
sqrt((p-a) * (p-b) * (p-c)*(p-d))
// http://mathworld.wolfram.com/CyclicQuadrilateral.html
// http://www.spoj.pl/problems/QUADAREA/

//adicional existencia de trapezoide y altura
//http://en.wikipedia.org/wiki/Trapezoid

double areaHeron(double a, double b, double c)
{
     double s = (a + b + c) / 2;
     return sqrt(s * (s-a) * (s-b) * (s-c));
}

double circumradius(double a, double b, double c) { return a * b *
c / (4 * areaHeron(a, b, c)); }

double areaHeron(double a, double b, double c, double d)
{
     double s = (a + b + c + d) / 2;
     return sqrt((s-a) * (s-b) * (s-c) * (s-d));
}

double circumradius(double a, double b, double c, double d) {
return sqrt((a*b + c*d) * (a*c + b*d) * (a*d + b*c))  / (4 *
areaHeron(a, b, c, d)); }

//### DETERMINA SI P PERTENECE AL SEGMENTO AB
##########################################
bool between(const Point &A, const Point &B, const Point &P)
{
    return  P.x + EPS >= min(A.x, B.x) && P.x <= max(A.x, B.x) +
EPS &&
            P.y + EPS >= min(A.y, B.y) && P.y <= max(A.y, B.y) +
EPS;
}

bool onSegment(const Point &A, const Point &B, const Point &P)
{
    return abs(area(A, B, P)) < EPS && between(A, B, P);
```

```
}

//### DETERMINA SI EL SEGMENTO P1Q1 SE INTERSECTA CON EL SEGMENTO
P2Q2 ####################
//11343_UVA
bool intersects(const Point &P1, const Point &P2, const Point &P3,
const Point &P4)
{
    double A1 = area(P3, P4, P1);
    double A2 = area(P3, P4, P2);
    double A3 = area(P1, P2, P3);
    double A4 = area(P1, P2, P4);

    if( ((A1 > 0 && A2 < 0) || (A1 < 0 && A2 > 0)) &&
        ((A3 > 0 && A4 < 0) || (A3 < 0 && A4 > 0)))
            return true;

    else if(A1 == 0 && onSegment(P3, P4, P1)) return true;
    else if(A2 == 0 && onSegment(P3, P4, P2)) return true;
    else if(A3 == 0 && onSegment(P1, P2, P3)) return true;
    else if(A4 == 0 && onSegment(P1, P2, P4)) return true;
    else return false;
}

//### DETERMINA SI A, B, M, N PERTENECEN A LA MISMA RECTA
##############################
bool sameLine(Point P1, Point P2, Point P3, Point P4)
{
     return area(P1, P2, P3) == 0 && area(P1, P2, P4) == 0;
}
//### SI DOS SEGMENTOS O RECTAS SON PARALELOS
################################################
bool isParallel(const Point &P1, const Point &P2, const Point &P3,
const Point &P4)
{
     return abs( cross(P2 - P1, P4 - P3) ) <= EPS;
}

//### PUNTO DE INTERSECCION DE DOS RECTAS NO PARALELAS
################################
Point lineIntersection(const Point &A, const Point &B, const Point
&C, const Point &D)
{
    return A + (B - A) * (cross(C - A, D - C) / cross(B - A, D -
C));
}

Point circumcenter(const Point &A, const Point &B, const Point &C)
{
     return (A + B + (A - B).ort() * dot(C - B, A - C) / cross(A -
B, A - C)) / 2;
}
```

```
//### FUNCIONES BASICAS DE POLIGONOS
################################################
bool isConvex(const vector <Point> &P)
{
    int nP = P.size(), pos = 0, neg = 0;
    for(int i=0; i<nP; i++)
    {
        double A = area(P[i], P[(i+1)%nP], P[(i+2)%nP]);
        if(A < 0) neg++;
        else if(A > 0) pos++;
    }
    return neg == 0 || pos == 0;
}

double area(const vector <Point> &P)
{
    int nP = P.size();
    double A = 0;
    for(int i=1; i<=nP-2; i++)
        A += area(P[0], P[i], P[i+1]);
    return abs(A/2);
}


//### DETERMINA SI A ESTA EN EL INTERIOR DEL POLIGONO( sin
boundary ) ########################
// works in simple poly
bool pointInPoly(const vector <Point> &P, const Point &A)
{
    int nP = P.size(), cnt = 0;
    for( int i = 0 ; i < nP ; i++ )
    {
        int inf = i , sup = ( i + 1 )%nP;
        if( P[ inf ].y > P[ sup ].y ) swap( inf , sup );
        if( P[ inf ].y <= A.y && A.y < P[ sup ].y )
            if( area( A , P[ inf ] , P[ sup ] ) > 0 )
                cnt++;
    }
    return (cnt % 2) == 1;
}

/* TEOREMA DE PICK
A = I + B/2 - 1, donde:


A = Area de un poligono de coordenadas enteras
I = Numero de puntos enteros en su interior
B = Numero de puntos enteros sobre sus bordes
```

Haciendo un cambio en la formula : I=(2A-B+2)/2, tenemos una forma de calcular
el numero de puntos enteros en el interior del poligono

```
int IntegerPointsOnSegment(const point &P1, const point &P2){

    point P = P1-P2;
    P.x = abs(P.x); P.y = abs(P.y);

    if(P.x == 0) return P.y;

    if(P.y == 0) return P.x;

    return (__gcd(P.x,P.y));
}
```

Se asume que los vertices tienen coordenadas enteras. Sumar el valor de esta
funcion para todas las aristas para obtener el numero total de punto en el borde

del poligono.

```
*/

// O(n log n)
// Entender que el convexhull te elimina los puntos repetidos :)

vector <Point> ConvexHull(vector <Point> Poly)
{
    sort(Poly.begin(),Poly.end());
    int nP = Poly.size(),k = 0;
    Point H[ 2*nP ];

    for( int i = 0 ; i < nP ; ++i ){
        while( k >= 2 && area( H [ k - 2 ] , H[ k - 1 ] , Poly[ i
] ) <= 0) --k;
        H[ k++ ] = Poly[ i ];
    }
    for( int i = nP - 2 , t = k ; i >= 0 ; --i ){
        while( k > t && area( H[ k - 2 ] , H[ k - 1 ] , Poly[ i ]
) <= 0) --k;
        H[ k++ ] = Poly[ i ];
    }
    if( k == 0 )return vector <Point>();
    return vector <Point> ( H , H + k - 1 );
}
//### DETERMINA SI P ESTA EN EL INTERIOR DEL POLIGONO CONVEXO A
########################
```

```
// O (log n)
bool isInConvex(vector <Point> &A, const Point &P)
{
      int n = A.size(), lo = 1, hi = A.size() - 1;

      if(area(A[0], A[1], P) <= 0) return 0;
      if(area(A[n-1], A[0], P) <= 0) return 0;

      while(hi - lo > 1)
      {
            int mid = (lo + hi) / 2;

            if(area(A[0], A[mid], P) > 0) lo = mid;
            else hi = mid;
      }

      return area(A[lo], A[hi], P) > 0;
}

// O(n)
Point norm(const Point &A, const Point &O)
{
    Vector V = A - O;
    V = V * 10000000000.0 / V.mod();
    return O + V;
}

bool isInConvex(vector <Point> &A, vector <Point> &B)
{
    if(!isInConvex(A, B[0])) return 0;
    else
    {
        int n = A.size(), p = 0;

        for(int i=1; i<B.size(); i++)
        {
            while(!intersects(A[p], A[(p+1)%n], norm(B[i], B[0]),
B[0])) p = (p+1)%n;

            if(area(A[p], A[(p+1)%n], B[i]) <= 0) return 0;
        }

        return 1;
    }
}

// INTERSECCION DE CIRCULOS
vector <Point> circleCircleIntersection(Point O1, double r1, Point
O2, double r2)
{
      vector <Point> X;
      double d = dist(O1, O2);
```

```
	if(d > r1 + r2 || d < max(r2, r1) - min(r2, r1)) return X;
	else
	{
		double a = (r1*r1 - r2*r2 + d*d) / (2.0*d);
		double b = d - a;
		double c = sqrt(abs(r1*r1 - a*a));
		Vector V = (O2-O1).unit();
		Point H = O1 + V * a;
		X.push_back(H + V.ort() * c);
		if(c > EPS) X.push_back(H - V.ort() * c);
	}
	return X;
}

// LINEA AB vs CIRCULO (O, r)
// 1. Mucha perdida de precision, reemplazar por resultados de
formula.
// 2. Considerar line o segment

vector <Point> lineCircleIntersection(Point A, Point B, Point O,
long double r)
{
	vector <Point> X;
	Point H1 = O + (B - A).ort() * cross(O - A, B - A) / (B -
A).mod2();
	long double d2 = cross(O - A, B - A) * cross(O - A, B - A) /
(B - A).mod2();
	if(d2 <= r*r + EPS)
	{
		long double k = sqrt(abs(r * r - d2));
		Point P1 = H1 + (B - A) * k / (B - A).mod();
		Point P2 = H1 - (B - A) * k / (B - A).mod();
		if(between(A, B, P1)) X.push_back(P1);
		if(k > EPS && between(A, B, P2)) X.push_back(P2);
	}
	return X;
}
/*
// My own version
vector< Point > lineCircleIntersection( Point A , Point B , Point
O , ld R ){
	Vector V = ( B - A ).ort();
	Point H = lineIntersection( A , B , O , O + V );
	if( R < ( O - H ).dist() - EPS ) return vector< Point >();
	if( abs( R - ( O - H ).dist() ) < EPS ) return vector< Point
>( 1 , H );
	vector< Point > ans;
	Point P , Q;
	Vector W = ( B - A ).unit();
	ld d = sqrt( R*R - ( O - H ).dist2() );
	P = H + W*d , Q = H - W*d;
	ans.pb( P ) , ans.pb( Q );
```

```
	return ans;
}
*/
//### PROBLEMAS BASICOS
################################################################
void CircumscribedCircle()
{
	int x1, y1, x2, y2, x3, y3;
	scanf("%d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3, &y3);
	Point A(x1, y1), B(x2, y2), C(x3, y3);
	Point P1 = (A + B) / 2.0;
	Point P2 = P1 + (B-A).ort();
	Point P3 = (A + C) / 2.0;
	Point P4 = P3 + (C-A).ort();
	Point CC = lineIntersection(P1, P2, P3, P4);
	double r = dist(A, CC);
	printf("(%.6lf,%.6lf,%.6lf)\n", CC.x, CC.y, r);
}
void InscribedCircle()
{
	int x1, y1, x2, y2, x3, y3;
	scanf("%d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3, &y3);
	Point A(x1, y1), B(x2, y2), C(x3, y3);
	Point AX = A + (B-A).unit() + (C-A).unit();
	Point BX = B + (A-B).unit() + (C-B).unit();
	Point CC = lineIntersection(A, AX, B, BX);
	double r = abs(area(A, B, CC) / dist(A, B));
	printf("(%.6lf,%.6lf,%.6lf)\n", CC.x, CC.y, r);
}
vector <Point>  TangentLineThroughPoint(Point P, Point C, long
double r)
{
	vector <Point> X;
	long double h2 = (C - P).mod2();
	if(h2 < r*r) return X;
	else
	{
		long double d = sqrt(h2 - r*r);
		long double m1 = (r*(P.x - C.x) + d*(P.y - C.y)) / h2;
		long double n1 = (P.y - C.y - d*m1) / r;
		long double n2 = (d*(P.x - C.x) + r*(P.y - C.y)) / h2;
		long double m2 = (P.x - C.x - d*n2) / r;
		X.push_back(C + Point(m1, n1)*r);
		if(d != 0) X.push_back(C + Point(m2, n2)*r);
		return X;
	}
}
void TangentLineThroughPoint()
{
	int xc, yc, r, xp, yp;
	scanf("%d %d %d %d %d", &xc, &yc, &r, &xp, &yp);
	Point C(xc, yc), P(xp, yp);
```

```
	double hyp = dist(C, P);
	if(hyp < r) printf("[]\n");
	else
	{
		double d = sqrt(hyp * hyp - r*r);
		double m1 = (r*(P.x - C.x) + d*(P.y - C.y)) / (r*r +
d*d);
		double n1 = (P.y - C.y - d*m1) / r;
		double ang1 = 180 * atan(-m1/n1) / PI + EPS;
		if(ang1 < 0) ang1 += 180.0;
		double n2 = (d*(P.x - C.x) + r*(P.y - C.y)) / (r*r +
d*d);
		double m2 = (P.x - C.x - d*n2) / r;
		double ang2 = 180 * atan(-m2/n2) / PI + EPS;
		if(ang2 < 0) ang2 += 180.0;
		if(ang1 > ang2) swap(ang1, ang2);
		if(d == 0) printf("[%.6lf]\n", ang1);
		else printf("[%.6lf,%.6lf]\n", ang1, ang2);
	}
}
void CircleThroughAPointAndTangentToALineWithRadius()
{
	int xp, yp, x1, y1, x2, y2, r;
	scanf("%d %d %d %d %d %d %d", &xp, &yp, &x1, &y1, &x2, &y2,
&r);
	Point P(xp, yp), A(x1, y1), B(x2, y2);
	Vector V = (B - A).ort() * r / (B - A).mod();
	Point X[2];
	int cnt = 0;
	Point H1 = P + (B - A).ort() * cross(P - A, B - A) / (B -
A).mod2() + V;
	double d1 = abs(r + cross(P - A, B - A) / (B - A).mod());
	if(d1 - EPS <= r)
	{
		double k = sqrt(abs(r * r - d1 * d1));
		X[cnt++] = Point(H1 + (B - A).unit() * k);
		if(k > EPS) X[cnt++] = Point(H1 - (B - A).unit() * k);
	}
	Point H2 = P + (B - A).ort() * cross(P - A, B - A) / (B -
A).mod2() - V;
	double d2 = abs(r - cross(P - A, B - A) / (B - A).mod());
	if(d2 - EPS <= r)
	{
		double k = sqrt(abs(r * r - d2 * d2));
		X[cnt++] = Point(H2 + (B - A).unit() * k);
		if(k > EPS) X[cnt++] = Point(H2 - (B - A).unit() * k);

	}
	sort(X, X + cnt);
	if(cnt == 0) printf("[]\n");
	else if(cnt == 1) printf("[(%.6lf,%.6lf)]\n", X[0].x,
X[0].y);
```

```
	else if(cnt == 2) printf("[(%.6lf,%.6lf),(%.6lf,%.6lf)]\n",
X[0].x, X[0].y, X[1].x, X[1].y);
}
void CircleTangentToTwoLinesWithRadius()
{
	int x1, y1, x2, y2, x3, y3, x4, y4, r;
	scanf("%d %d %d %d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3,
&y3, &x4, &y4, &r);
	Point A1(x1, y1), B1(x2, y2), A2(x3, y3), B2(x4, y4);
	Vector V1 = (B1 - A1).ort() * r / (B1 - A1).mod();
	Vector V2 = (B2 - A2).ort() * r / (B2 - A2).mod();
	Point X[4];
	X[0] = lineIntersection(A1 + V1, B1 + V1, A2 + V2, B2 + V2);
	X[1] = lineIntersection(A1 + V1, B1 + V1, A2 - V2, B2 - V2);
	X[2] = lineIntersection(A1 - V1, B1 - V1, A2 + V2, B2 + V2);
	X[3] = lineIntersection(A1 - V1, B1 - V1, A2 - V2, B2 - V2);
	sort(X, X + 4);
	printf("[(%.6lf,%.6lf),(%.6lf,%.6lf),(%.6lf,%.6lf),(%.6lf,%.6
lf)]\n", X[0].x, X[0].y, X[1].x, X[1].y, X[2].x, X[2].y, X[3].x,
X[3].y);
}

void CircleTangentToTwoDisjointCirclesWithRadius()
{
	int x1, y1, r1, x2, y2, r2, r;
	scanf("%d %d %d %d %d %d %d", &x1, &y1, &r1, &x2, &y2, &r2,
&r);
	Point A(x1, y1), B(x2, y2);
	r1 += r;
	r2 += r;
	double d = dist(A, B);
	if(d > r1 + r2 || d < max(r1, r2) - min(r1, r2))
printf("[]\n");
	else
	{
		double a = (r1*r1 - r2*r2 + d*d) / (2.0*d);
		double b = d - a;
		double c = sqrt(abs(r1*r1 - a*a));
		Vector V = (B-A).unit();
		Point H = A + V * a;
		Point P1 = H + V.ort() * c;
		Point P2 = H - V.ort() * c;
		if(P2 < P1) swap(P1, P2);
		if(P1 == P2) printf("[(%.6lf,%.6lf)]\n", P1.x, P1.y);
		else printf("[(%.6lf,%.6lf),(%.6lf,%.6lf)]\n", P1.x,
P1.y, P2.x, P2.y);
	}
}
```

```
**************************UTILITIES*****************************++
ll modulo( int num ){
      ( ( num %= mod ) += mod ) %= mod ;
      return num ;
}
const ll mod = (int)( 1e+6 + 3 ) ;
const ld EPS=1e-6;

vector< int > pr , ex;
vector< int > getdivisors( ll x ){
      vector< int > divisors( 1 , 1 );
      for ( int i = 0 ; i < (int)pr.size() ; i++ ){
                        int m = (int)divisors.size();
            for ( int j = 0 ; j < ex[ i ]; j++ ){

                  for ( int k = 0 ; k < m; k++ ) divisors.push_back(
divisors[ m*j + k ]*pr[ i ] );
            }
      }
      return divisors;
}

void f( ll x ){
      for ( ll i = 2 ; i * i <= x ; i++ ){

            if ( x % i == 0 ){
                  int cnt = 0;
                  while ( x % i == 0 ){
                        x /= i;
                        cnt++;
                  }
```

```
                pr.push_back( i );
                ex.push_back( cnt );
            }

        }
        if ( x > 1 ){
            pr.push_back( x );
            ex.push_back( 1 );
        }
}//generador de divisores de un numero x

__builtin_popcountll(n); //cantidad de unos de n en binario;
n long long;
__builtin_popcount(n); //cantidad de unos de n en binario; n int;
31 - __builtin_popclz(n); // posicion del mayor uno
(maxima potencia de 2 menor a n); n int;
63 - __builtin_popclz(n);//posicion del mayor uno
(maxima potencia de 2 menor a n); n long long;
__builtin_ctz(n);//cantidad de '0' de n en binario

*****VALORES DE CARACTERES**
a en entero es 97
A.....  65
'.'   .......  46
'0'   .......  48
```

```
**************************DJISTRA************************
struct Node{
      int dist,u;
      Node(){}
      Node(int _dist,int _u){
            dist=_dist;
            u=_u;
      }
};
bool operator < (const Node a,const Node b){
      return a.dist > b.dist;
}
vector<int> djistra(int source){
      vector<int> d(998002, INF );
      priority_queue <Node> Q;
      Q.push(Node(0,source));
      d[source]=0;
      while(!Q.empty()){
            Node a=Q.top();
            Q.pop();
            for(int i=0;i<G[a.u].size();i++){
                  int v=G[a.u][i];
                  int w=C[a.u][i];
                  if(d[a.u] + w < d[v]){
                        d[v]=d[a.u] + w;
                        Q.push(Node(d[v],v));
                  }
            }
      }
      return d;}
```

```
**********BFS 0-1 **********
const int INF=(1e9);
char M[1005][1005];
int d[1005][1005];
int dx[]={0,0,-1,1};
int dy[]={-1,1,0,0};
int n,m;
void bfs(int x,int y){
      for(int i=1;i<=1000;i++){
            for(int j=1;j<=1000;j++) d[i][j]=INF;
      }
      d[x][y]=0;
      deque<pii> D;
      D.push_front(mp(x,y));
      while(!D.empty()){
            pii p = D.front();
            D.pop_front();
            for(int i=0;i<4;i++){
                  pii q = mp(p.fi + dx[i],p.se + dy[i]);
                  if(q.fi<1 || q.fi>n || q.se<1 || q.se>m) continue;
                  if(M[q.fi][q.se]=='X' &&
d[q.fi][q.se] > d[p.fi][p.se]){//EN CASO EL VALOR DEL EDGE ES 1
                        d[q.fi][q.se] = d[p.fi][p.se];
                        D.push_front(q);}
                        else if(M[q.fi][q.se]=='.' &&
d[q.fi][q.se] > d[p.fi][p.se] + 1{//EN CASO EL VALOR DEL EDGE ES 0
                        d[q.fi][q.se] = d[p.fi][p.se] + 1;
                        D.push_back(q);}
            }
      } }
```

**********VALORES CLASICOS**********

DESVIACION ESTANDAR:

```
int main(){
      ll n;
      while(cin>>n){
            if(n==0) break;
            ll sum=0;
            for(int i=1;i<=n;i++){
                  ll val=2*i - 1;
                  sum+=sqr(val-n);
            }
            double ans=sqrt( (double) sum / double(n-1) );
            printf("%.6f\n",ans);
      }

      return 0;
}
```

DP con mask:

```
int memo[12][4098];
int memo1[13];
int n;
int fact(int num){
      if(num==0) return 1;
      if(memo1[num] > 0) return memo1[num];
      int &ans=memo1[num]=1;
      ans=num*fact(num-1);
      return ans;
}

int dp(int num,int mask){
      if(num==(n-1)){
            if(mask & (1<<0) ) return 0;
            else return 1;
      }
      if(memo[num][mask] > 0) return memo[num][mask];
      int &ans=memo[num][mask]=0;
      for(int i=0;i<n;i++){
            if( mask & ( 1<<(n-i-1) ) ){
                  if(i==num) continue;
                  ans+=dp(num+1,mask ^ (1<<(n-i-1)));
            }
      }
      return ans;
}
```

```
int main(){
      int t;cin>>t;
      while(t>0){
            t--;
            cin>>n;
            int divi=fact(n);
            int num=dp(0, (1<<n) - 1);
            cout<<num<<"/"<<divi<<'\n';
      }

      return 0;
}
```

BFS MIKEMON:

```
int M[1001][1001];
char N[1001][1001];
int dx[]={-1,1,0,0};
int dy[]={0,0,-1,1};
bool vis[1001][1002];

int n,m;

void bfs(int x,int y){
      vis[x][y]=1;
      queue<pii> Q;
      Q.push(mp(x,y));
      while(!Q.empty()){
            pii p=Q.front();
            int px=p.fi,py=p.se;
            Q.pop();
            for(int i=0;i<4;i++){
                  int xx=px+dx[i];
                  int yy=py+dy[i];
                  if( xx < 1 || xx > n || yy < 1 || yy > m)
continue;
                  if(N[xx][yy]=='T') continue;
                  if(!vis[xx][yy]){
                        M[xx][yy]=M[px][py]+1;
                        vis[xx][yy]=1;
                        Q.push(mp(xx,yy));
                  }
            }
      }
}
```

```
int main(){
      cin>>n>>m;
      memset(M,-1,sizeof(M));
      int x,y;
      int xx,yy;
      vector< pair < pii,int > > mik;
      for(int i=1;i<=n;i++){
            for(int j=1;j<=m;j++){
                  cin>>N[i][j];
                  if(N[i][j]=='S'){
                        x=i;y=j;
                  }
                  if(N[i][j]=='E'){
                        xx=i;yy=j;
                  }
                  if(N[i][j]>='1' && N[i][j]<='9') mik.pb(mp(mp(i,j)
, N[i][j]-'0'));
            }
      }
      bfs(xx,yy);
      int res=M[x][y];
      int ans=0;
      for(int i=0;i<sz(mik);i++){
            if(M[mik[i].fi.fi][mik[i].fi.se]==(-1)) continue;
            if(M[mik[i].fi.fi][mik[i].fi.se] <= res) ans+=mik[i].se;
      }
      cout<<ans<<endl;
      return 0;
}
```

DP TSP:

```
int M[12][102];
int memo[12][102];
int n,m;

int dp(int i,int j){
      if(memo[i][j]) return memo[i][j];
      if(j==m) {memo[i][j]=M[i][j];return M[i][j];}
      int &ans=memo[i][j]=0;
      ans+=M[i][j];
      ans+=min( min( dp(i-1 + n*(i==1),j+1) , dp(i , j+1) ) ,
dp(i+1 - n*(i==n),j+1) );
      return ans;
}
```

```
void rec(int val,int pos,int col){
	cout<<pos;
	val-=M[pos][col];
	if(col==m) return;
	cout<<" ";
	if(pos==1){
		if(memo[pos][col+1]==val){rec(val,pos,col+1);}
		else if(memo[pos+1][col+1]==val){rec(val,pos+1,col+1);}
		else rec(val,n,col+1);
	}
	else if(pos==n){
		if(memo[1][col+1]==val){rec(val,1,col+1);}
		else if(memo[pos-1][col+1]==val){rec(val,pos-1,col+1);}
		else rec(val,pos,col+1);
	}
	else{
		if(memo[pos-1][col+1]==val) {rec(val,pos-1,col+1);}
		else if(memo[pos][col+1]==val){rec(val,pos,col+1);}
		else {rec(val,pos+1,col+1);}
	}
}


int main(){
	//fast_io();
	while(cin>>n>>m){
		memset(M,0,sizeof(M));
		memset(memo,0,sizeof(memo));
		for(int i=1;i<=n;i++){
			for(int j=1;j<=m;j++){
				cin>>M[i][j];
			}
		}
		int mini=(1<<30);
		for(int i=1;i<=n;i++){
			mini=min(mini,dp(i,1));
		}
		for(int i=1;i<=n;i++){
			if(memo[i][1]==mini) {rec(mini,i,1);break;}
		}
		cout<<endl;
		cout<<mini<<endl;
	}


	return 0;
}
```

TWO POINTER-STL:

```
set<char> S;
map<char,int> M;


bool cumple(){
      map<char,int> :: iterator it2;
      for(it2=M.begin();it2!=M.end();it2++){
            if((*it2).se==0) return false;
      }
      return true;
}

int main(){
      //fast_io();
      int n;cin>>n;
      string s;cin>>s;
      int val=0;
      for(int i=0;i<n;i++){
            S.insert(s[i]);
      }
      set<char> :: iterator it;
      for(it=S.begin();it!=S.end();it++){
            M[(*it)]=0;
      }
      int j=-1;
      int mini=1000000;
      for(int i=0;i<n;i++){
            if(cumple()){
                  mini=min(mini,j-i+1);
                  M[s[i]]--;
                  continue;
            }
            while( (j+1) < n ){
                  j++;
                  M[s[j]]++;
                  if(cumple()){
                        mini=min(mini,j-i+1);
                        break;
                  }
            }
            M[s[i]]--;
      }
      cout<<mini<<endl;

      return 0;
}
```

TWO POINTER-BINARY SEARCH:

```
vector<ll> city;
vector<ll> tower;

bool f(ll r){
      int j=-1;
      for(int i=0;i<sz(tower);i++){
            while((j+1)<sz(city)){
                  if( city[j+1] >= tower[i]-r && city[j+1] <=
tower[i] + r ) j++;
                  else break;
            }
      }
      if(j+1==sz(city)) return true;
      else return false;
}

int main(){
      fast_io();
      int n,m;cin>>n>>m;
      for(int i=0;i<n;i++){
            ll a;cin>>a;city.pb(a);
      }
      for(int i=0;i<m;i++){
            ll a;cin>>a;tower.pb(a);
      }
      sort(all(city));
      sort(all(tower));
      if(f(0)) {cout<<0<<endl;return 0;}
      ll lo=0.0,hi=(2e9);
      while((hi-lo) > 1){
            ll mi=(lo+hi)/2;
            if(f(mi)) hi=mi;
            else lo=mi;
      }
      cout<<hi<<endl;

      return 0;
}
```

TWO POINTER CLASSIC:

```
map<int,int> M;
bool cumple(){
      map<int,int> :: iterator it;
      if(M.size() > 2) return false;
      if(M.size() < 2) return true;
      for(it=M.begin();it!=M.end();it++){

      }
}


int main(){
      //fast_io();
      int n;cin>>n;
      vi v(n);
      for(int i=0;i<n;i++) cin>>v[i];
      int maxi=0;
      int j=-1;
      for(int i=0;i<n;i++){
            while((j+1) < n){
                  if(cumple()) j++;
                  else{

                        maxi=max(maxi,j-i);
                  }
            }
      }

      return 0;
}
```

TERNARY SEARCH:

```
double f(double val){
      //funcion que rige la cuadratica;
}

int main(){
      //fast_io();
      double hi,lo;
      for(int i=0;i<100;i++){
            int mi1=hi - (hi-lo)/3.0;
            int mi2=lo + (hi-lo)/3.0;
            if(f(mi2) < f(mi1)) lo=mi2;
            else hi=mi1;
      }
      printf("%.10f\n",(hi+lo)/2.0);

      return 0;
}
```

UNION FIND (CON RANK):

```
int pa[1002]; //todos se inicializa en pa[i] = i;
int ranked[1002];

int Find(int i){
     if(pa[i]==i) return i;
     return find(pa[i]);
}

void Union(int x,int y){
     int xset=find(x);
     int yset=find(y);
     if(ranked[xset]<ranked[yset]){
          pa[xset]=yset;
     }
     else if(ranked[xset]>ranked[yset]){
          pa[yset]=xset;
     }
     else{
          pa[yset]=xset;
          ranked[xset]++;
     }
}
```

UNION FIND (ENEMIES ANS FRIENDS): //WAR UVA 10158

```
const int N=(1e4);
int pa[2*N+5];
int ranked[2*N+5];

int Find(int i){
     if(pa[i]==i) return i;
     return Find(pa[i]);
}

void Union(int x,int y){
     int xset=Find(x);
     int yset=Find(y);
     if(ranked[xset]<ranked[yset]){
          pa[xset]=yset;
     }
     else if(ranked[xset]>ranked[yset]){
          pa[yset]=xset;
     }
     else{
          pa[yset]=xset;
          ranked[xset]++;
     }
}
// Para setear amigos Union(a,b);Union(a+n,b+n);
// Para setear enemigos Union(a+n,b);Union(a,b+n);
```

NUMBER THEORY

EXTENDIDO DE EUCLIDES:

```
//Se utiliza para resolver ecuaciones del tipo ax+by=gcd(a,b);
typedef pair<ll,pair<ll,ll> > tup;

tup extGcd(ll a,ll b){
      if(b==0) return mp(a,mp(1,0));
      tup ret =  extGcd(b,a%b);
      return mp(ret.fi , mp(ret.se.se, ret.se.fi - (a/b)*
ret.se.se));
}
/*Si deseas hallar para una ecuacion diofantica en general se debe
cumplir:
ax+by=k , k es multiplo de gcd(a,b)*/
```

INVERSO MODULAR:

```
//Debe cumplirse gcd(a,n)=1;
SI n ES PRIMO entonces:

const ll MOD=(1e9 + 7);
ll pot(ll a,ll b){
      if(b==0) return 1;
      if(b==1) return a;
      ll ans=1;
      if(b&1) ans*=a;
      ans*=pot(a,b/2);
      ans%=MOD;
      ans*=pot(a,b/2);
      ans%=MOD;
      return ans;
}

ll inv(ll a){
      return pot(a,MOD-2)%MOD;
}

SI n NO ES PRIMO entonces:

ll inv(ll a,ll n){
      tup t= extGcd(a,n);
      ll inver=((t.se.fi%n) + n)%n;
      return inver;
}

Se utiliza la función de Extendido de Euclides
```

CHINESSE THEOREM REMAINDER

```
      x = a1 (mod m1)
      x = a1 (mod m2)
            .
            .
            .
      x = ak (mod mk)
```

m1, m2, m3 ,...., mk son PESI

entonces:

```
      x = a1m1y1 + a2m2y2 + .... + akmkyk
```

donde mi = inverso modular de yi mod ni

```
ll chinese(vector<ll>&rem , vector<ll>&mod){
      int k=sz(mod);
      ll n=1;
      for(int i=0;i<k;i++) n*=mod[i];
      ll x=0;
      for(int i=0;i<k;i++){
            ll m=n/mod[i];
            ll y=inv(m,mod[i]);
            y%=n;
            x+=(rem[i] * ( ( m*y) % n))%n;
            x%=n;
      }
      return x;
}
```

TEOREMA DE LUCAS:

```
ll C[105][105];

int Lucas(int n, int r, int p){
   if (r==0) return 1;

   int ni = n%p, ri = r%p;

   return (Lucas(n/p, r/p, p) * C[ni][ri] % p) % p;
}

for(int i=0;i<=50;i++) C[i][0]=1; // inicializamos
for(int i=1;i<=50;i++){
      for(int j=i;j<=50;j++){
            if(i==j) C[i][j]=1;
            else C[j][i]=C[j-1][i-1]+C[j-1][i];
      }
}
```

HACKERRANK PROBLEM – TEOREMA DEL CHINO Y LUCAS

```
#include <bits/stdc++.h>
typedef long long ll;
using namespace std;
ll mod;
vector<ll> pr;
vector<ll> res;

ll pot(ll a,ll b,ll c){
      if(b==0) return 1;
      if(b==1) return a;
      ll ans=1;
      if(b&1) ans*=a;
      ans*=pot(a,b/2,c);
      ans%=c;
      ans*=pot(a,b/2,c);
      ans%=c;
      return ans;
}

ll inv(ll a,ll b){
      return pot(a,b-2,b)%b;
}

void f(ll x){
    for(ll i=2;i*i<=x;i++){
        if(x%i==0){
            pr.push_back(i);
            x/=i;
        }
    }
    if(x>1) pr.push_back(x);
}

ll chino(){
      ll x=0;
      for(int i=0;i<pr.size();i++){
            ll m=mod/pr[i];
            ll y=inv(m,pr[i]);
            y%=mod;
            x+=(res[i] * ( ( m*y) % mod))%mod;
            x%=mod;
      }
      return x;
}
ll C[105][105];
```

```
int Lucas(int n, int r, int p)
{
   if (r==0)
      return 1;

   int ni = n%p, ri = r%p;

   return (Lucas(n/p, r/p, p) * // Last digits of n and r
           C[ni][ri] % p) % p;  // Remaining digits
}


int main() {
    int t;cin>>t;
    ll a,b;
    for(int i=0;i<=50;i++) C[i][0]=1;
    for(int i=1;i<=50;i++){
     for(int j=i;j<=50;j++){
          if(i==j) C[i][j]=1;
          else C[j][i]=C[j-1][i-1]+C[j-1][i];
          }
     }

    while(t--){
        cin>>a>>b>>mod;
        pr.clear();
        res.clear();
        f(mod);
        for(int i=0;i<pr.size();i++){
            res.push_back(Lucas(a,b,pr[i]));
        }
        ll ans=chino();
        cout<<ans<<endl;
    }
    return 0;
}
```

EXPONENCIACION RAPIDA EN COMPLEJOS:

```
typedef long long ll;
using namespace std;
ll MOD;

pair<ll,ll> mult(pair<ll,ll> a,pair<ll,ll> b){
    pair<ll,ll> ans=make_pair(0,0);
    ans.first+=(a.first*b.first);
    ans.first%=MOD;
    ans.second+=(a.second*b.first);
    ans.second%=MOD;
    ans.second+=(a.first*b.second);
    ans.second%=MOD;
    ans.first-=(a.second*b.second);
    ans.first%=MOD;
    ans.first+=MOD;
    ans.first%=MOD;
    return ans;
}

pair<ll,ll> pot(pair<ll,ll> a,ll b){
    if(b==0) return make_pair(1,0);
    if(b==1) return a;
    pair<ll,ll> ans=make_pair(1,0);
    if(b&1) ans=a;
    pair<ll,ll> val = pot(a,b/2);
    ans=mult(ans,val);
    ans=mult(ans,val);
    return ans;
}

int main() {

    int q;cin>>q;
    ll a,b,k;
    while(q--){
        cin>>a>>b>>k>>MOD;
        pair<ll,ll> p = pot(make_pair(a,b),k);
        cout<<p.first<<" "<<p.second<<endl;
    }
    return 0;
}
```

NUMERO DE FIBONACCI EFICIENTE CON DISTINTAS INICIALES

```
using namespace std;

#define long long ll
const ll MOD = 1000000007;
map<ll, ll> M;

ll f(ll n) {
      if (M.count(n)) return M[n];
      long k=n/2;
      if (n%2==0)
      return M[n] = ((f(k)*f(k))%MOD + (f(k-1)*f(k-1))%MOD) %MOD;
      else
      return M[n] = ((f(k)*f(k+1))%MOD + (f(k-1)*f(k))%MOD) % MOD;
}

int main(){
      ll n;
      int t;cin>>t;
      M[0]=M[1]=1;
      ll a,b;
      while (t--){
         cin>>a>>b>>n;
         if(n==0) cout<<a<<endl;
         else if(n==1) cout<<b<<endl;
         else cout<<( (a*f(n-2))%MOD + (b*f(n-1))%MOD )%MOD<<endl;
     }
```

MOBIUS:

MOBIUS, es una funcion multiplicativa que esta definida de la siguiente forma:

u(n) = 1 , si n es LC y cantidad de factores primos par
u(n) = -1 , si n es LC y cantidad de factores primos impar
u(n) = 0 , si n es no LC

LC: Libre de Cuadrados

para hallar el mobius de manera eficiente utilizamos criba

```
const int UP=(1e4);
int fact[UP + 5];
int mu[UP + 5];
ll D[UP + 5];
```

```
void criba(){
      for(int i=0;i<=UP;i++) fact[i]=-1;
      for(int i=2;i*i<=UP;i++){
            if(fact[i]==-1){
                  for(int j=i*i;j<=UP;j+=i){
                        if(fact[j]==-1) fact[j]=i;
                  }
            }
      }
}

void mobius(){
      mu[1]=1;
      for(int i=2;i<=UP;i++){
            if(fact[i]==-1) mu[i]=-1;
            else{
                  int nx=i/fact[i];
                  if(nx % fact[i]==0) mu[i]=0;
                  else mu[i]=-mu[nx];
            }
      }
}

int main(){
      fast_io();

      int n;
      criba();
      mobius();
      while (cin>>n){
            memset( D,0,sizeof(D));
            for ( int i =0; i < n ; i++ ){
                  int x; cin>>x;
                  for ( int j = 1; j <= x ; j++ ){
                        if ( x % j == 0 ) D[j]++;
                  }
            }
            long long ans = 0;
            for ( int i = 1; i < UP;i++ ){
                  long long val = D[i];
                  val = (val)*(val-1)*(val-2)*(val-3)/24; ans +=
            val*mu[i];
            }
            cout<<ans<<endl;
      }

      return 0 ;
}
```

```
**********RANGE MINIMUN QUERY**********
//Usando Sparse Table

const int N=(1e5);
const int MAXN=(60);
using namespace std;
int M[N+5][MAXN+5];
int n;

int f(int x,int y){
    return log2(y-x+1);
}

int main() {

    cin>>n;
    vector<int> A(n);
    for(int i=0;i<n;i++) cin>>A[i];

    //initialize M for the intervals with length 1
    for (int i = 0; i < n; i++) M[i][0] = i;
    //compute values from smaller to bigger intervals
    for (int j = 1; 1 << j <= n; j++){
        for (int i = 0; i + (1 << j) - 1 < n; i++){
            if (A[M[i][j - 1]] < A[M[i + (1 << (j - 1))][j - 1]])
                M[i][j] = M[i][j - 1];
            else M[i][j] = M[i + (1 << (j - 1))][j - 1];
        }
    }

    int q;cin>>q;
    int a,b;
    while(q--){
        cin>>a>>b;
        int pos = f(a,b);
        cout<<min(A[M[a][pos]] ,
                          A[M[b - (1<<pos) + 1][pos]])<<endl;
    }


    return 0;
}
```