

$$\textcircled{2} \text{ a) } x^{(i)} = (0,5; 0,5; 0,5) \\ w^{(i)} = (0,5; 0,5; 0,5)$$

$$x_K^{(1)} = x_K^{(1)} - 2 \sum_{n(i,j)=1} (w^{(i)} \cdot x^{(i)} - y^{(i,j)}) w_K^{(i)} = 0,5 - 0,2 (0,75 - 5 + 0,75 - 5 + 0,75 + 0,75) \cdot 0,5 = \\ = 0,5 - \frac{2}{10} \cdot \frac{35}{10} = -0,2. \text{ Same for } x_K^{(2)} \text{ and } x_K^{(3)}, \text{ as all features are the same}$$

$$w_K^{(1)} = w_K^{(1)} - 2 \sum_{n(i,j)=1} (w^{(i)} \cdot x^{(i)} - y^{(i,j)}) x_K^{(i)} = 0,5 - 0,2 (\dots) \cdot 0,5 = -0,2$$

$$x_K^{(2)} = x_K^{(2)} - 2 \sum_{n(i,j)=1} (w^{(i)} \cdot x^{(i)} - y^{(i,j)}) \cdot w_K^{(i)} = 0,5 - 0,2 (0,75 - 5 + 0,75 - 4 + 0,75 + 0,75) \cdot 0,5 = \\ = 0,5 + \frac{2}{10} \cdot 6 \cdot \frac{5}{10} = 1,1$$

Since initial configurations are the same $\Rightarrow x^{(1)} = (-0,2; -0,2; -0,2)$

$$x^{(2)} = (1,1; 1,1; 1,1)$$

$$w^{(1)} = (-0,2; -0,2; -0,2)$$

$$w^{(2)} = (1,1; 1,1; 1,1)$$

Pred. for user 1 and movie 1: $x^{(1)} \cdot w^{(1)} = (-0,2; -0,2; -0,2) (-0,2; -0,2; -0,2) = 3 \cdot 0,04 = 0,12$

Pred. for user 2 and movie 2: $x^{(2)} \cdot w^{(2)} = (1,1; 1,1; 1,1) (1,1; 1,1; 1,1) = 3 \cdot 1,1 = 3,3$