STAT 6340 Mini Project 4

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March 27, 2019

Section 1

Section 2 is coded in Section 1

Question 1(a)

We make a scatterplot of gpa against act.

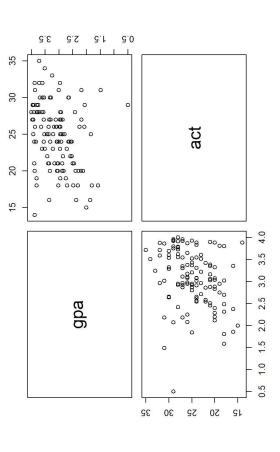
We notice there is a positve correlation but it is not strong (0.27)

```
gpa = read.csv("gpa.csv", header = T)
str(gpa)
```

'data.frame': 120 obs. of 2 variables: ## \$ gpa: num 3.9 3.88 3.78 2.54 3.03 ... ## \$ act: int 21 14 28 22 21 31 32 27 29 26 ... summary(gpa)

```
## Min. :0.500 Min. :14.00
## 1st Qu.:2.689 1st Qu.:21.00
## Median :3.078 Median :25.00
## Mean :3.074 Mean :24.73
## 3rd Qu.:3.593 3rd Qu.:28.00
## Max. :4.000 Max. :35.00
```

pairs(subset(gpa))



```
round(cor(subset(gpa)), 2)

## gpa act
## act 0.27 1.00
```

1(b)

There is a positive correlation between gpa and act # the relationship is not very strong (0.27) p is our population correlation between gpa and act.

Here, we gather the bootstrap estimates of bias and standard error of
the point estimate and show the 95% confidence interval from bootstrap

```
library(boot)
corr(gpa)
```

[1] 0.2694818

```
# Point estimate, bootstrap bias, and bootstrap se
                                                                                                                                                                         corr.fn <- function(data, i=c(1:length(data))) {
    result = corr(data[i,])</pre>
                                   corr.fn <- function(data, i=c(1:length(data))) {</pre>
                                                                                                                                                                                                                                                                                                                                                         corr.boot <- boot(gpa, corr.fn, R = 1000)
                                                                                                      return(cor(result$gpa, result$act))
# either function below will work
                                                                      result <- data[i,]
                                                                                                                                                                                                                                               return(result)
                                                                                                                                                                                                                                                                                                                   set.seed(1)
                                                                                                                                                                                                                                                                                                                                                                                                                            corr.boot
```

```
## Call:
## boot(data = gpa, statistic = corr.fn, R = 1000)
                                                                                                                                                        std. error
                                                                                                                                                                        0.1072831
##
## ORDINARY NONPARAMETRIC BOOTSTRAP
##
                                                                                                                                                                        ## t1* 0.2694818 0.007800885
                                                                                                                                                        bias
                                                                                                                                    ## Bootstrap Statistics :
## original bias
                                                                                                     #
```

```
boot.ci(corr.boot, type = "perc")
# 95% bootstrap conf int
```

```
## CALL :
## boot.ci(boot.out = corr.boot, type = "perc")
                                                                                                                                                                                                                               ## Calculations and Intervals on Original Scale
## BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
## Based on 1000 bootstrap replicates
                                                                                                                                                  ## Intervals :
## Level Percentile
## 95% ( 0.0728, 0.4917 )
                                                      #
                                                                                                                             #
```

```
sort(corr.boot$t)[c(25, 975)]
# verified below
```

```
## [1] 0.07274536 0.49136740
```

our original ho is contained in the bootstrap interval and the bias is only # 0.004196114 which implies good bootstrap estimates.

Using gpa~act, we fit a SLR. We show the least square estimates, standard errors and a 95% CI. We include verifications of our model assumptions

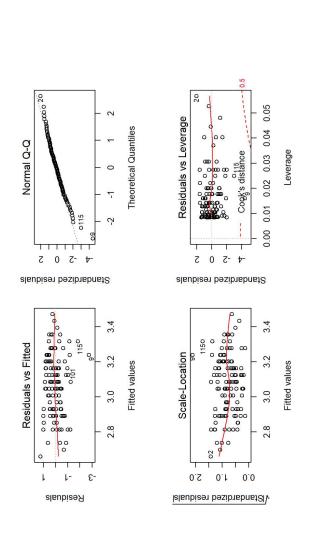
```
## Signif. codes: 0 '*** 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ## Residual standard error: 0.6231 on 118 degrees of freedom
## Multiple R-squared: 0.07262, Adjusted R-squared: 0.00
fit = lm(gpa~act, data = gpa)
# Least square estimate of coefficients, SE, and 95% CI
summary(fit)
                                                                                                                                                                                                                                                                                                                                                                                       0.32089 6.588 1.3e-09 ***
                                                                                                                                                                                                                                                                                                                                                                                                             3.040 0.00292 **
                                                                                                                                                                                                                                                                                                                                                             Estimate Std. Error t value Pr(>|t|)
                                                                                                                                                                                                                          ## Residuals:
## Min 1Q Median 3Q Max
## -2.74004 -0.33827 0.04062 0.44064 1.22737
                                                                                                                                           ## Call:
## lm(formula = gpa ~ act, data = gpa)
                                                                                                                                                                                                                                                                                                                                                                                                                 0.01277
                                                                                                                                                                                                                                                                                                                                                                                       ## (Intercept) 2.11405
                                                                                                                                                                                                                                                                                                                                                                                                                 0.03883
                                                                                                                                                                                                                                                                                                                                 ## Coefficients:
                                                                                                                                                                                                                                                                                                                                                                                                               ## act
                                                                                                                                                                                                                                                                                                                                                             #
                                                                                                                                                                                                                                                                                                         #
```

```
## 2.5 % 97.5 %
## (Intercept) 1.47859015 2.74950842
                                                                                          0.01353307 0.06412118
                                                    2.5 %
confint(fit)
```

Adjusted R-squared: 0.06476

F-statistic: 9.24 on 1 and 118 DF, p-value: 0.002917

```
par(mfrow = c(2,2))
               plot(fit)
```



```
par(mfrow = c(1,1)) # it appears the residual plot could do better via a transformation but not bad # the qq plot is not bad but does show some outliers.
```

boot.ci(fit.boot, type = "perc", index = 2) # act

1(d)

We use a nonparametric bootstrap to estimate the previous question's parameters. The bootstrap estimates are higher than was in the linear model

Also, the 95% CI is wider than the linear model

```
library(boot)
# function to output coefficients from linear model
fit.fn <- function(data, index) {
    result <- coef(lm(gpa ~ act , data = gpa, subset = index))
    return(result)
}
set.seed(1)
fit.boot = boot(gpa, fit.fn, R = 1000)
fit.boot</pre>
```

```
## CALL :
## boot.ci(boot.out = fit.boot, type = "perc", index = 1)
                                                                                                                                                                                                                                                                                                                                                                 boot.ci(fit.boot, type = "perc", index = 1) # intercept
                                                                                                          ## boot(data = gpa, statistic = fit.fn, R = 1000)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ## Calculations and Intervals on Original Scale
                                                                                                                                                                                                                                                                                                                                                                                                                                        ## BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
## Based on 1000 bootstrap replicates
                                                                                                                                                                                                                                                           0.35962727
                                                                                                                                                                                                                                 std. error
                                                                                                                                                                                                                                                                                     0.01455027
## ORDINARY NONPARAMETRIC BOOTSTRAP
                                                                                                                                                                                                                                                  ## t1* 2.11404929 -0.0108361368
                                                                                                                                                                                                                                                                                     ## t2* 0.03882713 0.0004350197
                                                                                                                                                                                                                               bias
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ## Level Percentile
## 95% ( 1.387, 2.812 )
                                                                                                                                                                                                ## Bootstrap Statistics
                                                                                                                                                                                                                                   original
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ## Intervals :
                                                                                   ## Call:
                                                                                                                                                                      #
```

```
## BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
## Based on 1000 bootstrap replicates
##
## CALL:
## boot.ci(boot.out = fit.boot, type = "perc", index = 2)
## Intervals:
## Level Percentile
## 95% ( 0.0110, 0.0674 )
## Calculations and Intervals on Original Scale
```

Question 2(a)

We want to examine StoreID, STORE and Store7 variables form the OJ data.

After a short EDA we determine that StoreID seems to contain all the info
in STORE and Store7. Thus, we can drop STORE and Store7.

We then use Purchase as our response, take StoreID as categorical, and split our data into a train set and test set for training and predicting

```
"SalePriceCH"
                                                                         "SpecialCH"
                                                         'PriceCH"
                                                                                        "SalePriceMM"
                                                         'WeekofPurchase" "StoreID"
                                                                         "DiscMM"
                                                                                        'LoyalCH"
                                                                         'DiscCH"
                                                  ## [1] "purchase"
## [5] "PriceMM"
## [9] "SpecialMM"
## [13] "PriceDiff"
## [17] "ListPriceDif
library(ISLR)
                names(01)
```

"PctDiscCH"

'PctDiscMM"

'Store7" "STORE"

[17] "ListPriceDiff"

03 = subset(03, select = c(Purchase, StoreID, Store7, STORE)) # use only these 4 variables str(0])

: \$ Store7 : Factor w/ 2 levels "No", "Yes": 1 1 1 1 2 2 2 2 2 ## 'data.frame': 1070 obs. of 4 variables:

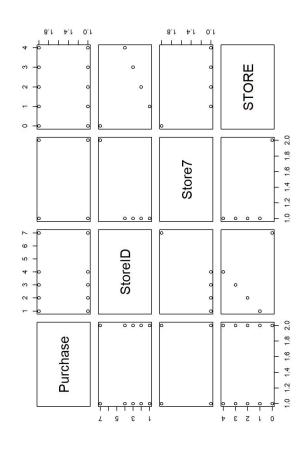
\$ Purchase: Factor w/ 2 levels "CH","MM": 111211111

\$ StoreID : num 1111777777...

\$ Store7 : Factor w/ 2 levels "No","Yes": 111122222

\$ STORE : num 1111000000...

STORE is a subset of StoreID and Store7 is transitive through StoreID pairs(01)



It appears that only StoreID and factor level "No" (intercept) from

rm(0))

Store7 have any significance when all predictors are used.

we drop Store7 and STORE

newOl = subset(Ol, select = c(-Store7, -STORE)) # I do not see any reason to force MM = 1 and CH = θ

new01\$StoreID = as.factor(new01\$StoreID) # take StoreID as factor # When I experimented, I was able to produce the same results

str(newOJ) # uncomment to verify is factor

split data 50/50, train/test

sampler = sample(1:n, n/2) # n/2 is the 50/50 splitter

train = newOJ[sampler,] test = newOJ[-sampler,]

n = nrow(new0J)

set.seed(1)

```
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' 1
                                                                                                   ## glm(formula = Purchase ~ ., family = binomial, data = Ol)
                                                                                                                                                                                                                                                                                                                                                                      \#\# (Dispersion parameter for binomial family taken to be 1) \#\#
                                                                                                                                                                                                                                                                                                                                                                                                        degrees of freedom
                                                                                                                                                                                                           ## Coefficients: (1 not defined because of singularities)
                                                                                                                                                                                                                                                                                                                                                                                                                             degrees of freedom
                                                                                                                                                                                                                                                               0.0010 **
                                                                                                                                                                                                                                             2.402 0.0163 *
                                                                                                                                                                                                                               Estimate Std. Error z value Pr(>|z|)
                                                                                                                                                                                                                                                                                 0.9583
fit = glm(Purchase~., family = binomial, data = 03)
                                                                                                                                                         Max
1.7136
                                                                                                                                                                                                                                                               0.07339 -3.290
                                                                                                                                                                                                                                                                                 0.052
                                                                                                                                                                                                                                                                                                    ¥
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ## Number of Fisher Scoring iterations: 4
                                                                                                                                                      3Q
1.1852
                                                                                                                                                                                                                                                                                                                                                                                                        ## Residual deviance: 1360.4 on 1067
                                                                                                                                                                                                                                               0.19347
                                                                                                                                                                                                                                                                                 0.36632
                                                                                                                                                                                                                                                                                                    ¥
                                                                                                                                                                        -0.9733 -0.7236
                                                                                                                                                         Median
                                                                                                                                                                                                                            ## Estimate
## (Intercept) 0.46471
                                                                                                                                                                                                                                                               -0.24147
                                                                                                                                                                                                                                                                                 0.01916
                                                                                                                                       ## Deviance Residuals:
                                                                                                                                                       10
                                                                                                                                                                                                                                                                                                                                                                                                                                             ## AIC: 1366.4
                                                                                                                                                                                                                                                                              ## Store7Yes
## STORE
                   summary(fit)
                                                                                                                                                                      ## -1.2736
                                                                                                                                                                                                                                                               ## StoreID
                                                                                 ## Call:
                                                                                                                                                       #
                                                                                                                                                                                                                                                                                                                     #
                                                                                                                                                                                         #
                                                                                                                                                                                                                                                                                                                                                    #
```

2(b)

The caret package does all of this nicely and compactly, so we proceed Here we train a logisitc regression model and use the confusion matrix plot the ROC curve and estimate using a 10 fold cross validation to obtain sensitivity, specificity, overall misclassification, then

through the next few questions using similar coding.

The accuracy from our model (train data) has accuracy (1-test error) very close to our confusion matrix accuracy (test data, predicted)

The ROC curve has a nice left corner shape, notice that the graph continues to the left til -0.5, needs to be fixed to origin preferably (sorry!) pROC shapes it this way with asp = 1 to keep the shape square

```
# 10 fold cv
# lobary(crossval) # could not make sense of its inner workings
# Library(crossval) # could not make sense of its inner workings
# Even their examples needed tailoring, and even after that
# it was not very intuitive. I instead proceed with Caret package.
# When using K-fold CV, we use the original dato set unsplit.
# However, I split the data beforehand so I could make a predict set
# with the test data. But in general this package's function should
# do its own K splits as it trains/tests on the data.
# A rother robust way of estimating accuracy (or test error rate)
| library(caret)
| set.seed(1)
| tc <- trainControl(method = "cv", number = 10, verboselter = F)
| model <- trainCoutrolsev., train, | method="glm", family="binomial", trControl = tc)
| model</pre>
```

```
## Generalized Linear Model

## 535 samples

## 15 predictor

## 2 classes: 'CH', 'MM'

## No pre-processing

## Resampling: Cross-Validated (10 fold)

## Summary of sample sizes: 481, 482, 481, 482, ...

## Accuracy Kappa

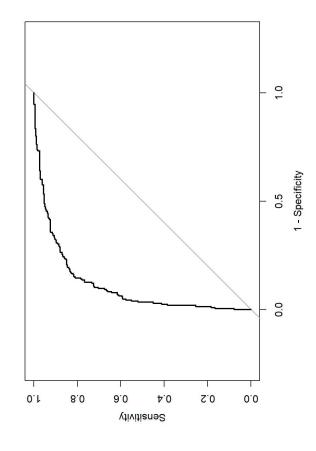
## Accuracy Kappa

## 0.8204403 0.6202817
```

```
# 10-fold CV estimated test error rate = 1 - overall misclassification
# also, this is 1 - accuracy = test error rate (estimated)
glm.err = 1 - model&results[,2]
prob = predict(model, test, type = "prob")
# pred = predict(model, test, two = "prob")
prod = predict(model, test, m or
pred < i felse(prob&mm >= 0.5, "Mm", "CH")
con.mat = table(test[, "purchase"], pred)
confusionMatrix(con.mat)
```

```
95% CI : (0.7854, 0.8522)
                                                                                    Accuracy : 0.8206
                                                                                                            No Information Rate : 0.6355
                                                                                                                        P-Value [Acc > NIR] : <2e-16
                                                                                                                                               Kappa : 0.6169
Mcnemar's Test P-Value : 0.3583
                                                                                                                                                                                                                      Neg Pred Value : 0.7415
                                                                                                                                                                                                                                   Prevalence: 0.6355
                                                                                                                                                                                               Specificity : 0.7795
                                                                                                                                                                                                                                                            Detection Prevalence : 0.6168
                                                                                                                                                                                                                                                                        Balanced Accuracy : 0.8118
                                                                                                                                                                                    Sensitivity: 0.8441
                                                                                                                                                                                                            Pos Pred Value : 0.8697
                                                                                                                                                                                                                                                Detection Rate : 0.5364
## Confusion Matrix and Statistics
                                                                                                                                                                                                                                                                                                'Positive' Class : CH
                                   CH MM 287 43
                                                          53 152
                       pred
                                               CH 287
                                                                      # # # # # # # # # # # # # # # # # # # #
```

```
library(pROC)
roc <- roc(test[, "Purchase"], prob$MM, levels = c("MM","CH"))
plot(roc, legacy.axes = T)</pre>
```



2(c)

We employ the same methods but using LDA instead

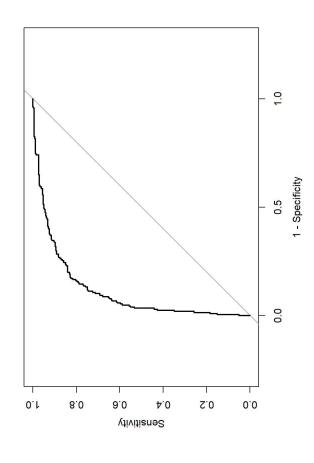
```
library(caret)
set.seed(1)
model <- train(Purchase~., train,
    method="lda", trControl = tc)
model
## Linear Discriminant Analysis
##
##</pre>
```

roc <- roc(test\$Purchase, prob\$MM, levels = c("MM","CH"))</pre>

plot(roc, legacy.axes = T)

1ibrary(pROC)

```
## Linear Discriminant Analysis
##
## 535 samples
## 2 classes: 'CH', 'MM'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 481, 482, 481, 482, 482, ...
## Resampling results:
##
## Accuracy Kappa
### 0.8205101 0.6215449
```



2(d)

We employ the same methods but using QDA instead QDA fails if there is rank deficiency, in other words we have columns that fully or partially (near fully) explain other columns. This means our data has linear dependency or multicollinearity. If we can't invert a matrix then we cannot use qda effectively or at all. Below is what would be the qda procedure if there were no multicollinearity. However, it will result in rank deficiency and ultimately fail.

```
# Library(caret)
# set.seed(1)
# model <- train(Purchase~., train,
# model <- train(Purchase~., train,
# model
# model
# model
# prob = predict(model, test, type = "prob")
# prob = predict(model, test, type = "prob")
# prof <- ifelse(prob$MM >= 0.5, "MM", "CH")
# confusionMatrix(table(test$Purchase, pred))
# Library(pRoC)
# roc <- roc(test$Purchase, prob$MM, Levels = c("MM", "CH"))
# plot(roc, legacy.axes = T)</pre>
```

2(e)

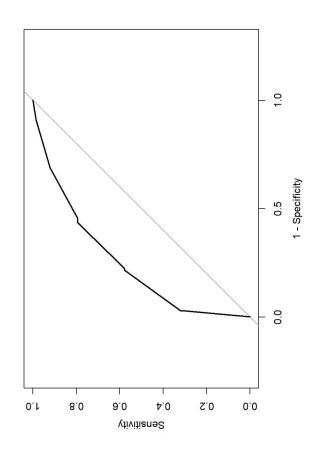
We employ the same methods but using KNN, we also use caret to find the optimal KNN k value for lowest test error rate

```
## Accuracy was used to select the optimal model using the largest value. ## The final value used for the model was k = 5.
                                                                                                                                                                                                                                                                                                                               ## Summary of sample sizes: 481, 482, 481, 482, 482, 482, ...
## Resampling results across tuning parameters:
##
                                                                                        model # optimal k is 5, caret automatically uses this k
                                                                   method="knn", trControl = tc)
                                                                                                                                                                                                                                                                                                            ## Resampling: Cross-Validated (10 fold)
                                         model <- train(Purchase~., train,
                                                                                                                                                                                                                                                                                                                                                                                                                                              0.3045327
                                                                                                                                                                                                                                                                                                                                                                                                                         0.6895178 0.3432383
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       9 0.6633124 0.2722348
                                                                                                                                                                                                                                           2 classes: 'CH', 'MM'
                                                                                                                                                                                                                                                                                                                                                                                                       k Accuracy Kappa
                                                                                                                                                  ## k-Nearest Neighbors
                                                                                                                                                                                                                                                               ##
## No pre-processing
                                                                                                                                                                                                                                                                                                                                                                                                                                              7 0.6743885
                                                                                                                                                                                                                        15 predictor
                                                                                                                                                                                             ## 535 samples
## 15 predictor
1ibrary(caret)
                      set.seed(1)
                                                                                                                                                                                                                                           #
                                                                                                                                                                                                                                                                                                                                                                                                     #
                                                                                                                                                                                                                                                                                                                                                                                                                         # # #
```

```
knn.err = 1 - model&results[,2]
prob = predict(model, test, type = "prob")
pred <- ifelse(prob&MM >= 0.5, "MM", "CH")
confusionMatrix(table(test&Purchase, pred))
```

```
## Confusion Matrix and Statistics
## pred
## CH AMM
## CH 262 68
## Accuracy : 0.7065
## Accuracy : 0.7065
## P-Value [Acc > NIR] : 0.007396
## Kappa : 0.3669
## Kappa : 0.3669
## Specificity : 0.7464
## Sensitivity : 0.7464
## Pos Pred Value : 0.110450
## Specificity : 0.6894
## Detection Rate : 0.6561
```

```
library(pROC)
roc <- roc(test$Purchase, prob$MM, levels = c("MM","CH"))
plot(roc, legacy.axes = T)</pre>
```



2(f)

Now lets combine all the test error rates together and see which is the lowest It seems that Ida is our best model for 10 fold CV

KNN had nearly double of the other models

rbind(glm.err, lda.err, qda.err, knn.er = min(knn.err))

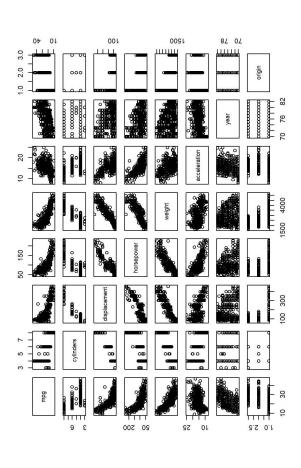
```
## glm.err "0.179559748427673"
## lda.err "0.179489867225716"
## qda.err "No good"
## knn.er "0.310482188293501"
```

Question 3(a)

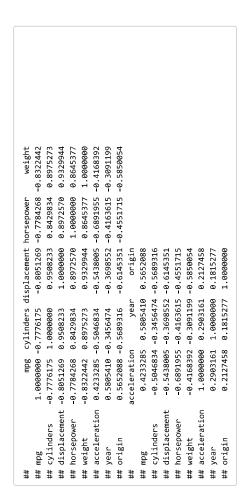
Let us dive into the Auto data from ISLR and use MPG as our response

```
: :
                                                                                                                                                                     8 8 8 8 8 8 8 8 8 ...
307 350 318 304 302 429 454 440 455 390
130 165 150 150 140 198 220 215 225 190
                                                                                                                                                                                                                                          12 11.5 11 12 10.5 10 9 8.5 10 8.5 ...
70 70 70 70 70 70 70 70 70 ...
                                                                                                                                                      18 15 18 16 17 15 14 14 14 15 ...
                                                                                                                                                                                                                          3504 3693 3436 3433 3449 ...
                                                                                                                                                                                                                                                                              11111111111...
                                                                                                                                    obs. of 8 variables:
                                                     auto = subset(Auto, select = -name)
                                                                                                                                                                        mnu :
                                                                                                                                                                                          $ displacement: num
                                                                                                                                                                                                          $ horsepower : num
                                                                                                                                                                                                                             mnu :
                                                                                                                                      392
                                                                                                                                                                                                                                                               mnu .
                                                                                                                                                        unu :
                                                                                                                                                                                                                                             $ acceleration: num
                                                                                                                                                                                                                                                                               unu:
                                                                                                                                   ## 'data.frame':
## $ mpg
## $ cylinders
## $ horsepower
## $ weight
## $ acceleration
## $ year
## $ year
                   library(leaps)
1ibrary(ISLR)
                                   set.seed(1)
                                                                                       str(auto)
                                                                      # eda
```

summary(auto) # nice way to get some quick stats, but messy so I commented
Just Looking at the scatterplots we see that mpg has many trends with others
pairs(subset(auto))

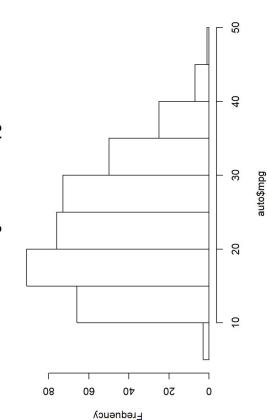


cor(auto)



seems to be right skewed
hist(auto\$mpg)

Histogram of auto\$mpg



here we look at what would be worthy predictor variables. However, # we are using all of them and whittling down with variable selection methods.

3(p)

For this part we want to use MLR using least squares

To make this part short we simply fit all predictors as our full model

Then run a summary and refit using only the significant ones

Lastly, we compare the models using partial F test and see that
the reduced model is better.

```
# fit a MLR
fit = lm(mpg~, data = auto)
summary(fit)
```

```
## Residual standard error: 3.328 on 384 degrees of freedom
                                                                                                                                                                                                                                                                                                                                           ## Multiple R-squared: 0.8215, Adjusted R-squared: 0.8182
                                                                                                                                                                                                                < 2e-16 ***
                                                                                                                                                    4.644294 -3.707 0.00024 ***
                                                                                                                                                                                                                                               14.729 < 2e-16 ***
                                                                                                                                                                                                                                                                                                                                                          ## F-statistic: 252.4 on 7 and 384 DF, p-value: < 2.2e-16
                                                                                                                                                                                   2.647 0.00844 **
                                                                                                                                                                                                                                                              5.127 4.67e-07 ***
                                                                                                                                                                                                -1.230 0.21963
-9.929 < 2e-16
                                                                                                                                                                     0.12780
                                                                                                                                                                                                                                  0.41548
                                                                                                                                       Estimate Std. Error t value Pr(>|t|)
                                                                                                                                                                                                                                  0.815
                                                                                                                                                                     -1.526
                                                                                      ## -9.5903 -2.1565 -0.1169 1.8690 13.0604
## Coefficients:
                                                                           Мах
                                                                                                                                                                     0.323282
                                                                                                                                                                                   0.007515
                                                                                                                                                                                                                0.000652
                                                                                                                                                                                                                                                  0.050973
                            ## lm(formula = mpg ~ ., data = auto)
                                                                                                                                                                                                   0.013787
                                                                                                                                                                                                                                  0.098845
                                                                                                                                                                                                                                                                0.278136
                                                                                                                                                      -17.218435
                                                                           1Q Median
                                                                                                                                                                     -0.493376
                                                                                                                                                                                   0.019896
                                                                                                                                                                                                   -0.016951
                                                                                                                                                                                                                  -0.006474
                                                                                                                                                                                                                                  0.080576
                                                                                                                                                                                                                                                  0.750773
                                                                                                                                                                                                                                                                1,426141
                                                                                                                                                                                  ## displacement
## horsepower
## weight
                                                                                                                                                   ## (Intercept)
## cylinders
                                                                                                                                                                                                                                  ## acceleration
                                                           ## Residuals:
                                                                                                                                                                                                                                                ## year
## origin
##
## Call:
                                                                         #
                                                                                                                                      #
                                                                                                                                                                                                                                                                               #
```

Lets refit using only significant values seen in summary anova(fit, lm(mpg~.-cylinders-horsepower-acceleration, data = auto))

	Res.Df	RSS	<u></u>	Sum of Sq	ட	Pr(>F)
	< qp>	< qp>	<qp></qp>	< qp>	< qp>	< qp>
_	384	4252.213	NA	NA	NA	NA
2	387	4332.729	ဇှ	-80.51617	2.423696	0.06542561
2 rows						

```
# we reject the null saying they are equal thus we use the reduced model
fit = lm(mpg~.-cylinders-horsepower-acceleration, data = auto)
lm.ar2 = summary(fit)$adj.r.squared
```

3(c)

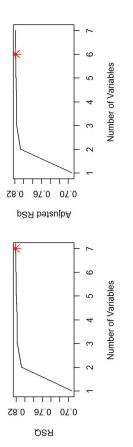
We use best subest variable selection method here to and use R-square alongside Adjusted R-square to determine our model.

```
# best subset method

totpred <- ncol(auto) - 1
  fit.full <- regsubsets(mpg~., auto, nvmax = totpred)
  fit.summary <- summary(fit.full)
  fit.summary</pre>
```

```
cylinders displacement horsepower weight acceleration year origin
                                                                                                                                                           *
                                                                                                                                                                    *
                                                                                                                                                                              *
                                                                                                                                                                                       :
*
                                                                                                                                                                                                 *
                                                                                                                                                          * * * * *
## Subset selection object ## Call: regsubsets.formula(mpg \sim ., auto, nvmax = totpred)
                                                                                                                                                                                      = =
*
                                                                                                                                                          *
                                                                                                                                                                    *
*
                                                                                                                                                                              =
*
=
                                                                                                                                               : : : :
                                                                                       FALSE
FALSE
                                                                    FALSE
                                                                             FALSE
                                                           FALSE
                             Forced in Forced out
                                                                                                                    ## Selection Algorithm: exhaustive
## cylinders displacement
                                                                                                            ## 1 subsets of each size up to 7
                  ## 7 Variables (and intercept)
                                                                                                                                                : :
                                                                    FALSE
                                                                             FALSE
                                                                                       FALSE
                                       FALSE
                                                FALSE
                                                         FALSE
                                                                                                 FALSE
                                                                                                                                                                    <del>*</del>
                                                                                                                                               ## 1 (1)""
                                                                                                                                                                              (1)""
                                                ## displacement
                                                                             ## acceleration
                                                                                                                                                                                                 (1)"*"
                                                                                                                                                                                         (1)"*"
                                                         ## horsepower
                                       ## cylinders
                                                                                      ## year
## origin
                                                                  ## weight
                                                                                                                                                 # 2
                                                                                                                                                                    ## 4
                                                                                                                                                                               # 2
                                                                                                                                                                                         9 ##
```

```
## (Intercept) cylinders displacement horsepower weight
## -15.563492306 -0.506685137 0.019269286 -0.023895029 -0.006218311
## year origin
## 0.747515952 1.428241885
```



3(d)

Now we use forward stepwise selection

```
fit.fwd = regsubsets(mpg~., auto, nvmax = totpred, method = "forward")
fit.summary <- summary(fit.fwd)
fit.summary</pre>
```

```
## Call: regsubsets.formula(mpg ~ ., auto, nvmax = totpred, method = "forward")
## 7 Variables (and intercept)
## Forced in Forced out
## cylinders FALSE FALSE
## displacement FALSE FALSE
## horsepower FALSE FALSE
                                                                                                            cylinders displacement horsepower weight acceleration year origin
                                                                                                                                     :
*
                                                                                                                                             *
                                                                                                                                                      *
                                                                                                                                                              *
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*
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                                                                                                                                                             * *
                                                                                                                                                                      -X-
                                                                                                                                  * * * * *
                                                                                                                           *
                                                                                                                                   : :
                                                        FALSE
                                                                          FALSE
                                                                  FALSE
                                                                                    FALSE
## Subset selection object
                                        FALSE
FALSE
FALSE
```

```
plot(fit.summary$adjr2, xlab = "Number of Variables", ylab = "Adjusted RSq",
                                                                               # Plot model fit measures for best model of each size against size
                                                                                                                                                                                            plot(fit.summary$rsq, xlab = "Number of Variables", ylab = "RSQ"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 # Get coefficients of best model for a given size
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      point = as.numeric(which.max(fit.summary$adjr2))
                                                                                                                                                                                                                                                                        point = as.numeric(which.max(fit.summary$rsq))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       points(point, fit.summary$adjr2[point],
                                                                                                                                                                                                                                                                                                                   points(point, fit.summary$rsq[point],
    col = "red", cex = 2, pch = 8)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  col = "red", cex = 2, pch = 8)
fwd.ar2 = mean(fit.summary$adjr2)
                                                                                                                   par(mfrow = c(2, 2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         coef(fit.fwd, 6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              type = "l")
                                                                                                                                                                                                                                                                                                                                                                                                  # Adjusted R^2
```

weight -0.006218311

horsepower

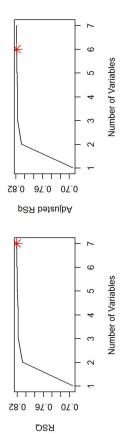
cylinders displacement

-0.506685137 origin 1.428241885

(Intercept) ## -15.563492306 ## year 0.747515952

#

0.019269286 -0.023895029



3(e)

Last but not least is backward stepwise selection

```
fit.bwd = regsubsets(mpg \sim, auto, nvmax = totpred, method = "backward") \\ fit.summary <- summary(fit.bwd)
                                                                                fit.summary
```

```
## Call: regsubsets.formula(mpg ~ ., auto, nvmax = totpred, method = "backward")
## 7 Variables (and intercept)
## 7 Variables (and intercept)
## cylinders FALSE FALSE
## displacement FALSE FALSE
## horsepower FALSE FALSE
## horsepower
                                                                                                                            cylinders displacement horsepower weight acceleration year origin
                                                                                                                                                        *
                                                                                                                                                                  *
                                                                                                                                                                            *
                                                                                                                                                                                     *
                                                                                                                                                                                              *
                                                                                                                                                        *
                                                                                                                                                                 *
                                                                                                                                                                            *
                                                                                                                                                                                              -X-
                                                                                                                                                       * *
                                                                                                                                                                          * * *
                                                                                                                                             *
                                                                  FALSE
                                                                                     FALSE
                                                                FALSE
                                                                                                FALSE
## Subset selection object
                                              FALSE
FALSE
FALSE
```

```
plot(fit.summary$adjr2, xlab = "Number of Variables", ylab = "Adjusted RSq",
# Plot model fit measures for best model of each size against size
                                                                                                                       plot(fit.summary$rsq, xlab = "Number of Variables", ylab = "rsq",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      # Get coefficients of best model for a given size
                                                                                                                                                                                                                                                                                                                                                                                                                                                  point = as.numeric(which.max(fit.summary$adjr2))
                                                                                                                                                                                                  point = as.numeric(which.max(fit.summary$rsq))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              points(point, fit.summary$adjr2[point],
                                                                                                                                                                                                                                            points(point, fit.summary$rsq[point],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    col = "red", cex = 2, pch = 8)
                                                                                                                                                                                                                                                                                     col = "red", cex = 2, pch = 8)
                                         par(mfrow = c(2, 2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               coef(fit.bwd, 6)
                                                                                                                                                                                                                                                                                                                                                                                                            type = "l")
                                                                                                                                                                                                                                                                                                                              # Adjusted R^2
```

```
bwd.ar2 = mean(fit.summary$adjr2)
```

weight -0.006218311

horsepower

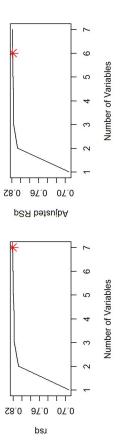
cylinders displacement

-0.506685137 origin 1.428241885

(Intercept) ## -15.563492306 ## year 0.747515952

#

0.019269286 -0.023895029



Now we compare each model against a LOOCV on the data to see which model Interestingly all subest methods resulted in the same model is closest to the LOOCV adjusted R-square

```
tc <- trainControl(method = "loocv", verboseIter = F)</pre>
and our quick and easy MLR model is the best of the 4
                                                        # we compare each model using LOOCV from caret
                                                                                                                                                                              1ibrary(caret)
                                                                                                                                     set.seed(1)
                                                                                                                                                                                                                                        model
```

```
## Linear Regression
## 1 Janear Regression
## 392 samples
## 7 predictor
##
## 7 predictor
##
## No pre-processing
## Resampling: Leave-One-Out Cross-Validation
## Resampling results:
## Resampling results:
## 2.556369 NaN 2.556369
## 1.556369 NaN 2.556369
## Tuning parameter 'intercept' was held constant at a value of TRUE

loocv.ar2 = summary(model)$adj.r.squared

rbind(loocv.ar2, lm.ar2, best.ar2, fwd.ar2, bwd.ar2)

## Loocv.ar2 0.888238
## lm.ar2 0.888238
## ha.ar2 0.9797419
## best.ar2 0.7979419
## best.ar2 0.7979419
## bwd.ar2 0.7979419
```