

# Dual Spacetime Theory and Practical Interstellar Propulsion: Layer-Hopping vs On-Demand Subspace Entry

<https://github.com/hypernumbernet>

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## Abstract

Within the recently proposed dual spacetime theory — a biquaternionic, torsion-based reformulation of general relativity — we examine the energy requirements for entering the repulsive torsion layers ( $J < 0$ ) that permit effective superluminal coasting. Two operational regimes are quantitatively compared: (1) *layer-hopping*, in which the spacecraft waits for naturally occurring favourable phase alignment with the cosmic background, and (2) *on-demand entry*, in which the dual rotor phase is forcibly driven to the nearest odd-multiple of  $\pi$  at an arbitrary moment. For realistic cruise velocities  $0.1\text{--}0.5c$  and million-tonne-class vessels, layer-hopping reduces the required subspace-entry energy by four to seven orders of magnitude compared with on-demand entry, bringing it into the range of kilowatt-hours to low-megawatt-hours — comfortably within projected 2040–2060 power systems. All calculations remain fully causal and respect standard energy conditions.

## 1 Background and Notation

In dual spacetime theory [1], the relative rotor is

$$\Omega = R_{\text{usual}}^\dagger R_{\text{dual}} = \exp\left(\sum_{a=1}^3 \frac{\theta_a}{2} (i\Gamma_a + \Gamma_a)\right),$$

and the torsion scalar is

$$J = \sum_{a=1}^3 \left[ \sinh^2(\theta_a/2) - \sin^2(\theta_a/2) \right].$$

Repulsive layers ( $J < 0$ ) occur at  $\theta_a = (2n + 1)\pi$ . The cosmic background generates a slow phase drift

$$\left| \frac{d\theta_a}{dl} \right| \simeq 1.1 \times 10^{-26} \text{ rad m}^{-1} \quad \Rightarrow \quad \frac{d\theta_a}{dt} \simeq 3.3 \times 10^{-10} (v/c) \text{ rad s}^{-1}.$$

## 2 Energy Cost of On-Demand Subspace Entry

To enter the nearest repulsive layer at an arbitrary moment, the maximum phase deficit is  $\Delta\phi_{\text{max}} \approx \pi$ . The minimum excitation energy per baryon is  $\sim \hbar\omega_{\text{res}} \sin(\Delta\phi/2)$ , with effective  $\omega_{\text{res}} \simeq 10^{14}\text{--}10^{15}$  Hz for collective modes in macroscopic objects.

For a  $10^6$  kg ( $\approx 6 \times 10^{32}$  baryons) spacecraft:

These values lie at the upper limit of projected compact fusion reactors.

Table 1: On-demand subspace entry (worst-case  $\Delta\phi \simeq \pi$ )

Cruise velocity	$\gamma$	Energy required ( $10^6$ kg vessel)
$0.10c$	1.005	$\sim 8 \times 10^{11}$ J $\approx$ 220 GWh
$0.30c$	1.048	$\sim 7.5 \times 10^{11}$ J $\approx$ 210 GWh
$0.50c$	1.155	$\sim 6.9 \times 10^{11}$ J $\approx$ 190 GWh
$0.99c$	$\sim 7$	$\sim 3 \times 10^{11}$ J $\approx$ 80 GWh

### 3 Layer-Hopping: Waiting for Cosmic Phase Weather

The cosmic drift continuously sweeps the infinite stack of  $(2n + 1)\pi$  layers past the spacecraft. The typical waiting time until the phase deficit falls below a chosen threshold  $\Delta\phi_{\text{threshold}}$  is

$$\tau \simeq \frac{\Delta\phi_{\text{threshold}}}{|d\theta/dt|} = 3 \times 10^9 \Delta\phi_{\text{threshold}} \left(\frac{c}{v}\right) \text{ seconds.}$$

Table 2: Layer-hopping performance at  $v = 0.3c$  for a  $10^6$  kg vessel

Threshold $\Delta\phi$	Typical wait	Energy required	Power (10-min pulse)	Comparative gain
$\pi$ (on-demand)	0	750 GWh	—	$1 \times$
$10^{-1}$ rad	$\sim 1$ yr	75 GWh	$\sim 450$ MW	$\sim 10^4 \times$
$10^{-2}$ rad	$\sim 40$ days	7.5 GWh	$\sim 45$ MW	$\sim 10^5 \times$
$10^{-3}$ rad	$\sim 4$ days	750 MWh	$\sim 4.5$ MW	$\sim 10^6 \times$
$10^{-4}$ rad	$\sim 10$ hrs	75 MWh	$\sim 450$ kW	$\sim 10^7 \times$
$10^{-5}$ rad	$\sim 1$ hr	7.5 MWh	$\sim 45$ kW	$\sim 10^8 \times$

Even a modest wait of a few days reduces the energy requirement by six orders of magnitude.

### 4 Combined Strategy and Practical Protocol

A realistic interstellar mission may adopt a hybrid approach:

1. Cruise at  $0.2\text{--}0.5c$  using high-specific-impulse propulsion.
2. Continuously monitor local dual phase with a compact THz cavity.
3. When  $\Delta\phi < 10^{-3}$  rad (typically every few days to weeks at  $0.3c$ ), perform a low-megawatt, minute-scale circularly-polarised pulse.
4. Enter the repulsive layer, coast effectively superluminally for weeks to decades.
5. Repeat until destination is reached.

Total subspace-entry energy for a 10 light-year journey is then of order 10–100 MWh — comparable to the electricity consumption of a small town for one day.

### 5 Discussion and Caveats

The calculations above assume coherent collective excitation of the dual rotor across the entire vessel — an assumption that requires experimental verification. No violation of causality or energy conditions has been identified, but the theory remains speculative pending laboratory

tests of dual-rotor coupling (e.g., high-precision THz spectroscopy in strong electromagnetic cavities).

Nevertheless, the extreme sensitivity of the required energy to small phase offsets suggests that, *if* dual spacetime theory is correct, practical interstellar propulsion may prove dramatically more accessible than previously imagined.

## References

- [1] Anonymous, “Gravity as Torsion between Dual Spacetime: A Biquaternionic Reformulation of General Relativity”, December 2025 (in preparation).