

# ABOUT THE BANDWIDTH

## ASSUMPTIONS

#1

$m_i$  IS THE MESSAGE PROCESSED BY THE  $i$ -TH NODE OF THE NETWORK; IT CONTAINS 2 (INTERESTING) FIELDS:

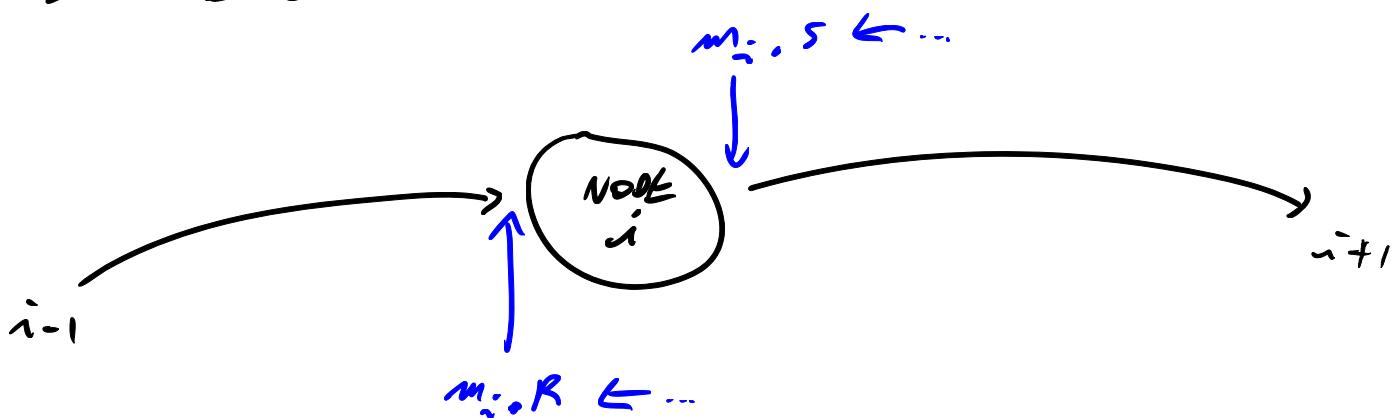
$m_i.R$  RECEIVING TIME

$m_i.S$  SENDING TIME

#2

WHEN A NODE RECEIVES THE MESSAGE, IT REWRITES  $m_i.R$  IMMEDIATELY AFTER THE SYS CALL READ(), AND WHEN IT HAS TO SEND THE MESSAGE TO THE NEXT NODE, IT REWRITES IMMEDIATELY THE FIELD  $m_i.S$ .

SEE THE DRAWING:



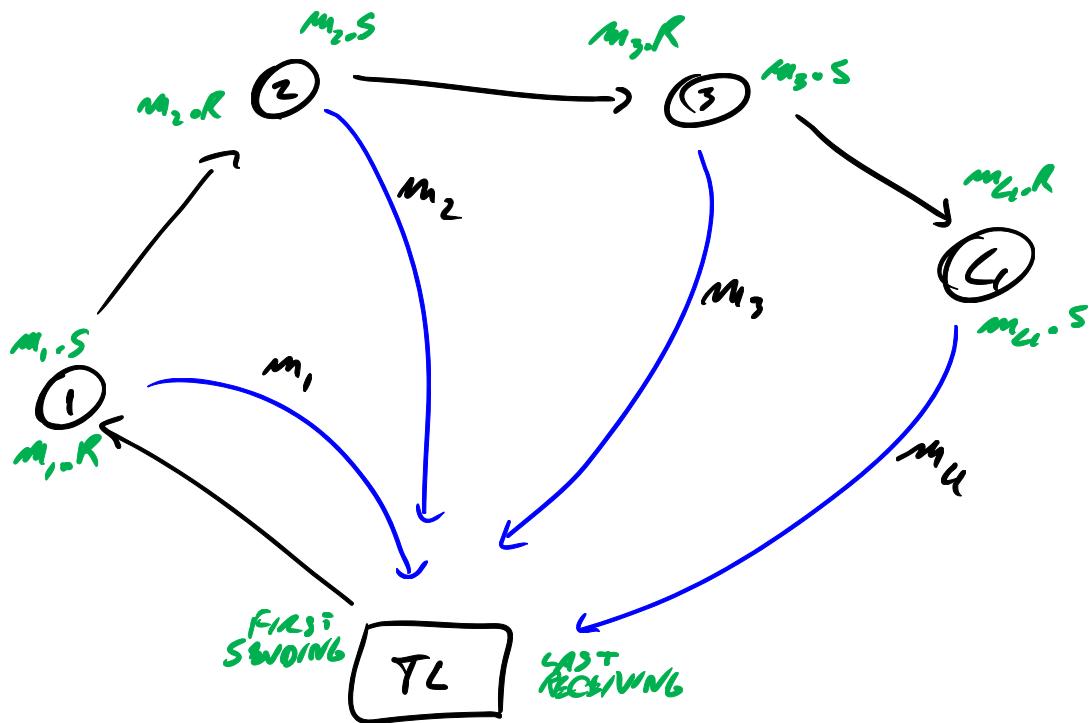
#3

THE NODE SENDS A COPY OF THE MESSAGE TO THE TURN LEADER ONLY AFTER THE HOP.

#4

THE TURN LEADER HAS TWO VARS **FIRST-SENDING** AND **LAST-RECEIVING**, BOTH INSTANTS OF TIME. (SEE #2)

## AN EXAMPLE



	R	S	$\Delta m$	
$m_1$	1	3	2	FIRST\_SENDING : 0
$m_2$	5	7	2	LAST - RECEIVING: 17
$m_3$	9	10	1	
$m_4$	11	15	4	$\Delta m_i := m_i.S - m_i.R$

TOTAL TIME:

$$Tot-T = LAST\_RECEIVING - FIRST\_SENDING = 17$$

COMPUTATION TIME:

$$Comp-T = \sum_i^4 \Delta m_i = 2+2+1+4 = 9$$

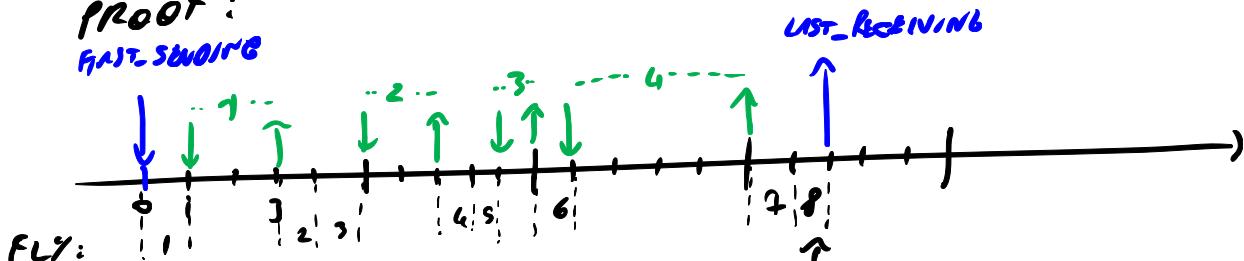
FLY TIME:

$$Fly-T = Tot-T - Comp-T = 17 - 9 = 8$$

PROOF:

FIRST-SENDING

LAST RECEIVING



## AVERAGE TIME

$$\bar{T}_{\text{tot\_T\_average}} = \frac{1}{\text{INNERLOOPS}} \sum_i^{\text{INNERLOOPS}} \bar{T}_{\text{tot\_T}(i)}$$

$$\bar{F}_{ly\_T\_average} = \frac{1}{\text{INNERLOOPS}} \sum_i^{\text{INNERLOOPS}} \bar{F}_{ly\_T}(i)$$

## BANDWIDTH

$$BITS := 8 * \text{sizeof}(\text{MESSAGE\_T})$$

$$\bar{T}_{\text{tot\_BW}} = \frac{BITS}{\bar{T}_{\text{tot\_T\_average}}}$$

$$\bar{F}_{ly\_BW} = \frac{BITS}{\bar{F}_{ly\_T\_average}}$$