

Introduction to Machine Learning

Lecture 11: Neural Networks

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Machine Intelligence Research and Applications Lab



Contents

- Introduction
- Multi-Layer Perception
- Tips

2

Introduction

Breakthroughs by Deep Learning

Face recognition



SENSETIME
商汤科技

Face++ 旷视

云从科技
CLOUDWALK

阿里云
aliyun.com

3

4

Breakthroughs by Deep Learning

Machine translation

Microsoft | The AI Blog | The official research blog | Microsoft on Medium | Twitter

Microsoft reaches a historic milestone, using AI to match human performance in translating news from Chinese to English

March 16, 2019 @Microsoft



5

Breakthroughs by Deep Learning

Speech recognition

Microsoft AI Beats Humans at Speech Recognition

By Richard Adelman
Oct 26, 2016 11:40 AM PT

Print
Email



6

Breakthroughs by Deep Learning

Self-driving



7

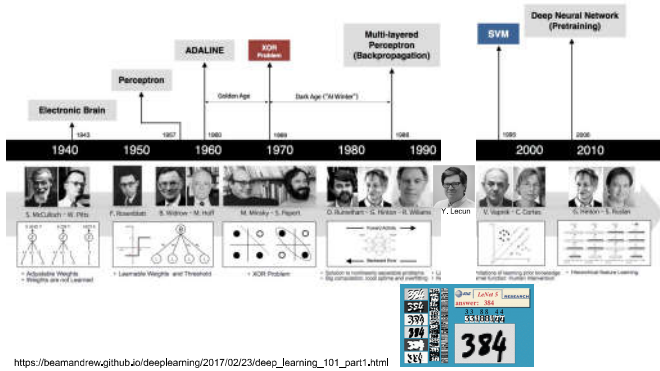
Breakthroughs by Deep Learning

Machine reading comprehension

SQuAD					Home
SQuAD1.1 Leaderboard					
Since the release of SQuAD1.0, the community has made rapid progress, with the best models now rivaling human performance on the task. Here are the ExactMatch (EM) and F1 scores evaluated on the test set of v1.1.					
Rank	Model	EM	F1		
	Human Performance Stanford University (Rajpurban et al. '18)	82.304	91.221		
1	rlmnet (unsupervised) Microsoft Research Asia	85.356	93.202	view on SQuAD	
2	QANet (unsupervised) Google Brain & CMU	84.454	90.490	view on SQuAD	
3	rlmnet (unsupervised) Microsoft Research Asia	84.003	90.147	view on SQuAD	

8

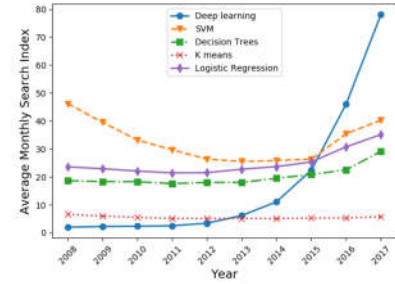
Milestones of Deep Learning



https://beamandrew.github.io/deeplearning/2017/02/23/deep_learning_101_part1.html

9

Google Trend of Deep Learning



Mehdi Mohammadi, et al, Deep Learning for IoT Big Data and Streaming Analytics: A Survey, IEEE Communications Surveys and Tutorials Journal, 2018.

10

Motivation of Neural Networks

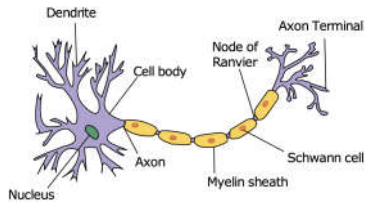


Diagram of neuron

<https://simple.wikipedia.org/wiki/Neuron>

11

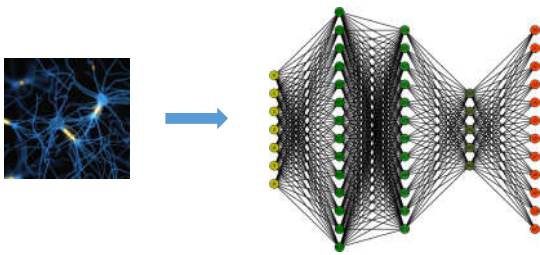
Motivation of Neural Networks



<http://news.mit.edu/2015/how-brain-recognizes-objects-1005>

12

What is Neural Network?



Biological Neural Network

Artificial Neural Network

13

Multi-Layer Perceptron

Hand-written Digits Recognition

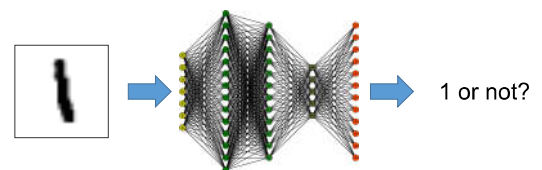
The MNIST dataset



By Josef Steppan - Own work, CC BY-SA 4.0, <https://commons.wikimedia.org/w/index.php?curid=64810040>

15

Hand-written Digits Recognition



16

Vector representation

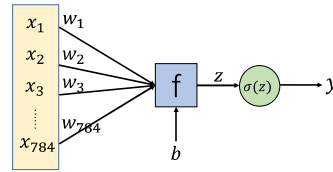
x : image

28×28 pixels \rightarrow 28×28 pixels \rightarrow $\begin{bmatrix} 0 \\ 1 \\ \dots \\ 0 \end{bmatrix} \in \mathbb{R}^{784}$ 1: for ink
0: otherwise

Input domain

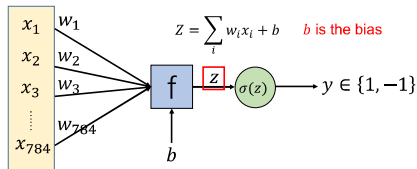
17

Single Neuron



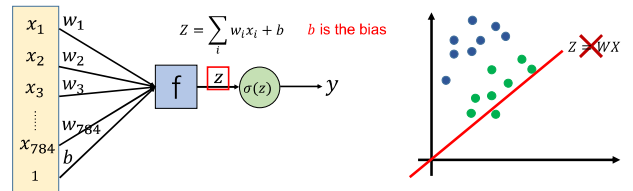
18

Single Neuron



19

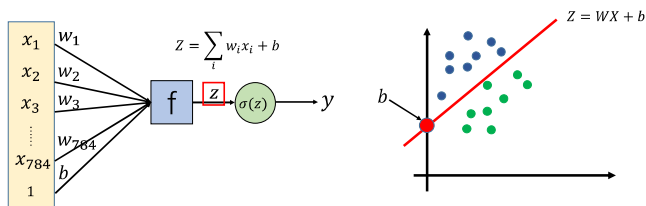
Single Neuron



Why do we need a bias b ?

20

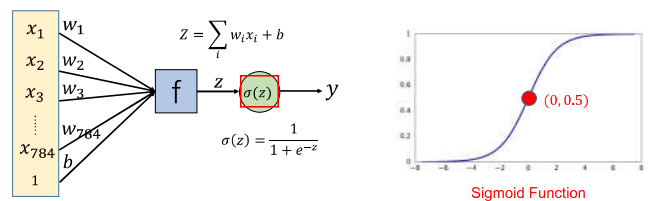
Single Neuron



Why do we need a bias b ?

21

Single Neuron

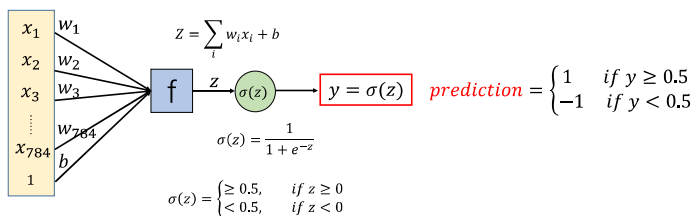


Sigmoid Function

$$\sigma(z) = \begin{cases} \geq 0.5, & \text{if } z \geq 0 \\ < 0.5, & \text{if } z < 0 \end{cases}$$

22

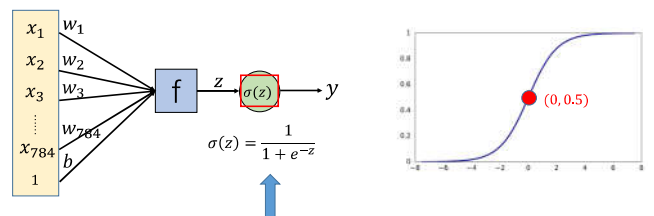
Single Neuron



This is a linear classifier.

23

Activation Function



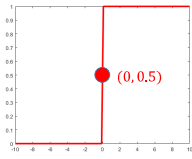
Activation function: The function that acts on the weighted combination of inputs.

We also have other activation function.

24

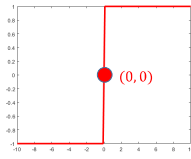
Activation Function

Boolean



$$\sigma(z) = \begin{cases} 1 & z > 0 \\ 0.5 & z = 0 \\ 0 & z < 0 \end{cases}$$

Unit step function



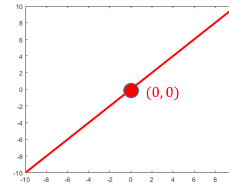
$$\sigma(z) = \begin{cases} 1 & z > 0 \\ 0 & z = 0 \\ -1 & z < 0 \end{cases}$$

Sign function

25

Activation Function

Linear



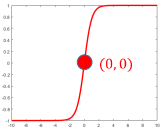
$$\sigma(z) = z$$

Linear function

26

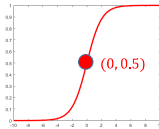
Activation Function

Non-linear



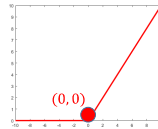
$$\sigma(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

Tanh function



$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

Sigmoid function



$$\sigma(z) = \max(0, z)$$

ReLU function

Non-linear activation functions are frequently used in neural networks.

Why?

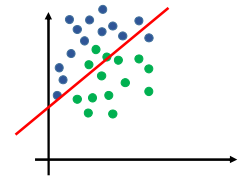
27

Why Non-Linearity?

Without non-linearity

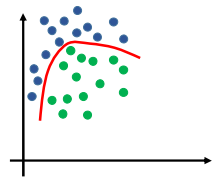
- Deep neural networks are equivalent to linear transforms.

$$W_1(W_2(W_3 \cdot x)) = Wx$$



With non-linearity

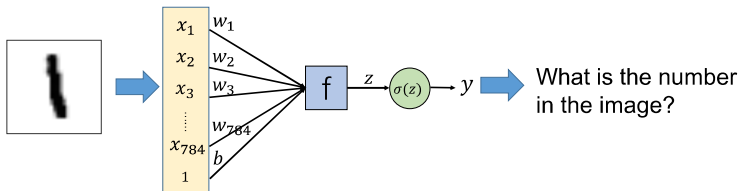
- The neural networks can approximate complicated functions.



<http://cs224d.stanford.edu/lectures/CS224d-Lecture4.pdf>

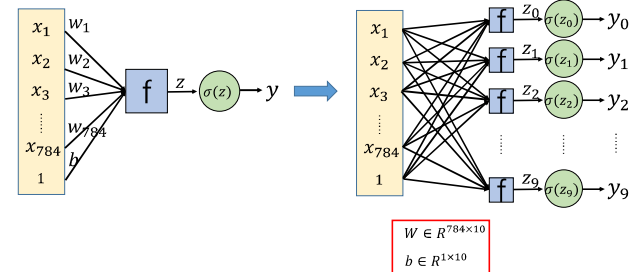
28

A More Complicated Task



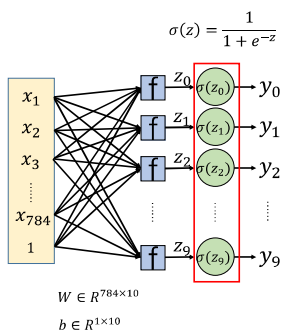
29

Multiple Outputs



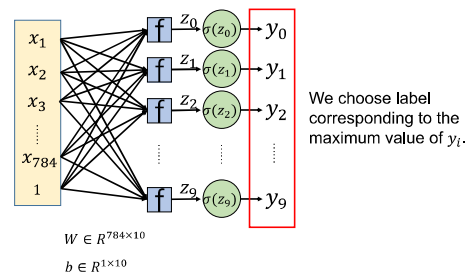
30

Multiple Outputs



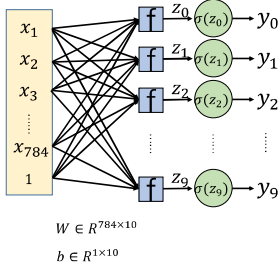
31

Multiple Outputs



32

Multiple Outputs

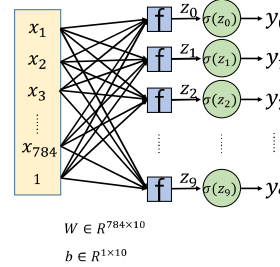


Question :

How do we evaluate the performance of the model?

33

Loss Function



Ground truth: $Q = \begin{bmatrix} 0 \\ 1 \\ \dots \\ 0 \end{bmatrix} \in R^{10}$ One hot vector
The component corresponding to the true label is "1".

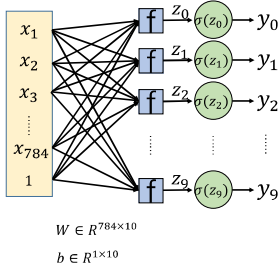
$$p_i = \text{softmax}(y_i) = \frac{e^{y_i}}{\sum_i e^{y_i}}$$

$$\text{Loss} = \text{cross entropy} = - \sum_i q_i \log(p_i)$$

The goal is to minimize the loss!

34

Model Parameters



$$y = f(x) = \sigma(Wx + b)$$

Model parameter set $\theta = \{W, b\}$

Minimize the loss = Pick the best θ

35

Optimization

Any idea to pick the optimal parameter values ?



36

Optimization

Any idea to pick the optimal parameter values ?

(Stochastic) Gradient Descent

Backpropagation

37

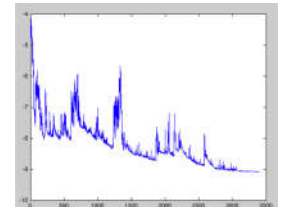
Stochastic Gradient Descent

$$\min_x F(x) = \sum_{i=1}^n f_i(x)$$

- Initialize the parameter x and learning rate η
- Repeat until the termination condition is met
 - Randomly shuffle examples in the training set
 - For $i = 1, \dots, n$

$$x_{k+1} \leftarrow x_k - \eta \nabla f_i(x_k)$$

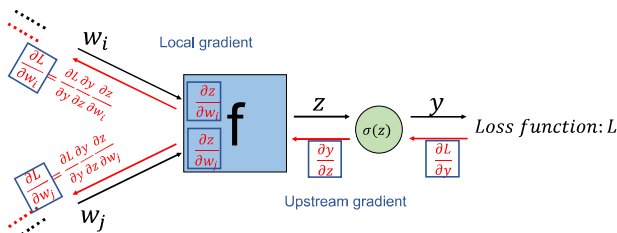
Descent is in the sense of expectation.



By Joe pharos at the English language Wikipedia. CC BY-SA 3.0. <https://commons.wikimedia.org/w/index.php?curid=42498187>

38

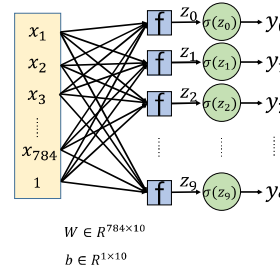
Backpropagation



Upstream gradient * Local gradient

39

Backpropagation



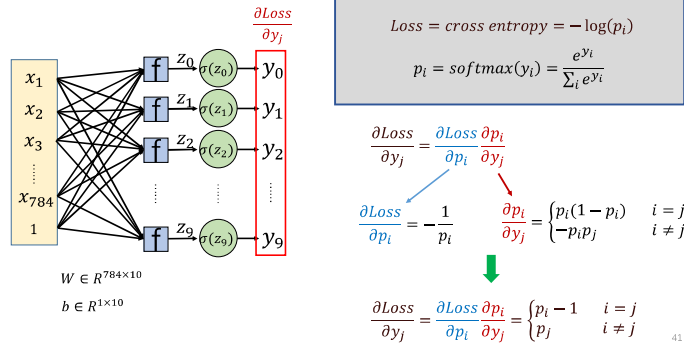
Ground truth: $Q = \begin{bmatrix} 0 \\ 1 \\ \dots \\ 0 \end{bmatrix} \in R^{10}$ One hot vector:
the component corresponding to the true label is "1".

$$p_i = \text{softmax}(y_i) = \frac{e^{y_i}}{\sum_i e^{y_i}}$$

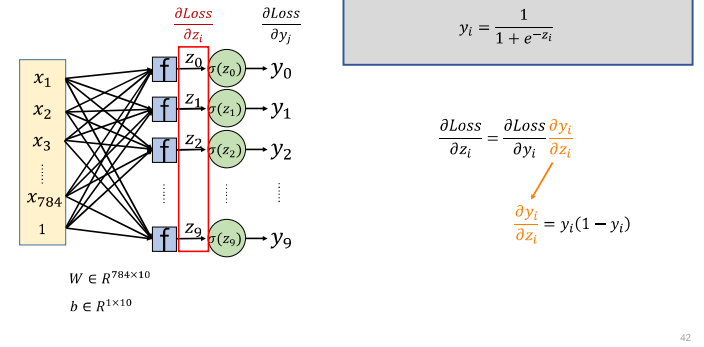
$$\text{Loss} = \text{cross entropy} = - \sum_i q_i \log(p_i) = - \log(p_i)$$

40

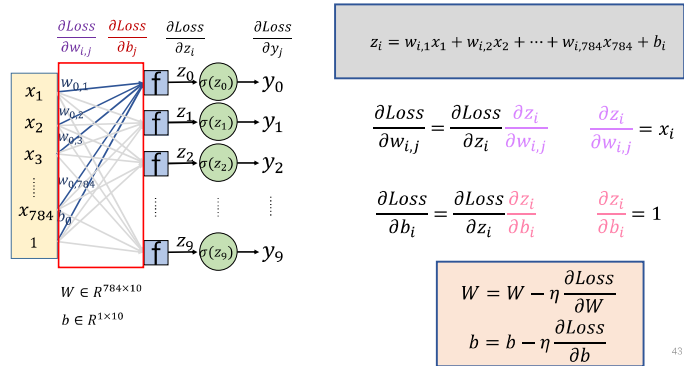
Backpropagation



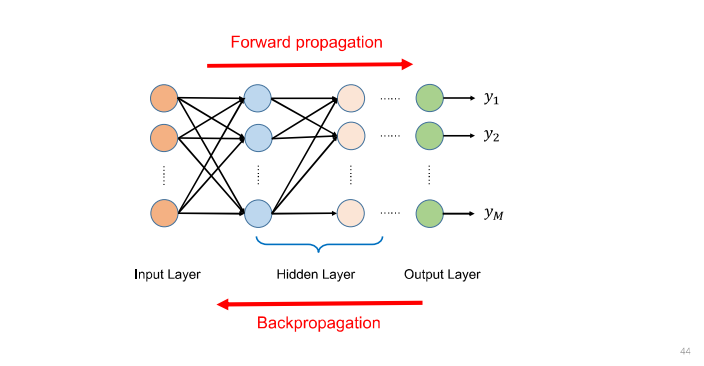
Backpropagation



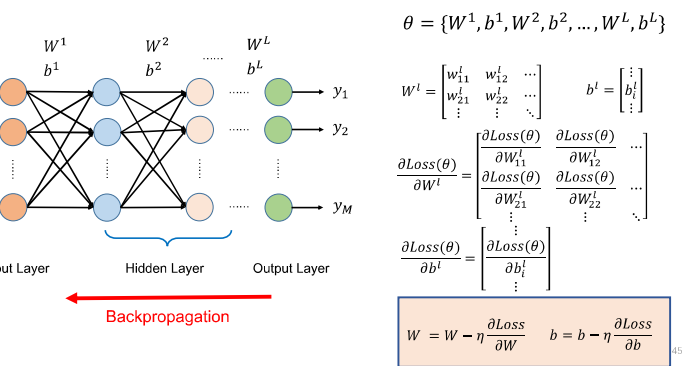
Backpropagation



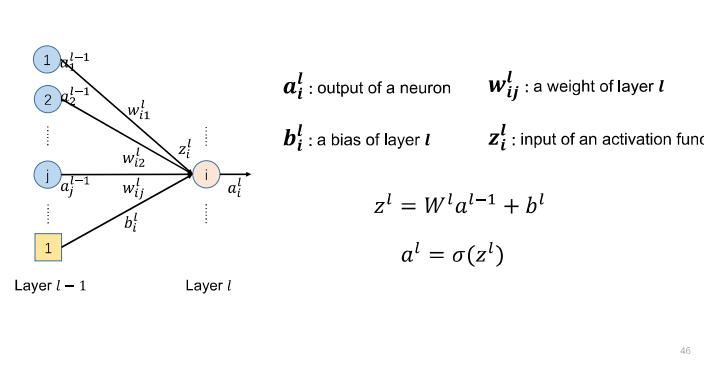
Backpropagation : Multi-Layer Perceptron



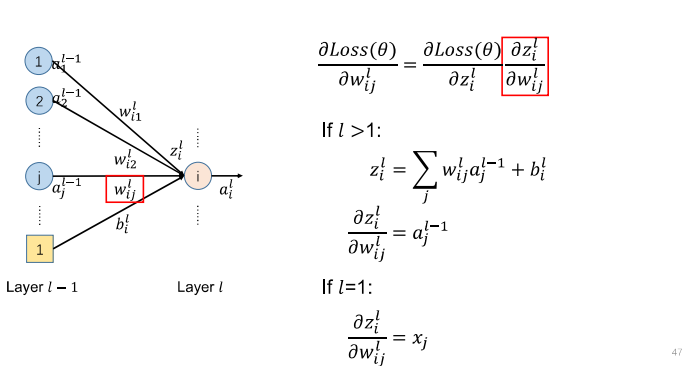
Backpropagation : Multi-Layer Perceptron



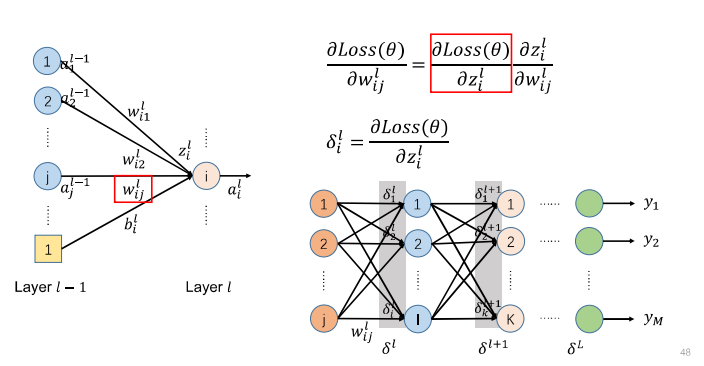
Backpropagation : Multi-Layer Perceptron



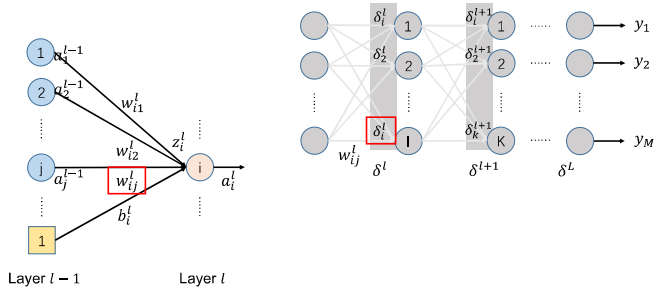
Backpropagation : Multi-Layer Perception



Backpropagation : Multi-Layer Perception

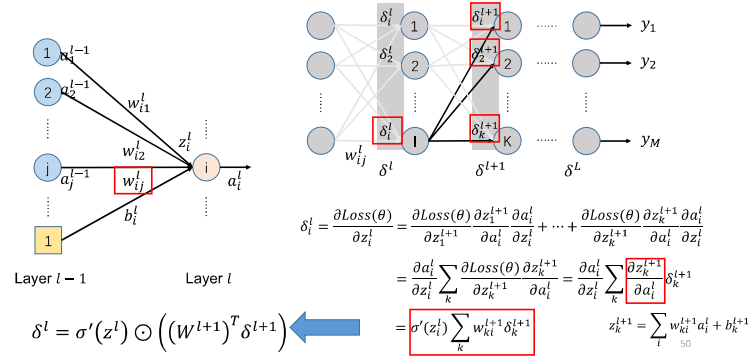


Backpropagation : Multi-Layer Perception

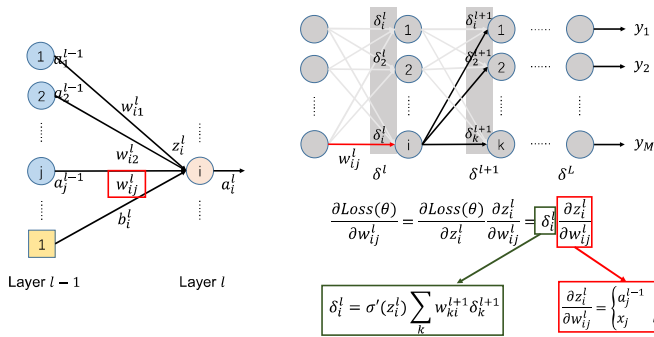


49

Backpropagation : Multi-Layer Perception



Backpropagation : Multi-Layer Perception



51

Universal Function Approximator



- Input domain: document, word, image, voice, etc.
- Output domain: probability distribution, single label, etc.

52

Universal Function Approximator

The learning algorithm is to map the input domain X into the output domain Y

$$f : X \rightarrow Y$$

- Handwriting Recognition

$$f(\text{1}) = \text{"1"}$$

- Speech Recognition

$$f(\text{Hello, MIRA}) = \text{"Hello, MIRA"}$$

In fact, the neural networks are universal function approximators!

53

Universal Function Approximator

$$y = f(x; \theta) = \sigma(W^L \dots \sigma(W^2 \sigma(W^1 x + b^1) + b^2) \dots + b^L)$$

Different model parameters W and b determine different mappings.

Standard multilayer feedforward networks with as few as one hidden layer using arbitrary squashing functions are capable of approximating any Borel measurable function from one finite dimensional space to another to any desired degree of accuracy.

----- "Multilayer feedforward networks are universal approximators"

Pick a function f = pick a set of model parameters θ

54

Universal Function Approximator

- A good function: The output of the function is close to the label.

$$f(x; \theta) \sim y$$

- An example loss function:

$$\text{Loss} = \sum_k \|y_k - f(x_k; \theta)\|^2$$

where k is the number of training examples

55

Commonly Used Loss Functions

- Square loss

$$\text{Loss} = (1 - f(x; \theta))^2$$

- Hinge loss

$$\text{Loss} = \max(0, 1 - yf(x; \theta))$$

- Logistic loss

$$\text{Loss} = -y \log(f(x; \theta))$$

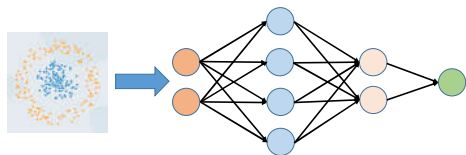
- Cross entropy loss

$$\text{Loss} = -\sum y \log(f(x; \theta))$$

56

Demonstration

Classification Problem

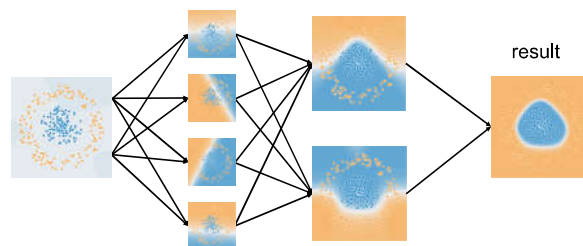


The input is the coordinates of the points.

57

Demonstration

Classification Problem: 500 Epoches



An epoch= one forward pass and one backward pass of **all** the training examples

58
<http://playground.tensorflow.org>

Tips

Deeper \neq Better performance



59

60

Deeper is Better?

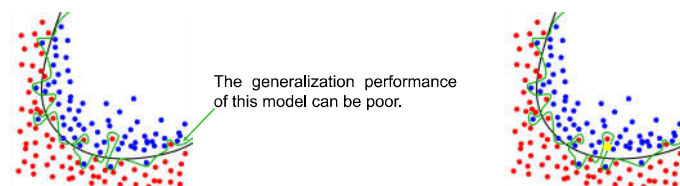
Model	Depth(layers)	Performance(error rate)
AlexNet[Hinton, et. al, 2012]	8	16,4%
GoLeNet[Simonyan, et. al, 2014]	22	6,7%
ResNet[Kaiming He, et. al, 2015]	152	3,57%

Dataset: ImageNet, which is a benchmark dataset for image classification.

Deep structure can capture complex patterns more efficiently than the shallow one.

61

Overfitting



The generalization performance of this model can be poor.

Which one is better ?

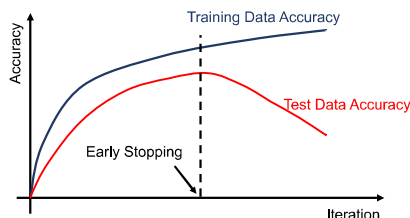
The predicted label is **bad!**

A good model is the one that generalizes well on the unseen data.

62

Preventing Overfitting in DNN

- Early Stopping
- Regularization
- Dropout
- ...



63

Preventing Overfitting in DNN

- Early Stopping
- Regularization
- Dropout
- ...

$$Loss'(\theta) = Loss(\theta) + \lambda ||\theta||_p$$

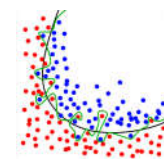
regularization term

➤ ℓ_2 norm

$$||\theta||_2^2 = (\theta_1)^2 + (\theta_2)^2 + \dots$$

➤ ℓ_1 norm

$$||\theta||_1 = |\theta_1| + |\theta_2| + \dots$$



Small weights usually imply smooth decision boundary.

64

L2 Regularization

$$Loss'(\theta) = Loss(\theta) + \lambda \frac{1}{2} \|\theta\|_2^2$$

$$\|\theta\|_2^2 = (\theta_1)^2 + (\theta_2)^2 + \dots$$

$$\frac{\partial Loss'}{\partial \theta} = \frac{\partial Loss}{\partial \theta} + \lambda \theta$$

$$\Rightarrow \theta^{t+1} = \theta^t - \eta \frac{\partial Loss'}{\partial \theta^t}$$

$$= \theta^t - \eta \left(\frac{\partial Loss}{\partial \theta^t} + \lambda \theta^t \right)$$

$$= (1 - \eta \lambda) \theta^t - \eta \frac{\partial Loss}{\partial \theta^t}$$

65

L1 Regularization

$$Loss'(\theta) = Loss(\theta) + \lambda \|\theta\|_1$$

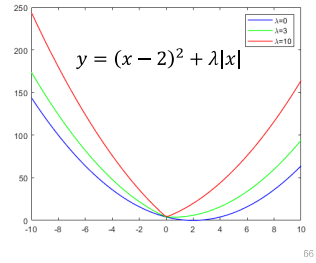
$$\|\theta\|_1 = |\theta_1| + |\theta_2| + \dots$$

$$\frac{\partial Loss'}{\partial \theta} = \frac{\partial Loss}{\partial \theta} + \lambda * sgn(\theta)$$

$$\theta^{t+1} = \theta^t - \eta \frac{\partial Loss'}{\partial \theta^t}$$

$$= \theta^t - \eta \left(\frac{\partial Loss}{\partial \theta^t} + \lambda sgn(\theta^t) \right)$$

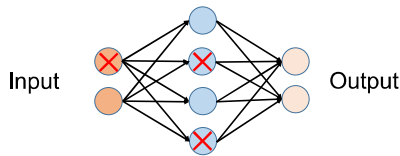
$$= \theta^t - \eta \lambda sgn(\theta^t) - \eta \frac{\partial Loss}{\partial \theta^t}$$



66

Preventing Overfitting in DNN

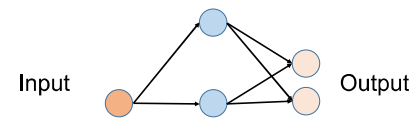
- Early Stopping
- Regularization
- **Dropout**
- ...



Training: We drop each neuron with probability p

67

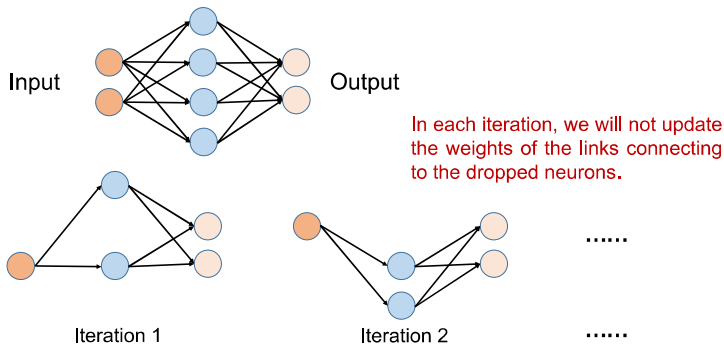
Dropout



Training: We dropout each neuron with probability p. Then, we train the resulting network for one iteration.

68

Dropout

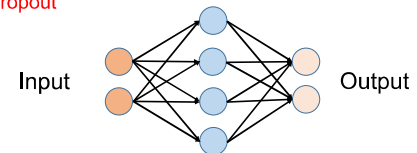


An iteration = a **batch** of training data passing through the network

69

Dropout

Testing: No dropout



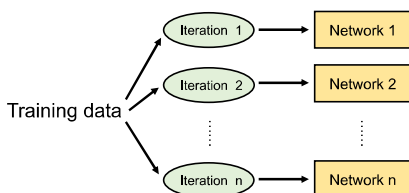
$$W_{test} = (1 - p) W_{train}$$

Why?

70

Why Dropout

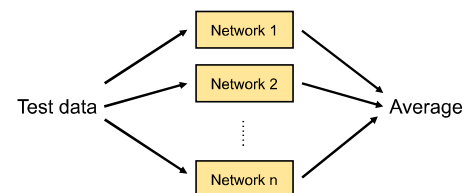
Dropout is a kind of ensemble



72

Why Dropout

Dropout is a kind of ensemble



With N neurons, there are 2^N possible sub-networks.

- The average can relieve overfitting
- Dropout can learn more robust patterns

73

Design Deep model



http://www.sohu.com/a/100823811_114877

Questions

