## Final Solutions

July 16, 2020

#### **Problem Definition**

Chest pain can be an early indicator of a fatal heart disease, which can be restricted from progression if diagnosed in early stages. Intuition-based analysis of a patients diagnostic reports and health records in order to decide of it is due to a heart desiese or due to some other minor circumstances, has been the traditional way of approaching such cases of chest pain. There is a significant room for enhancing the accuracy, efficiency and reliablity of this process using a data-driven approach, which goes in-hand with the domain experts (Cardiologists).

```
[1]: %reload_ext nb_black
```

<IPython.core.display.Javascript object>

```
[2]: import warnings
     import numpy as np
     import pandas as pd
     import scipy.stats as stats
     import statsmodels.api as sm
     from statsmodels.api import add_constant
     from statsmodels.stats.outliers influence import variance inflation factor
     from sklearn.model selection import train test split, GridSearchCV
     from sklearn.preprocessing import StandardScaler
     from sklearn.svm import SVC
     from sklearn.linear_model import LogisticRegression
     from sklearn.ensemble import RandomForestClassifier
     from sklearn.pipeline import Pipeline
     from sklearn.metrics import confusion matrix, classification report
     import matplotlib.pyplot as plt
     import seaborn as sns
     %matplotlib inline
```

```
[3]: def print_vif(x):
        \verb"""Utility for checking multicollinearity assumption
        :param x: input features to check using VIF. This is assumed to be a pandas.
     \hookrightarrow DataFrame
        :return: nothing is returned the VIFs are printed as a pandas series
        # Silence numpy FutureWarning about .ptp
        with warnings.catch_warnings():
            warnings.simplefilter("ignore")
            x = sm.add\_constant(x)
        vifs = []
        for i in range(x.shape[1]):
            vif = variance_inflation_factor(x.values, i)
            vifs.append(vif)
        print("VIF results\n----")
        print(pd.Series(vifs, index=x.columns))
        print("----\n")
```

```
[4]: def get_95_ci(x1, x2):
    # Calculate the difference of means in the observed data
    signal = x1.mean() - x2.mean()

# How much data is there? (sample size with len)
# How consistent is the data (standard deviation with std)
noise = np.sqrt(x1.std() ** 2 / len(x1) + x2.std() ** 2 / len(x2))

# Signal plus or minus noise (1.96 relates to 95% confidence level)
ci_lower_bound = signal - 1.96 * noise
ci_upper_bound = signal + 1.96 * noise
return (ci_lower_bound, ci_upper_bound)
```

```
[5]: path = "heart.csv"
    df_heart = pd.read_csv(path)

rename_map = {
        "cp": "pain_type",
        "trestbps": "rest_bp",
        "fbs": "fast_bp",
```

```
"restecg": "test_ecg",
    "thalach": "max_hr",
    "exang ": "ex_angina",
    "oldpeak": "st_depression",
    "ca": "number_vessels",
    "target": "heart_des",
}

df_heart = df_heart.rename(columns=rename_map)
```

Data Cleaning for any missing (NaN) values

```
[6]: df_heart.isnull().sum()
```

```
[6]: age
                        0
                        0
     sex
                        0
     pain_type
     rest_bp
                        0
                        0
     chol
                        0
     fast_bp
     test_ecg
                        0
                        0
     max_hr
                        0
     exang
     st_depression
                        0
     slope
                        0
     number_vessels
                        0
                        0
     thal
                        0
     heart_des
     dtype: int64
```

<IPython.core.display.Javascript object>

CHECK POINT 1 : Exploratory Data Analysis

Questions and Solutions

1. How many people are suffering from heart disease? Also plot the stats.

```
[7]: df_heart["heart_des"].value_counts()
```

```
[7]: 1    165
      0    138
      Name: heart_des, dtype: int64

<IPython.core.display.Javascript object>
```

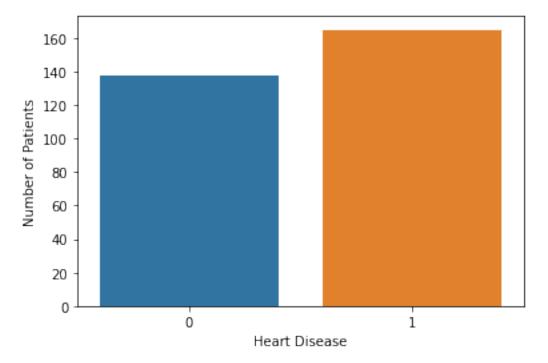
```
[8]: df_heart["heart_des"].value_counts(normalize=True)
```

[8]: 1 0.544554 0 0.455446

Name: heart\_des, dtype: float64

<IPython.core.display.Javascript object>

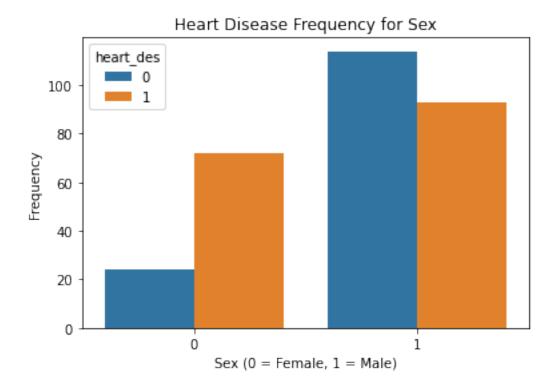
```
[9]: sns.countplot("heart_des", data=df_heart)
  plt.xlabel("Heart Disease")
  plt.ylabel("Number of Patients")
  plt.show()
```



<IPython.core.display.Javascript object>

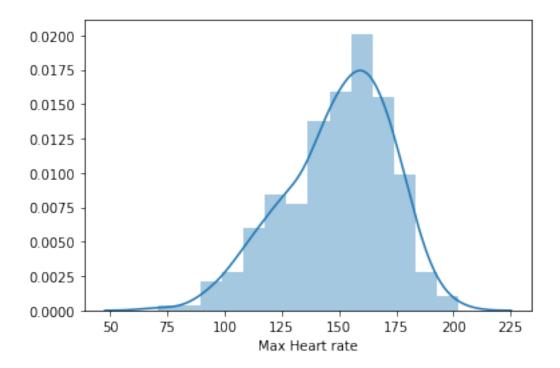
2. What is the split up by gender for the patients

```
[10]: sns.countplot("sex", hue="heart_des", data=df_heart)
   plt.title("Heart Disease Frequency for Sex")
   plt.xlabel("Sex (0 = Female, 1 = Male)")
   plt.ylabel("Frequency")
   plt.show()
```

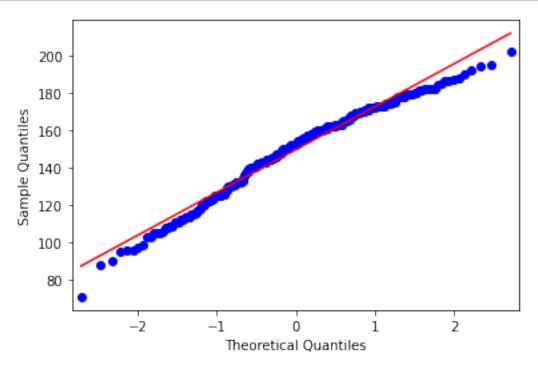


3. Visualize frequency distribution of the thalach (max heart rate) variable and find what's the heart rate and heart disease relation?

```
[11]: sns.distplot(df_heart["max_hr"])
   plt.xlabel("Max Heart rate")
   plt.show()
```







```
[13]: stats.describe(df_heart["max_hr"])
```

[13]: DescribeResult(nobs=303, minmax=(71, 202), mean=149.64686468646866, variance=524.6464057001726, skewness=-0.5347455419075503, kurtosis=-0.08068888039194055)

<IPython.core.display.Javascript object>

- $H_o$ : Data IS Normal
- $H_a$ : Data IS NOT Normal

Note: this test is very sensitive to deviations from normality. With the sample size, qqplot, and skewness/kurtosis metrics, I'd say we're normal enough for most tests.

```
[14]: t, p = stats.shapiro(df_heart["max_hr"])
p
```

[14]: 6.620309432037175e-05

<IPython.core.display.Javascript object>

```
[15]: stats.pearsonr(df_heart["heart_des"], df_heart["max_hr"])
```

[15]: (0.4217409338106744, 1.697337638656172e-14)

<IPython.core.display.Javascript object>

Since the heart desease and max heart rate are positively correlated, chances of Heart Disease increase with increase in heart rate.

Hypothesis test of mean heart rate of patients with and without heart Disease

 $H_0: \mu_{HeartRateOfHeartDisease} = \mu_{HeartRateOfNoHeartDisease}$ 

 $H_0: \mu_{HeartRateOfHeartDisease}! = \mu_{HeartRateOfNoHeartDisease}$ 

Forming two groups and testing for normality of both the groups.

```
[16]: no_heart_des = df_heart[df_heart["heart_des"] == 0]
yes_heart_des = df_heart[df_heart["heart_des"] == 1]

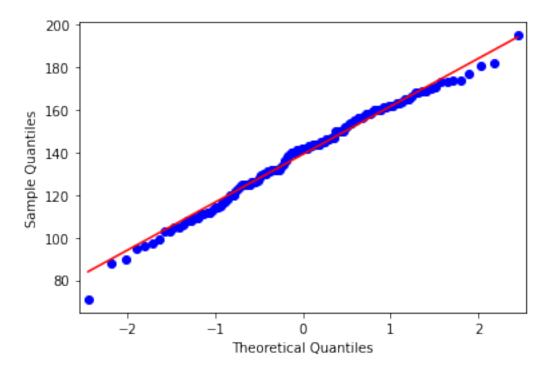
t1, p1 = stats.shapiro(no_heart_des["max_hr"])
t2, p2 = stats.shapiro(yes_heart_des["max_hr"])
```

```
print(f"The p-value for shapiro test of `no_heart_des`: {p1:.4f}")
print(f"The p-value for shapiro test of `yes_heart_des`: {p2:.4f}")
```

The p-value for shapiro test of `no\_heart\_des`: 0.4253
The p-value for shapiro test of `yes\_heart\_des`: 0.0004
<IPython.core.display.Javascript object>

```
[17]: print(stats.describe(no_heart_des["max_hr"]))
sm.qqplot(no_heart_des["max_hr"], line="s")
plt.show()
```

DescribeResult(nobs=138, minmax=(71, 195), mean=139.1014492753623, variance=510.7049613879192, skewness=-0.2935472748025849, kurtosis=-0.23176522769519403)

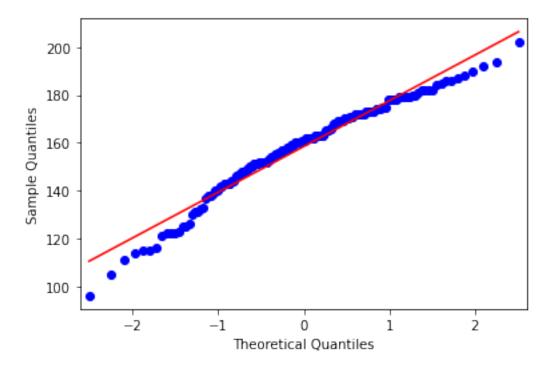


<IPython.core.display.Javascript object>

```
[18]: print(stats.describe(yes_heart_des["max_hr"]))
sm.qqplot(yes_heart_des["max_hr"], line="s")
plt.show()
```

DescribeResult(nobs=165, minmax=(96, 202), mean=158.46666666666667, variance=367.65284552845526, skewness=-0.7012606169032712,

#### kurtosis=0.41075760014691554)



<IPython.core.display.Javascript object>

Both seem normal enough despite shapiro test failing

```
[19]: t, p = stats.ttest_ind(no_heart_des["max_hr"], yes_heart_des["max_hr"])
    (t, p)
```

[19]: (-8.069702869452568, 1.697337638656049e-14)

<IPython.core.display.Javascript object>

Since the p-value is less than 0.05, we reject the null and state that The mean heart rates of both the groups is NOT the same.

Now we perform post-hoc analysis to analyse the mean heart rates of both the groups

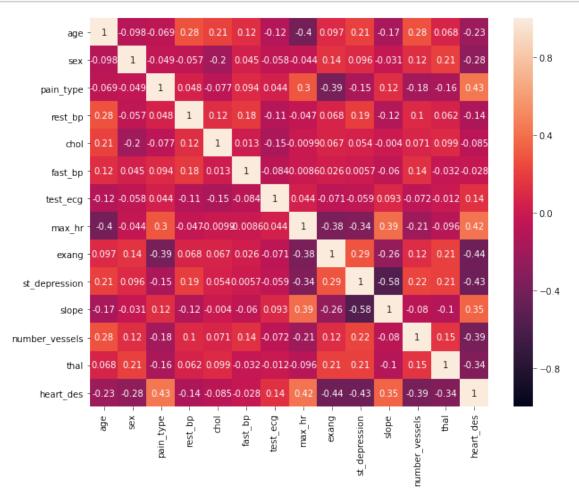
95% confidence interval of the difference of means is (-24, -15). This is indicating that the max heart rate for no\_heart\_disease is lower than yes\_heart\_des (by about 20 give or take).

```
[20]: get_95_ci(no_heart_des["max_hr"], yes_heart_des["max_hr"])
```

[20]: (-24.137710597709045, -14.592724184899668)

4. Find correlation matrix for all the variables with target.

```
[21]: plt.figure(figsize=(10, 8))
sns.heatmap(df_heart.corr(), annot=True, vmax=1.0, vmin=-1.0)
plt.show()
```



```
[22]: heart_des_corrs = df_heart.corr()[["heart_des"]]

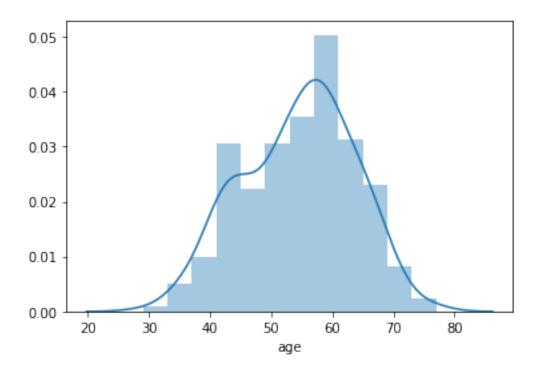
# Rename for clarity
heart_des_corrs.columns = ["heart_des_corr"]

# Sort by abs corr to find most powerful correlations + or -
heart_des_corrs["abs_heart_des_corr"] = heart_des_corrs["heart_des_corr"].abs()
```

```
heart_des_corrs = heart_des_corrs.sort_values("abs_heart_des_corr", _
       →ascending=False)
      # Show top
      heart_des_corrs.head(7)
[22]:
                      heart_des_corr abs_heart_des_corr
     heart_des
                            1.000000
                                                 1.000000
                                                 0.436757
                           -0.436757
      exang
     pain_type
                            0.433798
                                                 0.433798
      st_depression
                           -0.430696
                                                 0.430696
     max_hr
                                                 0.421741
                            0.421741
     number_vessels
                           -0.391724
                                                 0.391724
      slope
                            0.345877
                                                 0.345877
     <IPython.core.display.Javascript object>
     5. Find Mean, Min & Max of age and plot its distribution.
[23]: df_heart["age"].describe()
[23]: count
               303.000000
                54.366337
     mean
      std
                 9.082101
     min
                29.000000
      25%
                47.500000
      50%
                55.000000
      75%
                61.000000
                77.000000
     max
     Name: age, dtype: float64
     <IPython.core.display.Javascript object>
```

[24]: sns.distplot(df\_heart["age"])

plt.show()

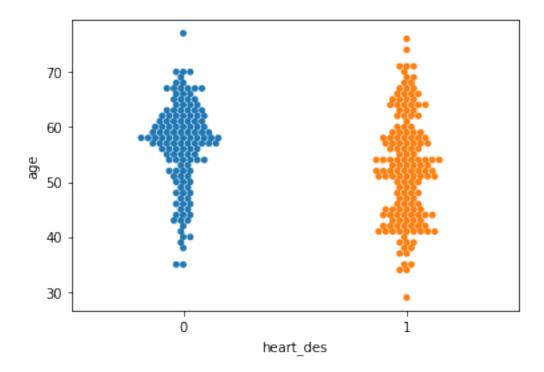


6. Age and its relation to heart disease. Is a particular set age of population (say age group 40-50) prone to heart disease than the rest of population age (50+)?

```
[25]: df_heart[["heart_des", "age"]].groupby("heart_des").mean()
```

[25]: age heart\_des 0 56.601449 1 52.496970

```
[26]: sns.swarmplot(x="heart_des", y="age", data=df_heart)
plt.show()
```



<IPython.core.display.Javascript object>

Mean and visual seem to show heart disease is less common in older group (sets off alarms for survivor bias in mind, but I have no medical background to back any of that skepticism.

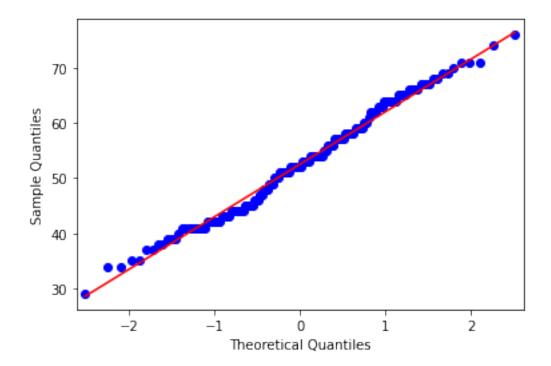
This is also about to be our second statistical test in a span of like 15 cells, we should be thinking about the increase in a chance of a type 1 error. Consider correcting your alpha level for multiple testing (google "statsmodels multiple tests")

Skipping shapiro, too senstive for my taste with these 'large' sample sizes from a traditional stats perspective.

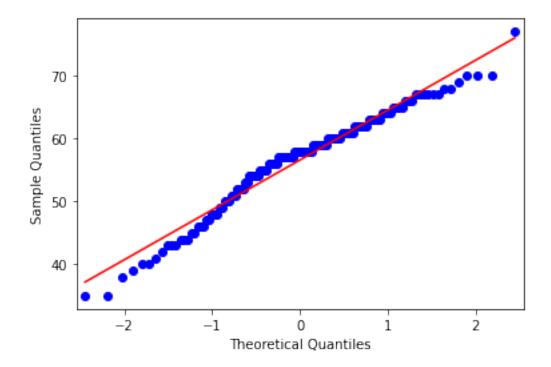
```
[27]: print(stats.describe(yes_heart_des["age"]))
    sm.qqplot(yes_heart_des["age"], line="s")
    plt.show()

    print(stats.describe(no_heart_des["age"]))
    sm.qqplot(no_heart_des["age"], line="s")
    plt.show()
```

DescribeResult(nobs=165, minmax=(29, 76), mean=52.4969696969697, variance=91.21492978566148, skewness=0.11984858651650541, kurtosis=-0.6334761098775341)



DescribeResult(nobs=138, minmax=(35, 77), mean=56.60144927536232, variance=63.39474240981699, skewness=-0.5425219384500629, kurtosis=0.08111820394037306)



```
[28]: t, p = stats.ttest_ind(yes_heart_des["age"], no_heart_des["age"])
(t, p)
```

[28]: (-4.014560975148874, 7.524801303442373e-05)

<IPython.core.display.Javascript object>

Since the p-value is less than 0.05, we reject the null and state that The mean age of both the groups is NOT the same.

Now we perform post-hoc analysis to analyse the mean age of both the groups

```
[29]: get_95_ci(yes_heart_des["age"], no_heart_des["age"])
```

[29]: (-6.076399282361516, -2.132559874423725)

<IPython.core.display.Javascript object>

To view the effects of both max\_hr and age on heart\_des at once, include in the same model. The age variable is not a significant predictor when included in the same model with max\_hr.

```
[30]: X = df_heart[["max_hr", "age"]]
y = df_heart["heart_des"]

X_const = sm.add_constant(X)
logit_results = sm.Logit(y, X_const).fit()

logit_results.summary()
```

Optimization terminated successfully.

Current function value: 0.590193

Iterations 5

/usr/local/lib/python3.7/site-packages/numpy/core/fromnumeric.py:2542: FutureWarning: Method .ptp is deprecated and will be removed in a future version. Use numpy.ptp instead.

return ptp(axis=axis, out=out, \*\*kwargs)

[30]: <class 'statsmodels.iolib.summary.Summary'>

#### Logit Regression Results

-----

Dep. Variable: heart\_des No. Observations: 303
Model: Logit Df Residuals: 300

Method:			MLE	Df Mo	odel:		2
Date:	•	Γhu, 16 Jul	2020	Pseud	do R-squ.:		0.1436
Time:		21:	02:16	Log-I	Likelihood:		-178.83
converged:			True	LL-Nı	ıll:		-208.82
Covariance	Type:	nonr	obust	LLR 1	p-value:		9.448e-14
	coef	std err		z	P> z	[0.025	0.975]
const	-4.9264	1.504	-3	.276	0.001	-7.874	-1.979
${\tt max\_hr}$	0.0413	0.007	6	.032	0.000	0.028	0.055
age	-0.0194	0.015	-1	.262	0.207	-0.049	0.011
	=======		======	=====		:======	=======
11 11 11							

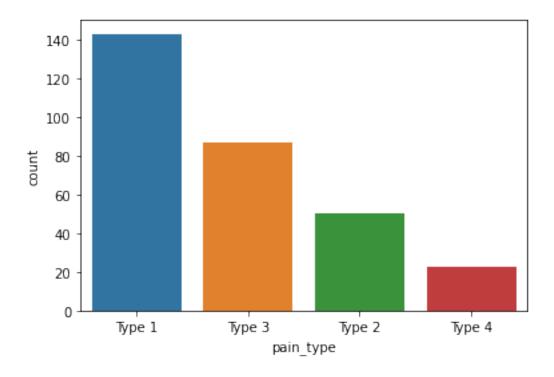
Good quick example of interpreting logistic regression coefficients.

7. Plot chest pain type pie chart. ...No

```
[31]: plot_df = df_heart["pain_type"].value_counts()
    plot_df = plot_df.sort_values(ascending=False)
    plot_df = plot_df.reset_index()
    plot_df.columns = ["pain_type", "count"]

    pain_type_map = {0: "Type 1", 1: "Type 2", 2: "Type 3", 3: "Type 4"}
    plot_df["pain_type"] = plot_df["pain_type"].replace(pain_type_map)

# set order to be ordered by count (we sorted by count above)
    sns.barplot(x="pain_type", y="count", order=plot_df["pain_type"], data=plot_df)
    plt.show()
```



People suffer Type-1 Chest pain more than other types

8. What is the max heart rate achieved in non heart disease patients?

```
[32]: no_heart_des["max_hr"].max()
```

[32]: 195

<IPython.core.display.Javascript object>

CHECK POINT 2 : Testing various ML Models

Implement different MLs and decide which model fits best

```
[33]: X = df_heart.drop(columns="heart_des")
y = df_heart["heart_des"]

X_train, X_test, y_train, y_test = train_test_split(
          X, y, test_size=0.25, random_state=42
)
```

# [34]: print\_vif(X\_train)

```
const
                 201.286970
                   1.475669
age
                   1.246904
sex
                   1.287448
pain_type
rest_bp
                   1.170844
chol
                   1.202035
fast_bp
                   1.127679
test_ecg
                   1.056053
max_hr
                   1.588077
exang
                   1.427913
st_depression
                 1.724941
slope
                   1.547418
number_vessels
                  1.222578
thal
                   1.158137
dtype: float64
```

VIF results

<IPython.core.display.Javascript object>

```
[35]: param_grid = [
          {
              # Compare if scaling is better than doing nothing
              "preprocessing": [StandardScaler(), "passthrough"],
              # Compare Logistic Regression vs SVM (both use C param)
              "clf": [LogisticRegression(), SVC()],
              "clf__C": [1, 10, 100, 1000],
          },
          {
              "preprocessing": [StandardScaler(), "passthrough"],
              "clf": [RandomForestClassifier()],
              "clf__n_estimators": [20, 50, 100],
              "clf__max_depth": [3, 6, 9],
              "clf__n_estimators": [20, 50, 100],
              "clf_max_features": [0.5, 0.75, 1.0],
          },
      ]
```

```
[36]: # Gonna have the param grid select stuff for us
```

```
# LogisticRegression is pretty much a placeholder here, the param grid is qonna_{\sqcup}
       ⇒swap it out in grid search
      pipeline = Pipeline([("preprocessing", "passthrough"), ("clf", __
       →LogisticRegression())])
     <IPython.core.display.Javascript object>
[37]: pipeline_cv = GridSearchCV(pipeline, param_grid, verbose=1)
      \# Silencing Convergence Warnings.. dangerous in case a different important \sqcup
      →warning comes up
      with warnings.catch warnings():
          warnings.simplefilter("ignore")
          pipeline_cv.fit(X_train, y_train)
      model = pipeline_cv.best_estimator_
      pipeline_cv.best_params_
     Fitting 5 folds for each of 70 candidates, totalling 350 fits
     [Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent workers.
     [Parallel(n_jobs=1)]: Done 350 out of 350 | elapsed: 19.2s finished
[37]: {'clf': RandomForestClassifier(bootstrap=True, ccp_alpha=0.0, class_weight=None,
                              criterion='gini', max depth=3, max features=0.5,
                              max_leaf_nodes=None, max_samples=None,
                              min_impurity_decrease=0.0, min_impurity_split=None,
                              min_samples_leaf=1, min_samples_split=2,
                              min_weight_fraction_leaf=0.0, n_estimators=50,
                              n_jobs=None, oob_score=False, random_state=None,
                              verbose=0, warm_start=False),
       'clf__max_depth': 3,
       'clf__max_features': 0.5,
       'clf n estimators': 50,
       'preprocessing': 'passthrough'}
     <IPython.core.display.Javascript object>
[38]: y_pred = model.predict(X_test)
      confusion_mat = confusion_matrix(y_test, y_pred)
      confusion df = pd.DataFrame(
          confusion mat,
          columns=["Predicted 0", "Predicted 1"],
          index=["Actual 0", "Actual 1"],
```

```
display(confusion_df)
print(classification_report(y_test, y_pred))
```

		Predicted 0	Predicted 1
Actual	0	27	8
Actual	1	5	36

	precision	recall	f1-score	support
0	0.84	0.77	0.81	35
1	0.82	0.88	0.85	41
accuracy			0.83	76
macro avg	0.83	0.82	0.83	76
weighted avg	0.83	0.83	0.83	76

<sup>&</sup>lt;IPython.core.display.Javascript object>