Worksheet 3 Review

March 20, 2020

Question 1

- a. $Correct(my_prog) \land Python(my_prog)$
- b. $\exists x \in P, \neg Correct(x) \Rightarrow Python(x)$
- c. $\forall x \in P, Python(x) \Rightarrow \neg Correct(x)$
- d. $\forall x \in P, \neg Correct(x) \Rightarrow Python(x)$
- e. There is a program that is written in Python and is correct.
- f. Every program is not written in Python and is correct.
- g. There is a program that is correct but is not written in Python.
- h. All running programs not written in Python are correct, and all correctly running programs are not written in Python.

Question 2

- a. All programs written in Python is correct, or all program written in python is not correct.
- b. $(\exists x \in P, Python(x) \Rightarrow Correct(x)) \Rightarrow (\forall y \in P, Python(y) \Rightarrow Correct(y))$

Correct Solution:

$$(\exists x \in P, \, Python(x) \land Correct(x)) \Rightarrow (\forall y \in P, \, Python(y) \Rightarrow Correct(y))$$

c. x_1 and x_2 in first statement could have different values. Where as the x in second statement has the same value.

The first statement is true, but the second is false. Assume x is divisible by 7. Then, 165 must be divisible by 7, but this is false.

Question 3

a. $\forall n \in \mathbb{N}, \ Odd(n) \Rightarrow \exists k \in \mathbb{Z}, n = 2k + 1$

Correct Solution:

$$Odd(n): \exists k \in \mathbb{Z}, n = 2k + 1, \text{ where } n \in \mathbb{Z}$$

- b. $\forall n, m \in \mathbb{N}, Odd(n) \wedge Odd(m) \Rightarrow Odd(nm)$
- c. $\forall n, m \in \mathbb{N}, \ \exists k, l \in \mathbb{Z}, \ n = 2k 1 \land m = 2l 1 \Rightarrow \exists o \in \mathbb{Z}, \ nm = 2o 1$
- d. $\forall n, m \in \mathbb{N}, \exists o \in \mathbb{Z}, nm = 2o 1 \Rightarrow \exists k, l \in \mathbb{Z}, n = 2k 1 \land m = 2k 1$

Question 4

- a. $((\neg a \lor \neg b) \land c) \lor ((a \land b) \land \neg c)$
- b. $\exists x, y \in S, \forall z \in S, \neg P(x, y) \lor \neg Q(x, z)$
- c. $(\exists x \in S, P(x)) \land (\forall y \in S, \neg Q(y))$

Question 5