CSC236 Worksheet 8 Solution

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Question 1

Rough Works:

1. Build L_1

$$Q = \{E, O\}$$

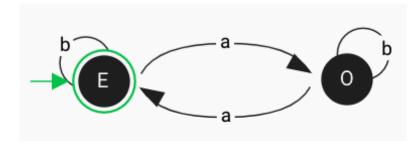
$$\Sigma = \{a, b\}$$

$$\delta = \begin{bmatrix} a & b \\ *E & O & E \\ O & E & O \end{bmatrix}$$

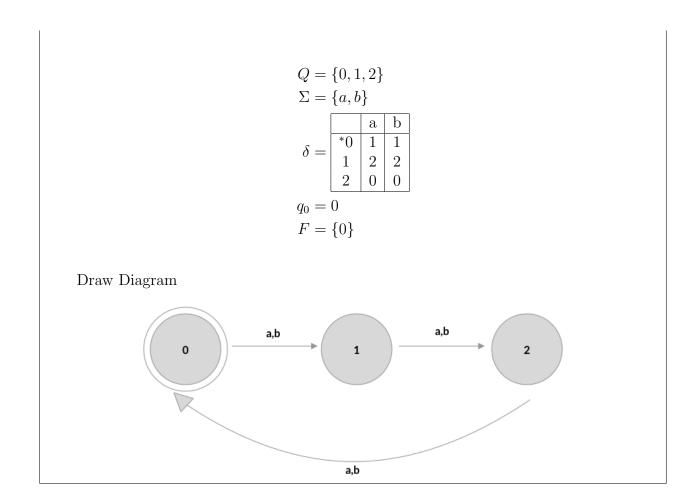
$$q_0 = E$$

$$F = \{E\}$$

Draw Diagram

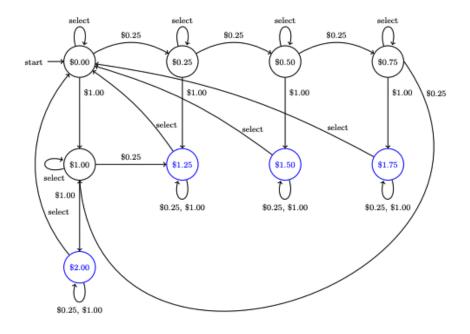


2. Build L_2



Notes:

- Deterministic Finite State Automaton (DFSA): is a mathematical method of machine which, given any input string x, accepts or rejects x.
- Applications of DFSA
 - 1. Vending Machine



- 2. Protocol analysis
- 3. Text parsing
- 4. Video game character behavior

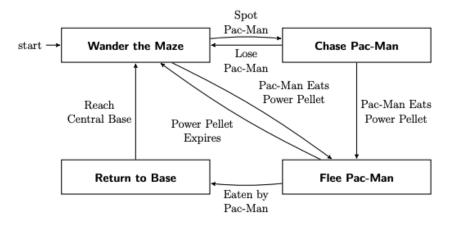
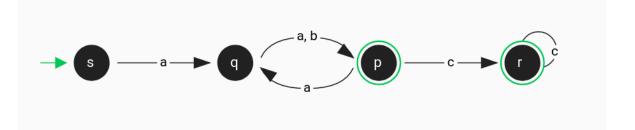


Figure 3: Behavior of a Pac-Man Ghost

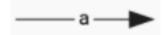
- 5. Security Analysis
- 6. <u>CPU control units</u> (**)
- 7. Natural Language Processing (**)
- 8. Speech Recognition (**)
- Definitions and Syntax



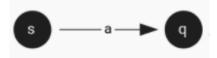
- DFSA M is a quintuple $M = (Q, \Sigma, q_0, F, \delta)$, where
 - * Q: a finite set of **states**.
 - · Represents status of system
 - · Is represented by a black circle, i.e. s,q



- · i.e. automatic sliding door at walmart has two states: either close or open
- · i.e. traffic light has three states: red, yellow, green
- * Σ : a finite non-empty alphabet
 - · is set of symbols in each transition, i.e. a, b, c



- * $q_0 \in Q$: the start or initial state
- * $\delta: Q \times \sigma \to Q$: a transition function
 - · is a connection between two states.
 - · is represented by an arrow

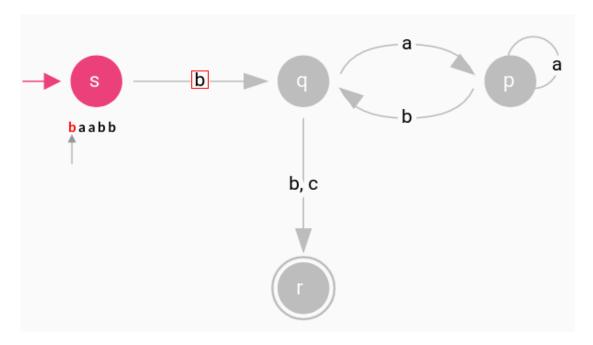


- * $F \subseteq Q$: the set of accepting or final states
 - · Is represented by a double circle



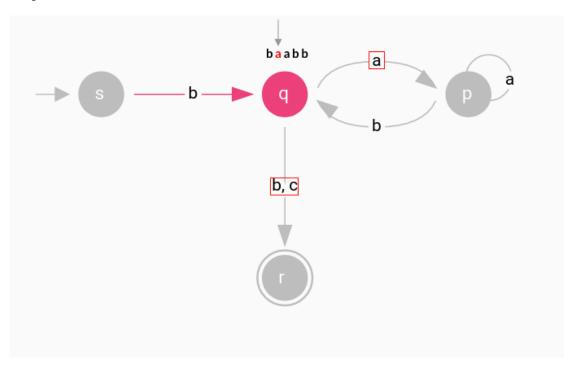
- · Multiple accepting states may exists
- · Purpose: When processing ends, the output is either accept or reject
- Simple Example

- Step 1



- 1. First symbol of the input **baabb** is \mathbf{b} and the current state is s.
- 2. Ask, is there any exiting transition from s that contains the symbol **b**?
- 3. The answer is yes, so move to q

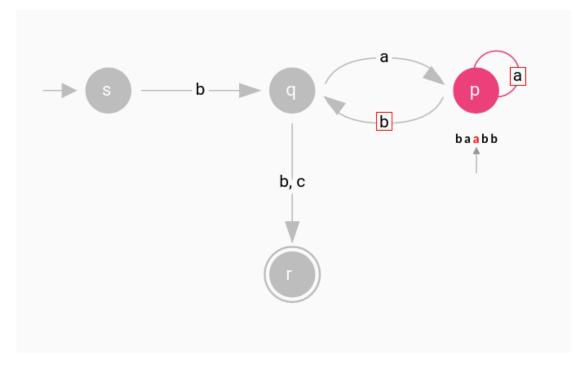
- Step 2



- 1. Next symbol of the input **baabb** is \mathbf{a} and the current state is q.
- 2. Ask, is there any exiting transition from q that contains the symbol \mathbf{a} or \mathbf{b}, \mathbf{c} ?

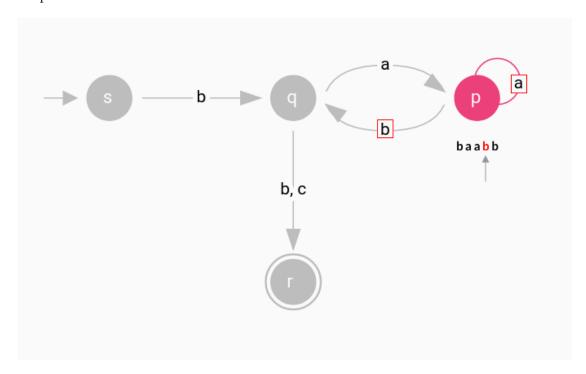
3. The answer is yes, and it's \mathbf{a} . So move to p

- Step 3



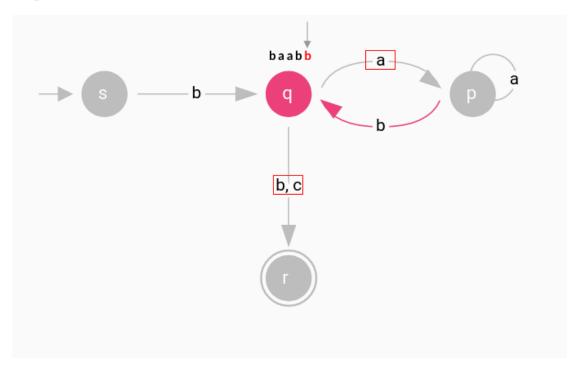
- 1. Next symbol of the input **baabb** is \mathbf{a} and the current state is p.
- 2. Ask, is there any exiting transition from p that contains the symbol \mathbf{a} or \mathbf{b} ?
- 3. The answer is yes, and it's ${\bf a}$. So move to p

- Step 4



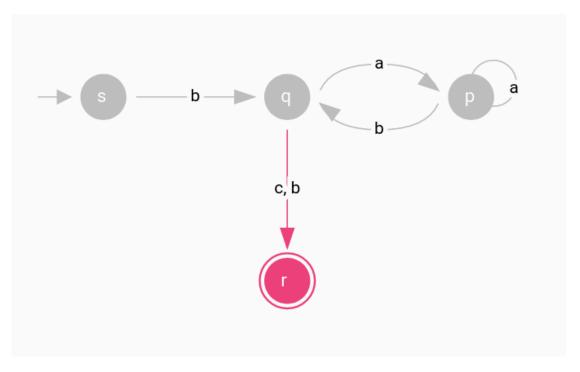
- 1. Next symbol of the input **baabb** is **b** and the current state is p.
- 2. Ask, is there any exiting transition from p that contains the symbol \mathbf{a} or \mathbf{b} ?
- 3. The answer is yes, and it's **b**. So move to q

- Step 5



- 1. Next symbol of the input **baabb** is \mathbf{b} and the current state is q.
- 2. Ask, is there any exiting transition from q that contains the symbol \mathbf{a} or \mathbf{b} , \mathbf{c} ?
- 3. The answer is yes, and it's **b**. So move to r

- Step 6



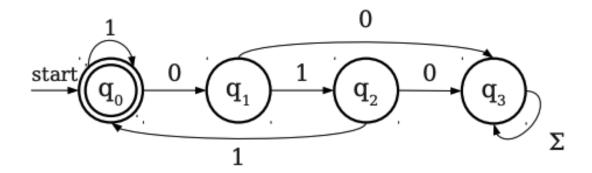
- 1. Next symbol of the input **baabb** is **b** and the current state is r.
- 2. Ask, if it satisfies the accepting or final state (i.e, has the end of string been reached?). If so, the output is accept. Otherwise, it's reject.

• Formal Languages

- is a <u>subset</u> of all possible words Σ * formed by symbols of alphabet Σ .
 - * Σ * is set of all possible strings over the alphabet Σ .
 - * i.e. $\Sigma = \{a, b\}, \ \Sigma * = \{a, b, aa, ab, ba, bb, aaa, aab, \cdots \}$
- Example
 - 1. $L = \{w \mid w \text{ has at most seventeen 0's}\}$
 - 2. $L = \{w \mid w \text{ has equal number of 0's and 1's} \}$
 - 3. $L = \{x \in \{a, b\}^* \mid \text{the number of as in } x \text{ is even}\}$
 - * * in $\{a, b\}$ * means all possible combinations
 - * i.e. $\{a, b, aa, ab, ba, bb, aaa, baa, aba, \cdots\}$

• Tabular DFAs

- Example



$$\delta = \begin{bmatrix} & 0 & 1 \\ *q_0 & q_1 & q_0 \\ q_1 & q_3 & q_2 \\ q_2 & q_3 & q_0 \\ q_3 & q_3 & q_3 \end{bmatrix}$$

Note: * means it's an accepting state