## Worksheet 4 Solution

## March 13, 2020

## Question 1

- a.  $\exists n \in \mathbb{N}, (n > 3) \land (n^2 1.5n \ge 5)$
- b. The variable is existentially quantified
- c. Concrete natural number
- d. Let n = 5.

Then,

$$(5)^2 - 1.5(5) \tag{1}$$

Then,

$$25 - 7.5$$
 (2)

Then,

$$17.5 \tag{3}$$

which is greater than 5. So, the statement is True

e.  $\forall n \in \mathbb{N}, n > 3 \Rightarrow n^2 - 1.5n > 4$ 

Here  $\Rightarrow$  should be used because n>3 is a given, and we are using it to show that the statement  $n^2-1.5n>4$  is True

- f. The variable is universally quantified
- g. In this proof the variable must be arbitrary natural number
- h. The assumption made is that the any natural number greater than 3 satisfies the statement  $n^2 1.5n > 4$ .

This assumption is made since the predicate logic is the proof of an implication

i. Let  $n \in \mathbb{N}$  be an arbitruary number of  $\mathbb{N}$ , and assume n > 3. Then,

$$n^2 > 3n \tag{1}$$

$$n^2 - 1.5n > 3n - 1.5n \tag{2}$$

$$n^2 - 1.5n > 1.5n \tag{3}$$

Because we know that n > 3, we can conclude

$$n^2 - 1.5n > 1.5(3) \tag{4}$$

$$n^2 - 1.5n > 4.5 \tag{5}$$

It follows that the statement  $\forall n \in \mathbb{N}, n > 3 \Rightarrow n^2 - 1.5n > 4$  is true.

## Question 2

a.  $\forall n \in \mathbb{N}, n > 5 \Rightarrow n \mid 2 \vee n \mid 3$