

# Worksheet 5 Review

March 22, 2020

## Question 1

- **Predicate Logic:**  $\forall x, y \in \mathbb{Z}, \text{Odd}(x) \wedge \text{Odd}(y) \Rightarrow \text{Odd}(xy)$

Let  $x, y \in \mathbb{Z}$ . Assume  $\text{Odd}(x)$  and  $\text{Odd}(y)$ .

Then,  $\exists k, m \in \mathbb{Z}$ ,

$$x = 2k - 1 \tag{1}$$

$$y = 2m - 1 \tag{2}$$

Then,

$$xy = (2k - 1)(2m - 1) \tag{3}$$

$$xy = (4km - 2k - 2m + 2) - 1 \tag{4}$$

$$xy = 2(2km - k - m + 1) - 1 \tag{5}$$

$$xy = 2o - 1 \tag{6}$$

by setting  $o = 2km - k - m + 1$ .

Since,  $o \in \mathbb{Z}$ , it follows from the definition of odd that the statement  $\forall x, y \in \mathbb{Z}, \text{Odd}(x) \wedge \text{Odd}(y) \Rightarrow \text{Odd}(xy)$  is true.

Question 2

Question 3

Question 4