CSC148 Worksheet 7 Solution

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Question 1

- Noticed that there are 11 students in total.
- Students should be grouped by year as closest as possible.

Notes:

- 형모 해낼 뚜 있쬬!
- 형모 화이팅!

Question 2

Name	Year	College		
Priya	3	Victoria		
Alain	2	New	Group 1	
Zoe	3	Woodsworth		
 Francesco	3	Victoria		
Mohammed	4	Woodsworth		
Xiaoyuan	5	New	Group 2	
Rohit	2	New		
 Yimin	3	Trinity		
Grace	5	Woodsworth		
Claire	1	Woodsworth	Group 3	
Kai	1	Woodsworth		

Question 3

• First, we need to find the group as homogenous as possible in terms of year students are in.

The definition tells us group needs to be in 4, and the following table tell us there are $4 \ 3^{rd}$ year students.

Student Year	Number of Students		
1	2		
2	2		
3	4		
4	1		
5	2		

It follows from these facts that the group of 3^{rd} year students best satisfy this criterion.

Next, we need to find the group as not homogenous as possible in terms of year students are in.

The same table tells us with 2 5^{th} year students, 1 4^{th} year students and 1 3^{rd} year student, a group spanning 3 years can be created.

Since we know there can't be a group spanning 4 years, we can conclude the group of 3 years (2 5^{th} year students, 1 4^{th} year students and 1 3^{rd} year student) best satisfy this criterion.

Correct Solution:

Group 1 is the most homogeneous.

Group 3 is the least homogeneous.

Question 4

• We will calculate the group score based on the code below. The code is also included in worksheet_7_q4_solution.py

```
def get_group_score(group):
    """Evaluates the group score

Precondition: len(group) == 4

"""

n = 4
```

```
max_year = get_max_year(group)
8
           min_year = get_min_year(group)
           similarity_list = []
10
11
          i = 0
12
13
           while i < 4:
14
               j = 0
15
               while j < 4:
16
                   # find the scaled distance
17
                   scaled_distance = 0
                   if max_year != min_year:
19
                        scaled_distance = abs(group[i]['year'] - group[j][
20
      'year']) / float(max_year - min_year)
                   # find the similarity
                   similarity = 1 - scaled_distance
23
24
25
                   # add to list
                   similarity_list.append(similarity)
26
27
                   j += 1
28
               i += 1
29
30
          # find the average
31
           average = float(sum(similarity_list))/len(similarity_list)
32
           return average.as_integer_ratio()
33
34
      def get_max_year(group):
35
           """returns max value of year in group"""
36
37
           max_value = -1
38
39
40
           for student in group:
               max_value = max(student['year'], max_value)
41
42
           return max_value
43
      def get_min_year(group):
45
           """returns min value of year in group"""
46
47
           min_value = 100 # this is impossible value
48
49
           for student in group:
50
               min_value = min(student['year'], min_value)
           return min_value
53
54
      if __name__ == '__main__':
56
           group_1 = [{'name': 'Primya', 'year': 3},
57
           {'name': 'Zoe', 'year': 3},
58
           {'name': 'Francesco', 'year': 3},
59
           {'name': 'Yimin', 'year': 3}]
```

```
61
            group_2 = [{'name': 'Primya', 'year': 5},
62
            {'name': 'Zoe', 'year': 5},
{'name': 'Francesco', 'year': 4},
63
64
            {'name': 'Yimin', 'year': 3}]
65
66
            score_1 = get_group_score(group_1)
68
            print(score_1)
69
            score_2 = get_group_score(group_2)
            print(score_2)
72
73
74
```

For the most homogeneous group, the group score is 1.

For the least homogeneous group, the group score is $\frac{9}{16}$.

Correct Solution:

We will calculate the group score using the code below. The code is also included in worksheet_7_q4_solution.py

```
def get_similarity_list(group):
     """Evaluates the list of similarities""" # <- Correct solution
     similarity_list = []
    i = 0
    while i < len(group): # <- correct solution</pre>
         j = i + 1 # <- correct solution
         while j < len(group): # <- correct solution</pre>
             # find the scaled distance
             scaled_distance = abs(group[i]['year'] - group[j]['year
']) / 5.0 \# <- correct solution
             # find the similarity
             similarity = 1 - scaled_distance
             # add to list
             similarity_list.append(similarity)
             j += 1
         i += 1
    return similarity_list
```

```
if __name__ == '__main__':
    # Correct Solution
    group_1 = [{'name': 'Primya', 'year': 3},
    {'name': 'Alain', 'year': 2},
    {'name': 'Zoe', 'year': 3},
    {'name': 'Francesco', 'year': 3}]
    # Correct Solution
    group_2 = [{'name': 'Mohammed', 'year': 4},
{'name': 'Xiaoyuan', 'year': 5},
    {'name': 'Rohit', 'year': 2},
    {'name': 'Yimin', 'year': 3}]
    # Correct Solution
    group_3 = [{'name': 'Grace', 'year': 5},
    {'name': 'Claire', 'year': 1},
    {'name': 'Kai', 'year': 1}]
    # Correct Solution
    list_1 = get_similarity_list(group_1)
    print(list_1)
    # Correct Solution
    list_2 = get_similarity_list(group_2)
    print(list_2)
    # Correct Solution
    list_3 = get_similarity_list(group_3)
    print(list_3)
```

We will calculate the score of each group in parts.

Part 1 (Score of Group 1):

We need to calculate the score of group 1.

The problem tells us the group score is

Group Score =
$$\frac{\sum \text{similarities}}{\text{# of elements in list of similarities}}$$
 (1)

and the above program tells us that the list of similarities are

$$[0.8, 1.0, 1.0, 0.8, 0.8, 1.0] (2)$$

Then, using these facts, we can conclude that

Group Score =
$$\frac{0.8 + 1.0 + 1.0 + 0.8 + 0.8 + 1.0}{6}$$

$$= \frac{\frac{4}{5} + 1 + 1 + \frac{4}{5} + \frac{4}{5} + 1}{6}$$

$$= \frac{\frac{4}{5} + \frac{5}{5} + \frac{5}{5} + \frac{4}{5} + \frac{4}{5} + \frac{5}{5}}{6}$$

$$= \frac{\frac{27}{4}}{6}$$

$$= \frac{27}{30}$$

$$= \frac{9}{10}$$
(8)

Part 2 (Score of Group 2):

We need to calculate the score of group 2.

The problem tells us the group score is

Group Score =
$$\frac{\sum \text{similarities}}{\text{# of elements in list of similarities}}$$
(9)

and the above program tells us that the list of similarities are

$$[0.8, 0.6, 0.8, 0.4, 0.6, 0.8] (10)$$

Then, we can conclude that the value of group score is

$$\frac{0.8 + 0.6 + 0.8 + 0.4 + 0.6 + 0.8}{6} = \frac{\frac{4}{5} + \frac{3}{5} + \frac{4}{5} + \frac{2}{5} + \frac{3}{5} + \frac{4}{5}}{6}$$

$$= \frac{\frac{20}{5}}{6}$$

$$= \frac{20}{30}$$

$$= \frac{2}{30}$$

$$= \frac{2}{3}$$

$$(11)$$

Part 3 (Score of Group 3):

We need to calculate the score of group 3.

The problem tells us the group score is

Group Score =
$$\frac{\sum \text{similarities}}{\text{# of elements in list of similarities}}$$
 (15)

and the above program tells us that the list of similarities are

$$[0.2, 0.2, 1.0] \tag{16}$$

Then, we can conclude that the value of group score is

$$\frac{0.2 + 0.2 + 1.0}{3} = \frac{\frac{1}{5} + \frac{1}{5} + \frac{5}{5}}{3}$$

$$= \frac{\frac{7}{5}}{3}$$

$$= \frac{7}{15}$$
(17)
(18)

$$=\frac{\frac{7}{5}}{3}\tag{18}$$

$$=\frac{7}{15}\tag{19}$$

Notes:

• Realized that 'group' in question means 'group 1', 'group 2' and 'group 3' in question 2:(.

Question 5

• We need to find the highest and the lowest possible score on this criterion.

We will do so in parts.

Part 1 (Calculating highest possible group score):

We need to find the highest possible group score on this criterion.

The definition of group score tells us that

Group Score =
$$\frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} \left(1 - \frac{|student_year_i - student_year_j|}{5}\right)}{\# \text{ of elements in list of similarities}}$$
(1)

By observation, we can conclude that the highest possible group score happens when $|student_year_i - student_year_i| = 0$.

Then, using this fact, we can calculate that

Group Score =
$$\frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} \left(1 - \frac{|student_year_i - student_year_j|}{5}\right)}{\# \text{ of elements in list of similarities}}$$
(2)

$$= \frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} 1}{\text{# of elements in list of similarities}}$$
 (3)

Then, because we know $\sum_{i=0}^{n-1}\sum_{j=i+1}^{n-1}1=\#$ of elements in list of similarities, we can conclude

$$= \frac{\text{# of elements in list of similarities}}{\text{# of elements in list of similarities}}$$
 (4)

$$=1 (5)$$

Part 2 (Calculating lowest possible group score):

We need to find the lowest possible group score achievable on this criterion.

The definition of group score tells us that

Group Score =
$$\frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} \left(1 - \frac{|student_year_i - student_year_j|}{5}\right)}{\# \text{ of elements in list of similarities}}$$
(6)

By observation, we can conclude that the lowest possible group score happens when $|student_year_i - student_year_j| = 5$.

Then, using this fact, we can calculate that

Group Score =
$$\frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} \left(1 - \frac{|student_year_i - student_year_j|}{5}\right)}{\# \text{ of elements in list of similarities}}$$
(7)

$$= \frac{\sum_{i=0}^{n-1} \sum_{j=i+1}^{n-1} 0}{\text{# of elements in list of similarities}}$$

$$= \frac{0}{\text{# of elements in list of similarities}}$$
(8)

$$= \frac{0}{\text{# of elements in list of similarities}} \tag{9}$$

$$=0 (10)$$

Notes:

- 형모야. 차분히. 한걸음 더.
- 문제 안풀린다고 주저 앉지마.
- 사랑하는 내 여보 향해 가는거야.
- 보고싶은 내 여보 향해.
- 형모야 화이팅 :)

Question 6

	Name	Year	College		l I
	Priya	3	Victoria	Group 1	0
	Alain	2	New		
	Zoe	3	Woodsworth		
[Francesco	3	Victoria		
	Mohammed	4	Woodsworth	Group 2	0
	Xiaoyuan	5	New		
	Rohit	2	New		
	Yimin	3	Trinity		
	Grace	5	Woodsworth	Group 3	1
	Claire	1	Woodsworth		
	Kai	1	Woodsworth		
_					

Question 7

• We need to evaluate the total score for each group.

We will do so in parts.

Part 1 (Calculating the total score of Group 1):

We need to calculate the total score of group 1.

The answer from question 4 tells us group 1 has value of $\frac{9}{10}$, and for criterion a) and has 0 for criterion b).

Since we know criterion a) has weight of 0.8 and criterion has weight of 0.2, we can conclude the total score is

$$(0.8 \times \frac{9}{10}) + (0.2 \times 0) = 0.72 \tag{1}$$

$$\approx 1$$
 (2)

Part 2 (Calculating the total score of Group 2):

We need to calculate the total score of group 2.

The answer from question 4 tells us group 2 has value of $\frac{2}{3}$, and for criterion a) and has 0 for criterion b).

Since we know criterion a) has weight of 0.8 and criterion has weight of 0.2, we can conclude the total score is

$$(0.8 \times \frac{2}{3}) + (0.2 \times 0) = 0.53333333 \tag{3}$$

$$\approx 1$$
 (4)

Part 3 (Calculating the total score of Group 3):

We need to calculate the total score of group 3.

The answer from question 4 tells us group 3 has value of $\frac{7}{15}$, and for criterion a) and has 1 for criterion b).

Since we know criterion a) has weight of 0.8 and criterion has weight of 0.2, we can conclude the total score is

$$(0.8 \times \frac{7}{15}) + (0.2 \times 1) = 0.573333 \tag{5}$$

$$\approx 1$$
 (6)

Correct Solution:

We need to evaluate the total score for each group.

We will do so in parts.

Part 1 (Calculating the total score of Group 1):

We need to calculate the total score of group 1.

The formula for total score tells us

Total Score = (Score of Criterion
$$a \times 80$$
) + (Score of Criterion $b \times 20$) (1)

Since we know group 1 has score of $\frac{9}{10}$ for criteron a) and score of 0 for criterion b), we can conclude the total score is

$$\left(\frac{9}{10} \times 80\right) + \left(0 \times 20\right) = 72\tag{2}$$

Part 2 (Calculating the total score of Group 2):

We need to calculate the total score of group 2.

The formula for total score tells us

Total Score = (Score of Criterion
$$a \times 80$$
) + (Score of Criterion $b \times 20$) (3)

Since we know group 2 has score of $\frac{2}{3}$ for criteron a) and score of 0 for criterion b), we can conclude the total score is

$$\left(\frac{2}{3} \times 80\right) + \left(0 \times 20\right) = 53.33333\tag{1}$$

$$\approx 53$$
 (2)

Part 3 (Calculating the total score of Group 3):

We need to calculate the total score of group 3.

The formula for total score tells us

Total Score = (Score of Criterion
$$a \times 80$$
) + (Score of Criterion $b \times 20$) (3)

Since we know group 3 has score of $\frac{7}{15}$ for criteron a) and score of 1 for criterion b), we can conclude the total score is

$$\left(\frac{7}{15} \times 80\right) + (1 \times 20) = 57.33333\tag{1}$$

$$\approx 57$$
 (2)

Question 8

Rough Work:

Part 1 (Calculating the highest possible total score):

We need to calculate the highest possible total score.

• State the formula

The formula for total score tells us that

Total Score = (Score of Criterion
$$a \times 80$$
) + (Score of Criterion $b \times 20$) (3)

• Show the maximum occurs when score of criterion a and score of criterion b is maximum

By observation, we can conclude the maximum total score occurs when Score of Criterion a and Score of Criterion b are both at maximum.

• Calculate maximum possible total score using the fact 1 is the highest possible score for both criterion a and criterion b.

Because we know the maximum possible score for criterion a and b are 1, we can conclude the maximum possible total score is

$$Total Score = (1 \times 80) + (1 \times 20) \tag{4}$$

$$= 100 \tag{5}$$

Part 2 (Calculating the lowest possible total score):

We need to calculate the lowest possible total score.

• State the formula

The formula for total score tells us that

Total Score = (Score of Criterion
$$a \times 80$$
) + (Score of Criterion $b \times 20$) (6)

• Show the minimum occurs when score of criterion a and score of criterion b is minimum

By observation, we can conclude the minimum total score occurs when Score of Criterion a and Score of Criterion b are both at minimum.

• Calculate minimum possible total score using the fact 1 is the highest possible score for both criterion a and criterion b.

Because we know the minimum possible score for criterion a and b are 0, we can conclude the minimum possible total score is

$$Total Score = (0 \times 80) + (0 \times 20) \tag{7}$$

$$=0 (8)$$

Question 9

Question 10