## CSC373 Worksheet 2 Solution

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## 1. Notes:

- Greedy Algorithm
  - Always makes the choice that looks best at the moment
    - \* Locally optimal solution leads to globally optimal solution
- Activity-selection Problem (Greedy algorithm using dynamic programming)
  - Goal: Selecting maximum size set of mutually compatible activities

## Example:

- Suppose a set exists  $S = \{a_1 = [s_1, f_1), a_2 = [s_2, f_2), ..., a_n = [s_n, f_n)\}$ 
  - \*  $a_i$  represents an  $i^{th}$  activity
  - \*  $s_i$  represents starting time
  - \*  $f_i$  represents finishing time
  - \*  $0 \le s_i < f_i < \infty$
  - \*  $a_1, ..., a_n$  sorted in monotonically increasing order of finish time

i.e.

$$f_1 \le f_2 \le f_3 \le \dots \le f_{n-1} \le f_n$$

\*  $a_i$  and  $a_j$  are **compatible**, if intervals  $[s_i, f_i)$  and  $[s_j, f_j)$  don't overlap

i.e

$$s_i \ge f_i$$
 and  $s_j \ge f_i$ 

## - Steps

- 1. Think about dynamic programming solution
  - \*  $S_{ij}$ : activities that start after activity  $a_i$  finishes and before activity  $a_j$  starts

i.e.

$$S_{19} = \{a_4 = [5, 7), a_6 = [5, 9), a_7 = [6, 10)\}\$$

- \*  $A_{ij}$ : maximum set of mutually compatible activities in  $S_{ij}$  (including  $a_k$ )
  - $A_{ik} = A_{ij} \cap S_{ik}$
  - $A_{kj} = A_{ij} \cap S_{kj}$
  - $A_{ij} = A_{ik} \cup \{a_k\} \cup Akj$
  - · So,  $|A_{ij}| = |A_{ik}| + |A_{kj}| + 1$
- 2. Observe that only one choice greedy choice, and that when we make the greedy choice, only one subproblem remains
- 3. Develop recursive greedy solution
- 4. Convert the recursive algorithm into iterative one