Midterm 1 Version 1 Review 2

July 17, 2020

- 1. a) aaa, aab, aac, bba, bbb, bbc, cca, ccb, ccc
 - b) **Solution:**

p	q	r	$p \lor q$	$(p \lor q) \Rightarrow \neg r$
T	Τ	Т	${ m T}$	${ m T}$
Т	Т	F	Т	F
Т	F	Т	Т	Т
F	Т	Т	Т	Т
Т	F	F	Т	F
F	Т	F	Т	F
F	F	Т	F	Т
F	F	F	F	Т

c) $\exists x \in \mathbb{N}, \forall y \in \mathbb{N}, \neg P(x, y) \land \neg Q(x, y)$

Correct Solution:

Let $x = \dots$. Let $y \in P$.

We need to prove $\neg P(x, y)$ and $\neg Q(x, y)$ are true.

- 2. a) $\exists x \in P, Student(x) \land Attends(x)$
 - b) $\forall x \in P, \exists y \in P, Student(y) \land Attends(y) \Rightarrow Loves(x, y)$

Correct Solution:

 $\forall x \in P, \exists y \in P, Student(y) \land Attends(y) \land \underline{Loves(x,y)}$

c) $\forall x \in P, Student(x) \land Attends(x) \Rightarrow Loves(x, x)$