CSC148 Worksheet 11 Solution

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Question 1

a. Here, the constant time means the running time of accessing and assigning element by index doesn't depend on the length of the list.
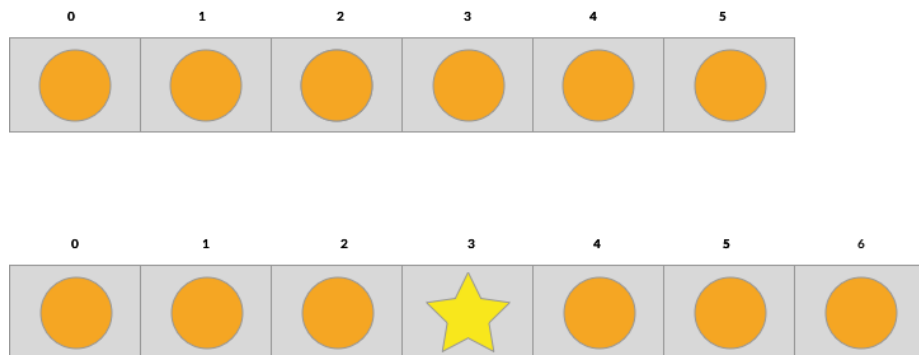
b.

$$n - i$$

many elements need to be shifted to right.

<u>Notes:</u>

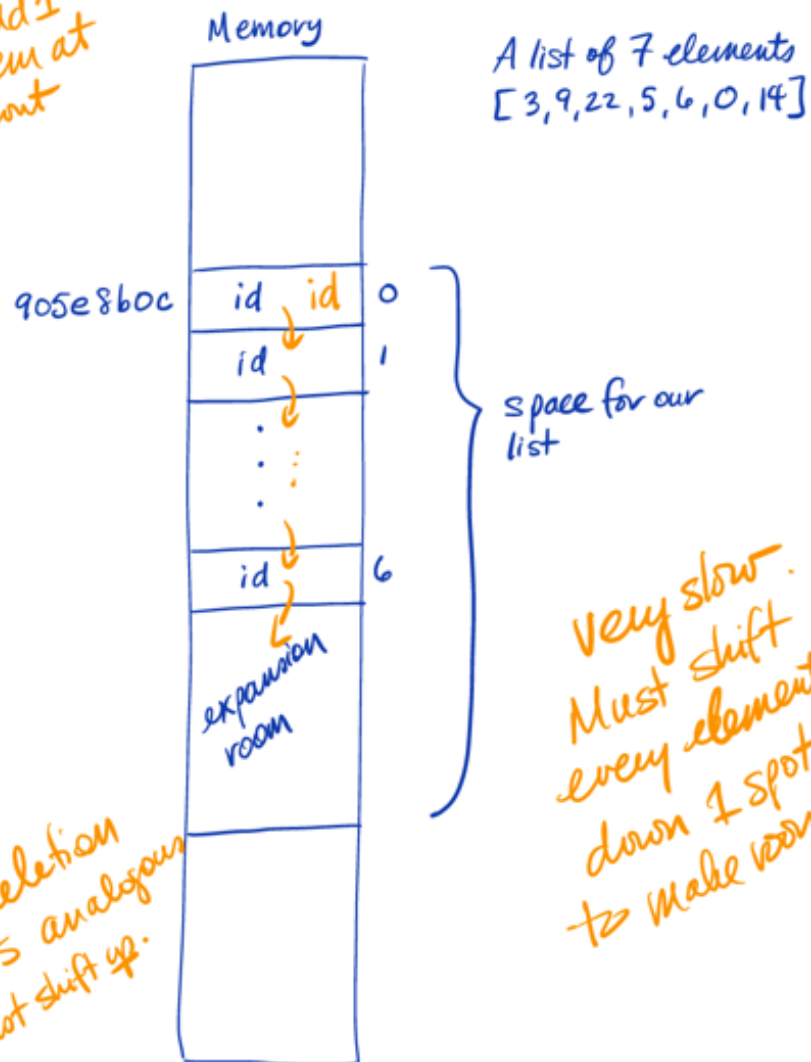- The following example tells us

  to position an element at index $i = 3$ of the list, $n - i = 6 - 3 = 3$ elements must be moved over.

  Using this fact, we can generalize that to position an element at index i of the list, $n - i$ many elements must be shifted.

- Learned that when items shifts, it shifts into the expansion room.

Updates at the front of our list

Add 1 item at front

Memory

A list of 7 elements
$[3, 9, 22, 5, 6, 0, 14]$

905e8b0c | id , id | 0
id | 1
· ⋮
id | 6

space for our list

expansion room

deletion is analogous. Must shift up.

very slow. Must shift every element down 1 spot to make room

c. Because we know the list size stays as is when an element is removed, we can conclude 0 many list elements must be moved.

Correct Solution:

The following example tells us

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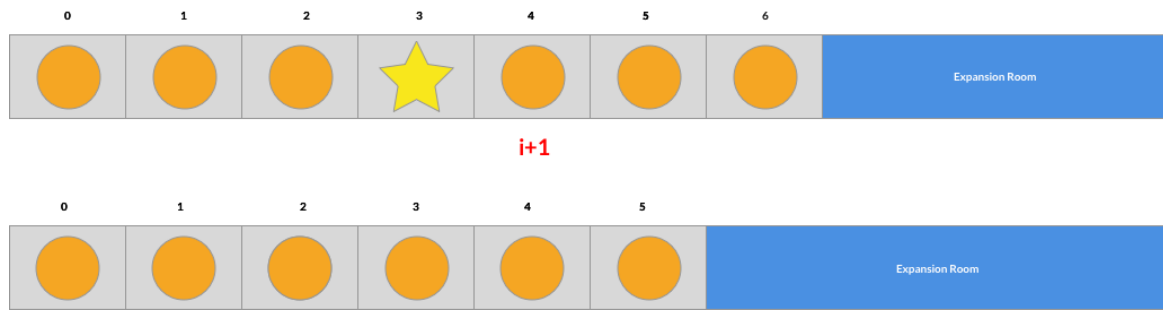
when an element at index $i = 3$ is removed from the list $n - (i + 1) = 7 - (3 - 1) = 3$ many elements must be moved.

Using this fact, we can generalize that when an element is removed, $n - (i+1) = n - i - 1$ many elements must be shifted to left.

d.   i. A solution is *LIST.remove(...)*.

The answer to question 1.d tells us when an element is removed, $n - i$ must be shifted to left.

Using this fact, we can write a list of smaller size needs to shift elements less.

Then, it follows from this fact that $n = 100$ works faster than $n = 1,000,000$.

   ii. A solution is *LIST.append(...)*

The definition of append tells us that upon call, an element is added to the end of a list, it takes a constant time to add an element as long as the expansion room is not filled.

It follows from this fact that $n = 100$ and $n = 1,000,000$ takes roughly the same amount of time.

e. The definition of *Queue* tells us *Queue* is FIFO. That is, the first element inserted is the first to come out.

Since we know the front of *Queue* is the front of the list, we can conclude *LIST.insert(...)* and *LIST.pop(0)* are used to support *QUEUE.enqueue* and *QUEUE.dequeue*, respectively.

Since we know *LIST.insert(...)* requires shifting of elements by $n - i = n - 0 = n$ and *LIST.pop(0)* requires shifting of $n - i - 1 = n - 1$ many elements, we can conclude both *QUEUE.enqueue* and *QUEUE.dequeue* takes longer time as size increases.

> **Correct Solution:**
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> The definition of *Queue* tells us *Queue* is FIFO. That is, the first element inserted is the first to come out.
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> Since we know the front of *Queue* is the front of the list, we can conclude *LIST.append(...)* and *LIST.pop(0)* are used to support *QUEUE.enqueue* and *QUEUE.dequeue*, respectively.
>
> Since we know *LIST.append(...)* requires the shifting of elements by $n - i = n - n = 0$ and *LIST.pop(0)* requires shifting of $n - i - 1 = n - 1$ many elements, we can conclude *QUEUE.dequeue* takes longer time as size increases.

Notes:

- Learned that the **front of queue** is where *QUEUE.dequeue* occurs.

Question 2

1.