## Worksheet 3 Solution

#### March 12, 2020

# Question 1

#### Part 1

- a)  $Correct(my\_prog) \land Python(my\_prog)$
- b)  $\exists x \in P, \neg Correct(x) \Rightarrow Python(x)$
- c)  $\forall x \in P, \neg Python(x) \Rightarrow Correct(x)$
- d)  $\forall x \in P, \neg Correct(x) \Rightarrow Correct(x)$
- e) A program is written in Python and is correct
- f) All programs are not written in Python and is correct
- g) It is not true that all programs written in python is correct
- h) All programs that are not written in python is correct, and all correctly running programs are not written in python

#### Question 2

- a) All program written in Python is correct, or all program written in Python is not correct
- b)  $(\exists x \in P, Python(x) \Rightarrow Correct(x)) \Rightarrow (\forall y \in P, Python(x) \Rightarrow Correct(x))$

c) The first statement considers two different natural numbers, where as the second uses the same number

The first statement is True (with  $x_1 = 5$  and  $x_2 = 35$ ), but the second statement is False (165 cannot be in multiples of 7)

### Question 3

- a)  $Odd(x): \exists n \in \mathbb{Z}, 2 \mid (n+1)$
- b)  $(\forall m \in \mathbb{Z}, Odd(m)) \land (\forall n \in \mathbb{Z}, Odd(n)) \Rightarrow Odd(mn)$
- c)  $\forall m, n \in \mathbb{Z}, \exists k, l \in \mathbb{Z}, ((m+1) = 2k) \land ((n+1) = 2l) \Rightarrow \exists o \in \mathbb{Z}, (mn+1) = 2o$
- d)  $\forall m, n \in \mathbb{Z}, \exists k \in \mathbb{Z}, ((mn+1) = 2k) \Rightarrow \exists l, o \in \mathbb{Z}, ((m+1) = 2l) \land ((n+1) = 2o)$

### Question 4

$$\neg((a \land b) \Leftrightarrow c) \tag{1}$$

Expanding definition of iff:

$$\neg(((a \land b) \land c) \lor (\neg(a \land b) \lor \neg c)) \tag{2}$$

Using  $\neg (p \lor q) \Rightarrow \neg p \land \neg q$ :

$$\neg((a \land b) \land c) \land \neg(\neg(a \land b) \lor \neg c) \tag{3}$$

Using  $\neg(p \land q) \Rightarrow \neg p \lor \neg q$  lhs and  $\neg(p \lor q) \Rightarrow \neg p \land \neg q$  rhs:

$$\neg(a \land b) \lor \neg c) \land ((a \land b) \land c) \tag{4}$$

(5)

### Question 5