Problem Set 2 Solution

March 17, 2020

Question 1

a.

b. Let $k, n \in \mathbb{Z}^+$, and $p \in \mathbb{N}$. Assume $Prime(p)$, and $p^k < n < p^k + p$.

Then, p^k can either be divided by 1 or p by fact 3.

Since, $p^k < n < p^k + p$, n cannot be written in multiples of p.

Then, it follows from the definition of divisibility that $p \nmid n$.

Since $p \nmid n$, but $1 \mid p^k$ and $1 \mid n$, $gcd(p^k, n) = 1$.

Question 2

Question 3