Worksheet 7 Solution

March 16, 2020

Question 1

a. Case 1 $(n \ge 1)$:

No more proof required. This is exactly what we want to show.

Case 2 ($\exists d \in \mathbb{N}, d \mid n \wedge d \neq 1 \wedge d \neq n$):

Let a = d and b = k.

Because we know $\forall n \in \mathbb{Z}^+$, and $l \in \mathbb{Z}, l \mid n \Rightarrow l \leq n, a \leq n$.

Then $n \mid a$ is true only when a = n and b = 1, by the fact that any lower value of a results in non-integer value.

Then it follows from the assumption $a \neq 1 \land a \neq n$ that $n \nmid a$.

The same logic holds for $n \nmid b$.

Lastly, since n=ab, and $\forall x\in\mathbb{Z},\ x\mid x,\ n\mid ab.$

Question 2

Question 3