

Midterm 1 Version 1 Review 2

July 17, 2020

1. a) $aaa, aab, aac, bba, bbb, bbc, cca, ccb, ccc$

b) **Solution:**

p	q	r	$p \vee q$	$(p \vee q) \Rightarrow \neg r$
T	T	T	T	T
T	T	F	T	F
T	F	T	T	T
F	T	T	T	T
T	F	F	T	F
F	T	F	T	F
F	F	T	F	T
F	F	F	F	T

- c) $\exists x \in \mathbb{N}, \forall y \in \mathbb{N}, \neg P(x, y) \wedge \neg Q(x, y)$

Correct Solution:

Let $x = \dots$. Let $y \in P$.

We need to prove $\neg P(x, y)$ and $\neg Q(x, y)$ are true.

2. a) $\exists x \in P, Student(x) \wedge Attends(x)$

- b) $\forall x \in P, \exists y \in P, Student(y) \wedge Attends(y) \Rightarrow Loves(x, y)$

Correct Solution:

$\forall x \in P, \exists y \in P, Student(y) \wedge Attends(y) \wedge Loves(x, y)$

- c) $\forall x \in P, Student(x) \wedge Attends(x) \Rightarrow Loves(x, x)$

- d) $\forall x, y \in P, x \neq y \Rightarrow Loves(x, y) \Rightarrow Attends(x) \vee Attends(y)$

3. a) $\forall a, b, c \in \mathbb{Z}, \exists k_1, k_2, k_3 \in \mathbb{Z}, a = k_1b \wedge b = k_2c \Rightarrow c = k_3c$