CSC373 Worksheet 2 Solution

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1. **Notes:**

- Greedy Algorithm
  - Always makes the choice that looks best at the moment
    - Locally optimal solution leads to globally optimal solution
- Activity-selection Problem (Greedy algorithm using dynamic programming)
  - Goal: Selecting maximum size set of mutually compatible activities

    Example:

i	1	2	3	4	5	6	7	8	9	10	11
s_i	1	3	0	5	3	5	6	8	8	2	12
f_i	4	5	6	7	9	9	10	11	12	14	16

  - Suppose a set exists $S = \{a_1 = [s_1, f_1), a_2 = [s_2, f_2), ..., a_n = [s_n, f_n)\}$
    - a_i represents an i^{th} activity
    - s_i represents starting time
    - f_i represents finishing time
    - $0 \leq s_i < f_i < \infty$
    - $a_1, ..., a_n$ sorted in monotonically increasing order of finish time

      i.e.

      $f_1 \leq f_2 \leq f_3 \leq ... \leq f_{n-1} \leq f_n$

    - a_i and a_j are **compatible**, if intervals $[s_i, f_i)$ and $[s_j, f_j)$ don't overlap

      i.e

      $s_i \geq f_j$ and $s_j \geq f_i$

- Steps
  1. Think about dynamic programming solution
     - S_{ij} activities that start after activity a_i finishes and before activity a_j starts

       i.e.

       $S_{19} = \{a_4 = [5, 7), a_6 = [5, 9), a_7 = [6, 10)\}$
  2. Observe that only one choice - greedy choice, and that when we make the greedy choice, only one subproblem remains
  3. Develop recursive greedy solution
  4. Convert the recursive algorithm into iterative one