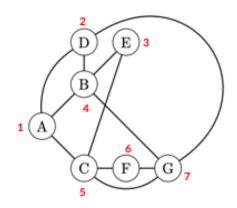
Worksheet 19 Solution

Hyungmo Gu

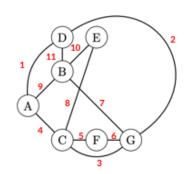
April 7, 2020

Question 1

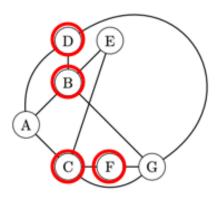
a. By the figure below, we can conclude there are 7 vertices.



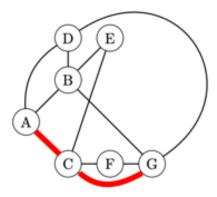
b. By the figure below, we can conclude there are 11 edges.



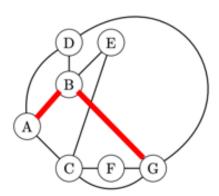
c. By the figure below, we can conclude there are 4 vertices adjacent to G.



d. By the figure below, we can conclude the distance between A ang G is 2.

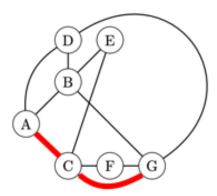


There are 2 shortest paths between A and G. One is the path from A to C to G as shown above, and the other is the path from A to B to G

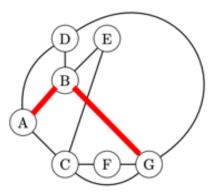


Correct Solution:

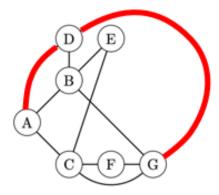
By the figure below, we can conclude the distance between A ang G is 2.



There are 3 shortest paths between A and G. One is the path from A to C to G as shown above, and the other is the path from A to B to G

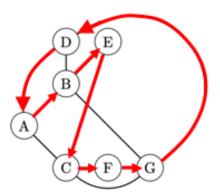


and the last one is from A to D to G



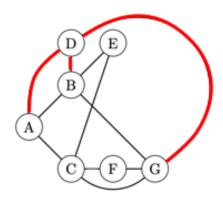
Notes:

- **Distance** is the number of edges in a shortest path.
- e. Path [C,F,G,D,A,B,E] is one example that goes through all vertices of the graph.



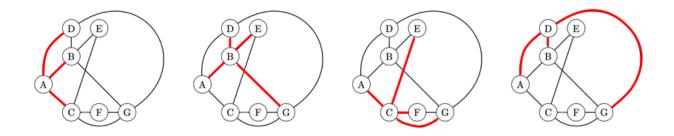
Question 2

a. By the figure below, we can conclude the degree of vertex D is 3.



- b. By the figure below, we can see
 - vertex A has degree of 3
 - vertex B has degree of 4
 - ullet vertex C has degree of 4
 - $\bullet\,$ vertex D has degree of 3
 - ullet vertex E has degree of 2
 - $\bullet\,$ vertex F has degree of 2
 - vertex G has degree of 4

Using this fact, we can conclude the vertices with the largest degree are B,C and G.



Question 3