CSC343 Worksheet 12 Solution

June 30, 2020

1. • Keys

- {id of molecule}
- {x position, y position, z position}
- Functional Dependencies
 - 1. id of molecule \rightarrow x position, y position, z position, x velocity, y velocity, z velocity
 - 2. x position, y position, z position \rightarrow id of molecule, x velocity, y velocity, z velocity

Notes:

- Function Dependencies
 - Functional Dependency is a relationship between two attributes typically between the key and other non-key attributes within a table.

Example:

 $SIN \rightarrow Name$, Address, Birthdate

Example 2:

 $ISBN \rightarrow Title$

- Key of Relations
 - One or more attributes $\{A_1, A_2, ..., A_n\}$ is a key for a relation R if
 - 1. Those attributes functionally determine all other attributes of the relation
 - 2. No proper subset of $\{A_1, A_2, ... A_n\}$ functionally determines all other attributes of R

Example:

Given relation

R = Movies1(title, year, length, genre, studioName, starName)

i. {title, year, starName } form a key for the relation Movies1

- ii. { year, starName } is not a key. Same star can be in multiple movies per year
- Superkeys
 - * Means a set of attributes that contains a key
 - * Don't need to be minimal

Example:

Given relation

R = Movies1(title, year, length, genre, studioName, starName)

- · { title, year, starName } is a key and superkey
- · { title, year, starName, title, year, length} is a superkey

References:

- 1) OpenTextBC, Chapter 11 Functional Dependencies, link
- 2. a) 1. $AB \rightarrow C$
 - 2. $AB \rightarrow D$
 - 3. $C \rightarrow A$
 - 4. $C \rightarrow B$
 - 5. $D \rightarrow B$
 - 6. $D \rightarrow C$
 - 7. $C \rightarrow D$
 - 8. $D \rightarrow A$

Second Attempt:

 $\{A,B\}^+=\{A,B,C,D\}$, so the following non-trivial FDs follows: $AB\to C$ and $AB\to D$.

 $\{C\}^+ = \{D,A\}$, so the following non-trivial FDs follows $C \to D$ and $C \to A$.

 $\{D\}^+ = \{A\}$, so the following non-trivial FDs follows: $D \to A$.

Notes:

- The Splitting / Combining Rule
 - Combining Rule

*
$$A_1, A_2, \dots, A_n \to B_i$$
 for $i = 1, 2, ..., m$ to
$$A_1, A_2, \dots A_n \to B_1, B_2, \dots B_m$$

Example:

Given

```
title year \rightarrow length
  title year \rightarrow genre
  title year \rightarrow studioName
  it's combined form is
  title year \rightarrow length genre studioName
- Splitting Rule
```

*
$$A_1, A_2, \cdots A_n \rightarrow B_1, B_2, \cdots B_m$$

to
 $A_1, A_2, \cdots, A_n \rightarrow B_i \text{ for } i = 1, 2, ..., m$

Example:

Given

title year \rightarrow length

It's splitted form is

 $title \rightarrow length$ $year \rightarrow length$

- Trivial Functional Dependencies
 - A functional dependency $FD: X \to Y$ is **trivial** if Y is a subset of X

Exmaple:

title year \rightarrow title

Example 2:

 $title \rightarrow title$

- Non-trivial Functional Dependencies
 - is a case where some but not all of the attributes on the R.H.S of an FD are also on L.H.S

Example:

title year \rightarrow title movieLength

- Can be simplified using **tirivial-dependency rule**
 - * The FD $A_1A_2\cdots A_n\to B_1B_2\cdots B_m$ is equivalent to $A_1A_2\cdots A_n\to C_1C_2\cdots C_k$

where C's are all those B's that are not in A's.



Figure 3.3: The trivial-dependency rule

- Computing the Clousre of Attributes
 - Closure of attribute set $\{X\}$ is denoted as $\{X\}^+$.
 - The closure means a given set of attributes A satisfying FD, are a sets of all attributes B such that $A \to B$

Example:

Given attributes A, B, C, D, E, F and FDs $AB \to C, BC \to AD, D \to E$ and $CF \to B$, What is the closure of $\{A, B\}$ or $\{A, B\}^+$

- 1. Start with $\{A, B\}$.
- 2. Split $BC \to AD$
 - * We have $BC \to A$ and BCtoD
 - * Since A is in $\{A, B\}$, this is not included
 - * Since D is not in $\{A, B\}$, this IS included

So, we have $\{A, B, D\}$

- 3. Since C in $AB \to C$ is NOT in $\{A, B, C, D\}$, C is included and we have $\{A, B, C, D\}$
- 4. Since A in $BC \to A$ is in $\{A, B, C, D\}$, this is skipped
- 5. Since E is not in $D \to E$, E is included and we have $\{A, B, C, D, E\}$ as our solution
- Why the Closure Algorithm Works
- Transitive Rule
 - Definition

If
$$A_1A_2 \cdots A_n \to B_1B_2 \cdots B_m$$
 and $B_1B_2 \cdots B_m \to C_1C_2 \cdots C_k$ hold in relation $R, A_1A_2 \cdots A_n \to C_1C_2 \cdots C_k$ also holds in R .

Example:

Given

title year \rightarrow studioName studioName \rightarrow studioAddr

Transitive rule says the above is equal to the following

title year \rightarrow studioAddr

- Inference Rules
 - Is allso called Armstrong's Axioms
 - Has 3 axioms
 - 1. Reflexivity

* If
$$\{B_1, B_2, ..., B_n\} \subseteq \{A_1, A_2, ..., A_n\}$$
 then $A_1 A_2 \cdots A_n \to B_1 B_2 \cdots B_m$

- * also called **trivial FDs**
- 2. Augmentation

* If
$$A_1 A_2 \cdots A_n \to B_1 B_2 \cdots B_m$$

then $A_1 A_2 \cdots A_n C_1 C_2 \cdots C_k \to B_1 B_2 \cdots B_m C_1 C_2 \cdots C_k$

- * $C_1C_2\cdots C_k$ are any set of attributes
- 3. Transitivity

* If
$$A_1A_2\cdots A_n \to B_1B_2\cdots B_m$$
 and $B_1B_2\cdots B_m \to C_1C_2\cdots C_k$
then $A_1A-2\cdots A_n \to C_1C_2\cdots C_k$

b) A, B is the only key of R.

Notes:

- Key of Attributes
 - **Definition:** A set of attributes $\{A_1, A_2, \cdots, A_n\}$ is a key for a relation R if
 - 1. Those attributes functionally determine all other attributes

- 2. No proper subset of $\{A_1, A_2, ..., A_n\}$ functionally determines all other attributes of R.
- c) The superkeys that are not keys are: $\{A,B,C\},\ \{A,B,D\},\ \{A,B,C,D\}$
- 3. i) a) $\{A\}^+=\{A,B,C,D\}$, so we have $A\to A,\,A\to B,\,A\to C,\,A\to D$ $\{B\}^+=\{C,D\}, \text{ so we have }B\to C \text{ and }B\to D$