CSC343 Worksheet 4 Solution

June 17, 2020

1. a) $[(1,0,1),(5,4,9),(1,0,1),(6,4,16),(7,9,16)]$

   b) $[(1,0),(3,3),(3,4),(4,3),(1,1),(4,3)]$

   c) $[(0,1),(0,1),(2,3),(2,4),(3,4)]$

   Notes:

   - $\tau_L(R)$ sorts tuples in order indicated by L.
     - e.g.

       $\tau_{C,B}(R)$ in $R(A,B,C)$ orders the tuples of R by their values of C, and tuples with the same C-value are ordered by their B value.

   d) $[(0,1),(0,2),(2,4),(2,5),(3,4),(3,4)]$

   e) $[(0,1),(2,4),(2,5),(3,4),(0,2)]$

   Notes:

   - $\delta(R)$ converts a bag into a set
     - e.g.

       Let $R = [(1,2),(3,4),(1,2),(1,2)]$

       $\delta(R(A,B)) = [(1,2),(3,4)]$

   f) $[(0,2),(2,7),(3,4)]$

   Notes:

   - $\gamma_L(R)$ is an operator that groups a relation and/or aggregate some columns.
     - L in $\gamma_L(R)$ is either
       1. **Grouping attribute** or an attribute by which R will be grouped.

2. **Aggregated attribute** or an attribute where an aggregation operator is applied to.

Example:

$\gamma_{starName,MIN(year)\rightarrow minYear,COUNT(title)\rightarrow ctTitle}(\text{StarsIn})$

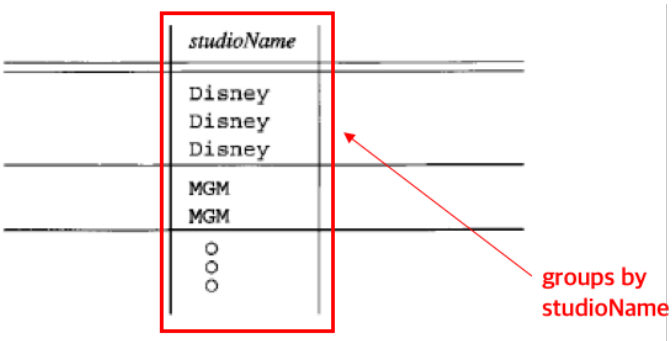

Figure 5.4: A relation with imaginary division into groups

g) $[(0, 1.5), (2, 4.5), (3, 4)]$

h) $[(0, 1), (0, 1), (2, 3), (2, 4), (3, 4)]$

i) $\gamma_{A,MAX(C)}([(2, 3, 4), (2, 3, 4)]) \rightarrow [(2, 4)]$

j) $[(0, 1, \perp), (2, 3, 4), (2, 3, 4), (0, 1, \perp), (2, 4, \perp), (3, 4, \perp)]$

Notes:

- $\overset{\circ}{\bowtie}$ is an outerjoin operator
  - $\overset{\circ}{\bowtie}_L$ means Natural Left Outer Join
  - $\overset{\circ}{\bowtie}_R$ means Natural Right Outer Join
  - $\overset{\circ}{\bowtie}$ means Natural Full Outer Join
  - $\perp$ means null
- e.g. $U \overset{\circ}{\bowtie} V$

A	B	C
1	2	3
4	5	6
7	8	9

(a) Relation U

B	C	D
2	3	10
2	3	11
6	7	12

(b) Relation V

A	B	C	D
1	2	3	10
1	2	3	11
4	5	6	$\perp$
7	8	9	$\perp$
$\perp$	6	7	12

(c) Result $U \overset{\circ}{\bowtie} V$

k) $[(\perp, 0, 1), (\perp, 2, 4), (\perp, 2, 5), (2, 3, 4), (\perp, 0, 2), (2, 3, 4)]$

l) $[(0, 1, \perp), (2, 3, 4), (2, 3, 4), (0, 1, \perp), (2, 4, \perp), (3, 4, \perp),$
$(\perp, 0, 1), (\perp, 2, 4), (\perp, 2, 5), (2, 3, 4), (\perp, 0, 2), (2, 3, 4)]$