# CSC373 Worksheet 4 Solution

## August 4, 2020

#### 1. • Calculating out-degree

Let G = (V, E) be a directed graph. Let  $[v_1, ..., v_n]$  be a list of vertices in graph G.

I need to calculate the outdegree of every vertex using adjacency list.

We know that in addition to counting each  $v_i$  in adjacency list where i = 1, ..., n, we are also counting  $|Adj[v_i]|$  edges.

Since there are |V| = n many vertices, we can write that the total count is  $|V| + \sum_{i=1}^{n} |Adj[v_i]| = |V| + |E|$ , which is  $\mathcal{O}(|V| + |E|)$ .

#### • Calculating In-degree

The outdegree of a vertex is indegree of another vertex.

Using this fact, we can conclude the running time of computing indegree of every vertax is  $\mathcal{O}(|V| + |E|)$ .

#### Notes:

#### • Vertex

- Is a fundamental unit of which graphs are formed
- Also means node



### • Adjacency-list Representation

- Associates each vertax in a graph with the collection of its neighbouring vertices or edges
- Is represented by Adj[v]
  - \* Means all vertices that are neighbour to vertex v
  - \* In a directed graph, Adj[v] are all out-degree vertices of vertax v
  - \* |Adj[v]| means the total number of outdegree of vertax v







### • Directed graph

 Is a graph that is made up of a set of vertices connected by edges, where the edges have a direction associated with them



#### • Out-degrees

- For a directed graph G = (V(G), E(G)) and a vertex  $x_1 \in V(G)$ , the Out-Degree of  $x_1$  refers to the number of arcs incident from  $x_1$ . That is, the number of arcs directed away from the vertex  $x_1$ .



#### • In-degrees

- For a directed graph G = (V(G), E(G)) and a vertex  $x_1 \in V(G)$ , the In-Degree of  $x_1$  refers to the number of arcs incident to  $x_1$ . That is, the number of arcs directed <u>towards</u> the vertex  $x_1$ .



• Computing the outdegree of every vertex using adjacency list





$$(v_1 + v_2) + (e_1 + e_2 + e_3)$$

3)



$$(v_1 + v_2 + v_3) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

3)



$$(v_1 + v_2 + v_3) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

4)



$$(v_1 + v_2 + v_3 + v_4) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

4)



 $(v_1 + v_2 + v_3 + v_4) + (e_1 + e_2 + e_3 + e_4 + e_5)$ 

6)



So it has  $\mathcal{O}(V+E)$ 

• Computing the outdegree of every vertex using adjacency list

The outdegree of a vertex is indegree of another vertex.

Using this fact, we can conclude the running time of computing indegree of every vertax is  $\mathcal{O}(V+E)$ .

2. • Computing  $G^T$  from G in Adjacency List



```
COMPUTE-G-TRANSPOSE-ADJ-MATRIX(Adj,V)

Let Adj' be a new adjacency list containing keys v_i...v_n

for i = 1 to |V|

for every vertax w in Adj[v_i]

Insert(Adj'[w], v_i)

return Adj'
```

# • Computing $G^T$ from G in Adjacency-Matrix



```
COMPUTE-G-TRANSPOSE-ADJ-MATRIX(A,V)

Let A'[1..|V|, 1..|V|] be a new adjacency matrix

for i = 1 to |V|

for j = 1 to |V|

A'[j,i] = A[i,j]

return A'
```

#### **Correct Solution:**

• Computing  $G^T$  from G in Adjacency List



```
COMPUTE-G-TRANSPOSE-ADJ-MATRIX(Adj,V)

Let Adj' be a new adjacency list containing keys v_i...v_n

for i = 1 to |V|

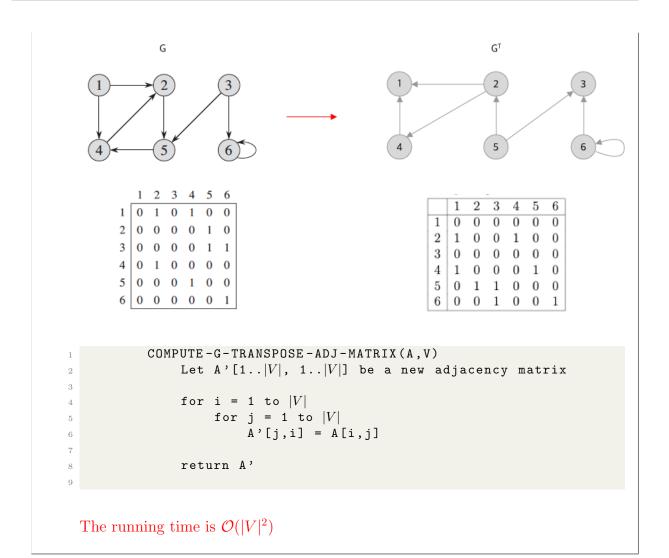
for every vertax w in Adj[v_i]

Insert(Adj'[w], v_i)

return Adj'
```

### The running time is $\mathcal{O}(|V| + |E|)$

 $\bullet$  Computing  $G^T$  from G in Adjacency-Matrix



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#### Notes:

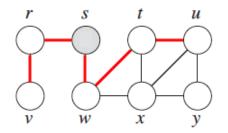
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#### • Breadth First Search

- Is an algorithm for searching or traversing a graph
- Is one of the simplest algorithm

# • Largest of All Shortest Path Distance

– Means the shortest distance between two furthest apart nodes



OR

