CSC236 Worksheet 8 Solution

Hyungmo Gu

May 13, 2020

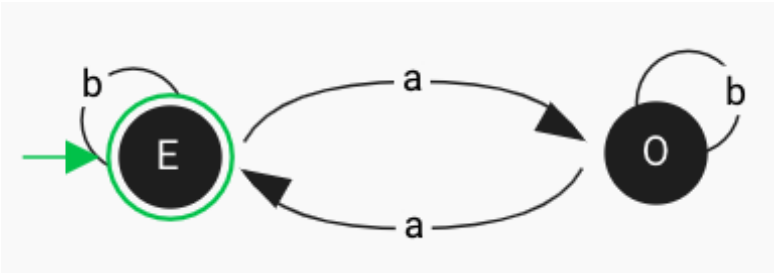
Question 1

Rough Works:

1. Build L_1

$$Q = \{E, O\}$$
$$\Sigma = \{a, b\}$$
$$\delta = \begin{array}{|c|c|c|} \hline & \text{E} & \text{O} \\ \hline \text{a} & \text{O} & \text{E} \\ \hline \text{b} & \text{E} & \text{O} \\ \hline \end{array}$$
$$q_0 = E$$
$$F = \{E\}$$

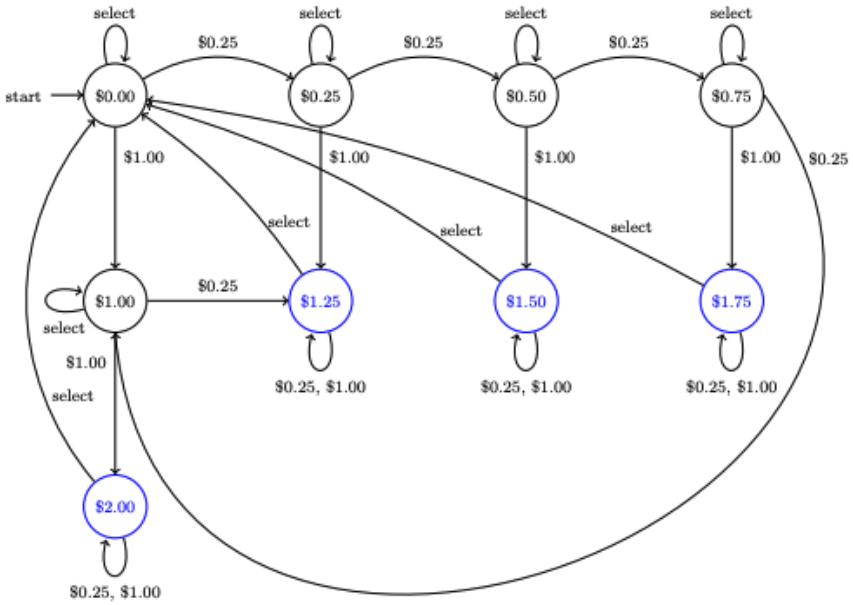
Draw Diagram



2. Build L_2

Notes:

- **Deterministic Finite State Automaton (DFSA)**: is a mathematical method of machine which, given any input string x, **accepts** or **rejects** x.
- Applications of DFSA
    1. Vending Machine



    2. Protocol analysis
    3. Text parsing
    4. Video game character behavior

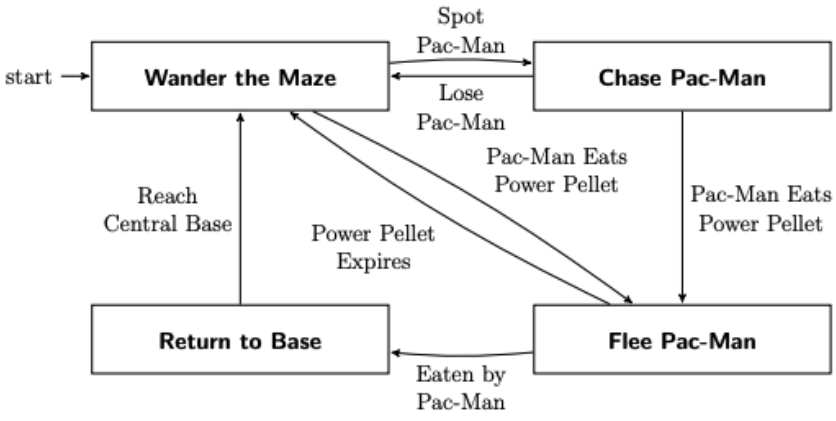
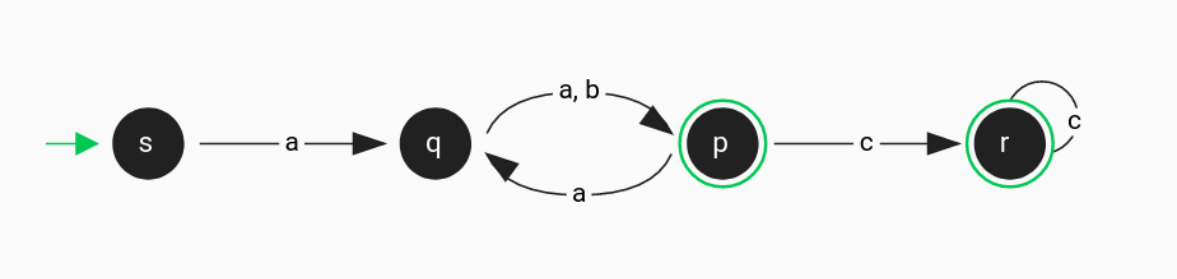


Figure 3: Behavior of a Pac-Man Ghost

    5. Security Analysis

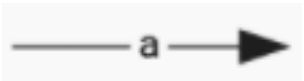
6. CPU control units (**)
7. Natural Language Processing (**)
8. Speech Recognition (**)

- Definitions and Syntax

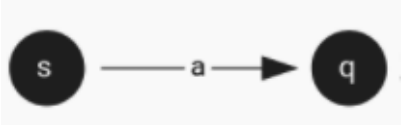


  - *DFSA* M is a quintuple $M = (Q, \Sigma, q_0, F, \delta)$, where
    - Q : a finite set of **states**.
      - Represents status of system
      - Is represented by a black circle, i.e. s,q

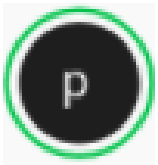
      - i.e. automatic sliding door at walmart has two states: either close or open
      - i.e. traffic light has three states: red, yellow, green
    - Σ : a finite non-empty alphabet
      - is set of symbols in each transition, i.e. a, b, c



    - $q_0 \in Q$: the start or initial state
    - $\delta : Q \times \sigma \rightarrow Q$: a transition function
      - is a connection between two states.
      - is represented by an arrow

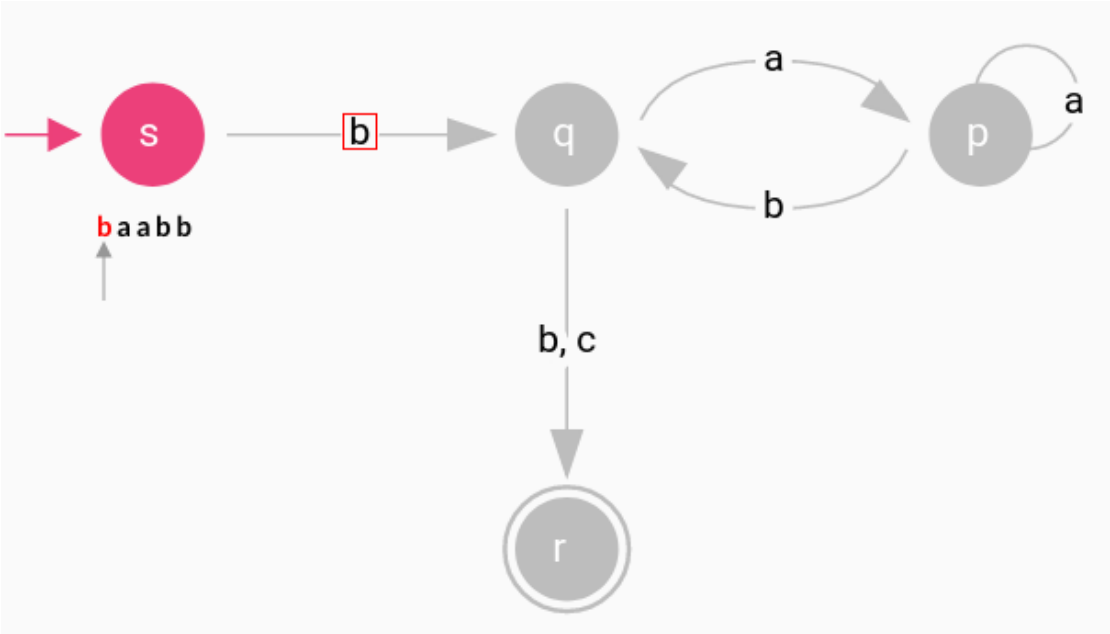


    - $F \subseteq Q$: the set of accepting or final states
      - Is represented by a double circle



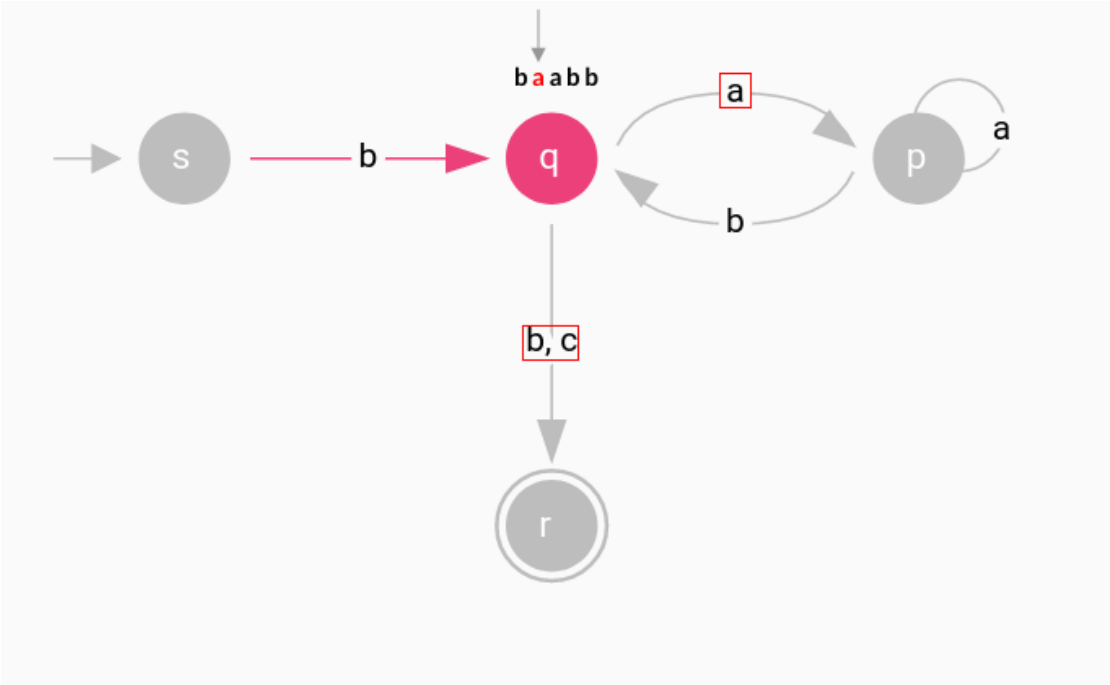
- Multiple accepting states may exists
- Purpose: When processing ends, the output is either *accept* or *reject*

- Simple Example
  - Step 1



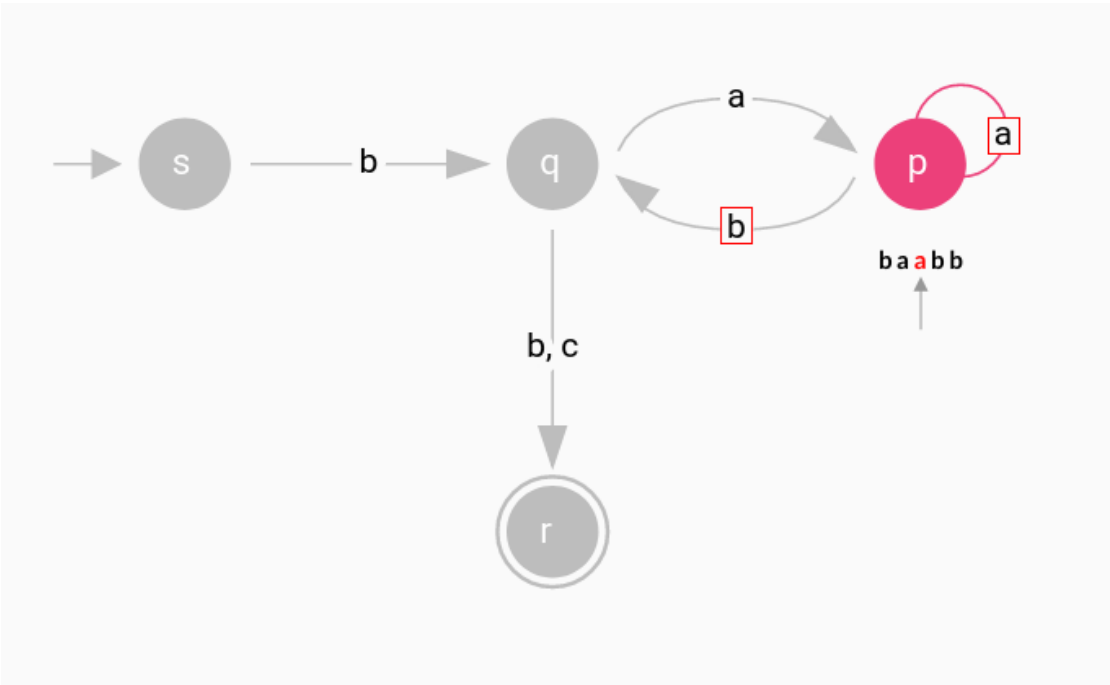
1. First symbol of the input **baabb** is **b** and the current state is s.
2. Ask, is there any exiting transition from s that contains the symbol **b**?
3. The answer is yes, so move to q

  - Step 2



1. Next symbol of the input **baabb** is **a** and the current state is q.
2. Ask, is there any exiting transition from q that contains the symbol **a** or **b,c**?
3. The answer is yes, and it's **a**. So move to p

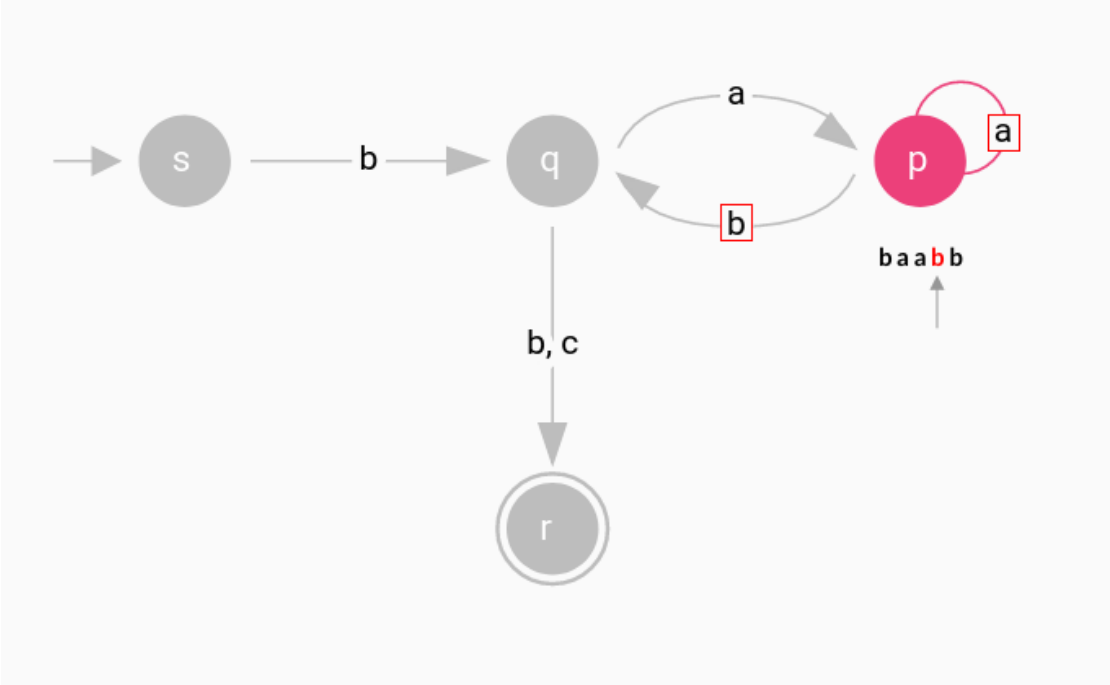
– Step 3



1. Next symbol of the input **baabb** is **a** and the current state is p.
2. Ask, is there any exiting transition from p that contains the symbol **a** or **b**?

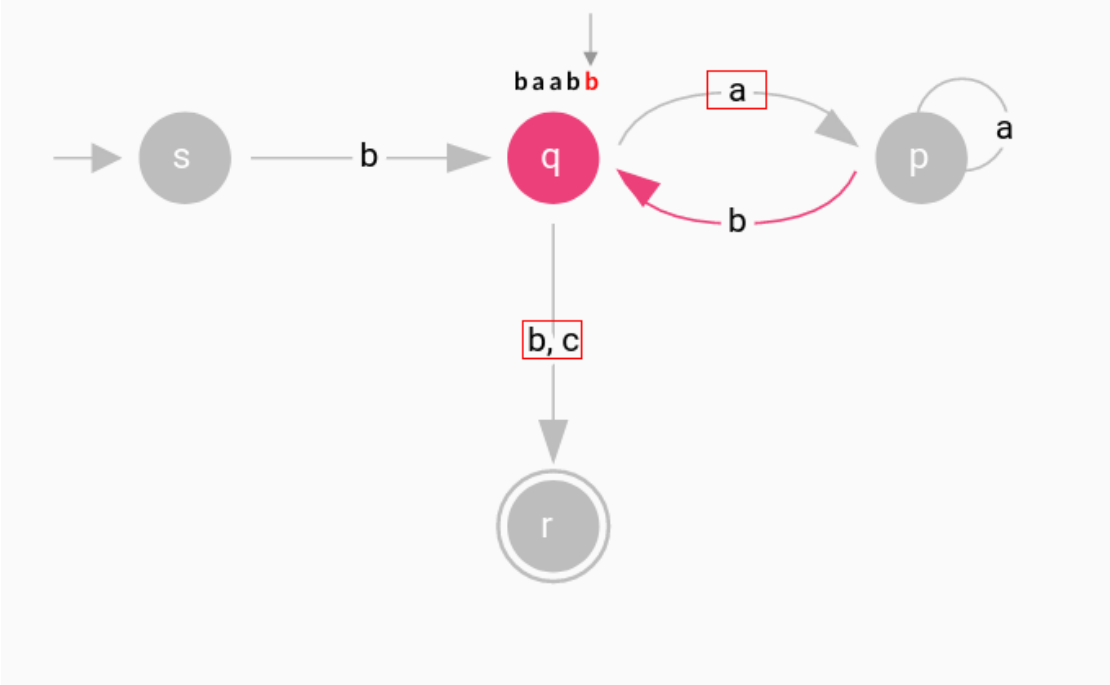
3. The answer is yes, and it's **a**. So move to p

– Step 4



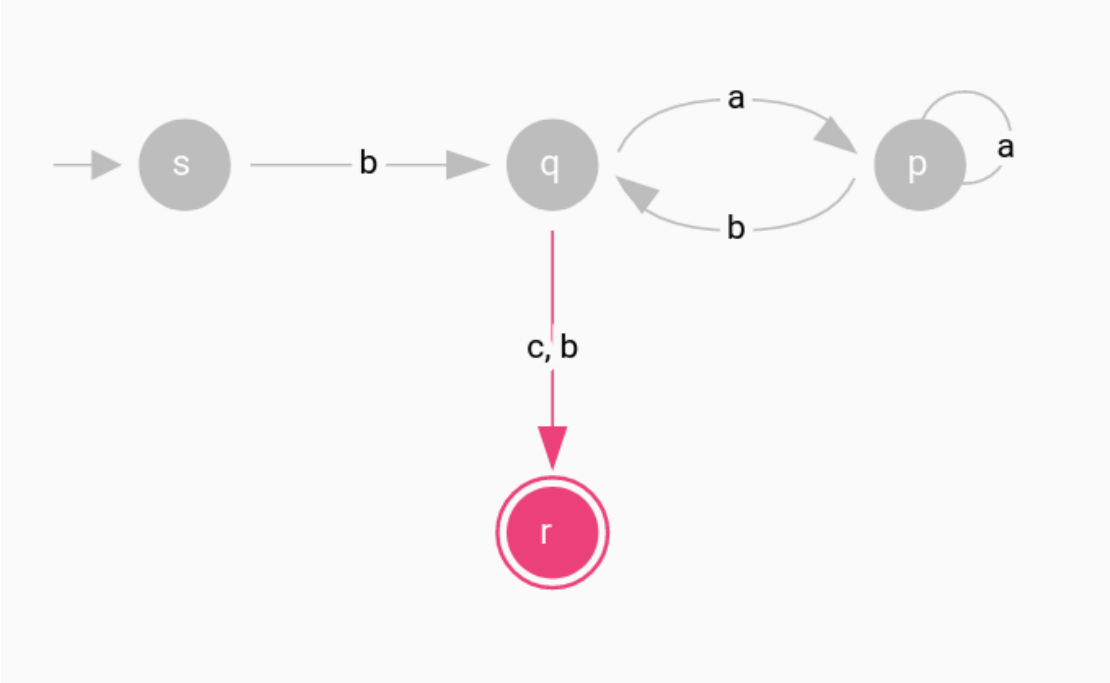
1. Next symbol of the input **baabb** is **b** and the current state is p.
2. Ask, is there any exiting transition from p that contains the symbol **a** or **b**?
3. The answer is yes, and it's **b**. So move to q

– Step 5



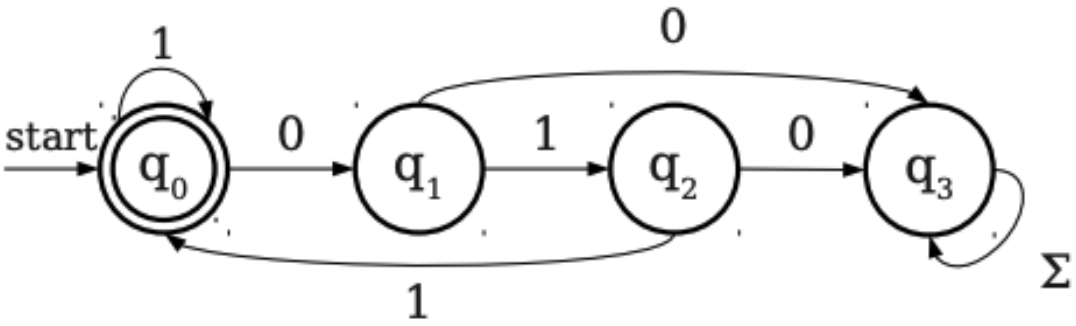
1. Next symbol of the input **baabb** is **b** and the current state is q.
2. Ask, is there any exiting transition from q that contains the symbol **a** or **b,c**?
3. The answer is yes, and it's **b**. So move to r

– Step 6



1. Next symbol of the input **baabb** is **b** and the current state is r.
2. Ask, if it satiesfies the accepting or final state (i.e, has the end of string been reached?). If so, the output is accept. Otherwise, it's reject.

- Formal Languages
  - is a subset of all possible words $\Sigma*$ formed by symbols of alphabet Σ.
    - $\Sigma*$ is set of all possible strings over the alphabet Σ.
    - i.e. $\Sigma = \{a, b\}$, $\Sigma* = \{a, b, aa, ab, ba, bb, aaa, aab, \cdots\}$
  - Example
    1. $L = \{w \mid w \text{ has at most seventeen 0's}\}$
    2. $L = \{w \mid w \text{ has equal number of 0's and 1's}\}$
    3. $L = \{x \in \{a, b\}^* \mid \text{the number of as in } x \text{ is even}\}$
       - * in $\{a, b\}^*$ means all possible combinations
       - i.e. $\{a, b, aa, ab, ba, bb, aaa, baa, aba, \cdots\}$
- Tabular DFAs
  - Example



$$\delta = \begin{array}{|c|c|c|} \hline & 0 & 1 \\ \hline {}^{*}q_0 & q_1 & q_0 \\ q_1 & q_3 & q_2 \\ q_2 & q_3 & q_0 \\ q_3 & q_3 & q_3 \\ \hline \end{array}$$

Note: * means it's an accepting state