

# CSC373 Worksheet 4 Solution

August 3, 2020

1. • Calculating out-degree

Let  $G = (V, E)$  be a directed graph. Let  $[v_1, \dots, v_n]$  be a list of vertices in graph  $G$ .

I need to calculate the outdegree of every vertex using adjacency list.

We know that in addition to counting each  $v_i$  in adjacency list where  $i = 1, \dots, n$ , we are also counting  $|Adj[v_i]|$  edges.

Since there are  $|V| = n$  many vertices, we can write that the total count is  $|V| + \sum_{i=1}^n |Adj[v_i]| = |V| + |E|$ , which is  $\mathcal{O}(|V| + |E|)$ .

• Calculating In-degree

The outdegree of a vertex is indegree of another vertex.

Using this fact, we can conclude the running time of computing indegree of every vertex is  $\mathcal{O}(|V| + |E|)$ .

Notes:

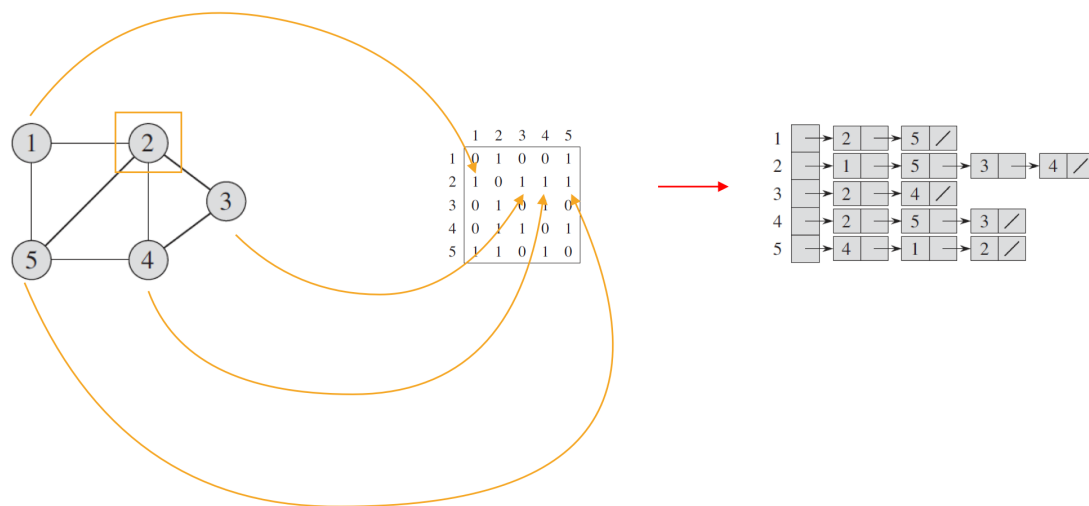
• **Vertex**

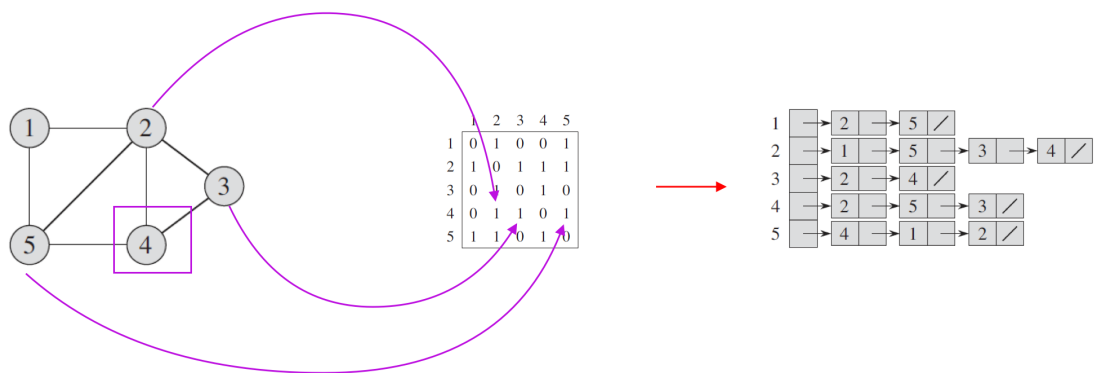
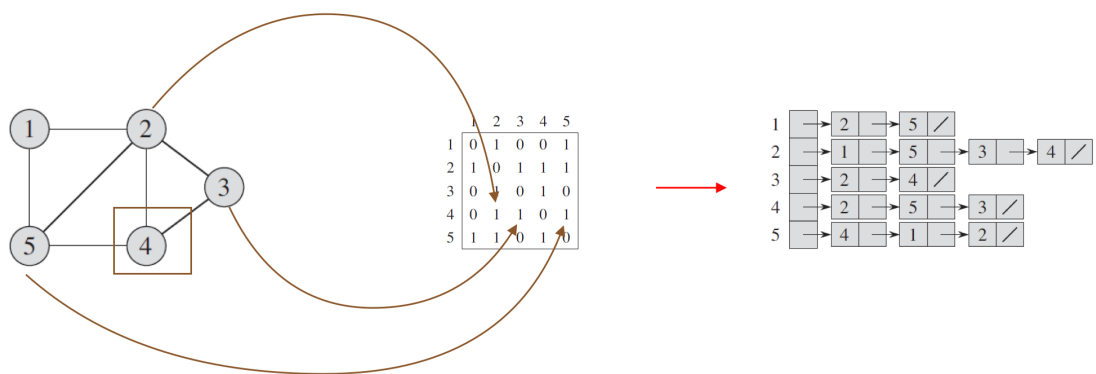
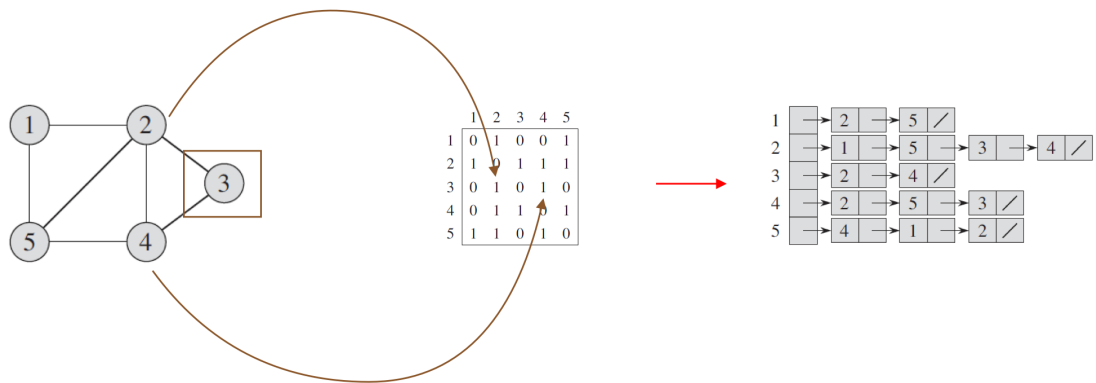
- Is a fundamental unit of which graphs are formed
- Also means node



### • Adjacency-list Representation

- Associates each vertex in a graph with the collection of its neighbouring vertices or edges
- Is represented by  $Adj[v]$ 
  - \* Means all vertices that are neighbour to vertex  $v$
  - \* In a directed graph,  $Adj[v]$  are all out-degree vertices of vertex  $v$
  - \*  $|Adj[v]|$  means the total number of outdegree of vertex  $v$







### • Directed graph

- Is a graph that is made up of a set of vertices connected by edges, where the edges have a direction associated with them



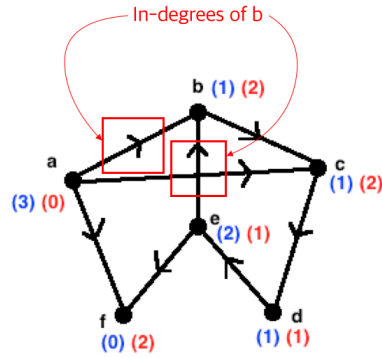
### • Out-degrees

- For a directed graph  $G = (V(G), E(G))$  and a vertex  $x_1 \in V(G)$ , the Out-Degree of  $x_1$  refers to the number of arcs incident from  $x_1$ . That is, the number of arcs directed away from the vertex  $x_1$ .



### • In-degrees

- For a directed graph  $G = (V(G), E(G))$  and a vertex  $x_1 \in V(G)$ , the In-Degree of  $x_1$  refers to the number of arcs incident to  $x_1$ . That is, the number of arcs directed towards the vertex  $x_1$ .



- Computing the outdegree of every vertex using adjacency list



3)



$$(v_1 + v_2 + v_3) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

3)



$$(v_1 + v_2 + v_3) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

4)



$$(v_1 + v_2 + v_3 + v_4) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

4)



$$(v_1 + v_2 + v_3 + v_4) + (e_1 + e_2 + e_3 + e_4 + e_5)$$

6)



$$(v_1 + v_2 + v_3 + v_4 + v_5 + v_6) + (e_1 + e_2 + e_3 + e_4 + e_5 + e_6 + e_7 + e_8)$$

So it has  $\mathcal{O}(V + E)$

- Computing the outdegree of every vertex using adjacency list

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Using this fact, we can conclude the running time of computing indegree of every vertex is  $\mathcal{O}(V + E)$ .