

# CSC343 Worksheet 4 Solution

June 17, 2020

1. a)  $[(1, 0, 1), (5, 4, 9), (1, 0, 1), (6, 4, 16), (7, 9, 16)]$   
b)  $[(1, 0), (3, 3), (3, 4), (4, 3), (1, 1), (4, 3)]$   
c)  $[(0, 1), (0, 1), (2, 3), (2, 4), (3, 4)]$

## Notes:

- $\tau_L(R)$  sorts tuples in order indicated by  $L$ .
  - e.g.

$\tau_{C,B}(R)$  in  $R(A, B, C)$  orders the tuples of  $R$  by their values of  $C$ , and tuples with the same  $C$ -value are ordered by their  $B$  value.

- d)  $[(0, 1), (0, 2), (2, 4), (2, 5), (3, 4), (3, 4)]$   
e)  $[(0, 1), (2, 4), (2, 5), (3, 4), (0, 2)]$

## Notes:

- $\delta(R)$  converts a bag into a set
  - e.g.

Let  $R = [(1, 2), (3, 4), (1, 2), (1, 2)]$

$\delta(R(A, B)) = [(1, 2), (3, 4)]$

- f)  $[(0, 2), (2, 7), (3, 4)]$

## Notes:

- $\gamma_L(R)$  is an operator that groups a relation and/or aggregate some columns.
  - $L$  in  $\gamma_L(R)$  is either
    1. **Grouping attribute** or an attribute by which  $R$  will be grouped.

2. **Aggregated attribute** or an attribute where an aggregation operator is applied to.

**Example:**

$\gamma_{starName, MIN(year) \rightarrow minYear, COUNT(title) \rightarrow ctTitle} (StarsIn)$

studioName
Disney
Disney
Disney
MGM
MGM

groups by studioName

Figure 5.4: A relation with imaginary division into groups

- g)  $[(0, 1.5), (2, 4.5), (3, 4)]$   
 h)  $[(0, 1), (0, 1), (2, 3), (2, 4), (3, 4)]$   
 i)  $\gamma_{A, MAX(C)}([(2, 3, 4), (2, 3, 4)]) \rightarrow [(2, 4)]$   
 j)  $[(0, 1, \perp), (2, 3, 4), (2, 3, 4), (0, 1, \perp), (2, 4, \perp), (3, 4, \perp)]$

**Notes:**

- $\bowtie$  is an outerjoin operator
  - $\bowtie_L$  means Natural Left Outer Join
  - $\bowtie_R$  means Natural Right Outer Join
  - $\bowtie$  means Natural Full Outer Join
  - $\perp$  means null
- e.g.  $U \bowtie V$

$A$	$B$	$C$
1	2	3
4	5	6
7	8	9

(a) Relation  $U$ 

$B$	$C$	$D$
2	3	10
2	3	11
6	7	12

(b) Relation  $V$ 

$A$	$B$	$C$	$D$
1	2	3	10
1	2	3	11
4	5	6	$\perp$
7	8	9	$\perp$
$\perp$	6	7	12

(c) Result  $U \bowtie V$ 

- k)  $[(\perp, 0, 1), (\perp, 2, 4), (\perp, 2, 5), (2, 3, 4), (\perp, 0, 2), (2, 3, 4)]$
- l)  $[(0, 1, \perp), (2, 3, 4), (2, 3, 4), (0, 1, \perp), (2, 4, \perp), (3, 4, \perp), (\perp, 0, 1), (\perp, 2, 4), (\perp, 2, 5), (2, 3, 4), (\perp, 0, 2), (2, 3, 4)]$
- m)  $[(0, 1, \perp), (2, 3, 4), (2, 3, 4), (0, 1, \perp), (2, 4, \perp), (3, 4, \perp), (\perp, 0, 1), (\perp, 2, 4), (\perp, 2, 5), (2, 3, 4), (\perp, 0, 2), (2, 3, 4)]$

**Notes:**

- $R \bowtie_C S$  is equivalent form of  $\sigma_C(R \times S)$  but with dangling tuples filled with null.