Worksheet 3 Review 2

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Question 1

- a. $Correct(my_prog) \land Python(my_prog)$
- b. $\forall x \in P, \neg Correct(x) \Rightarrow Python(x)$

Correct Solution:

 $\exists x \in P, \neg Correct(x) \land Python(x)$

Notes:

• I feel that '∧' operator is used instead of '⇒' if 'is' is used with an existential quantifier

Example:

An incorrect program is written in Python

• I also feel '⇒' is used when 'is' is used with universal quantifier

Example:

Every incorrect program is written in python

- c. $\forall x \in P, Python(x) \Rightarrow \neg Correct(x)$
- d. $\forall x \in P, \neg Correct(x) \Rightarrow Python(x)$
- e. There is a program that is written in *Python* and is *Correct*
- f. All programs are not written in *Python* and is *Correct*
- g. There is a program that is Correct and not written in Python
- h. All programs that are correct is not written in *Python*, and all programs that are *Correct* is not written in *Python*.

Question 2

- a. Either all programs that are written in *Python* is *Correct*, or all programs that are written in *Python* are not *Correct*
- b. $(\exists x \in P, Python(x) \land Correct(x)) \Rightarrow (\forall x \in P, Python(x) \land Correct(x))$
- c. The difference is that in statement 1, each divisibility claims can be validated with different natural numbers where as in statement 2, the two claims must be validated with a single natural number.

The statement 1 is true, where as statement 2 is false (consider counter example of x = 7)

Question 3

a. $Odd(n): \forall n \in \mathbb{Z}, \exists \in \mathbb{Z}, n+1=2k$

Correct Solution:

 $Odd(n): \exists \in \mathbb{Z}, n+1=2k, \text{ where } n \in \mathbb{Z}$

Notes:

- Noticed professor defines variable in predicate (i.e. n in P(n)) in where (i.e where $n \in \mathbb{Z}$)
- b. $\forall m, n \in \mathbb{Z}, Odd(m) \wedge Odd(n) \Rightarrow Odd(mn)$
- c. $\forall m, n \in \mathbb{Z}, \exists k_1, k_2 \in \mathbb{Z}, (n+1=2k_1) \land (m+1=2k_2) \Rightarrow \exists k_3 \in \mathbb{Z}, (mn+1=2k_3)$

Correct Solution:

 $\forall m, n \in \mathbb{Z}, (\exists k_1 \in \mathbb{Z}, n+1 = 2k_1) \land (\exists k_1 \in \mathbb{Z}, m+1 = 2k_2) \Rightarrow \exists k_3 \in \mathbb{Z}, mn+1 = 2k_3$

Notes:

- Noticed professor didn't pull out existential quantifier from parenthesis
- d. $\forall m, n \in \mathbb{Z}, \exists k_1 \in \mathbb{Z}, mn+1=2k_1 \Rightarrow (\exists k_2 \in \mathbb{Z}, m+1=2k_2) \wedge (\exists k_3 \in \mathbb{Z}, n+1=2k_3)$

Question 4

Question 5