CSC148 Worksheet 16 Solution

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Question 1

a. The doctests for the base case is

```
"""

>>> nested_list_contains(1,1)

True

>>> nested_list_contains(1,2)

False
"""
```

Using this fact, we can write

```
from typing import Union, List
      def nested_list_contains(obj: Union[int, List], item: int) -> bool:
          """Return whether the given item appears in <obj>.
          Note that if <obj> is an integer, this function checks whether
          <item> is equal to <obj>.
6
          >>> nested_list_contains(1,1)
          True
          >>> nested_list_contains(1,2)
10
          False
11
          0.00
12
13
          if isinstance(self, int):
14
              return obj == item
15
16
```

Listing 1: worksheet_16_q1a_solution

b. Consider the following doctest

```
"""

>>> nested_list_contains([4,2,2,[6,5,7,[8]]],8)

True
    """

5
```

Using the base case from question 1.a, and the basic recursive design recipe, we can conclude the algorithm will behave as follows

```
1) 4 \rightarrow 4 == item? \rightarrow False

2) 2 \rightarrow 2 == item? \rightarrow False

3) 2 \rightarrow False

4) [6,5,7,[8]] \rightarrow Recursion

5) 6 \rightarrow 6 == item? \rightarrow False

6) 5 \rightarrow 5 == item? \rightarrow False

7) 7 \rightarrow 7 == item? \rightarrow False

8) [8] \rightarrow Recursion

9) 8 \rightarrow 8 == item? \rightarrow True (function terminates)
```

Now, no new parameters other than *obj* and *item* are required, since

- 1. for the traversing and checking of elements, they are done using the two parameters.
- 2. for bringing the value 'True' to user, it is done by repeatedly ending the recursive function call early with the value
- 3. for brining the value 'False' to user, it is done by returning False at the end.

```
from typing import Union, List
c_1
3
      def nested_list_contains(obj: Union[int, List], item: int) -> bool:
           """Return whether the given item appears in <obj>.
5
           Note that if <obj> is an integer, this function checks whether
           <item> is equal to <obj>.
           >>> nested_list_contains([4,2,2,[6,5,7,[8]]],8)
9
           >>> nested_list_contains([4,2,2,[6,5,7,[8]]],9)
12
           False
           \Pi_{i}\Pi_{j}\Pi_{j}
13
14
           if isinstance(self, int):
15
               return obj == item
           else:
17
                                    ==== (Solution) =====
18
               for sublist in obj:
19
                    result = nested_list_contains(sublist, item)
20
                    if result:
22
```

Listing 2: worksheet_16_q1c_solution

Question 2

a. The doctests for the base case is

Using this fact, we can write

```
from typing import Union, List, Optional
3
      def first_at_depth(obj: Union[int, List], d: int) -> Optional[int]:
4
          """Return the first (leftmost) item in <obj> at depth <d>.
          Return None if there is no item at depth <d>.
6
          Precondition: d \ge 0.
          >>> first_at_depth(1,2)
9
          None
11
12
          if isinstance(obj, int):
13
              return None
14
```

Listing 3: worksheet_16_q2a_solution

b. Rough Work:

1. Write a doctest for the function call on input of some complexity

First, we need to write a doctest for the function call on input of some complexity

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Consider the following doctests.

2. Write down the relevant recursive calls for each sub-nested-list of input.

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The recursive calls for the example $first_at_depth([1,2,[3,4,[5,6]]],3)$ is as follows

- 1) 1 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
- 2) 2 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
- 3) $[3,4,[5,6]] \rightarrow \text{Recursion}$
 - 4) 3 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
 - 5) 4 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
 - 6) [5,6] \rightarrow Recursion
 - 7) 5 \rightarrow is current_depth == 3? \rightarrow True \rightarrow return 5
- 8) Function Terminates with return value 5 until the end of recursion
- 3. Think about the extra parameters for each function.

Finally, we need to think about the extra parameters for each function.

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It follows from above that the extra parameter required for this function is $current_depth$. To add this parameter, we need to change function $first_at_depth$ from

First, we need to write doctests for the function call on input of some complexity.

Consider the following doctests.

```
"""

>>> first_at_depth([1,2,[3,4,[5,6]]],1)

1

>>> first_at_depth([1,2,[3,4,[5,6]]],3)

5

>>> first_at_depth([1,2,[3,4,[5,6]]],4)

None

>>> first_at_depth([[1,2,[3,4,[5,6]]],4)

None

>>> first_at_depth([[1,2,[3]],4,[[5],6]],3)

"""
```

Second, we need to write down the relevant recursive calls for each sub-nested-list of input.

The recursive calls for the example $first_at_depth([1,2,[3,4,[5,6]]],3)$ is as follows

- 1) $1 \rightarrow \text{is current_depth} == 3? \rightarrow \text{False} \rightarrow \text{return None}$
- 2) 2 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
- 3) $[3,4,[5,6]] \rightarrow \text{Recursion}$
 - 4) 3 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
 - 5) 4 \rightarrow is current_depth == 3? \rightarrow False \rightarrow return None
 - 6) $[5,6] \rightarrow \text{Recursion}$
 - 7) 5 \rightarrow is current_depth == 3? \rightarrow True \rightarrow return 5
- 8) Function Terminates with return value 5 until the end of recursion

Finally, we need to think about the extra parameters for each function.

It follows from above that the extra parameter required for this function is $current_depth$. To add this parameter, we need to change function $first_at_depth$ from