# CSC343 Worksheet 13 Solution

July 5, 2020

|       | A     | B     | $\mid C \mid$ | D     | $\mid E \mid$ |
|-------|-------|-------|---------------|-------|---------------|
| 1 2)  | a     | b     | c             | $d_1$ | $e_1$         |
| 1. a) | $a_1$ | b     | c             | d     | $e_2$         |
|       | a     | $b_1$ | c             | $d_2$ | e             |

# Step 1 $(B \rightarrow E)$ :

| A     | В     | С | D     | Е     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | $e_1$ |
| $a_1$ | b     | c | d     | $e_1$ |
| a     | $b_1$ | c | $d_2$ | e     |

# Step 2 ( $CE \rightarrow A$ ):

| A | В     | С | D     | Е     |
|---|-------|---|-------|-------|
| a | b     | c | $d_1$ | $e_1$ |
| a | b     | c | d     | $e_1$ |
| a | $b_1$ | c | $d_2$ | e     |

So in this case, an example of an instance of R that is not lossless is:

| Title              | Studio Name | President       | Year | President Address |
|--------------------|-------------|-----------------|------|-------------------|
| Toy Story          | Pixar       | Steve Jobs      | 2000 | 123 ABC Street    |
| Star Wars          | Fox         | Lachlan Murdoch | 1977 | Hollywood         |
| Return of the Jedi | Fox         | Lachlan Murdoch | 1983 | Hollywood         |

| • | $S_1 = \{A, B, C\}$ |             |                 |
|---|---------------------|-------------|-----------------|
|   | Title               | Studio Name | President       |
|   | Toy Story           | Pixar       | Steve Jobs      |
|   | Star Wars           | Fox         | Lachlan Murdoch |
|   | Return of the Jedi  | Fox         | Lachlan Murdoch |

•  $S_2 = \{C, D, E\}$ 

| President       | Year | President Address |
|-----------------|------|-------------------|
| Steve Jobs      | 2000 | 123 ABC Street    |
| Lachlan Murdoch | 1977 | Hollywood         |
| Lachlan Murdoch | 1983 | Hollywood         |

 $\bullet \ \overline{S_3 = \{C, E, A\}}$ 

| Title              | President       | President Address |
|--------------------|-----------------|-------------------|
| Toy Story          | Steve Jobs      | 123 ABC Street    |
| Star Wars          | Lachlan Murdoch | Hollywood         |
| Return of the Jedi | Lachlan Murdoch | Hollywood         |

•  $\overline{S_1 \bowtie S_2}$ 

| Title              | Studio Name | President       | Year | President Address |
|--------------------|-------------|-----------------|------|-------------------|
| Toy Story          | Pixar       | Steve Jobs      | 2000 | 123 ABC Street    |
| Star Wars          | Fox         | Lachlan Murdoch | 1977 | Hollywood         |
| Star Wars          | Fox         | Lachlan Murdoch | 1983 | Hollywood         |
| Return of the Jedi | Fox         | Lachlan Murdoch | 1977 | Hollywood         |
| Return of the Jedi | Fox         | Lachlan Murdoch | 1983 | Hollywood         |

•  $\overline{S_1 \bowtie S_2 \bowtie S_3}$ 

| _ 1 2 0            |             |                 |      |                   |
|--------------------|-------------|-----------------|------|-------------------|
| Title              | Studio Name | President       | Year | President Address |
| Toy Story          | Pixar       | Steve Jobs      | 2000 | 123 ABC Street    |
| Star Wars          | Fox         | Lachlan Murdoch | 1977 | Hollywood         |
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| Return of the Jedi | Fox         | Lachlan Murdoch | 1977 | Hollywood         |
| Return of the Jedi | Fox         | Lachlan Murdoch | 1983 | Hollywood         |

#### Notes:

- Decomposition: The good bad and ugly
  - 1) Elimination of Anomalies by decomposition as in Section 3
  - 2) **Recoverability of Information** Can we recover the original relation from the tuples in its decomposition?
  - 3) Preservation of Dependences (lossless join): Can we be sure that after reconstructing the original relation from the decompositions, the original FD's satisfy?

**BCNF:**  $\rightarrow$  satisfies 1) and 2) Not good. NONO

- The Chase Test for Lossless Join
  - Tests whether the decomposition is lossless

### Input:

- A relation R

- A decomposition of R
- A set of functional dependencies

#### Output:

- Whether the decomposition is loseless or not
- $\Pi_{S_1}(R) \bowtie \Pi_{S_2}(R) \bowtie \cdots \prod_{S_i}(R) = R$

### Three things to remember:

- 1. The natural join is associate and commutative
- 2. Any tuple t in R is surely in  $\pi_{S_1}(R) \bowtie \pi_{S_2}(R) \bowtie \cdots \bowtie \pi_{S_k}(R)$ .
- 3. We have to check to see any tuple in the  $\pi_{S_1}(R) \bowtie \pi_{S_2}(R) \bowtie \cdots \bowtie \pi_{S_k}(R)$ .

#### Example:

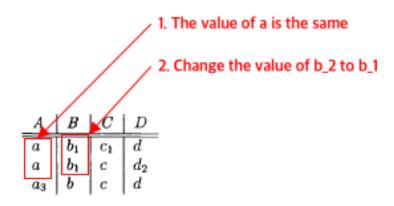
$$S_1 = \{A, D\}, S_2 = \{B, C\}, S_3 = \{A, C\}$$

$$A \to B, B \to C, CD \to A$$



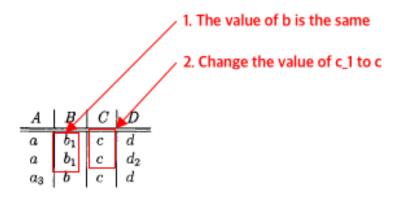
#### Step 1: $A \rightarrow B$

Set the value b with the same value of a to be the same. (e.g.  $b_2 \rightarrow b_1$ )



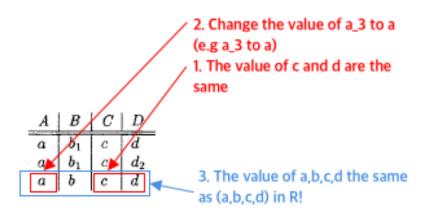
## Step 2: $B \rightarrow C$

Set the value c with the same value of b to be the same. (e.g.  $b_2 \rightarrow b_1$ )



Step 3:  $CD \rightarrow A$ 

Set the value a with the same value of c and d to be the same. (e.g.  $a_3 \rightarrow a$ )



So, we can conclude the join is lossless.

|    | Α     | В     | С | D     | E     |
|----|-------|-------|---|-------|-------|
| b) | a     | b     | c | $d_1$ | $e_1$ |
| D) | $a_1$ | b     | c | d     | $e_2$ |
|    | a     | $b_1$ | c | $d_2$ | e     |

Step 1  $(AC \rightarrow E)$ :

| A     | В     | С | D     | Е     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | e     |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_2$ | e     |

Step 2  $(BC \rightarrow D)$ :

| A     | В     | С | D     | E     |
|-------|-------|---|-------|-------|
| a     | b     | c | d     | e     |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_2$ | e     |

a, b, c, d, e exists. So by the Chast test, the decomposition of  $R(A, B, C, D, E) : AC \rightarrow E, BC \rightarrow D$  into  $\{A, B, C\}, \{B, C, D\}, \{A, C, E\}$  is lossless.

|    | Α     | В     | С | D     | Е     |
|----|-------|-------|---|-------|-------|
| c) | a     | b     | c | $d_1$ | $e_1$ |
| c) | $a_1$ | b     | c | d     | $e_2$ |
|    | a     | $b_1$ | c | $d_2$ | e     |

Step 1  $(A \rightarrow D)$ :

| A     | В     | С | D     | Е     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | $e_1$ |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_1$ | e     |

Step 2  $(D \rightarrow E)$ :

| A     | В     | С | D     | E     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | e     |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_1$ | e     |

Step 3  $(B \rightarrow D)$ :

| A     | В     | С | D | Е     |
|-------|-------|---|---|-------|
| a     | b     | c | d | e     |
| $a_1$ | b     | c | d | $e_2$ |
| a     | $b_1$ | c | d | e     |

a,b,c,d,e exists. So by the Chast test, the decomposition of  $R(A,B,C,D,E):A\to D,D\to E,B\to D$  into  $\{A,B,C\},\{B,C,D\},\{A,C,E\}$  is lossless.

|    | ,     |       | , |       |       |
|----|-------|-------|---|-------|-------|
|    | A     | В     | С | D     | Е     |
| d) | a     | b     | c | $d_1$ | $e_1$ |
| u) | $a_1$ | b     | c | d     | $e_2$ |
|    | a     | $b_1$ | c | $d_2$ | e     |

Step 1  $(A \rightarrow D)$ :

| A     | В     | С | D     | Е     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | $e_1$ |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_1$ | e     |

Step 2 ( $CD \rightarrow E$ ):

| A     | В     | С | D     | E     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | e     |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_1$ | e     |

Step 3  $(E \rightarrow D)$ :

| Α     | В     | С | D     | E     |
|-------|-------|---|-------|-------|
| a     | b     | c | $d_1$ | e     |
| $a_1$ | b     | c | d     | $e_2$ |
| a     | $b_1$ | c | $d_1$ | e     |

So in this case, the relation is not lossless.

An example of an instance of R that is not lossless is:

| Phone ID | Grade | Student Name | Phone #      | Physical Address |
|----------|-------|--------------|--------------|------------------|
| 1        | 89    | John Doe     | 111-222-3333 | 123 ABC Street   |
| 2        | 89    | John Doe     | 222-222-3333 | 123 ABC Street   |
| 1        | 62    | Josh Doe     | 111-222-3333 | 123 ABC Street   |
| 3        | 94    | Frank McKay  | 444-555-6666 | 234 ABC Street   |

$$\bullet \ S_1 = \{A, B, C\}$$

| Phone ID | Grade | Student Name |
|----------|-------|--------------|
| 1        | 89    | John Doe     |
| 2        | 89    | John Doe     |
| 1        | 62    | Josh Doe     |
| 3        | 94    | Frank McKay  |

$$\bullet \ S_2 = \{C, D, E\}$$

| Student Name | Phone #      | Physical Address |
|--------------|--------------|------------------|
| John Doe     | 111-222-3333 | 123 ABC Street   |
| John Doe     | 222-222-3333 | 123 ABC Street   |
| Josh Doe     | 111-222-3333 | 123 ABC Street   |
| Frank McKay  | 444-555-6666 | 234 ABC Street   |

$$\bullet \ S_3 = \{A, C, E\}$$

| Phone ID | Student Name | Physical Address |
|----------|--------------|------------------|
| 1        | John Doe     | 123 ABC Street   |
| 2        | John Doe     | 123 ABC Street   |
| 1        | Josh Doe     | 123 ABC Street   |
| 3        | Frank McKay  | 234 ABC Street   |

•  $S_1 \bowtie S_2$ 

| Phone ID | Grade | Student Name | Phone #      | Physical Address |
|----------|-------|--------------|--------------|------------------|
| 1        | 89    | John Doe     | 111-222-3333 | 123 ABC Street   |
| 2        | 89    | John Doe     | 111-222-3333 | 123 ABC Street   |
| 1        | 89    | John Doe     | 222-222-3333 | 123 ABC Street   |
| 2        | 89    | John Doe     | 222-222-3333 | 123 ABC Street   |
| 1        | 62    | Josh Doe     | 111-222-3333 | 123 ABC Street   |
| 3        | 94    | Frank McKay  | 444-555-6666 | 234 ABC Street   |

•  $S_1 \bowtie S_2 \bowtie S_3$ 

| 1 1 2 1 3 |       |              |              |                  |  |  |
|-----------|-------|--------------|--------------|------------------|--|--|
| Phone ID  | Grade | Student Name | Phone #      | Physical Address |  |  |
| 1         | 89    | John Doe     | 111-222-3333 | 123 ABC Street   |  |  |
| 2         | 89    | John Doe     | 111-222-3333 | 123 ABC Street   |  |  |
| 1         | 89    | John Doe     | 222-222-3333 | 123 ABC Street   |  |  |
| 2         | 89    | John Doe     | 222-222-3333 | 123 ABC Street   |  |  |
| 1         | 62    | Josh Doe     | 111-222-3333 | 123 ABC Street   |  |  |
| 3         | 94    | Frank McKay  | 444-555-6666 | 234 ABC Street   |  |  |

- 2. The sets of FDs in 1.b) and 1.c) are the ones where the dependencies are preserved from decomposition.
- 3. a) i) Find 3NF Violations
  - $\{A, B\}^+ = \{A, B\}$ 
    - Doesn't have C required for  $AB \to C$
    - $-\,$  Second and third don't imply first
  - $\{C\}^+ = \{C\}$ 
    - Doesn't have D required for  $C\to D$
    - First and third don't imply second
  - $\{D\}^+$ 
    - Doesn't have C required for  $AB \to C$
    - Second and third don't imply first

#### Notes:

- 3NF
  - Definition
    - \* A elation R is in 3NF if

For each nontrivial FD, the left side is a superkey (BCNF), or the right side consists of prime attributes only.

- Our expectation after decomposing are:
  - 1. Elimination of Anomalies
  - 2. Recoverability of Information (Recovering original relation after decomposition)

3. Preservation of Information (Recovering original tuples after decomposition)

Key: 3NF guarentees 2) and 3) but not 1)

- Synthesis algorithm for 3NF Schemas
  - 1. Check if the FD's are minimal
    - To verify, we should show that we cannot eliminate any of FD's. That is, using algorithm 3.7, no two of the FD's imply the third
  - 2. Find a minimal basis for F, say G
  - 3. For each functional dependency  $X \to A$  in G, use XA as the schema of one of the relations in the decomposition
  - 4. If none of the relation schemas from Step 3 is a superky for R, add another relation whose schema is a key for R. And drop redundant relations.

#### Example:

$$R(A, B, C, D, E) : AB \rightarrow C, C \rightarrow B, A \rightarrow D$$

- 1. Check if the FD's are minimal
  - To verify, we should show that we cannot eliminate any of FD's. That is, using algorithm 3.7, no two of the FD's imply the third
  - 1)  $\{A, B\}^+$

Using the FDs  $C \to B$ ,  $A \to D$ , we have  $\{A, B\}^+ = \{A, B, D\}$ .

Since C is required for  $AB \to C$ , we can conclude second and third doesn't imply the first

2)  $\{C\}^+$ 

Using the FDs  $AB \to C$ ,  $A \to D$ , we have  $\{C\}^+ = \{C\}$ .

Since B is required for  $C \to B$  but not in  $\{C\}^+ = \{C\}$ , we can conclude first and third doesn't imply the second

3)  $\{A\}^+$ 

Using the FDs  $AB \to C$ ,  $C \to D$ , we have  $\{A\}^+ = \{A\}$ .

Since D is required for  $C \to D$  but not in  $\{A\}^+ = \{A\}$ , we can conclude first and second doesn't imply the third

2. Find a minimal basis for F, say G

$$AB \to C$$
,  $C \to B$  and  $A \to D$ 

3. For each functional dependency  $X \to A$  in G, use XA as the schema of one of the relations in the decomposition

$$S_1(A, B, C), S_2(C, B), S_3(A, D)$$

4. If none of the relation schemas from Step 3 is a superky for R, add another relation whose schema is a key for R. And drop redundant relations.

Take all combinations of attributes A, B, C, D, E. We have  $\{A, B, C\}$  and  $\{A, B, E\}$  as keys.

Thus, adding one, the extra relation we have is  $S_4(A, B, E)$ .

And since B, C in  $S_2(B, C)$  is also in  $S_1(A, B, C)$ ,  $S_2$  needs to be dropped.

So, we have  $S_1(A, B, C)$ ,  $S_3(A, D)$ ,  $S_4(A, B, E)$ 

b)