

# Midterm 1 Version 3 Solution

March 19, 2020

## Question 1

- a. Since  $S_1 = \{ab, ba, aab, bba, baa, \dots\}$  and  $S_2 = \{aaa, aab, aba, baa, abb, bab, bba\}$ ,

$$S_2 \setminus S_1 = \{aaa, aab, aba, bab\}$$

### Correct Solution:

Since  $S_1 = \{ab, ba, aab, abb, bba, baa, \dots\}$  and  $S_2 = \{aaa, aab, aba, baa, abb, bab, bba, bbb\}$ ,  
 $S_2 \setminus S_1 = \{aaa, aba, bab, bbb\}$

- b. See table below

$p$	$q$	$r$	$\neg r$	$p \Rightarrow q$	$(p \Rightarrow q) \Leftrightarrow \neg r$
T	T	T	F	T	F
T	T	F	T	T	T
T	F	T	F	F	T
F	T	T	F	T	F
T	F	F	T	F	F
F	T	F	T	T	T
F	F	T	F	T	F
F	F	F	T	T	T

- c. Let  $x = \underline{\hspace{2cm}}$ , and  $y \in \mathbb{N}$ .

We will prove that  $P(x)$  is true and  $Q(x, y)$  or  $Q(x, y + 1)$  is false.

### Correct Solution:

Negation:  $\exists x \in \mathbb{N}, \forall y \in \mathbb{N}, P(x) \wedge (\neg Q(x, y) \wedge \neg Q(x, y + 1))$

Let  $x = \underline{\hspace{2cm}}$  and  $y \in \mathbb{N}$ .

We will prove that  $P(x)$  is true, and both  $Q(x, y)$  and  $Q(x, y + 1)$  are false.

## Question 2

a.  $\forall x \in T, \text{Canadian}(x) \wedge \text{Star}(x)$

b.  $\forall x \in T, \text{Canadian}(x) \Rightarrow \forall y \in T, \neg \text{Canadian}(y) \wedge \text{Defeated}(x, y)$

## Question 3

## Question 4