

Midterm 2 Version 1 Review

July 17, 2020

1. a) 1100100

b) $-\sum_{i=0}^{n-1} 3^i$

Notes:

- Balanced Ternary
 - is a way of representing numbers
 - balanced ternary is in base 3, and has values 1,0 or -1

$$\sum_{i=0}^{n-1} d_i \cdot 3^i \text{ where } d_i \in \{0, 1, -1\} \quad (1)$$

c) i. $f(n) \in \Omega(n)$

True (since $n^2 + 10n + 2 \geq cn$)

ii. $g(n) \in \Omega(n)$

False (Let $c = 100, n_0 = 100$. Then $100 \log_2 n < 100n$)

iii. $f(n) \in \mathcal{O}(g(n))$

False ($f(n) = n^2 + 10n + 2$ grows faster than $g(n) = 100 \log_2 n$)

Notes:

- $g \in \Omega(f) : \exists c, n_o \in \mathbb{R}^+, \forall n \in \mathbb{N}, n \geq n_o \Rightarrow g(n) \geq cf(n)$, where $f, g : \mathbb{N} \rightarrow \mathbb{R}^{\geq 0}$
- $g \in \mathcal{O}(f) : \exists c, n_o \in \mathbb{R}^+, \forall n \in \mathbb{N}, n \geq n_o \Rightarrow g(n) \leq cf(n)$, where $f, g : \mathbb{N} \rightarrow \mathbb{R}^{\geq 0}$