Worksheet 1 Solution

March 8, 2020

Question 1

- a) $A = \{2, 5\}$ $A^c = \{1, 3, 4, 6\}$
- b) $A^c = U \setminus A$
- c) $A^c \cap B^c = \{ x \mid x \in U, x \le 0 \text{ and } x \ge 4 \}$ $A^c \cap B^c = \{ x \mid x \in U, x < 1 \text{ and } x > 2 \}$ $(A \cap B)^c = \{ x \mid x \in U, x < 1 \text{ and } x > 2 \}$ $(A \cup B)^c = \{ x \mid x \in U, x \le 0 \text{ and } x \ge 4 \}$

Question 2

- a) $T_0 \to 0, 3, 6$
 - $T_1 \to 1, 4, 7$
 - $T_2 \rightarrow 2, 5, 8$
 - $T_3 \to 12, 18, 24$
- b) $\mathbb{Z}^+ = \{ T_0, T_1, T_2 \}$

 T_3 not included. A partition of a set must not have any common elements.

Question 3

- a) 000, 110, 001, 010, 011, 100, 101, 111
- b) $S_1 = \{aa, bb, cc, ab, ca, ba, ac, bc, cb\}$ $S_2 = \{a, b, c, aa, bb, cc, ab, ca, aaa, aba, aca, bab, bbb, bcb, cac, cbc, ccc...\}$ $S_1 \cap S_2 = \{aa, bb, cc\}$ $S_1 \setminus S_2 = \{ca, ba, ac, bc, cb\}$
- c) $(S_1 \cap S_2) = S_1 \setminus S_2$