Problem Set 1 Solution

March 14, 2020

Question 1

a. $\forall t \in T, Canadian(t) \Rightarrow \neg Stanley(t)$

b. $\forall t \in T,\ \exists d \in D,\ \neg Canadian(t) \wedge BelongsTo(t, d)$

c. $\forall t \in T,\ \exists d \in D,\ Stanley(t) \wedge BelongsTo(t, d)$

d. $\forall t \in T, \exists d \in D,\ BelongsTo(t, d) \Rightarrow \forall d' \in D, d' \neq d \wedge \neg BelongsTo(t, d')$

e. $\forall t_1 \in T, \exists d \in D, \exists t_2 \in T, t_1 \neq t_2 \wedge (BelongsTo(t_1, d) \wedge BelongsTo(t_2, d)) \Rightarrow \forall t_3 \in T, t_3 \neq t_1 \wedge t_3 \neq t_2 \wedge \neg BelongsTo(t_3, d)$

Question 2

a. $\forall x \in \mathbb{R}, f(-x) = f(x)$

$\forall x \in \mathbb{R}, -f(-x) = f(x)$

b. $\forall g, f : \mathbb{R} \to \mathbb{R},\ \exists h : \mathbb{R} \to \mathbb{R},\ Odd(f) \wedge Odd(g) \Rightarrow Odd(f) \times Odd(g) = Even(h)$

c. $f = 0$ is a solution, since $-f(-x) = -(-0) = 0 = f(x)$ and $f(-x) = -0 = 0 = f(x)$

d. $\forall f : \mathbb{R} \to \mathbb{R}, \exists g, h : \mathbb{R} \to \mathbb{R}, Odd(g) \wedge Even(h) \Rightarrow f = Odd(g) + Even(h)$

Question 3

Question 4