

CSC 209 Review 9 Solution

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1. a) 0

Notes

- a) is 0 because $(i \gg 1 + j \gg 1 = i \gg 10 \gg 1 = 0)$
- **Bitwise Shift Operators**
 - has lower precedence than arithmetic operators

Example:

$i \ll 2 + 1$ means $i \ll (2+1)$ and not $(i \ll 2) + 1$

- \ll : Left Shift
- \gg : Right Shift
- *Tip*: Always shift only on unsigned numbers for portability

Example

```
unsigned short i, j;

i = 13;          /* i is now 13 (binary 0000000000001101) */
j = i << 2;       /* j is now 52 (binary 0000000000110100) */
j = i >> 2;       /* j is now 3  (binary 0000000000000011) */
```

As these examples show, neither operator modifies its operands. To modify a variable by shifting its bits, we'd use the compound assignment operators $\ll=$ and $\gg=$:

```
i = 13;          /* i is now 13 (binary 0000000000001101) */
i <<= 2;         /* i is now 52 (binary 0000000000110100) */
i >>= 2;         /* i is now 13 (binary 0000000000001101) */
```

Shifts to left

Shifts to right

- $\gg=$ / $\ll=$: Are bitwise shift equivalent of $+=$

b) 0

Notes

- `i` is 1111111111111111
- `i` is 0000000000000000
- so `i & i = 0`
- `~`: Bitwise complement (NOT)

| a | $\sim a$ |
|---|----------|
| 0 | 1 |
| 1 | 0 |

Example:

```

1      0   1   1   1   //<- this is 7
2      -----
3      1   0   0   0   //<- this is 8
4
5      so, ~ 7 = 8

```

- `&`: Bitwise *and*

| a | b | a & b |
|---|---|-------|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

Example:

```

1      0   1   1   1   //<- this is 7
2      0   1   0   0   //<- this is 4
3      -----
4      0   1   0   0   //<- this is 4
5
6      so, 7 & 4 = 4

```

- `^`: Bitwise *exclusive or*
- `|`: Bitwise *inclusive or*

c) 1

Notes

- `i` is 1111111111111110
- `j` is 0000000000000000
- `i & j` is 0000000000000000 or 1
- `i & j ^ k` is 1

- \wedge : Bitwise XOR

| a | b | $a \wedge b$ |
|---|---|--------------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

Example:

```

1      0   1   1   1   //<- this is 7
2      0   1   0   0   //<- this is 4
3      -----
4      0   0   1   1   //<- this is 3
5
6      so,  $7 \wedge 4 = 3$ 
7

```

d) 0

Example

- i is 0000000000000111
- j is 0000000000001000
- $i \wedge j$ is 0000000000000000 or 0
- k is 0000000000001001
- $i \wedge j \& k$ is 0000000000000000 or 0

Correct Solution

15

Notes

- There is a precedence to the order of operations

| | |
|----------|----------|
| Highest: | \sim |
| | $\&$ |
| | \wedge |
| Lowest: | $ $ |

- e) • toggling from 0 to 1

```
i = 0x0000;
i |= 0x0001;
```

or

```
i |= 1 << 0; where i = 0x0000;
```

- toggling from 1 to 0

```
i = 0x0001;
i &= ~0x0001;
```

or

```
i &= ~(1 << 0); where i = 0x0001;
```

Correct Solution

- toggling from 0 to 1 of 4th bit

```
i = 0x0010;
i ^= 0x0000;
```

or

```
i ^= 1 << 4; where i = 0x0000;
```

- toggling from 1 to 0 of 4th bit

```
i = 0x0010;
i ^= 0x0010;
```

or

```
i ^= (1 << 4); where i = 0x0010;
```

Notes

- Toggling can be done using bitwise XOR
- **Setting a bit**
 - Is done using `|` or bitwise OR

```
i = 0x0000;          /* i is now 0000000000000000 */
i |= 0x0010;          /* i is now 0000000000010000 */
```

- The idiom of above is `i |= 1 << j`

- **Clearing a bit**

- Is done using `|` or bitwise AND

```
i = 0x00ff;          /* i is now 0000000011111111 */
i &= ~0x0010;        /* i is now 0000000011101111 */
```

- The idiom of above is `i &= ~(i << j)`

2. It swaps the elements between x and y.

Notes

- Preprocessor performs operations of statements in order from left to right

```

1           2           3
#define M(x,y) ((x)^(y) , (y)^(x) , (x)^(y) )

```

New value of x → New value of y, using x from 1 → New value of x, using y from 2, x from 1

3. `#define MK_COLOR(r,g,b) (long) ((b | (g << 8)) | (b | (r << 16)))`

Rough Work

1. store b in bit 0

b

2. store g in bit 8

b | g << 8

3. store r in bit 16

b | r << 16

Correct Solution

```
#define MK_COLOR(r,g,b) (long) ((r | (g << 8)) | (r | (b << 16)))
```

Notes

- First Byte is furthest from 0x and first byte is closest to 0x



4. • GET_RED

```
#define GET_RED(c) (long) (c & 0x007)
```

- GET_GREEN

```
#define GET_GREEN(c) (long) ((c >> 8) & 0x007)
```

- GET_BLUE

```
#define GET_BLUE(c) (long) ((c >> 16) & 0x007)
```

Notes

- 0x0007 in binary is 0x00000000000001111
- `c >> 4` shifts `c` to right by 4 bits and return overlapping value between `c >> 4` and `0x00000000000001111` (0x007)
- Test code is below

```
1  #include <stdio.h>
2  #include <stdlib.h>
3
4  #define MK_COLOR(r,g,b) (long) ( (r | (g << 8)) | (r | (b << 16)) )
5  #define GET_RED(c) (long) (c & 0x007)
6  #define GET_GREEN(c) (long) ((c >> 8) & 0x007)
7  #define GET_BLUE(c) (long) ((c >> 16) & 0x007)
8
9  int main() {
10     long i, r = 4, g = 5, b = 6, r2, g2, b2;
11
12     i = MK_COLOR(r,g,b);
```

```
13
14     r2 = GET_RED(i);
15     g2 = GET_GREEN(i);
16     b2 = GET_BLUE(i);
17
18     printf("%ld\n", i);
19     printf("%ld\n", r2);
20     printf("%ld\n", g2);
21     printf("%ld\n", b2);
22
23     return 0;
24 }
```

5. a)

```
    unsigned short swap_bytes(unsigned short i) {
2         unsigned short j, k;
3
4         j = i & 0x007; // extract first byte
5
6         i = i >> 4;
7         k = i & 0x007; // extract second byte
8
9         i = i >> 4; // shift down later two bytes
10
11        i |= j << 8; // add first byte to position of fourth byte
12        i |= k << 12; // add second byte to position of third byte
13
14    }
```

b)

```
    unsigned short swap_bytes(unsigned short i) {
2
3        i = i >> 8 | i << 8;
4
5        return i;
6    }
```

Rough Works

1. Extract first two bytes

```
j = i & 0x0007
i = i >> 4
k = i & 0x0007
```

2. Shift later two bytes down

```
i = i >> 4
```

3. Add first two bytes to last two bytes

```
i |= j << 8;
i |= k << 12;
```

```
6.1 unsigned int rotate_left(unsigned int i, int n) {
2     return i >> 28 | i << n;
3 }
4
5 unsigned int rotate_right(unsigned int i, int n) {
6     return i << 28 | i >> n;
7 }
```

7. a) Is a binary with n many 1s from the first bit

b) Extracts last n bits in i

Correct Solution

a) Is a binary with n many 1s from the first bit

b) Extracts last n bits **starting from position m** in i

```
8. a) unsigned int count_ones(unsigned char *ch)
2     {
3         unsigned char *p;
4         unsigned int count;
5
6         for (p = ch; *p != '\0'; p++){
7             if (*p == '1') {
8                 count++;
9             }
10        }
11
12        return count;
13    }
```

```
b) unsigned int count_ones(unsigned char ch)
2     {
3         int sum = 0;
4
5         sum += (i >> 0) & 1;
6         sum += (i >> 1) & 1;
7         sum += (i >> 2) & 1;
8         sum += (i >> 3) & 1;
9         sum += (i >> 4) & 1;
10        sum += (i >> 5) & 1;
11        sum += (i >> 6) & 1;
```



```

12     sum += (i >> 7) & 1;
13     return count;
14 }

```

Notes

- Unsigned char goes from 0 (00000000) to 255 (11111111)
- I am having trouble how to convert from loop to without loop :'. I need help
- Example

100010101 - Here there are 4 1s.

```

91 unsigned int reverse_bits (unsigned int n)
92 {
93     int m = 15, p = 0;
94     unsigned int byte_left_end, byte_right_end, res = 0;
95
96     while (m > p) {
97         byte_left_end = n >> m & 1;
98         byte_right_end = n >> p & 1;
99
100        res |= byte_left_end << (15 - m) | byte_right_end << (15 - p
101    );
102
103        m--;
104        p++;
105    }
106    return res;
107 }

```

Rough Work

- Start at $n = 15, m = 0$
- Swap bit at n with m
- Repeat until $m > n$

Notes

- unsigned int has 4 bytes or (0x0000) or (0000000000000000, 16 bits)

10. The precedence of $\&$, \wedge , and $_$ is lower than the precedence of the relational and equality operators.

As a result, the expression will first evaluate

`(SHIFT_BIT | CTRL_BIT | ALT_BIT) == 0`

first.

The work around is to put parenthesis around `key_code & (SHIFT_BIT | CTRL_BIT | ALT_BIT)`.

11. The function tries to insert `low_byte` to `high_byte` after shifting `high_byte` by 8 bits to left.

It doesn't work because `+` sign takes precedence over `<<`.

To fix this issue, a parenthesis is required around `high_byte << 8`.

12. It reduces the value of `n` by 1, then uses bitwise operator (`&`) to tract4