#### Worksheet 5 Review

#### March 22, 2020

#### Question 1

• Predicate Logic:  $\forall x, y \in \mathbb{Z}, Odd(x) \land Odd(y) \Rightarrow Odd(xy)$ 

Let  $x, y \in \mathbb{Z}$ . Assume Odd(x) and Odd(y).

Then,  $\exists k, m \in \mathbb{Z}$ ,

$$x = 2k - 1 \tag{1}$$

$$y = 2m - 1 \tag{2}$$

Then,

$$xy = (2k - 1)(2m - 1) \tag{3}$$

$$xy = (4km - 2k - 2m + 2) - 1 (4)$$

$$xy = 2(2km - k - m + 1) - 1 (5)$$

$$xy = 2o - 1 \tag{6}$$

by setting o = 2km - k - m + 1.

Since,  $o \in \mathbb{Z}$ , it follows from the definition of odd that the statement  $\forall x, y \in \mathbb{Z}, Odd(x) \wedge Odd(y) \Rightarrow Odd(xy)$  is true.

## Question 2

- a.  $\forall n, m \in \mathbb{Z}, \ Even(n) \wedge Odd(m) \Rightarrow m^2 n^2 = m + n$
- b. The flaw is that the value k in n=2k and m=2k+1 cannot be the same.

## Question 3

# Question 4