CSC373 Worksheet 6

August 12, 2020

1. CLRS 29.1-4: Convert the following linear program into standard form

Minimize

$$2x_1 + 7x_2 + x_3$$

Subject to

$$x_1 - x_3 = 7$$
$$3x_1 + x_2 \ge 7$$
$$x_2 \ge 0$$
$$x_3 \le 0$$

2. CLRS 29.1-5: Convert the following linear program into slack form:

Maximize

$$2x_1 - 6x_3$$

Subject to

$$x_1 + x_2 - x_3 \le 7$$
$$3x_1 - x_2 \ge 7$$
$$-x_1 + 2x_2 + 2x_3 \ge 0$$
$$x_1, x_2, x_3 \ge 0$$

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3. **CLRS 29.1-6:** Show the following linear program is infeasible:

Maximize

$$3x_1 - 2x_2$$

Subject to

$$x_1 + x_2 \le 2$$

$$-2x_1 - 2x_2 \le -10$$

$$x_1, x_2 \ge 0$$

4. CLRS 29.1-7: Show that the following linear program is unbounded:

Maximize

$$x_1 - x_2$$

Subject to

$$-2x_1 + x_2 \le -1$$

$$-x_1 - 2x_2 \le -2$$

$$x_1, x_2 \ge 0$$

- 5. **CLRS 29.1-8:** Suppose that we have a general linear program with n variables and m constraints, and suppose that we convert it into standard form. Give an upper bound on the number of variables and constraints in the resulting linear program.
- 6. **CLRS 29.1-9:** Give an example of a linear program for which the feasible region is not bounded, but the optimal objective value is finite.
- 7. CLRS 29.2-3: In the single-source shortest-paths problem, we want to find the shortest-path weights from a source vertex s to all vertices $v \in V$. Given a graph G, write a linear program for which the solution has the property that d_v is the shortest-path weight from s to v for each vertex $v \in V$.