

Time Unit Hierarchical Model with Stan

Prophet model

```
model {  
  //priors  
  k ~ normal(0, 5);  
  m ~ normal(0, 5);  
  delta ~ double_exponential(0, tau);  
  
  beta ~ normal(0, sigmas);  
  sigma_obs ~ normal(0, 0.5);  
  
  // likelihood  
  y ~ normal(  
    linear_trend(k, m, delta, t, A, t_change)  
    + X * (beta),  
    sigma_obs);  
}
```

TUH model

```
model{  
  //hyperprior  
  k_mu ~ normal  
  k_sigma ~ Inv-gamma  
  m_mu ~ normal  
  m_sigma ~ Inv-gamma  
  tau ~ normal  
  for (k in 1:K){ sigmas[k] ~ Inv-gamma }  
  
  //priors  
  for (c in 1:C){  
    k[c] ~ normal(k_mu, k_sigma);  
    m[c] ~ normal(m_mu, m_sigma);  
    delta[c] ~ double_exp(0,tau)  
    for (k in 1:K){ beta[c,k] ~ normal(0, sigmas[k]) }  
  }  
  sigma_obs ~ normal(0, 0.5)  
  
  //likelihood  
  for(t in 1:T){  
    y[t] ~ normal(  
      linear_trend( k[TUC[t]], m[TUC[t]], delta[TUC[t]], t, A, t_chg)  
      + X * (beta[TUC[t]]),  
      sigma_obs)  
  }  
}
```