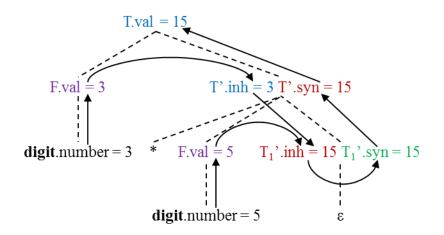
Syntax-Directed Translation



4190.409 Compilers, Spring 2016

- Idea: attach attributes and rules to productions of a context-free grammar
 - attributes are associated to grammar symbols and either synthesized or inherited.
 - rules are associated to productions.
 - example: infix-to-postfix translator

Produc	rtion		Semantic Rule
L	\rightarrow	E.	L.code = E.code
E	\rightarrow	$E_1 + T$	$E.code = E_{I}.code / T.code '+'$
E	\rightarrow	T	E.code = T.code
T	\rightarrow	$T_1 * F$	$T.code = T_1.code $
T	\rightarrow	F	T.code = F.code
F	\rightarrow	(E)	F.code = E.code
F	\rightarrow	digit	$F.code = \mathbf{digit}.number$

- Notation: Embedding semantic actions within production bodies
 - semantic actions are enclosed by curly braces
 - position of the semantic action in the production body determines the order in which the action is executed

Production

Semantic Rule

 $E_1 + T$ $E.code = E_1.code || T.code || '+'$

Syntax-Directed Translation Scheme

 \boldsymbol{E}

 \boldsymbol{E}

 \rightarrow $E_1 + T \{ print '+' \}$

 \boldsymbol{E}

 \rightarrow $E_1 + \{ \text{ print '+'} \} T$

 \boldsymbol{E}

{ print '+' } $E_1 + T$

Example: expression evaluation using SDD

Syntax-Directed Translation Scheme

Example: AST generation using SDD

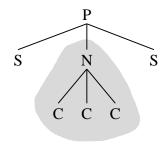
Syntax-Directed Translation Scheme

Syntax-Directed Definitions

- Why are SDDs useful?
 - on-the-fly code generation
 - rules are sequences of code
 - attributes designate memory addresses, registers
 - syntax tree generation
 - construct new class instances as a side-effect of executing a procedure in a recursive-descent parser. Return the node to the caller.

Synthesized vs. Inherited Attributes

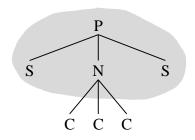
A synthesized attribute is defined only in terms of the attributes of the node itself and its children.



- may be defined in terms of inherited attributes
- terminal symbols can only have synthesized attributes
- attribute is attached to the head of the production or a terminal
- a grammar that has only synthesized attributes is called an S-attributed grammar

Synthesized vs. Inherited Attributes

An inherited attribute is defined only in terms of the attributes of the node itself, its siblings and its parent.



- inherited attributes may not be defined in terms of synthesized attributes
- attribute is attached to a non-terminal in the body of a production

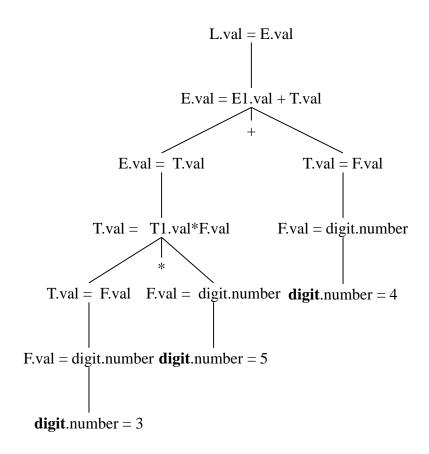
Evaluating SDDs w/ Annotated Parse Trees

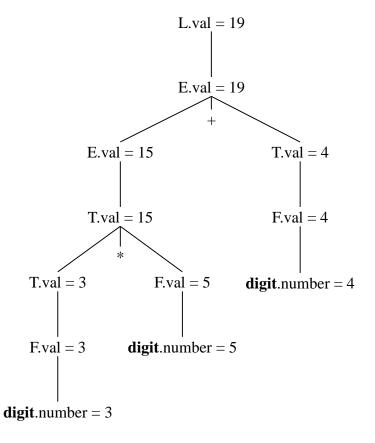
- An annotated parse tree is a visualization of syntax-directed definitions in the parse tree
 - attach attributes to nodes

- Problems to solve:
 - construction of the parse tree?
 - easy, just attach the attributes/rules to the node
 - evaluation of the attributes (order)?
 - synthesized: bottom-up
 - synthesized + inherited: use dependency graphs

Annotated Parse Tree w/ Synthesized Attributes

- Annotated parse tree for "3 * 5 + 4." with the SDD from slide 4
 - only synthesized attributes → bottom-up evaluation





Annotated Parse Tree w/ Inherited Attributes

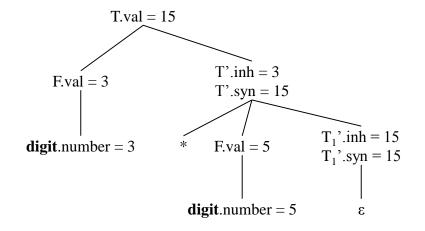
- Inherited attributes are useful when the structure of the grammar and the structure of the parse tree do not match
 - Elimination of left-recursion often leads to inherited attributes in SDDs:

Product	ion		Semantic Rule
T	\rightarrow	FT'	T'.inh = F.val $T.val = T'.syn$
T	\rightarrow	* FT_1 '	T_1 '.inh = T'.inh * F.val T'.syn = T_1 '.syn
T	\rightarrow	arepsilon	T'. $syn = T$ '. inh
F	\rightarrow	digit	$F.val = \mathbf{digit}.number$

Annotated Parse Tree w/ Inherited Attributes

Annotated parse tree for "3 * 5".

Produ	ction		Semantic Rule
T	\rightarrow	FT'	T'.inh = F.val T.val = T'.syn
T'	\rightarrow	$*FT_1'$	T_I '.inh = T'.inh * F.val T'.syn = T_I '.syn
T	\rightarrow	ε	T'.syn = T'.inh
F	\rightarrow	digit	$F.val = \mathbf{digit}.number$



Evaluation Order for SDDs

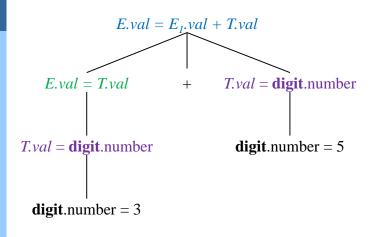
- Problem: in which order should we evaluate the attributes?
- Idea: use a dependency graph
 - dependency graph defines a topological order
 - follow the order to evaluate the attributes

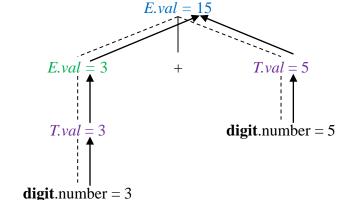
Dependency Graphs

- A dependency graph depicts the flow of information among the attribute instances in a particular parse tree
 - the dependency graph has a node for each attribute associated with X for every node labeled by grammar symbol X in the parse tree
 - for each synthesized attribute A.b defined in terms of the value of X.c, the dependency graph has an edge from X.c to A.b (note that the node representing X is a child of the node representing A)
 - for each inherited attribute B.c defined in terms of the value of X.a, the dependency graph has an edge from X.a to B.c (note that the node representing X can be a parent or a sibling of the node representing B)

Evaluation Order of Annotated Parse Trees

SDD with synthesized attributes for "3 * 5"





Production

$$E \longrightarrow E_1 + T$$

$$\Xi \rightarrow \Sigma$$

$$T \rightarrow digit$$

Semantic Rule

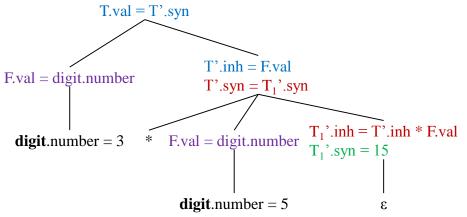
$$E.val = E_1.val + T.val$$

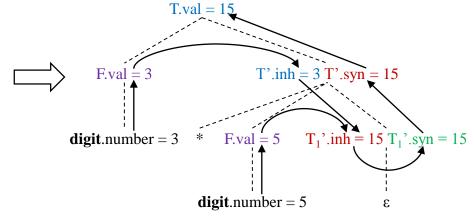
$$E.val = T.val$$

$$T.val = \mathbf{digit}.number$$

Evaluation Order of Annotated Parse Trees

SDD with inherited attributes for "3 * 5"





Production			Semantic Rule
T	\rightarrow	FT'	T'.inh = F.val T.val = T'.syn
T'	\rightarrow	$*FT_1'$	T_1 '.inh = T'.inh * F.val T'.syn = T_1 '.syn
T	\rightarrow	ε	T'.syn = T'.inh
F	\rightarrow	digit	$F.val = \mathbf{digit}.number$

Evaluation Order of Dependency Graphs

Evaluation order

- if the dependency graph has an edge from node M to N, then the attribute corresponding to M must be evaluated before N
- that is, the only valid order of evaluations are sequences N₁, N₂, ..., N_k such that if there is an edge in the dependency graph from N_i to N_j, then i < j (topological sort)
- if there is a cycle, there is exists no topological sort (and the graph cannot be evaluated); if there are no cycles, at least one topological sort exists.
- in general, it is hard to tell whether there exist any parse trees whose dependency graph have cycles.

S-Attributed Definitions

- S-attributed definitions describes the class of SDDs that only have synthesized attributes
 - there always exists a topological order
 - evaluate by postorder graph traversal (bottom up)

```
postorder(Node n)
{
  for (each child c of n, from the left) postorder(c);
  evaluate attributes of n;
}
```

this order corresponds exactly to the order in which an LR parser reduces a production to its head

L-Attributed Definitions

- L-attributed Definitions
 - class of SDDs with synthesized and inherited attributes, but dependency edges only go from "left-to-right"
 Each attribute must be either
 - synthesized or
 - inherited but with the following restrictions: for production A → X₁X₂...X_n and inherited attribute X_i.a computed by a rule associated with this production, the rule may use only
 - inherited attributes associated with the head A
 - inherited or synthesized attributes associated with the occurrences of symbols $X_1, X_2, ..., X_{i-1}$ located to the left of X_i .
 - inherited or synthesized attributes associated with the occurrence of X_i itself but only so that there are no cycles formed by the attributes of X_i
 - i.e., L-attributed definitions have no cycles and can thus always be evaluated
 - a top-down parser for a grammar with eliminated left-recursion leads to an Lattributed SDD

L-Attributed Definitions

Example

Production

$$T \rightarrow$$

$$\rightarrow$$
 FT'

$$*FT_1$$

Semantic Rule

$$T'.inh = F.val$$

$$T_I$$
'.inh = T'.inh * F.val

Production

$$\boldsymbol{A}$$

$$\rightarrow$$

BC

Semantic Rule

$$A.syn = B.b$$

$$B.inh = f(C.c, A.syn)$$

Rules with Controlled Side Effects

- Attribute grammars
 - no side effects
 - allow any evaluation order consistent with the dependency graph
- In practice, we need side effects → control side effects in SDDs
 - permit incidental side effects that do not constrain attribute evaluation i.e., permit side effects when attribute evaluation based on any topological sort of the dependency graph produces a correct translation

Production	on	Semantic Rule	
L	\rightarrow	E.	print (E.val)

- constrain the allowable evaluation orders so that the same translation is produced for any allowable order
 - implemented by adding implicit edges to the dependency graph

Rules with Controlled Side Effects

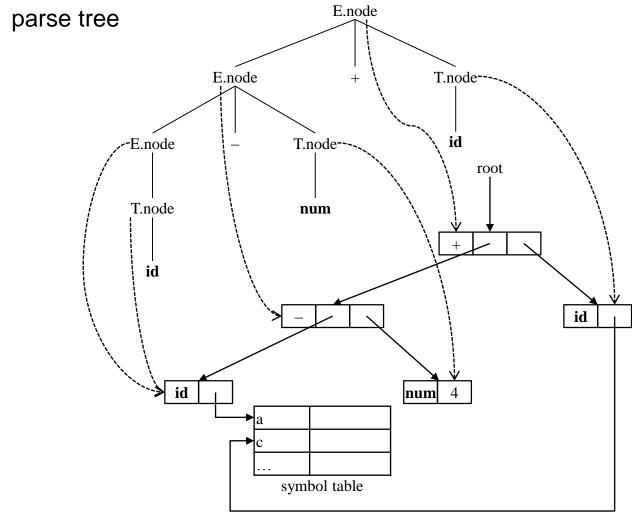
Example: variable declarations

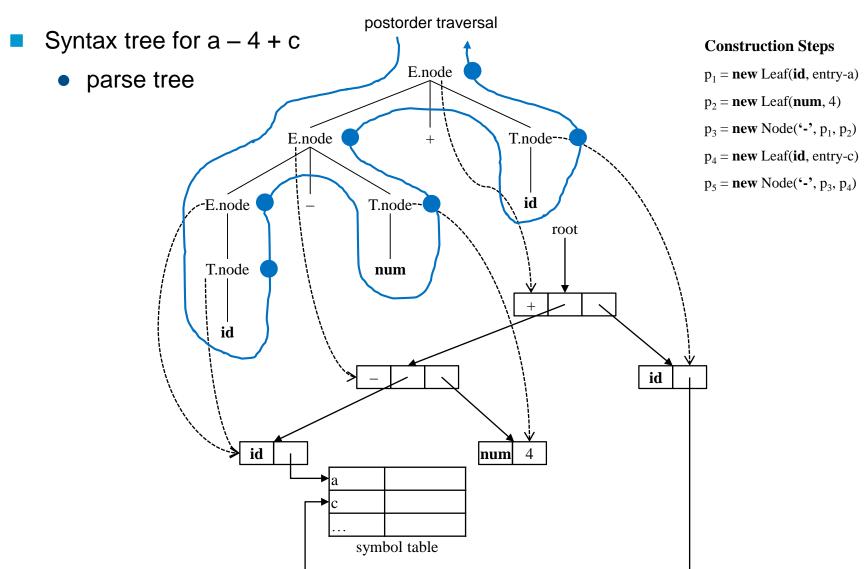
Produc	tion	Semantic Rule	
D	\rightarrow	TL	L.inh = T.type
T	\rightarrow	int	T.type = integer
T	\rightarrow	float	T.type = float
L	\rightarrow	L_{l} , id	$L_1.inh = L.inh$ addType(id .entry, L.inh)
L	\rightarrow	id	addType(id .entry, L.inh)

- During a bottom-up parse or a postorder traversal of the parse tree
 - S-attributed definition
 - actions comprise creating objects for nodes in the syntax tree

Prod	uction		Semantic Rule
\boldsymbol{E}	\rightarrow	$E_I + T$	$E.node = \text{new Node}('+', E_1.node, T.node)$
E	\rightarrow	$E_I - T$	$E.node = \text{new Node}(`-`, E_1.node, T.node)$
E	\rightarrow	T	E.node = T.node
T	\rightarrow	(E)	T.node = E.node
T	\rightarrow	id	<i>T.node</i> = new Leaf(id , id .entry)
T	\rightarrow	num	T.node = new Leaf(num , num .val)

■ Syntax tree for a – 4 + c

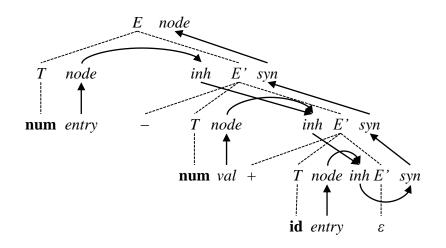


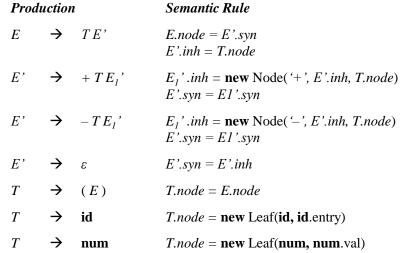


L-attributed definition for a top-down parser

Production			Semantic Rule
E	\rightarrow	TE'	E.node = E'.syn E'.inh = T.node
E	\rightarrow	$+ TE_{I}$ '	E_1 '.inh = new Node('+', E'.inh, T.node) E'.syn = E1'.syn
E	\rightarrow	$-TE_{I}$ '	E_1 '.inh = new Node('-', E'.inh, T.node) E'.syn = E1'.syn
E'	\rightarrow	ε	E'.syn = E'.inh
T	\rightarrow	(E)	T.node = E.node
T	\rightarrow	id	T.node = new Leaf(id , id .entry)
T	\rightarrow	num	<i>T.node</i> = new Leaf(num , num .val)

- Syntax tree for a 4 + c
 - parse tree and dependency graph





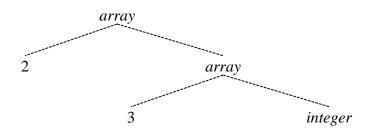
The Structure of a Type

Inherited attributes are useful when the structure of the parse tree differs from the abstract syntax of the input

In C

actually means

"array of 2 arrays of 3 integers", or array(2, array(3, integer))



The Structure of a Type

Inherited attributes are useful when the structure of the parse tree differs from the abstract syntax of the input

In C

actually means

"array of 2 arrays of 3 integers", or array(2, array(3, integer))

Prod	uction	<u>;</u>	Semantic Rule
T	\rightarrow	ВС	T.t = C.t $C.b = B.t$
B	\rightarrow	int	B.t = integer
B	\rightarrow	float	B.t = float
C	\rightarrow	[num] <i>C</i> ₁	$C.t = array(\mathbf{num}.val, C_1.t)$ $C_1.b = C.b$
C	\rightarrow	arepsilon	C.t = C.b

The Structure of a Type

C array types

int [2][3]

Production Semantic Rule BCT.t = C.tC.b = B.t \boldsymbol{R} B.t = integerint В float B.t = float \boldsymbol{C} [num] C_1 $C.t = array(\mathbf{num}.val, C_l.t)$ $C_1.b = C.b$ C \rightarrow C.t = C.b

C.b = integer C.t = array(2, array(3, integer)) C.b = integer C.t = array(2, array(3, integer)) C.b = integer C.t = array(3, integer) C.b = integer C.t = integer C.t = integer

Syntax-Directed Translation (SDT) Schemes

- Complementary notation to syntax-directed definitions
 - used to implement SDDs
- Semantic actions (program fragments) are embedded in the bodies of the production rules
- Execution (implementation) of an SDT:
 - build parse tree
 - perform actions left-to-right, depth-first (preorder traversal)

- Simplest method when the grammar can be parsed bottom-up and the SDD is Sattributed
 - semantic actions placed at the right end of the production body
 - actions are executed along with the reduction (i.e., when the body is reduced to the head)
 - results in a postorder traversal

Calculator Example

Postfix Syntax-Directed Translation Scheme

L	\rightarrow	E .	{ print(E.val); }
E	\rightarrow	$E_I + T$	{ $E.val = E_I.val + T.val$; }
E	\rightarrow	T	$\{E.val = T.val;\}$
T	\rightarrow	$T_I * F$	$\{T.val = T_I.val * F.val; \}$
T	\rightarrow	F	$\{ T.val = F.val; \}$
F	\rightarrow	(E)	$\{F.val = E.val; \}$
F	\rightarrow	digit	{ F.val = digit.number; }

- Parser-Stack Implementation
 - place attributes on stack along with handles
 - execute actions when reductions occur

	X	Y	Z	state/grammar symbol
	X.x	Y.y	Z.z	synthesized attribute(s)
			to	

Parser-Stack Implementation of the Calculator

Production			Action
L	\rightarrow	E .	{ print(stack[top-1]); top = top-1; }
E	\rightarrow	$E_I + T$	{ stack[top-2].val = stack[top-2].val + stack[top-1].val; top = top-2; }
\boldsymbol{E}	\rightarrow	T	
T	\rightarrow	$T_I * F$	{ stack[top-2].val = stack[top-2].val * stack[top-1].val; top = top-2; }
T	\rightarrow	F	
F	\rightarrow	(E)	{ $stack[top-2].val = stack[top-1].val$; $top = top-2$; }
F	\rightarrow	digit	

SDT's With Actions Inside Productions

Conceptually, an action within the body of a production is executed as soon as all symbols to its left have been processed.

$$B \rightarrow X \{ a \} Y$$

- Postfix and L-attributed SDT's can be implemented during a bottom-up and topdown parse, respectively.
- If the SDT is neither postfix nor L-attributed, it can be implemented as follows:
 - parse input and build a parse tree (ignoring all actions)
 - 2. for each (inner) node N add actions of node N as children in the order of appearance in the SDT
 - 3. during a preorder traversal, perform the actions of all actions nodes

■ Example: infix → prefix form translator

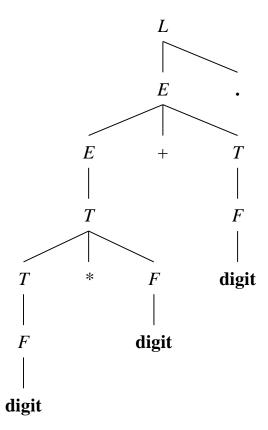
Postfix Syntax-Directed Translation Scheme

```
\begin{array}{cccc} L & \rightarrow & E. \\ E & \rightarrow & \{ \operatorname{print}(`+'); \} E_I + T \\ E & \rightarrow & T \\ T & \rightarrow & \{ \operatorname{print}(`*'); \} T_I * F \\ T & \rightarrow & F \\ F & \rightarrow & (E) \\ F & \rightarrow & \operatorname{digit} \{ \operatorname{print}(\operatorname{digit.lexval}); \} \end{array}
```

■ Example: infix → prefix form translator

$$3*5+4$$

parse tree



Postfix Syntax-Directed Translation Scheme

 $L \rightarrow E.$ $E \rightarrow \{ print('+'); \} E_I + T$ $E \rightarrow T$ $T \rightarrow \{ print('*'); \} T_I * F$ $T \rightarrow F$ $F \rightarrow (E)$

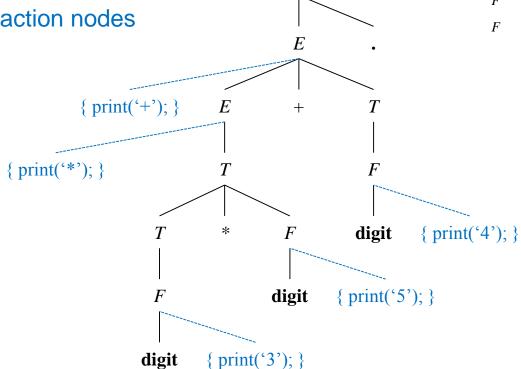
 $F \rightarrow \mathbf{digit} \{ \mathbf{print}(\mathbf{digit}.\mathbf{lexval}); \}$

Example: infix → prefix form translator

$$3 * 5 + 4$$

L

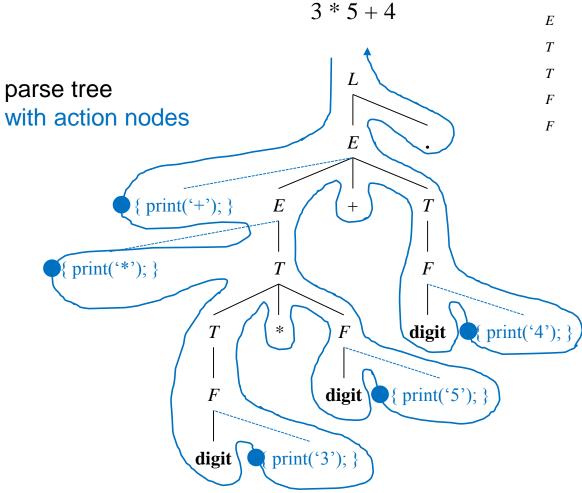
parse tree with action nodes



Postfix Syntax-Directed Translation Scheme

 $L \longrightarrow E.$ $E \longrightarrow \{ print('+'); \} E_I + T$ $E \longrightarrow T$ $T \longrightarrow \{ print('*'); \} T_I * F$ $T \longrightarrow F$ $F \longrightarrow (E)$ $F \longrightarrow \mathbf{digit} \{ print(\mathbf{digit}.lexval); \}$

Example: infix → prefix form translator



Postfix Syntax-Directed Translation Scheme

$$E \rightarrow E$$
.

$$E \qquad \Rightarrow \qquad \{ \text{ print('+'); } \} E_1 + T$$

$$E \rightarrow T$$

$$T \rightarrow \{ print(`*'); \} T_1 * F$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow \mathbf{digit} \{ print(\mathbf{digit}.lexval); \}$$

Executing actions during parsing

We have seen that an action within the body of a production must be executed as soon as all symbols to its left have been processed

$$B \rightarrow X \{ a \} Y$$

Therefore, during a

- bottom-up parse: perform action a as soon as X appears on top of the parsing stack
- top-down parse: perform action a immediately before expanding Y

Not all SDT's can be implemented during parsing

Consider again

Postfix Syntax-Directed Translation Scheme

```
\begin{array}{ccccc} L & \rightarrow & & E. \\ E & \rightarrow & & \{ \ print(\ '+\ '); \ \} \ E_I + T \\ E & \rightarrow & T \\ T & \rightarrow & \{ \ print(\ '*\ '); \ \} \ T_I * F \\ T & \rightarrow & F \\ F & \rightarrow & (E) \\ F & \rightarrow & \textbf{digit} \ \{ \ print(\textbf{digit}.lexval); \ \} \end{array}
```

the parser would have to perform the actions { print('+'); } / { print('*'); } before it knows which production will be applied

Which SDT's cannot be implemented during parsing?

Replace actions with marker nonterminals M_i and check for conflicts

Postfix Syntax-Directed Translation Scheme

L	\rightarrow	E .
E	\rightarrow	$M_1 E_1 + T$
E	\rightarrow	T
T	\rightarrow	$M_2 T_1 * F$
T	\rightarrow	F
F	\rightarrow	(E)
F	\rightarrow	$\mathbf{digit}M_{\mathfrak{Z}}$
M_{I}	\rightarrow	arepsilon
M_2	\rightarrow	${\cal E}$
M_3	\rightarrow	arepsilon

- bottom-up parser: conflicts on reductions $M_1 \to \varepsilon$, $M_2 \to \varepsilon$, and shifting the digit
- top-down parser: grammar is left recursive

Eliminating Left-Recursion from SDT's

- What happens to the actions when eliminating left-recursion from a SDT?
- Simple case when only the order of actions must be preserved (i.e., if all actions only print something)
 - 1. treat actions as terminal symbols
 - eliminate left-recursion as usual

$$E \rightarrow E_{l} + T \{ \text{ print '+'} \}; \}$$

$$E \rightarrow T$$

$$E \rightarrow T$$

$$E \rightarrow TR$$

$$R \rightarrow + T \{ \text{ print '+'} \}; \} R$$

$$R \rightarrow \varepsilon$$

$$E \rightarrow TR$$

$$R \rightarrow + T \{ \text{ print '+'} \}; \} R$$

$$R \rightarrow \varepsilon$$

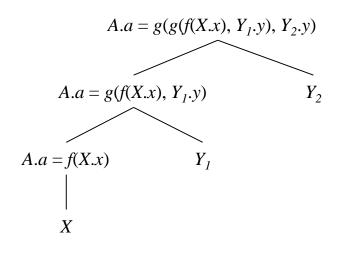
$$R \rightarrow \varepsilon$$

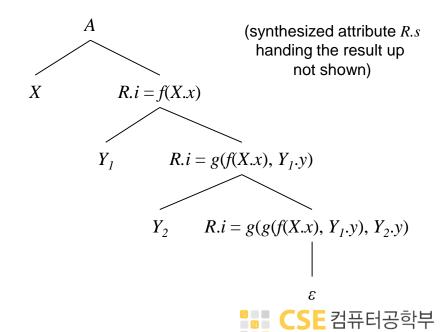
Eliminating Left-Recursion from SDT's

- If the actions compute attributes (instead of just printing some output), eliminating left-recursion is more complicated.
- The following always schema works for S-attributed SDT's

$$\begin{array}{ccc}
A & \rightarrow & A_1 Y \{ A.a = g(A_1.a, Y.y) \} \\
A & \rightarrow & X \{ A.a = f(X.x) \}
\end{array}$$
(goal)

• for XYY



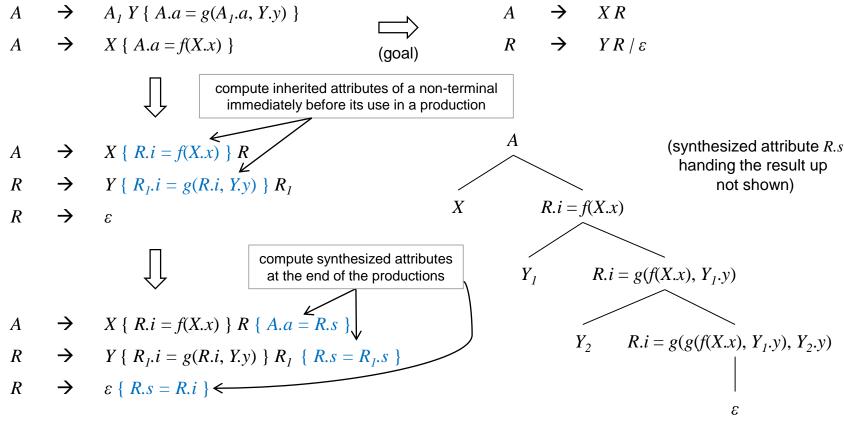


XR

 YR/ε

Eliminating Left-Recursion from SDT's

- If the actions compute attributes (instead of just printing some output), eliminating left-recursion is more complicated.
- The following always schema works for S-attributed SDT's



- Postfix translation schemes only work for S-attributed SDD's
- More general case: L-attributed SDD's

Conversion rules

- 1. embed the action that computes the *inherited* attribute for a non-terminal *A* immediately before that occurrence of *A* in the body of the production. If *A* has more than one inherited attribute, choose an order according to a topological sort of the dependence graph.
- 2. place the actions that compute a *synthesized* attribute for the head of a production at the end of the body of that production.

Example: immediate code generation for a while statement

$$S \rightarrow \text{while } (C) S_1$$

- code for the condition C and the statement sequence S_I are generated directly by the respective non-terminals
- control flow implemented by issuing statements of the form "label L"
- attributes
 - ▶ S.next labels the beginning of the code to be executed after S is finished
 - ▶ *S.code* intermediate code that implements *S* and ends with a jump to *S.next*
 - C.true labels the beginning of the code to be executed if C is true
 - C.false idem for C == false
 - C.code intermediate code that implements C and jumps to C.true/false depending on whether C evaluates to true or false

Example: immediate code generation for a while statement

$$S \rightarrow \text{while } (C) S_1$$

L-attributed SDD

Production Semantic Rule S → while (C) S_1 L1 = newLabel(); L2 = newLabel(); $S_1.next = L1;$ C.false = S.next; C.true = L2; S.code = label || L1 || C.code || label || L2 || S_1.code

Example: immediate code generation for a while statement

$$S \rightarrow \text{while } (C) S_1$$

- Conversion to SDT according to the rules establieshed before (slide <u>47</u>)
- remaining issue
 - L1, L2 are variables, not attributes
 - ▶ like before treat actions as dummy non-terminals
 → variables can be viewed as synthesized attributes of those non-terminals

SDT

```
S \rightarrow \text{while} ( \{ L1 = newLabel(); L2 = newLabel(); C.false = S.next; C.true = L2; \} 

C) \{ S_1.next = L1; \} 

S_1 \{ S.code = \text{label} \parallel L1 \parallel C.code \parallel \text{label} \parallel L2 \parallel S_1.code; \}
```

Translation of SDT's during Top-Down Parsing

- Given: a recursive-descent parser with one function per non-terminal
- For each non-terminal A extend the corresponding function A() as follows:
 - the arguments to A() are the inherited attributes of non-terminal A
 - the body of A() needs to parse as well as deal with actions in A
 - decide which production to apply (possibly using the lookahead)
 - consume terminals when they appear in the production
 - call functions corresponding to non-terminals and provide them with the proper arguments
 - (use local variables as needed to save/preserve attributes)
 - the return value of \mathbb{A} () is the collection of synthesized attributes of non-terminal A

Translation of SDT's during Top-Down Parsing

SDT

while example from earlier

```
S \rightarrow  while ( { L1 = newLabel(); L2 = newLabel(); }
                                                   C.false = S.next; C.true = L2; 
                                                  \{ S_1.next = L1; \}
                                            C)
string S(label next) {
                                                   \{ S.code = label \parallel L1 \parallel C.code \parallel label \parallel L2 \parallel S_1.code; \}
  string Scode, Ccode;
  label L1, L2;
  switch (token) {
     case tWHILE:
        consume (tWHILE); consume ('(');
        L1 = newLabel(); L2 = newLabel();
        Ccode = C(next, L2);
        consume(')');
        Scode = S(L1);
        return 'label' || L1 || Ccode || 'label' || L2 || Scode;
```

Translation of SDT's during Top-Down Parsing

Same example, but on-the-fly code-generation instead of returning strings

```
void S(label next) {
  label L1, L2;
  switch (token) {
    case tWHILE:
      consume(tWHILE); consume('(');
      L1 = newLabel(); L2 = newLabel();
      print("label %s\n", L1);
      C(next, L2);
      consume(')');
      S(L1);
      print("label %s\n", L2);
```