

## DSP2 Week 7 experiment Report

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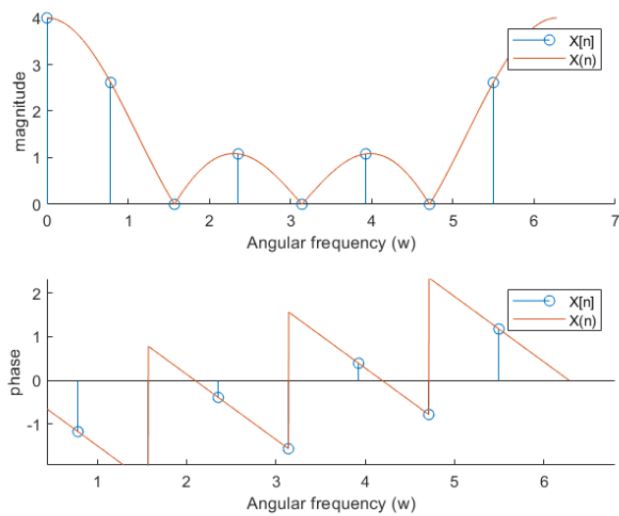
### EXERCISE 1

(Source Code)

```
1  n = 0:7;
2  N = length(n);
3  k = 0:N-1;
4  x = [1 1 1 1 0 0 0 0];
5  X=dft(x);
6  magX = abs(X);
7  angX = angle(X);
8  xw = ((2*pi)/N)*k;
9  yw = ((2*pi)/2000)*(0:1999);
10 Y = 1 + exp(-j.*yw) + exp(-j*2.*yw) + exp(-j*3.*yw);
11 magY = abs(Y);
12 angY = angle(Y);
13
14 subplot(2,1,1);
15 hold on;
16 stem(xw, magX);
17 plot(yw, magY);
18 legend('X[n]', 'X(n)');
19 ylabel('magnitude');
20 xlabel('Angular frequency (w)');
21 hold off;
22
23 subplot(2,1,2);
24 hold on;
25 stem(xw, angX);
26 plot(yw, angY);
27 legend('X[n]', 'X(n)');
28 ylabel('phase');
29 xlabel('Angular frequency (w)');
30 hold off;
```

X implements the 8-point DFT of  $x[n]$ . Y implements the DTFT of  $x[n]$ .  $xw$  and  $yw$  looks very similar, but  $xw$  is N-point sampled vector whereas  $yw$  is 2000-point which makes the  $yw$  looks like a continuous vector.

(Result)



As we can see in the above graph, DFT of  $x[n]$  is included in the DTFT of  $x[n]$ .

## Exercise 2

### a) (Source Code)

```

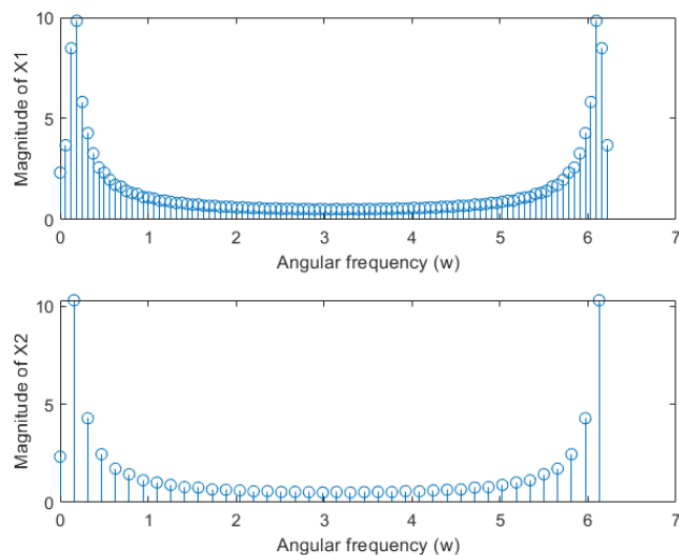
1  n = 0:63;
2  x = ((0.95).^n).*cos((pi/20)*n);
3
4  M1 = 100;
5  M2 = 40;
6
7  k1 = [0:M1-1];
8  k2 = [0:M2-1];
9
10 DT_samp = @(x, k, n) x*exp(-j*2*pi/length(k)).^(n'*k);
11
12 X1 = DT_samp(x, k1, n);
13 X2 = DT_samp(x, k2, n);
14
15 magX1 = abs(X1);
16 magX2 = abs(X2);
17
18 w1 = ((2*pi)/M1)*k1;
19 w2 = ((2*pi)/M2)*k2;
20
21 subplot(2,1,1);
22 stem(w1, magX1)
23 xlabel("Angular frequency (w)");
24 ylabel("Magnitude of X1");
25
26 subplot(2,1,2);
27 stem(w2, magX2);
28 xlabel("Angular frequency (w)");
29 ylabel("Magnitude of X2");

```

$x$  is the implementation of  $x[n] = (0.95)^n \cos\left(\frac{\pi}{20}n\right)$  for  $0 \leq n \leq 63$ . We plotted

2 kinds of DFT of  $x[n]$ ; One is 100-point DFT of  $x[n]$ , the other is 40-point DFT of  $x[n]$  where the length of  $x[n]$  is 64.

(Result)



b) (Source Code)

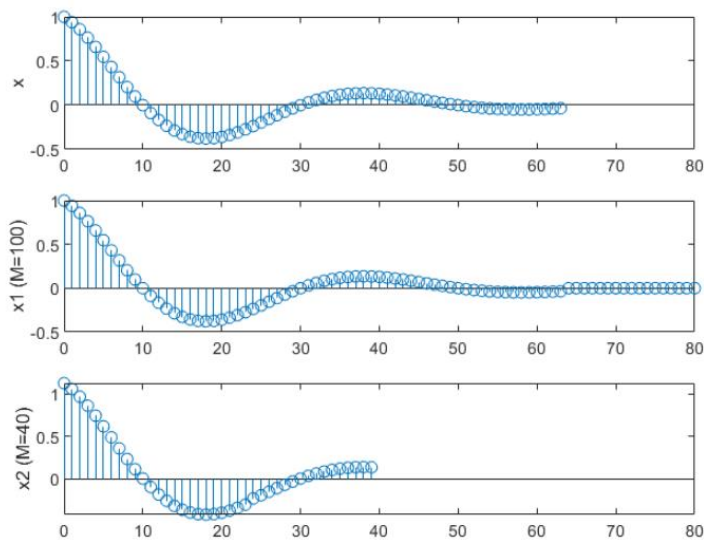
```

14     x1 = idft(X1)
15     x2 = idft(X2)
16
17     subplot(3,1,1);
18     stem(n, real(x));
19     ylabel("x");
20     xlim([0 80]);
21     subplot(3,1,2);
22     stem(k1, real(x1));
23     ylabel("x1 (M=100)");
24     xlim([0 80]);
25     subplot(3,1,3);
26     stem(k2, real(x2));
27     ylabel("x2 (M=40)");
28     xlim([0 80]);

```

I calculated the inverse dft of  $X1$  and  $X2$  using the `idft` function which I made on the last lecture.

(Result)



First graph is the original signal  $x[n]$ . Second graph is a recovered signal where  $M$  is 100 and it shows zero padding on  $64 < n \leq 80$ . May be there is more zero padding until  $n=100$ . Third graph is a recovered signal where  $M$  is 40, which is way less than the length of the original signal  $x$ . It perfectly recovered till the  $n$  is 40.

c) (Source Code)

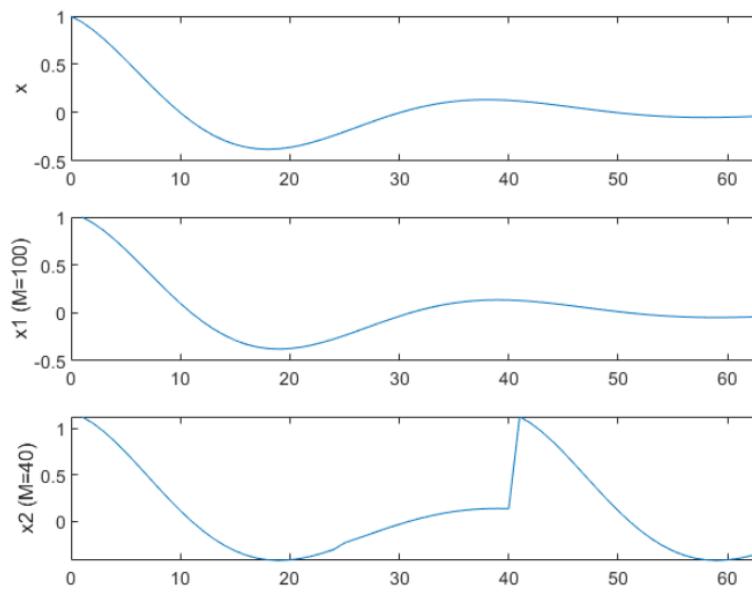
```

29     x1_ = idfs(X1)
30     x2_ = idfs(X2)
31
32     subplot(3,1,1);
33     plot(n, x);
34     ylabel("x");
35     xlim([0 63]);
36     subplot(3,1,2);
37     plot(real(x1_));
38     ylabel("x1 (M=100)");
39     xlim([0 63]);
40     subplot(3,1,3);
41     plot(real(x2_));
42     ylabel("x2 (M=40)");
43     xlim([0 63]);

```

$x1_$  and  $x2_$  is a inverse discrete Fourier series of  $X1$  and  $X2$  respectively.

(Result)



$x_1$  is exactly recovered from  $X_1$ .  $x_2$  is exactly recovered until 40 but it went wrong after 40. The temporal aliasing has occurred.