### Project

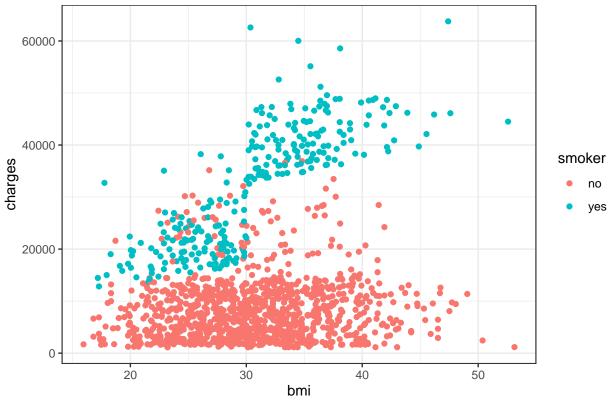
#### Hyun Suk (Max) Ryoo (hr2ee)

### 11/11/2021

```
## Data Processing
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.0.2
## -- Attaching packages ----- tidyverse 1.3
## v ggplot2 3.3.2
                    v purrr
                             0.3.4
## v tibble 3.0.1 v dplyr 1.0.2
                  v stringr 1.4.0
## v tidyr
          1.1.2
## v readr
          1.4.0
                    v forcats 0.5.0
## Warning: package 'ggplot2' was built under R version 4.0.2
## Warning: package 'tidyr' was built under R version 4.0.2
## Warning: package 'readr' was built under R version 4.0.2
## Warning: package 'dplyr' was built under R version 4.0.2
## Warning: package 'stringr' was built under R version 4.0.2
## Warning: package 'forcats' was built under R version 4.0.2
## -- Conflicts ----- tidyverse_conflicts
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(dplyr)
library(MASS)
## Warning: package 'MASS' was built under R version 4.0.2
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
      select
library(leaps)
## Warning: package 'leaps' was built under R version 4.0.2
setwd("/Users/maxryoo/Documents/MSDS/STAT6021/Project2")
data <- read.csv("data/insurance.csv")</pre>
head(data)
                bmi children smoker
    age
          sex
                                      region charges
## 1 19 female 27.900
                      0
                               yes southwest 16884.924
```

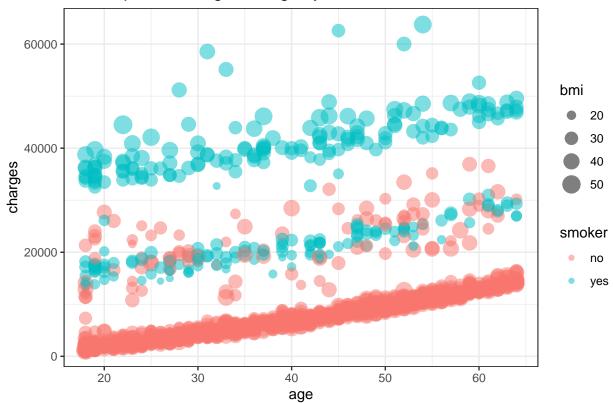
```
## 2
          male 33.770
                                   no southeast 1725.552
     18
          male 33.000
                                   no southeast 4449.462
## 3
     28
                              3
                                   no northwest 21984.471
          male 22.705
## 4 33
## 5 32
          male 28.880
                                   no northwest 3866.855
## 6 31 female 25.740
                                   no southeast 3756.622
data$significant.charge = as.factor(data$charges > median(data$charges))
data$smoker = as.factor(data$smoker)
data$region = as.factor(data$region)
head(data)
                  bmi children smoker
                                                   charges significant.charge
##
     age
                                         region
                                  yes southwest 16884.924
## 1
    19 female 27.900
                              0
                                                                         TRUE
     18
          male 33.770
                                   no southeast 1725.552
                                                                        FALSE
## 3
     28
          male 33.000
                              3
                                   no southeast 4449.462
                                                                        FALSE
          male 22.705
                                   no northwest 21984.471
## 4 33
                              0
                                                                        TRUE
## 5 32
          male 28.880
                                   no northwest 3866.855
                                                                        FALSE
## 6 31 female 25.740
                                                                        FALSE
                                   no southeast 3756.622
ggplot(aes(x=bmi, y=charges, color=smoker), data=data) +
  labs(title="Scatter Plot of Charges vs BMI by Smoker Status") +
  theme_bw() +
 geom_point()
```

### Scatter Plot of Charges vs BMI by Smoker Status



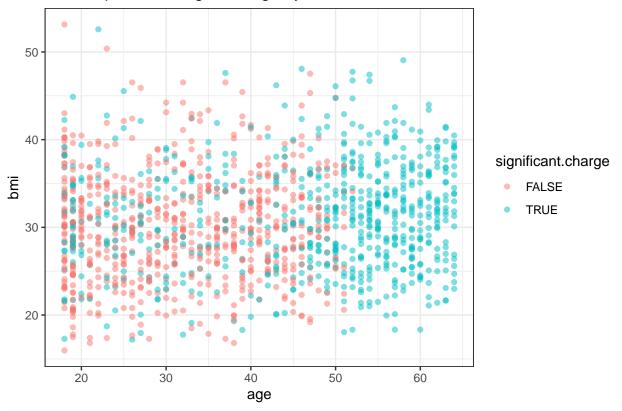
```
ggplot(aes(x=age,y=charges, color=smoker, size=bmi), data=data) +
labs(title="Scatter plot of Charges vs Age by BMI and Smoker Status") +
theme_bw() +
geom_point(alpha=0.5)
```

# Scatter plot of Charges vs Age by BMI and Smoker Status



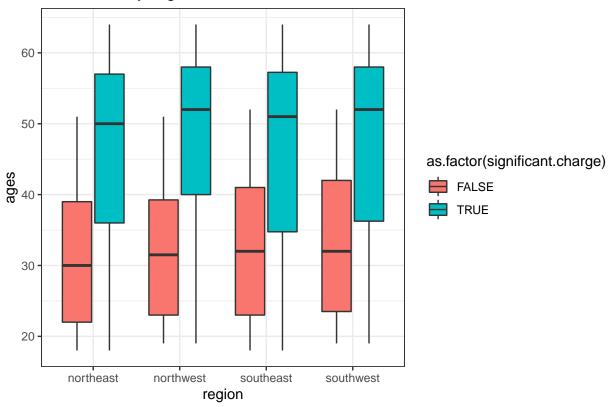
```
ggplot(aes(x=age,y=bmi, color=significant.charge), data=data) +
  labs(title="Scatter plot of Charges vs Age by BMI and Smoker Status") +
  theme_bw() +
  geom_point(alpha=0.5)
```

### Scatter plot of Charges vs Age by BMI and Smoker Status



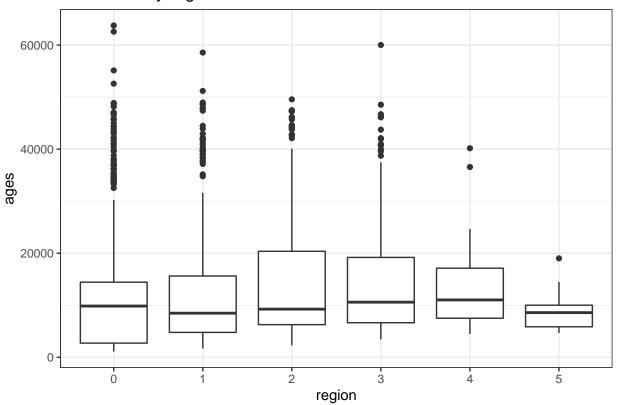
```
ggplot(data, aes(x=region, y=age, fill=as.factor(significant.charge)))+
  geom_boxplot() +
  theme_bw() +
  labs(x="region", y="ages", title="Dist of bmi by region and smoker status")
```

# Dist of bmi by region and smoker status



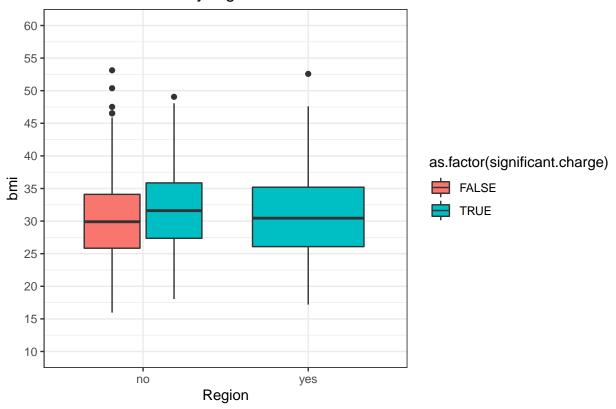
```
ggplot(data, aes(x=as.factor(children), y=charges))+
  geom_boxplot() +
  theme_bw() +
  labs(x="region", y="ages", title="Dist of bmi by region and smoker status")
```

# Dist of bmi by region and smoker status



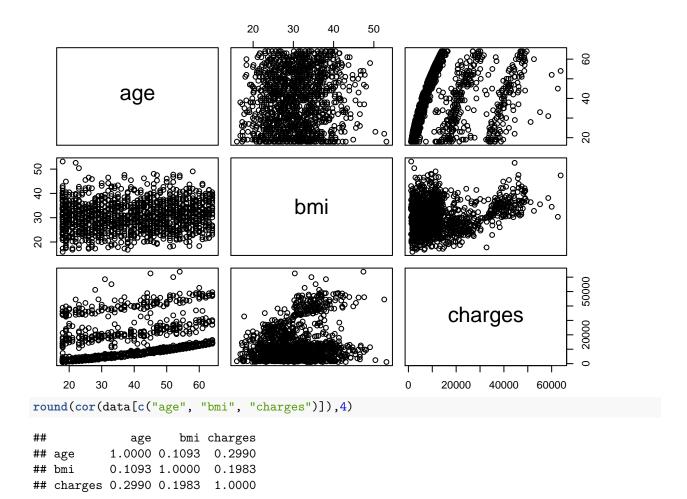
```
ggplot(data, aes(x=smoker, y=bmi, fill=as.factor(significant.charge)))+
  geom_boxplot() +
  theme_bw() +
  labs(x="Region", y="bmi", title="Distribution of bmi by region and smoker status") + scale_y_continu
```

# Distribution of bmi by region and smoker status



### Correlation

pairs(data[c("age", "bmi", "charges")])



### All possible regressions and pull based on adjusted R square, mallow, and BIC

```
no_class_predictor = data[1:7]
allreg2 <- regsubsets(charges ~., data=no_class_predictor, nbest=2)</pre>
summary(allreg2)
## Subset selection object
## Call: regsubsets.formula(charges ~ ., data = no_class_predictor, nbest = 2)
## 8 Variables (and intercept)
##
                   Forced in Forced out
                       FALSE
                                   FALSE
## age
                       FALSE
                                   FALSE
## sexmale
## bmi
                       FALSE
                                  FALSE
## children
                       FALSE
                                  FALSE
## smokeryes
                       FALSE
                                  FALSE
## regionnorthwest
                       FALSE
                                  FALSE
## regionsoutheast
                       FALSE
                                  FALSE
## regionsouthwest
                       FALSE
                                   FALSE
## 2 subsets of each size up to 8
## Selection Algorithm: exhaustive
##
            age sexmale bmi children smokeryes regionnorthwest regionsoutheast
                                      "*"
## 1 (2) "*" "
```

```
## 2 (1) "*" "
                    "*"
    (2)""
                               "*"
    (1)"*"""
                               "*"
    (2)"*"
## 3
                               "*"
    (1)"*"""
                               "*"
## 4
                               "*"
## 4
    (2)"*"
                               "*"
    (1)"*"
                                                     "*"
                               "*"
    (2)"*"
## 5
                                                     "*"
                               "*"
## 6
     (1)
          "*"
## 6
    (2) "*" "*"
                               "*"
                               "*"
                                                     "*"
    (1)"*"""
                               "*"
                                                     "*"
## 7
    (2) "*" "*"
                    "*" "*"
                               "*"
    (1) "*" "*"
                                                     "*"
##
          regionsouthwest
    (1)""
## 1
    (2)""
## 1
## 2
    (1)""
    (2)""
## 2
    (1)""
## 3
    (2)""
## 3
    (1)""
## 4
    (2)""
## 4
## 5
    (1)""
    (2)"*"
## 5
## 6 (1) "*"
    (2)""
    (1)"*"
## 7
## 7
    (2)"*"
## 8 (1) "*"
```

### Best for Adjusted R square

```
coef(allreg2, which.max(summary(allreg2)$adjr2))
##
       (Intercept)
                                                 bmi
                                                             children
                                                                            smokeryes
                                age
       -12165.3824
##
                           257.0064
                                            338.6413
                                                             471.5441
                                                                            23843.8749
## regionsoutheast regionsouthwest
##
         -858.4696
                          -782.7452
```

#### Best for Mallows

```
coef(allreg2, which.min(summary(allreg2)$cp))
##
       (Intercept)
                                                             children
                                                                             smokeryes
                                age
                                                 bmi
                                            338.6413
                                                             471.5441
                                                                            23843.8749
##
       -12165.3824
                           257.0064
## regionsoutheast regionsouthwest
##
         -858.4696
                          -782.7452
```

#### Best for BIC

```
coef(allreg2, which.min(summary(allreg2)$bic))
```

```
## (Intercept) age bmi children smokeryes
## -12102.7694 257.8495 321.8514 473.5023 23811.3998
```

#### Forward Selection

```
##intercept only model
regnull <- lm(charges~1, data=no_class_predictor)
##model with all predictors
regfull <- lm(charges ~ . , data=no_class_predictor)
Forward Selection
step(regnull, scope=list(lower=regnull, upper=regfull), direction="forward")
## Start: AIC=25160.18
## charges ~ 1
##
              Df Sum of Sq
##
                                   RSS
                                         AIC
              1 1.2152e+11 7.4554e+10 23868
## + smoker
## + age
              1 1.7530e+10 1.7854e+11 25037
## + bmi
              1 7.7134e+09 1.8836e+11 25108
## + children 1 9.0660e+08 1.9517e+11 25156
              3 1.3008e+09 1.9477e+11 25157
## + region
              1 6.4359e+08 1.9543e+11 25158
## + sex
## <none>
                            1.9607e+11 25160
##
## Step: AIC=23868.38
## charges ~ smoker
##
##
              Df Sum of Sq
                                   RSS
                                         AIC
## + age
              1 1.9928e+10 5.4626e+10 23454
              1 7.4856e+09 6.7069e+10 23729
## + bmi
## + children 1 7.5272e+08 7.3802e+10 23857
## <none>
                           7.4554e+10 23868
## + sex
              1 1.4213e+06 7.4553e+10 23870
## + region
              3 1.0752e+08 7.4447e+10 23872
##
## Step: AIC=23454.24
## charges ~ smoker + age
##
##
              Df Sum of Sq
                                         AIC
## + bmi
             1 5112896646 4.9513e+10 23325
## + children 1 459283727 5.4167e+10 23445
## <none>
                            5.4626e+10 23454
## + sex
                    2225509 5.4624e+10 23456
              3 138426748 5.4488e+10 23457
## + region
## Step: AIC=23324.76
## charges ~ smoker + age + bmi
##
              Df Sum of Sq
                                  RSS
                                        AIC
## + children 1 434769398 4.9078e+10 23315
              3 232012208 4.9281e+10 23324
## + region
## <none>
                           4.9513e+10 23325
                  3942912 4.9509e+10 23327
## + sex
##
## Step: AIC=23314.96
## charges ~ smoker + age + bmi + children
```

```
##
##
           Df Sum of Sq
                                RSS
                                      ATC
## + region 3 233200844 4.8845e+10 23315
## <none>
                         4.9078e+10 23315
## + sex
                 5486063 4.9073e+10 23317
##
## Step: AIC=23314.58
## charges ~ smoker + age + bmi + children + region
##
##
          Df Sum of Sq
                              RSS
                                    AIC
## <none>
                       4.8845e+10 23315
## + sex
         1 5716429 4.8840e+10 23316
##
## Call:
## lm(formula = charges ~ smoker + age + bmi + children + region,
       data = no_class_predictor)
##
## Coefficients:
##
       (Intercept)
                          smokeryes
                                                                  bmi
                                                 age
##
          -11990.3
                            23836.3
                                               257.0
                                                                338.7
##
          children regionnorthwest regionsoutheast regionsouthwest
##
             474.6
                             -352.2
                                             -1034.4
                                                               -959.4
(Intercept)
                                        bmi
                                                   children
                                                                  smokeryes regionsoutheast
                        age
-12165.3824
                                                   471.5441
                                                                 23843.8749
                   257.0064
                                   338.6413
                                                                                   -858.4696
regions
outhwest -782.7452
```

#### Backwards

```
step(regfull, scope=list(lower=regnull, upper=regfull), direction="backward")
## Start: AIC=23316.43
## charges ~ age + sex + bmi + children + smoker + region
##
##
             Df Sum of Sq
                                   RSS
                                         AIC
## - sex
              1 5.7164e+06 4.8845e+10 23315
## <none>
                           4.8840e+10 23316
## - region
              3 2.3343e+08 4.9073e+10 23317
## - children 1 4.3755e+08 4.9277e+10 23326
## - bmi
              1 5.1692e+09 5.4009e+10 23449
               1 1.7124e+10 6.5964e+10 23717
## - age
## - smoker
              1 1.2245e+11 1.7129e+11 24993
## Step: AIC=23314.58
## charges ~ age + bmi + children + smoker + region
##
##
             Df Sum of Sq
                                   RSS
## <none>
                            4.8845e+10 23315
              3 2.3320e+08 4.9078e+10 23315
## - region
## - children 1 4.3596e+08 4.9281e+10 23324
              1 5.1645e+09 5.4010e+10 23447
## - bmi
## - age
              1 1.7151e+10 6.5996e+10 23715
## - smoker
              1 1.2301e+11 1.7186e+11 24996
```

```
##
## Call:
  lm(formula = charges ~ age + bmi + children + smoker + region,
       data = no_class_predictor)
##
##
##
   Coefficients:
                                                                 children
##
       (Intercept)
                                                    bmi
                                  age
##
          -11990.3
                                257.0
                                                  338.7
                                                                    474.6
##
                     regionnorthwest
                                       regionsoutheast
                                                         regionsouthwest
         smokeryes
##
           23836.3
                               -352.2
                                                -1034.4
                                                                   -959.4
```

#### Based on forward and backward

We get the same model for forward and backward

Let's first make a multiple linear regression model with all the predictors.

```
mlr_full = lm(charges ~ age + bmi + children + smoker + region, data=data)
summary(mlr_full)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + region,
##
       data = data)
##
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                                             Max
## -11367.2 -2835.4
                        -979.7
                                 1361.9
                                         29935.5
##
  Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    -11990.27
                                  978.76 -12.250
                                                  < 2e-16 ***
## age
                       256.97
                                   11.89
                                         21.610
                                                  < 2e-16 ***
## bmi
                       338.66
                                   28.56
                                                  < 2e-16 ***
                                          11.858
                                  137.74
## children
                       474.57
                                           3.445 0.000588 ***
                    23836.30
                                                  < 2e-16 ***
## smokeryes
                                  411.86
                                          57.875
## regionnorthwest
                     -352.18
                                  476.12
                                          -0.740 0.459618
                    -1034.36
                                          -2.162 0.030834 *
## regionsoutheast
                                  478.54
## regionsouthwest
                      -959.37
                                  477.78
                                          -2.008 0.044846 *
## ---
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 6060 on 1330 degrees of freedom
## Multiple R-squared: 0.7509, Adjusted R-squared: 0.7496
## F-statistic: 572.7 on 7 and 1330 DF, p-value: < 2.2e-16
```

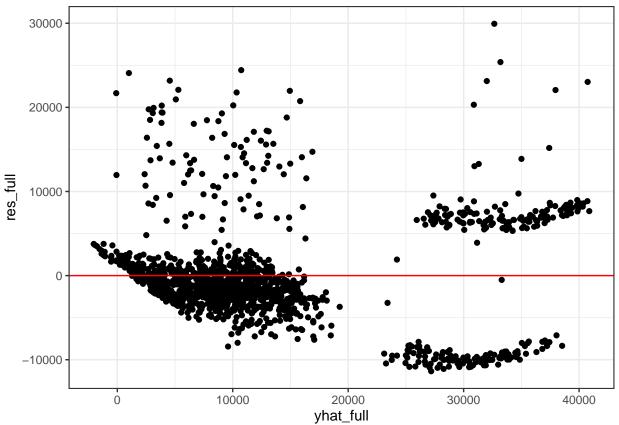
The full regression is as follows.

```
\hat{y} = -11938.5 + 256.9 \text{age} - 131.3I_1 + 339.2 \text{bmi} + 475.5 \text{children} + 23848.5I_2 - 353.0I_3 - 1035.0I_4 - 960.0I_5
```

 $I_1$  indicates whether the sex of the client is male. The value will be 0 for females.  $I_2$  indicates whether that a client smokes. The value will be 0 for non smokers.  $I_3$  indicates that the client is in the northwest region.  $I_4$  indicates that the client is located in the southeast.  $I_5$  indicates that the client is located in the southwest. If the client is in the northeast  $I_3$ ,  $I_4$ ,  $I_5$  will be zero, since this is the reference class.

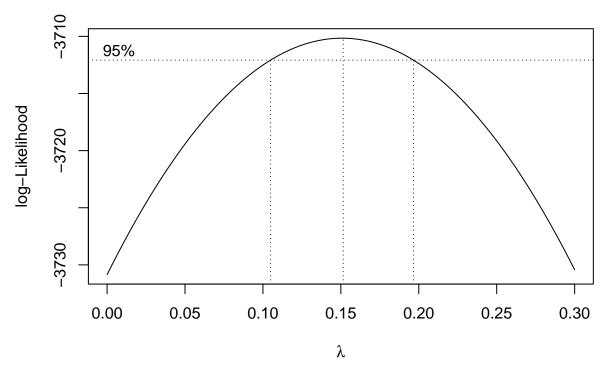
### Assumption Check of Full Model

```
yhat_full <- mlr_full$fitted.values
res_full <- mlr_full$residuals
data %>%
    ggplot(aes(yhat_full, res_full)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



The residuals are obviously not evenly scattered, which then we can utilize the boxcox method to give us information about transformation.

```
boxcox(mlr_full, lambda=seq(0,0.3, 0.01))
```

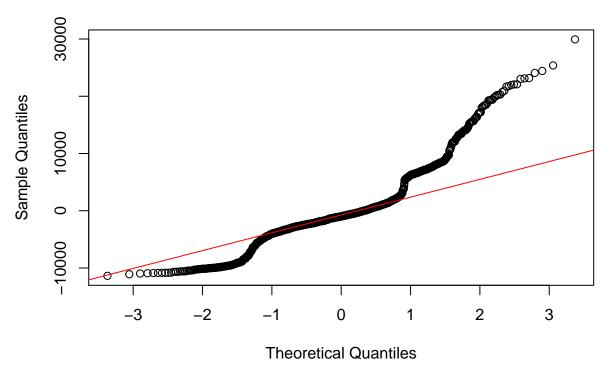


From the boxcox we can try a lambda value of 0.15 for transformation.

### QQPlot

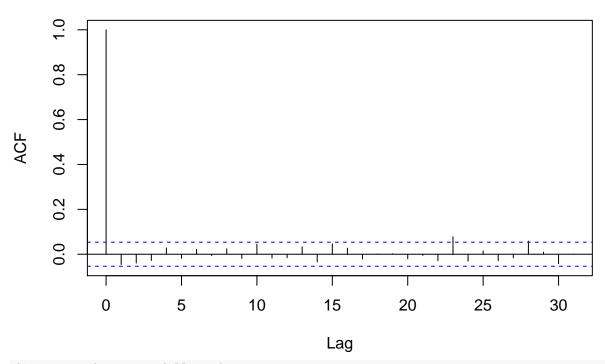
```
{
    qqnorm(mlr_full$residuals)
    qqline(mlr_full$residuals, col="red")
}
```

### Normal Q-Q Plot



```
acf(mlr_full$residuals, main="ACF")
```

### **ACF**



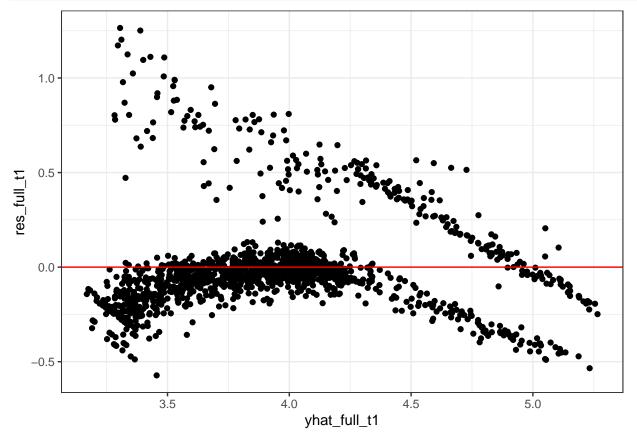
```
first_transformation_full <- data
first_transformation_full$charges <- first_transformation_full$charges^0.15
mlr_transform_first <- lm(charges ~ age + bmi + children + smoker + region, data=first_transformation_f
summary(mlr_transform_first)</pre>
```

```
##
## Call:
  lm(formula = charges ~ age + bmi + children + smoker + region,
##
      data = first_transformation_full)
##
## Residuals:
##
                 1Q
                      Median
## -0.57232 -0.12513 -0.04165 0.03000 1.26454
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   2.7239709  0.0416239  65.443  < 2e-16 ***
                   0.0191744 0.0005057
                                         37.916 < 2e-16 ***
## age
## bmi
                   0.0088624 0.0012145
                                          7.297 5.04e-13 ***
## children
                   0.0524721 0.0058577
                                          8.958 < 2e-16 ***
## smokeryes
                                                 < 2e-16 ***
                   0.9560821
                              0.0175151 54.586
## regionnorthwest -0.0345277 0.0202480
                                         -1.705
                                                  0.0884 .
## regionsoutheast -0.0845268 0.0203508
                                        -4.153 3.48e-05 ***
## regionsouthwest -0.0708940 0.0203185 -3.489
                                                  0.0005 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.2577 on 1330 degrees of freedom
## Multiple R-squared: 0.7754, Adjusted R-squared: 0.7742
## F-statistic: 655.9 on 7 and 1330 DF, p-value: < 2.2e-16</pre>
```

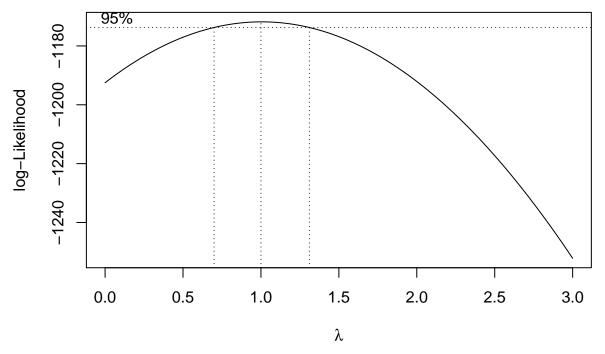
Residual Plot of the transformed model.

```
yhat_full_t1 <- mlr_transform_first$fitted.values
res_full_t1 <- mlr_transform_first$residuals
data %>%
    ggplot(aes(yhat_full_t1, res_full_t1)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



Violation in constant variance

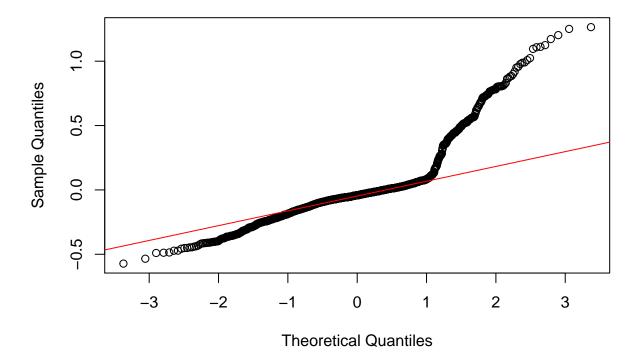
```
boxcox(mlr_transform_first, lambda=seq(0,3, 0.01))
```



### QQPLOT

```
{
    qqnorm(mlr_transform_first$residuals)
    qqline(mlr_transform_first$residuals, col="red")
}
```

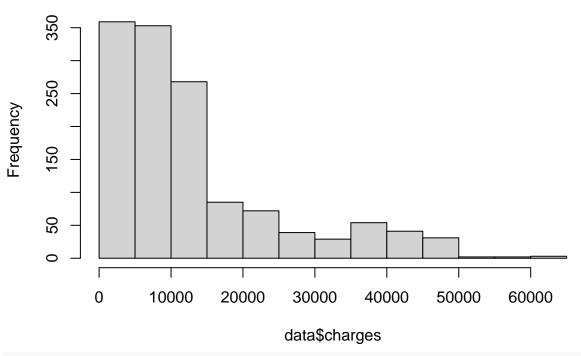
# Normal Q-Q Plot



Why is this happening? Is there some weird behavior in the response variable?

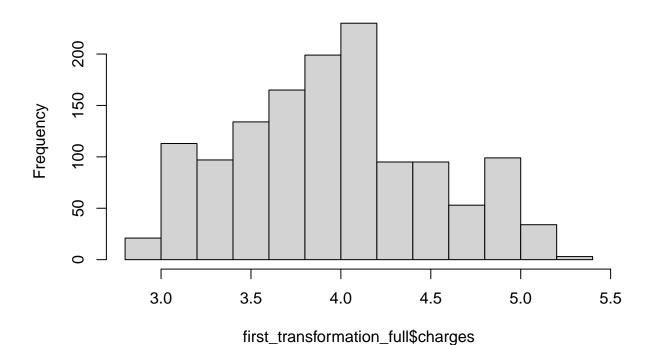
hist(data\$charges)

### Histogram of data\$charges



hist(first\_transformation\_full\$charges)

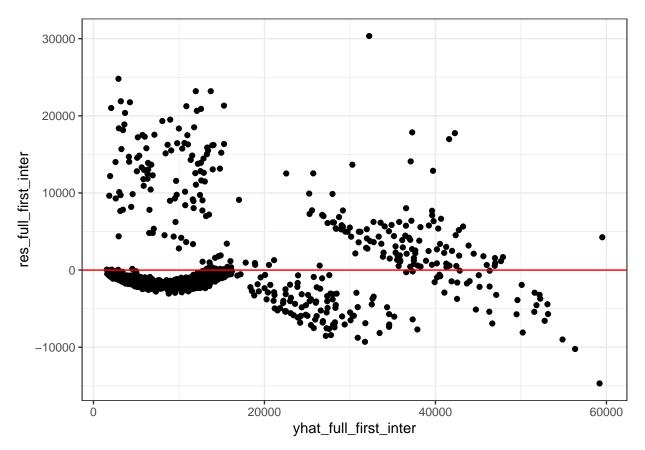
### **Histogram of first\_transformation\_full\$charges**



#### Trial of other predictors to fullfill the linearity assumption.

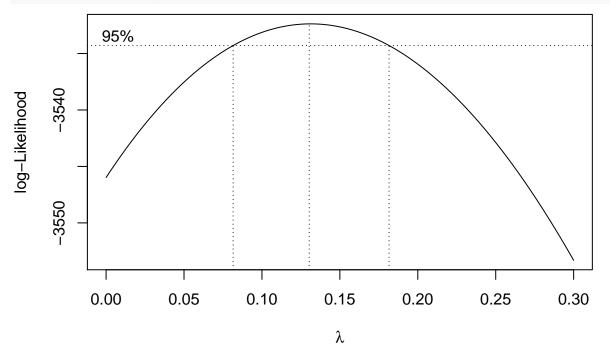
Maybe we can add some interaction terms to the model to see if we can fix the linearity assumption.

```
interaction_age_bmi_with_smoker = lm(charges ~ age*smoker + bmi*smoker + children + region, data=data
summary(interaction_age_bmi_with_smoker)
##
## Call:
## lm(formula = charges ~ age * smoker + bmi * smoker + children +
      region, data = data)
##
##
## Residuals:
                     Median
##
       Min
                 1Q
                                   3Q
                                           Max
## -14695.2 -1918.6 -1316.2
                               -480.3 30345.6
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -2469.101
                              870.166 -2.838 0.00462 **
                                 10.672 24.791 < 2e-16 ***
## age
                     264.558
## smokeryes
                  -20223.654 1831.889 -11.040 < 2e-16 ***
                                          0.874 0.38228
## bmi
                      22.444
                                 25.679
                                110.331
## children
                     512.956
                                          4.649 3.66e-06 ***
## regionnorthwest
                                381.383 -1.524 0.12774
                   -581.232
## regionsoutheast -1205.652
                                383.462 -3.144 0.00170 **
## regionsouthwest -1228.623
                                382.837
                                         -3.209 0.00136 **
## age:smokeryes
                      -2.542
                                 23.711 -0.107 0.91464
                    1438.525
## smokeryes:bmi
                                 52.793 27.249 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4853 on 1328 degrees of freedom
## Multiple R-squared: 0.8405, Adjusted R-squared: 0.8394
## F-statistic: 777.5 on 9 and 1328 DF, p-value: < 2.2e-16
Residual Plot
yhat_full_first_inter <- interaction_age_bmi_with_smoker$fitted.values</pre>
res_full_first_inter <- interaction_age_bmi_with_smoker$residuals
data %>%
 ggplot(aes(yhat_full_first_inter, res_full_first_inter)) +
 geom point() +
 theme bw() +
 geom_hline(yintercept = 0, color="red")
```



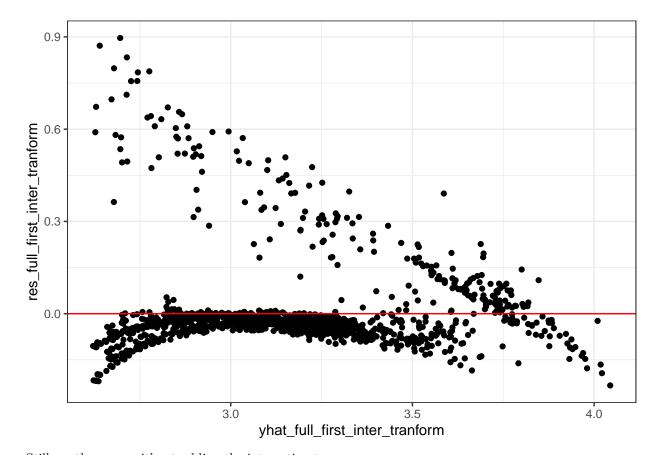
This residual plot is a little better, lets see if we can transform the response with this new equation.

boxcox(interaction\_age\_bmi\_with\_smoker, lambda=seq(0,0.3, 0.01))

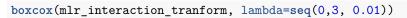


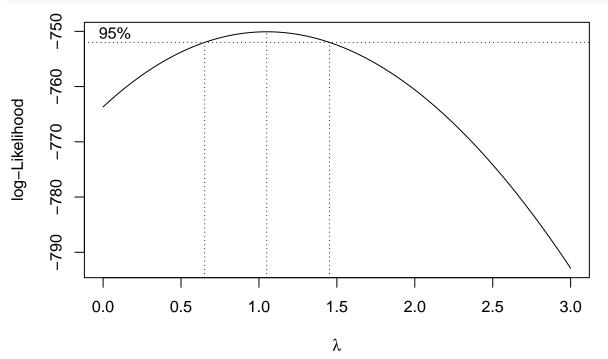
Maybe we can use a lambda value of 0.125

```
interaction_transform <- data</pre>
interaction_transform$charges <- interaction_transform$charges^0.125</pre>
mlr_interaction_tranform <- lm(charges ~ age*smoker + bmi*smoker + children + region, data=interaction
summary(mlr interaction tranform)
##
## Call:
## lm(formula = charges ~ age * smoker + bmi * smoker + children +
      region, data = interaction_transform)
##
## Residuals:
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -0.23325 -0.05925 -0.03216 -0.00578 0.89638
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   2.3898138  0.0268794  88.909  < 2e-16 ***
## age
                   ## smokeryes
                   0.3867297 0.0565870
                                         6.834 1.25e-11 ***
## bmi
                   0.0004622 0.0007932 0.583 0.5602
## children
                   0.0371914  0.0034081  10.913  < 2e-16 ***
## regionnorthwest -0.0243318  0.0117809 -2.065
                                                 0.0391 *
## regionsoutheast -0.0531652  0.0118451  -4.488  7.80e-06 ***
## regionsouthwest -0.0559589 0.0118258 -4.732 2.46e-06 ***
## age:smokeryes
                  -0.0115120  0.0007324  -15.717  < 2e-16 ***
                   0.0223756  0.0016308  13.721  < 2e-16 ***
## smokeryes:bmi
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1499 on 1328 degrees of freedom
## Multiple R-squared: 0.827, Adjusted R-squared: 0.8259
## F-statistic: 705.6 on 9 and 1328 DF, p-value: < 2.2e-16
Recheck Residual Plot
yhat_full_first_inter_tranform <- mlr_interaction_tranform$fitted.values</pre>
res_full_first_inter_tranform <- mlr_interaction_tranform$residuals
data %>%
 ggplot(aes(yhat_full_first_inter_tranform, res_full_first_inter_tranform)) +
 geom_point() +
 theme_bw() +
 geom hline(yintercept = 0, color="red")
```



Still see the same without adding the interaction terms.





Still no luck. We retried this many times, but weren't lucky.

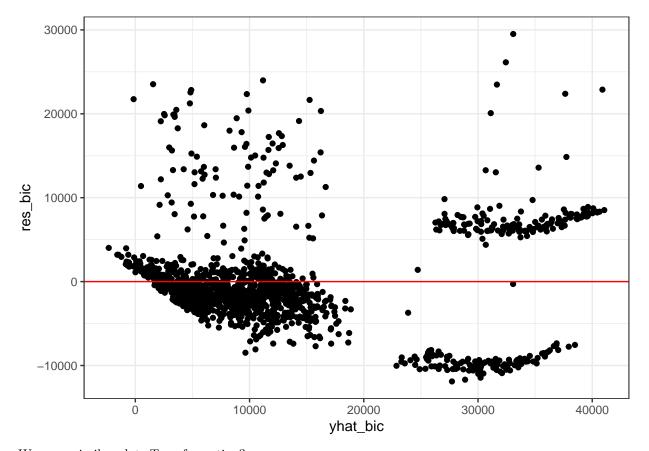
# Partial F test of the interaction vs simple model after two transformation of response variable

```
full <- mlr_interaction_tranform</pre>
reduced <- lm(charges ~ age + bmi + children + smoker + region, data=interaction_transform)
anova(reduced, full)
## Analysis of Variance Table
##
## Model 1: charges ~ age + bmi + children + smoker + region
## Model 2: charges ~ age * smoker + bmi * smoker + children + region
               RSS Df Sum of Sq
                                     F
      1330 38.959
## 1
## 2
      1328 29.842 2
                        9.1174 202.87 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
We can't drop the interaction terms.
```

### BIC Model selection model might be better

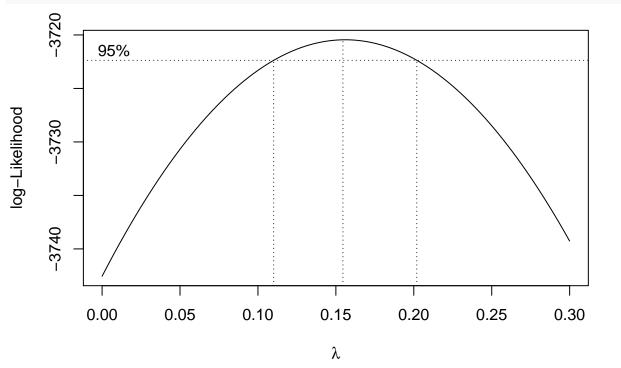
geom\_hline(yintercept = 0, color="red")

```
bic_selection_model = lm(charges ~ age + bmi + children + smoker, data=data)
summary(bic_selection_model)
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker, data = data)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                            Max
## -11897.9 -2920.8 -986.6
                              1392.2 29509.6
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -12102.77
                            941.98 -12.848 < 2e-16 ***
                 257.85
                              11.90 21.675 < 2e-16 ***
## age
## bmi
                 321.85
                             27.38 11.756 < 2e-16 ***
## children
                 473.50
                            137.79
                                    3.436 0.000608 ***
## smokeryes
               23811.40
                            411.22 57.904 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6068 on 1333 degrees of freedom
## Multiple R-squared: 0.7497, Adjusted R-squared: 0.7489
## F-statistic: 998.1 on 4 and 1333 DF, p-value: < 2.2e-16
Residual Plot
yhat_bic <- bic_selection_model$fitted.values</pre>
res_bic <- bic_selection_model$residuals</pre>
data %>%
  ggplot(aes(yhat_bic, res_bic)) +
  geom_point() +
  theme_bw() +
```



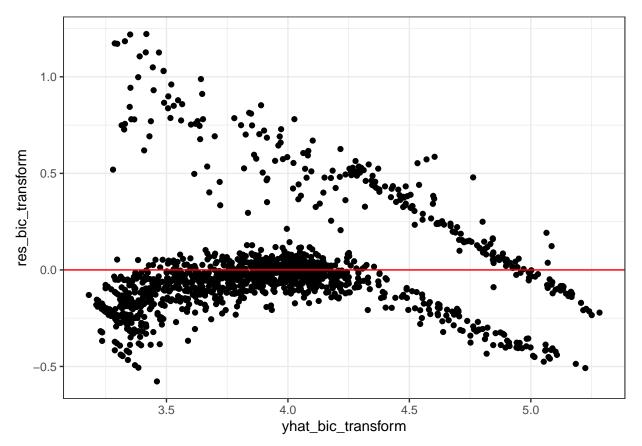
We see a similar plot. Transformation?

boxcox(bic\_selection\_model, lambda=seq(0,0.3, 0.01))

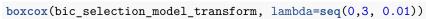


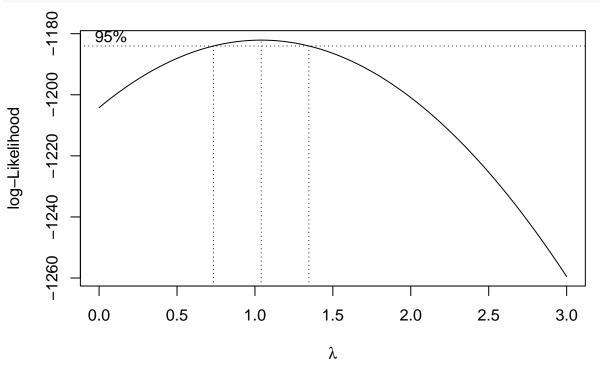
Again lambda of 0.15

```
bic_transform <- data</pre>
bic_transform$charges <- bic_transform$charges^(0.15)</pre>
bic_selection_model_transform = lm(charges ~ age + bmi + children + smoker, data=bic_transform)
summary(bic_selection_model_transform)
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker, data = bic_transform)
## Residuals:
       Min
                 1Q
                      Median
## -0.57755 -0.12028 -0.03776 0.03505 1.22187
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 2.7136331 0.0402741 67.379 < 2e-16 ***
## age
              0.0192458 0.0005086 37.839 < 2e-16 ***
## bmi
              0.0075402 0.0011705
                                    6.442 1.65e-10 ***
## children 0.0523899 0.0058912
                                    8.893 < 2e-16 ***
## smokeryes 0.9539751 0.0175815 54.260 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2594 on 1333 degrees of freedom
## Multiple R-squared: 0.7719, Adjusted R-squared: 0.7712
## F-statistic: 1128 on 4 and 1333 DF, p-value: < 2.2e-16
Residual Plot
yhat_bic_transform <- bic_selection_model_transform$fitted.values</pre>
res_bic_transform <- bic_selection_model_transform$residuals</pre>
  ggplot(aes(yhat_bic_transform, res_bic_transform)) +
 geom_point() +
 theme_bw() +
 geom_hline(yintercept = 0, color="red")
```



Same Stuff happening.

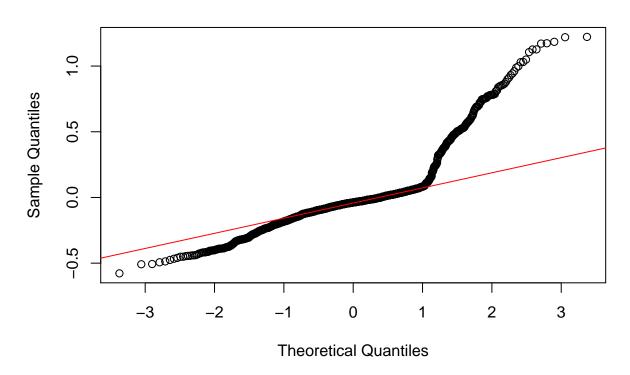




QQPlot

```
{
    qqnorm(bic_selection_model_transform$residuals)
    qqline(bic_selection_model_transform$residuals, col="red")
}
```

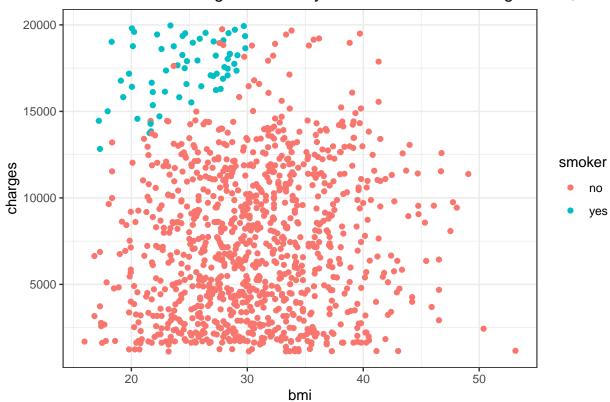
### Normal Q-Q Plot



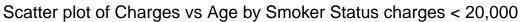
### Change the data split the data?

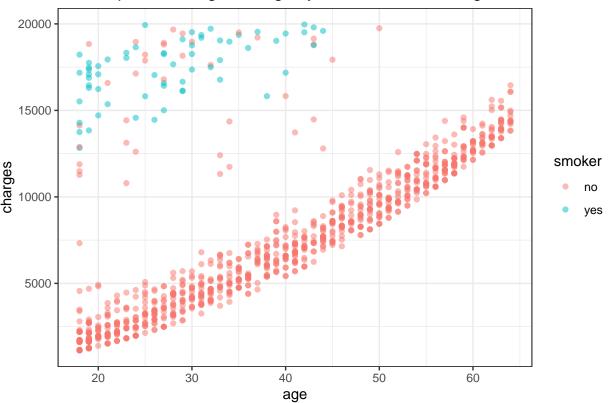
```
less_charge <- data[data$charges < 20000,]
more_change <- data[data$charges >= 20000, ]
library(tidyverse)
ggplot(aes(x=bmi, y=charges, color=smoker), data=less_charge) +
   labs(title="Scatter Plot of Charges vs BMI by Smoker Status for charges < 20,000") +
   theme_bw() +
   geom_point()</pre>
```

# Scatter Plot of Charges vs BMI by Smoker Status for charges < 20,000



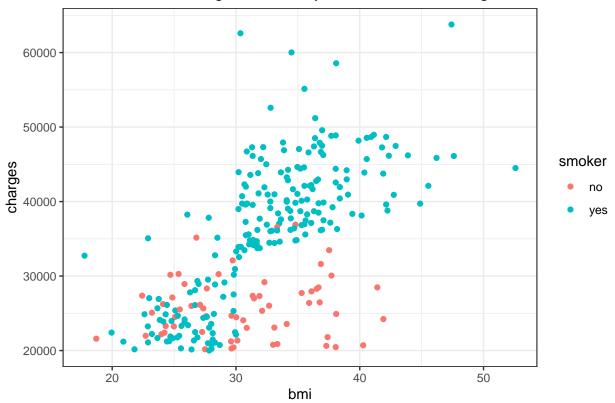
```
ggplot(aes(x=age,y=charges, color=smoker), data=less_charge) +
  labs(title="Scatter plot of Charges vs Age by Smoker Status charges < 20,000") +
  theme_bw() +
  geom_point(alpha=0.5)</pre>
```





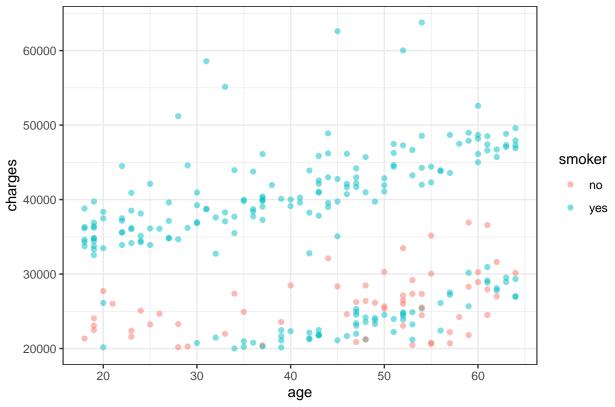
```
ggplot(aes(x=bmi, y=charges, color=smoker), data=more_change) +
labs(title="Scatter Plot of Charges vs BMI by Smoker Status charges > 20,000") +
theme_bw() +
geom_point()
```

### Scatter Plot of Charges vs BMI by Smoker Status charges > 20,000

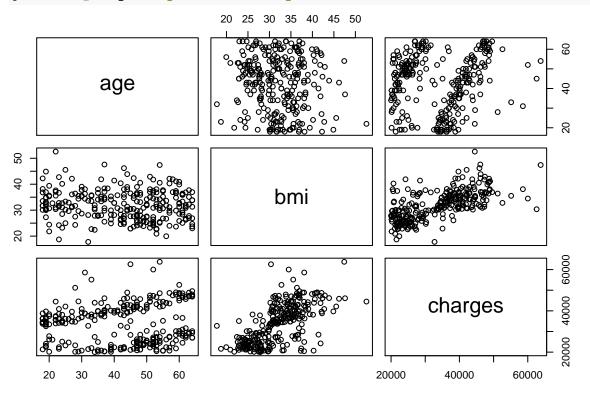


```
ggplot(aes(x=age,y=charges, color=smoker), data=more_change) +
labs(title="Scatter plot of Charges vs Age by Smoker Status charges > 20,000") +
theme_bw() +
geom_point(alpha=0.5)
```

# Scatter plot of Charges vs Age by Smoker Status charges > 20,000



pairs(more\_change[c("age", "bmi", "charges")])

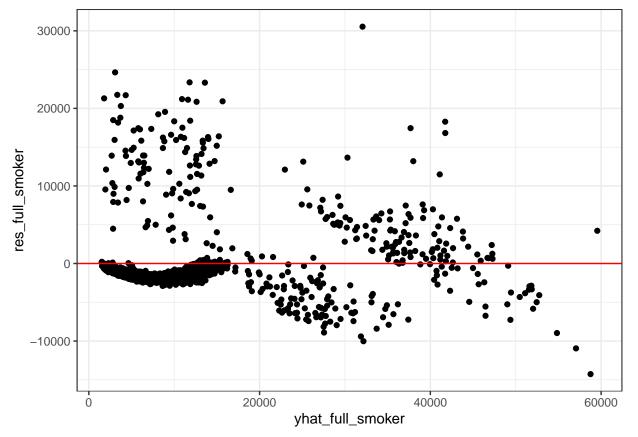


```
pairs(less_charge[c("age", "bmi", "charges")])
                                                50
                               20
                                     30
                                                                               9
            age
4
                                     bmi
30
                                                            charges
                                                                               5000
                       60
                                                         5000
                                                             10000 15000 20000
    20
         30
             40
                  50
mlr_full_smoker = lm(charges ~ (age + bmi + children + region) * smoker, data=data)
summary(mlr_full_smoker)
##
## Call:
## lm(formula = charges ~ (age + bmi + children + region) * smoker,
       data = data)
##
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                            Max
## -14260.4 -1922.0 -1299.4
                                -410.1
                                       30534.4
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
                                           878.080 -2.790 0.00534 **
## (Intercept)
                              -2450.179
                                            10.671 24.828 < 2e-16 ***
                                264.947
## age
## bmi
                                 17.939
                                            25.910
                                                     0.692 0.48883
## children
                                586.903
                                           122.242
                                                     4.801 1.76e-06 ***
## regionnorthwest
                               -552.249
                                           423.912
                                                   -1.303 0.19289
## regionsoutheast
                                           435.141
                                                    -2.274 0.02310 *
                               -989.701
## regionsouthwest
                              -1385.975
                                           424.969
                                                    -3.261 0.00114 **
## smokeryes
                                          1907.109 -10.650 < 2e-16 ***
                             -20310.836
## age:smokeryes
                                                     0.112 0.91067
                                  2.673
                                            23.819
                                                    26.323 < 2e-16 ***
## bmi:smokeryes
                               1453.239
                                            55.209
                                                   -1.474 0.14076
## children:smokeryes
                               -417.913
                                           283.549
## regionnorthwest:smokeryes
                               -105.947
                                           969.919 -0.109 0.91303
                                                   -0.976 0.32933
## regionsoutheast:smokeryes
                               -898.633
                                           920.894
## regionsouthwest:smokeryes
                                           977.752
                                                    0.957 0.33861
                                935.973
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4850 on 1324 degrees of freedom
## Multiple R-squared: 0.8412, Adjusted R-squared: 0.8396
## F-statistic: 539.5 on 13 and 1324 DF, p-value: < 2.2e-16</pre>
```

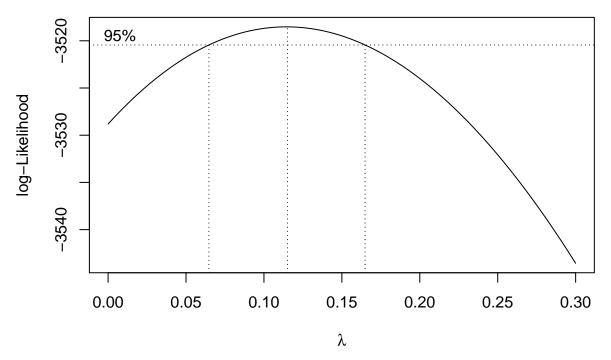
### Assumption Check of Full Model

```
yhat_full_smoker <- mlr_full_smoker$fitted.values
res_full_smoker <- mlr_full_smoker$residuals
data %>%
    ggplot(aes(yhat_full_smoker, res_full_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



The residuals are obviously not evenly scattered, which then we can utilize the boxcox method to give us information about transformation.

```
boxcox(mlr_full_smoker, lambda=seq(0,0.3, 0.01))
```

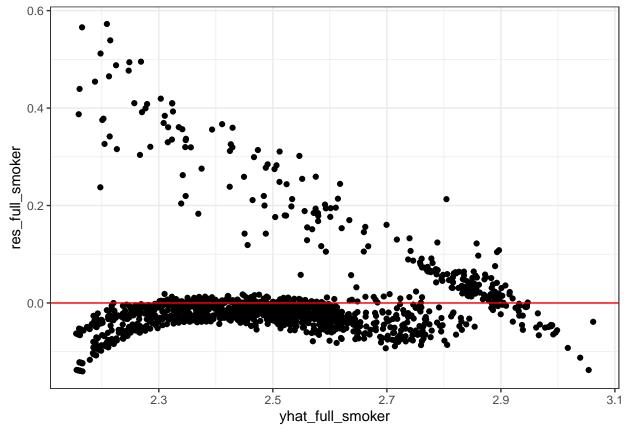


From the boxcox we can try a lambda value of 0.1 for transformation.

```
interaction_transform_smoker <- data</pre>
interaction_transform_smoker$charges <- interaction_transform_smoker$charges^0.1</pre>
mlr_interaction_tranform_smoker <- lm(charges ~ (age + bmi + children + region) * smoker, data=interac
summary(mlr_interaction_tranform_smoker)
##
## Call:
  lm(formula = charges ~ (age + bmi + children + region) * smoker,
       data = interaction_transform_smoker)
##
##
## Residuals:
##
        Min
                  1Q
                       Median
  -0.14041 -0.03918 -0.01973 -0.00012 0.57262
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              2.0103535
                                         0.0171453 117.254
                                                            < 2e-16 ***
## age
                              0.0098368
                                          0.0002084
                                                     47.209
                                                             < 2e-16 ***
                                                      0.679
                                                              0.4970
## bmi
                              0.0003437
                                          0.0005059
## children
                              0.0292642
                                         0.0023869
                                                     12.260
                                                             < 2e-16 ***
## regionnorthwest
                              -0.0180006
                                         0.0082773
                                                     -2.175
                                                              0.0298 *
## regionsoutheast
                              -0.0395694
                                         0.0084965
                                                     -4.657 3.53e-06 ***
## regionsouthwest
                              -0.0433088
                                         0.0082979
                                                     -5.219 2.08e-07 ***
## smokeryes
                              0.2783934 0.0372380
                                                      7.476 1.39e-13 ***
## age:smokeryes
                              -0.0073089
                                         0.0004651 -15.715
                                                             < 2e-16 ***
## bmi:smokeryes
                              0.0134167
                                          0.0010780
                                                     12.446
                                                             < 2e-16 ***
## children:smokeryes
                              -0.0273920
                                         0.0055365
                                                     -4.947 8.48e-07 ***
## regionnorthwest:smokeryes
                                          0.0189385
                                                      0.755
                                                              0.4507
                             0.0142893
## regionsoutheast:smokeryes
                              0.0237658
                                          0.0179813
                                                      1.322
                                                               0.1865
## regionsouthwest:smokeryes
                                         0.0190915
                                                      2.165
                                                              0.0305 *
                              0.0413423
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09469 on 1324 degrees of freedom
## Multiple R-squared: 0.83, Adjusted R-squared: 0.8283
## F-statistic: 497.3 on 13 and 1324 DF, p-value: < 2.2e-16

yhat_full_smoker <- mlr_interaction_tranform_smoker$fitted.values
res_full_smoker <- mlr_interaction_tranform_smoker$residuals
data %>%
    ggplot(aes(yhat_full_smoker, res_full_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```

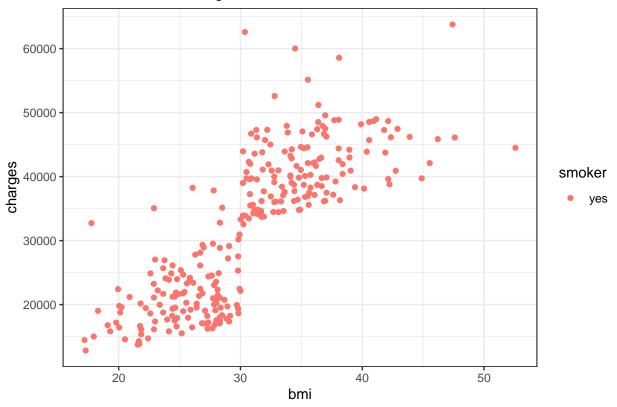


#### Lets SPLIT BY SMOKERS

```
smokers <- data[data$smoker == 'yes',]
non_smokers <- data[data$smoker != 'yes',]

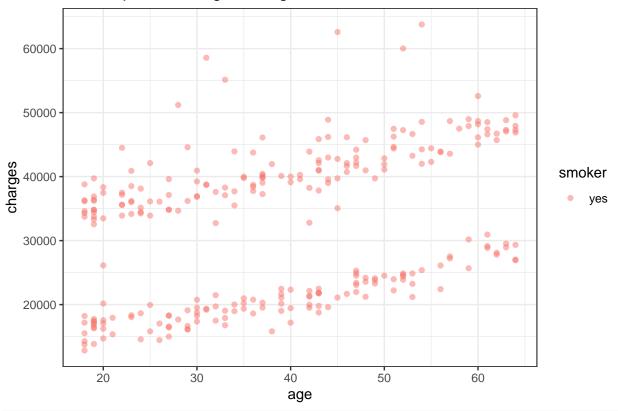
ggplot(aes(x=bmi, y=charges, color=smoker), data=smokers) +
  labs(title="Scatter Plot of Charges vs BMI For Smokers") +
  theme_bw() +
  geom_point()</pre>
```

# Scatter Plot of Charges vs BMI For Smokers



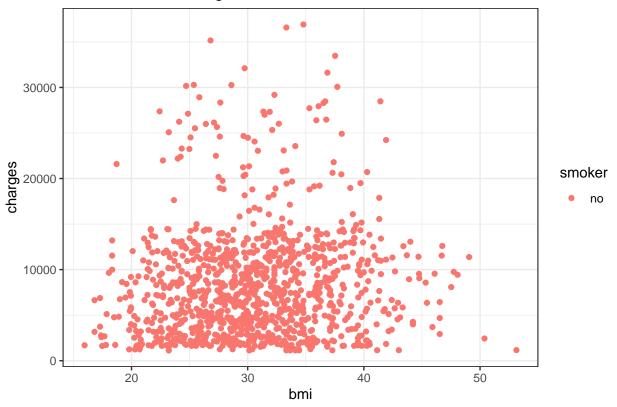
```
ggplot(aes(x=age,y=charges, color=smoker), data=smokers) +
labs(title="Scatter plot of Charges vs Age For Smokers") +
theme_bw() +
geom_point(alpha=0.5)
```

## Scatter plot of Charges vs Age For Smokers



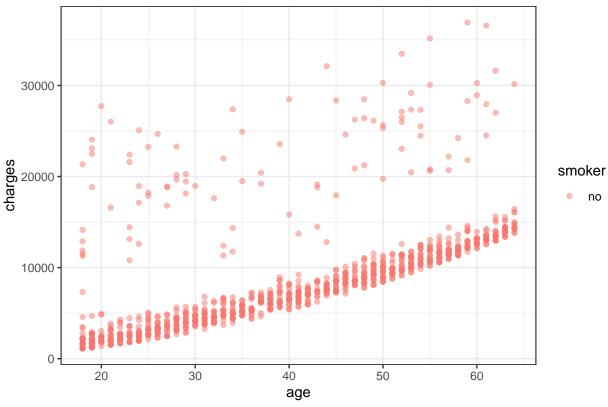
```
ggplot(aes(x=bmi, y=charges, color=smoker), data=non_smokers) +
labs(title="Scatter Plot of Charges vs BMI For Non_Smokers") +
theme_bw() +
geom_point()
```

## Scatter Plot of Charges vs BMI For Non\_Smokers



```
ggplot(aes(x=age,y=charges, color=smoker), data=non_smokers) +
labs(title="Scatter plot of Charges vs Age For Non_Smokers") +
theme_bw() +
geom_point(alpha=0.5)
```

## Scatter plot of Charges vs Age For Non\_Smokers



```
## Smokers
##intercept only model
regnull_smoker <- lm(charges~1, data=smokers)
##model with all predictors
regfull_smoker <- lm(charges ~ age + sex + bmi + children + region , data=smokers)</pre>
```

#### Forward Selection

```
step(regnull_smoker, scope=list(lower=regnull_smoker, upper=regfull_smoker), direction="forward")
```

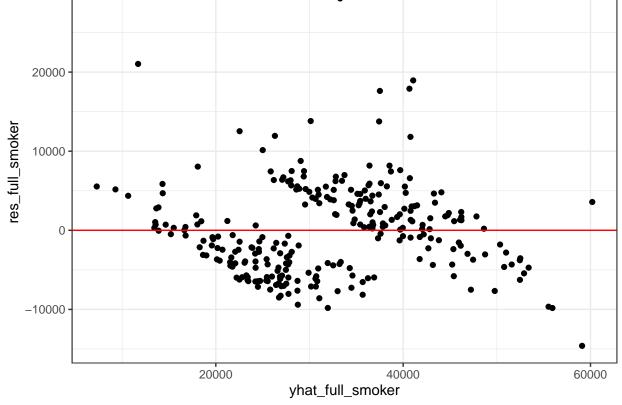
```
## Start: AIC=5126.83
## charges ~ 1
##
##
              Df Sum of Sq
                                   RSS
                                          AIC
## + bmi
               1 2.3653e+10 1.2713e+10 4840.9
## + age
               1 4.9308e+09 3.1435e+10 5088.9
               3 1.2923e+09 3.5073e+10 5122.9
## + region
## + sex
               1 3.7263e+08 3.5993e+10 5126.0
## <none>
                            3.6366e+10 5126.8
## + children 1 4.6986e+07 3.6319e+10 5128.5
##
## Step: AIC=4840.86
## charges ~ bmi
##
              Df Sum of Sq
##
                                   RSS
                                          AIC
               1 3739448620 8.9736e+09 4747.4
## + age
                            1.2713e+10 4840.9
## <none>
                   77371010 1.2636e+10 4841.2
## + children 1
```

```
1 12609906 1.2700e+10 4842.6
## + region
               3 112969895 1.2600e+10 4844.4
## Step: AIC=4747.41
## charges ~ bmi + age
##
##
              Df Sum of Sq
                                  RSS
                           8973564816 4747.4
## <none>
## + region
               3 149563719 8824001097 4748.8
## + children 1 14356763 8959208053 4749.0
## + sex
                 7002694 8966562122 4749.2
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers)
## Coefficients:
## (Intercept)
                        bmi
                                     age
      -22367.4
                     1438.1
                                   266.3
#Non smokers
regnull_non_smokers <- lm(charges~1, data=non_smokers)</pre>
##model with all predictors
regfull_non_smokers <- lm(charges ~ age + sex + bmi + children + region , data=non_smokers)
Forward Selection
step(regnull_non_smokers, scope=list(lower=regnull_non_smokers, upper=regfull_non_smokers), direction="
## Start: AIC=18511.36
## charges ~ 1
##
##
              Df Sum of Sq
                                   RSS
## + age
               1 1.5058e+10 2.3130e+10 17980
## + children 1 7.3709e+08 3.7452e+10 18493
              1 2.6969e+08 3.7919e+10 18506
## + bmi
               1 1.2113e+08 3.8068e+10 18510
## + sex
               3 2.3153e+08 3.7957e+10 18511
## + region
## <none>
                            3.8189e+10 18511
## Step: AIC=17979.87
## charges ~ age
##
              Df Sum of Sq
                                  RSS
## + children 1 531956489 2.2598e+10 17957
## + region
               3 248975743 2.2881e+10 17974
## + sex
               1 68342342 2.3062e+10 17979
## <none>
                           2.3130e+10 17980
                   1914187 2.3128e+10 17982
## + bmi
##
## Step: AIC=17957.12
## charges ~ age + children
##
##
            Df Sum of Sq
                                RSS
                                      AIC
## + region 3 262141210 2.2336e+10 17951
## + sex 1 69429619 2.2529e+10 17956
```

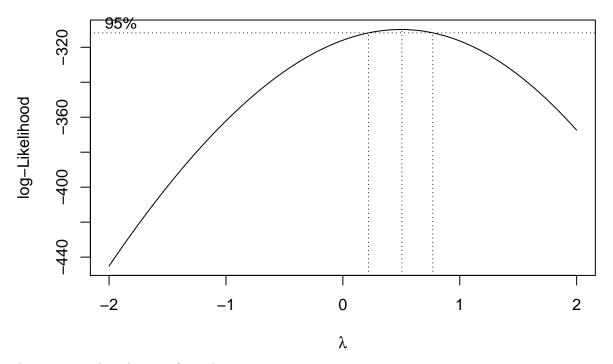
```
## <none>
                         2.2598e+10 17957
## + bmi
                1065536 2.2597e+10 17959
##
## Step: AIC=17950.7
## charges ~ age + children + region
##
         Df Sum of Sq
## + sex
          1 72093470 2.2264e+10 17949
## <none>
                       2.2336e+10 17951
## + bmi 1 11274021 2.2325e+10 17952
##
## Step: AIC=17949.26
## charges ~ age + children + region + sex
##
##
         Df Sum of Sq
                             RSS
## <none>
                       2.2264e+10 17949
## + bmi
          1 12614493 2.2251e+10 17951
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smokers)
##
## Coefficients:
##
       (Intercept)
                                            children regionnorthwest
                                age
          -1695.9
                              265.5
                                               589.1
                                                               -550.2
##
## regionsoutheast regionsouthwest
                                             sexmale
##
           -913.2
                            -1373.0
                                              -521.0
We get different models
mlr_full_smoker = lm(charges ~ bmi+age , data=smokers)
summary(mlr_full_smoker)
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers)
## Residuals:
       Min
                 1Q
                     Median
                                    3Q
                                            Max
## -14604.4 -4315.1
                      -240.5
                                3638.0 29316.7
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -22367.45
                           1931.86 -11.58
                                              <2e-16 ***
                1438.09
                              55.22
                                    26.05
                                              <2e-16 ***
## bmi
## age
                 266.29
                              25.06
                                    10.63
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5754 on 271 degrees of freedom
## Multiple R-squared: 0.7532, Adjusted R-squared: 0.7514
## F-statistic: 413.6 on 2 and 271 DF, p-value: < 2.2e-16
```

yhat\_full\_smoker <- mlr\_full\_smoker\$fitted.values
res\_full\_smoker <- mlr\_full\_smoker\$residuals</pre>

```
smokers %>%
  ggplot(aes(yhat_full_smoker, res_full_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



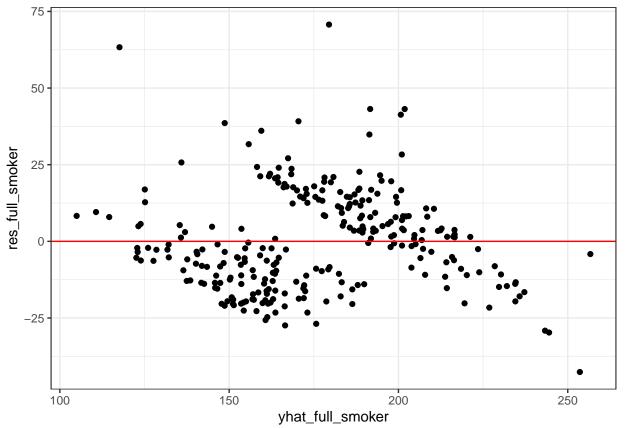
boxcox(mlr\_full\_smoker)



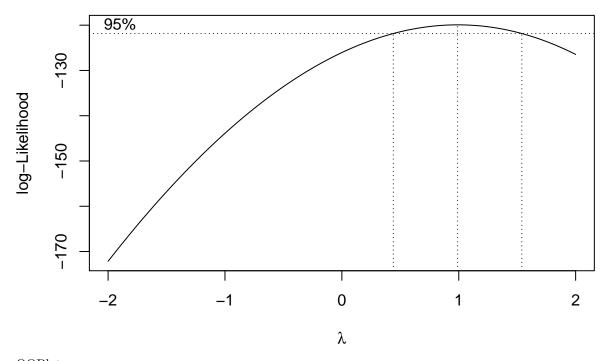
Rseponse needs to be transformed

```
smokers_transform <- smokers</pre>
smokers_transform$charges <- smokers_transform$charges^0.5</pre>
mlr_full_smoker_transform = lm(charges ~ bmi+age , data=smokers_transform)
mlr_full_smoker_transform_full = lm(charges ~ bmi+age + sex + region , data=smokers_transform)
summary(mlr_full_smoker_transform)
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers_transform)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -42.622 -12.877 -1.715 10.868
##
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 19.9145
                            5.4586
                                     3.648 0.000317 ***
                 4.1245
                            0.1560
                                    26.436 < 2e-16 ***
## bmi
                 0.7634
                            0.0708 10.781 < 2e-16 ***
## age
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.26 on 271 degrees of freedom
## Multiple R-squared: 0.7587, Adjusted R-squared: 0.7569
## F-statistic: 426.1 on 2 and 271 DF, p-value: < 2.2e-16
yhat_full_smoker <- mlr_full_smoker_transform$fitted.values</pre>
res_full_smoker <- mlr_full_smoker_transform$residuals</pre>
smokers %>%
```

```
ggplot(aes(yhat_full_smoker, res_full_smoker)) +
geom_point() +
theme_bw() +
geom_hline(yintercept = 0, color="red")
```

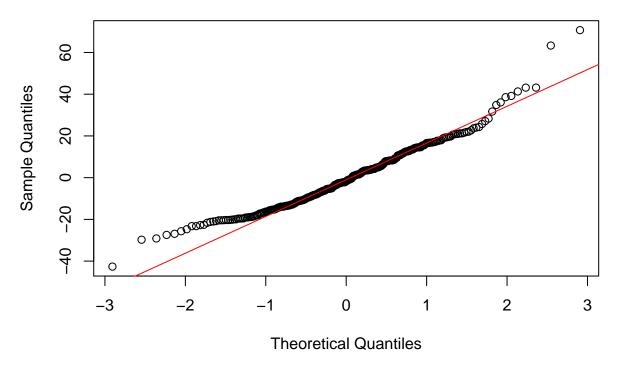


boxcox(mlr\_full\_smoker\_transform)



```
QQPlot
{
   qqnorm(mlr_full_smoker_transform$residuals)
   qqline(mlr_full_smoker_transform$residuals, col="red")
}
```

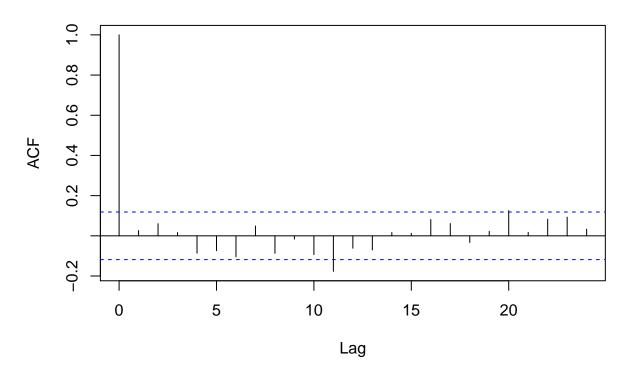
## Normal Q-Q Plot



ACF

acf(mlr\_full\_smoker\_transform\$residuals, main="ACF")

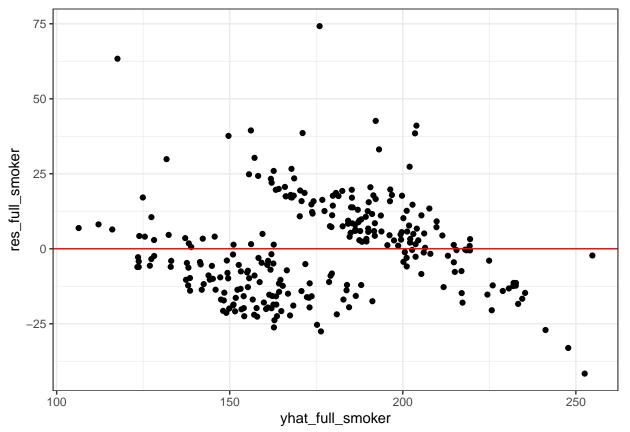
### **ACF**



## What about Region

```
mlr_full_smoker_full = lm(charges ~ bmi+age+children+region , data=smokers_transform)
summary(mlr_full_smoker_full)
##
## Call:
## lm(formula = charges ~ bmi + age + children + region, data = smokers_transform)
##
## Residuals:
       Min
                1Q Median
                                ЗQ
                                       Max
## -41.603 -12.339 -0.845
                             9.705 74.211
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   18.58918
                               5.66726
                                         3.280 0.00118 **
                    4.21653
                               0.16320
                                       25.837
                                               < 2e-16 ***
## bmi
## age
                    0.76698
                               0.07129
                                       10.759
                                               < 2e-16 ***
## children
                    0.53142
                               0.85647
                                        0.620 0.53547
## regionnorthwest -1.53030
                               2.92036
                                       -0.524 0.60071
## regionsoutheast -5.14260
                               2.71691
                                       -1.893 0.05946 .
## regionsouthwest -0.93879
                               2.94778 -0.318 0.75038
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 16.23 on 267 degrees of freedom
```

```
## Multiple R-squared: 0.763, Adjusted R-squared: 0.7577
## F-statistic: 143.3 on 6 and 267 DF, p-value: < 2.2e-16
yhat_full_smoker <- mlr_full_smoker_full$fitted.values
res_full_smoker <- mlr_full_smoker_full$residuals
smokers %>%
    ggplot(aes(yhat_full_smoker, res_full_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



Residual Seems Fine, can we drop these predictors?

```
summary(mlr_full_smoker_transform)
```

```
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers_transform)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
##
   -42.622 -12.877 -1.715 10.868
                                    70.699
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 19.9145
                            5.4586
                                     3.648 0.000317 ***
                 4.1245
                            0.1560 26.436 < 2e-16 ***
## bmi
## age
                 0.7634
                            0.0708 10.781 < 2e-16 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.26 on 271 degrees of freedom
## Multiple R-squared: 0.7587, Adjusted R-squared: 0.7569
## F-statistic: 426.1 on 2 and 271 DF, p-value: < 2.2e-16
anova(mlr_full_smoker_transform,mlr_full_smoker_transform_full )
## Analysis of Variance Table
##
## Model 1: charges ~ bmi + age
## Model 2: charges ~ bmi + age + sex + region
             RSS Df Sum of Sq
    Res.Df
                                   F Pr(>F)
## 1
       271 71645
        267 70442 4
## 2
                        1202.7 1.1396 0.3382
We can drop these other predictors
```

#### **Outliers**

```
##critical value using Bonferroni procedure
n<-dim(smokers_transform)[1]</pre>
p<-3
crit < -qt(1-0.05/(2*n), n-1-p)
##externally studentized residuals
ext.student.res<-rstudent(mlr_full_smoker_transform)
##identify
ext.student.res[abs(ext.student.res)>crit]
##
        129
                1301
## 4.041989 4.510779
##leverages
lev<-lm.influence(mlr_full_smoker_transform)$hat</pre>
##identify
round(lev[lev>2*p/n],4)
##
      251
             293
                    413
                            544
                                   550
                                           665
                                                  804
                                                         861
                                                                1048
                                                                       1125
                                                                              1157
## 0.0268 0.0284 0.0226 0.0326 0.0258 0.0224 0.0251 0.0301 0.0547 0.0225 0.0307
DFFITS<-dffits(mlr_full_smoker_transform)</pre>
round(DFFITS[abs(DFFITS)>2*sqrt(p/n)],3)
##
      129
             293
                    550
                            578
                                   820
                                           861
                                                  918
                                                        1048
                                                               1157
                                                                       1231
                                                                              1301
                                               0.246 -0.656 -0.225
## 0.569 -0.231 -0.297 0.260 0.218 -0.329
                                                                      0.244
                                                                             0.302
DFBETAS<-dfbetas(mlr_full_smoker_transform)</pre>
tempdfbetas = abs(DFBETAS)>2/sqrt(n)
tempdfbetas[(tempdfbetas[,1] == TRUE | tempdfbetas[,2] == TRUE | tempdfbetas[,3] == TRUE ) ,]
##
        (Intercept)
                      bmi
                             age
              FALSE TRUE FALSE
## 35
## 95
              FALSE FALSE TRUE
## 129
               TRUE TRUE FALSE
## 293
              FALSE
                     TRUE FALSE
## 477
              FALSE FALSE TRUE
## 531
               TRUE FALSE FALSE
               TRUE TRUE FALSE
## 550
```

```
## 578
             FALSE TRUE FALSE
## 675
              TRUE TRUE FALSE
## 820
             FALSE TRUE FALSE
## 861
              TRUE TRUE FALSE
## 918
              TRUE TRUE FALSE
## 952
              TRUE TRUE FALSE
## 1048
              TRUE TRUE TRUE
             FALSE FALSE TRUE
## 1140
## 1147
             FALSE FALSE TRUE
## 1157
             FALSE TRUE FALSE
             FALSE FALSE TRUE
## 1197
## 1224
              TRUE FALSE TRUE
## 1231
              TRUE FALSE TRUE
## 1232
              TRUE FALSE FALSE
## 1301
             FALSE FALSE TRUE
## 1302
             FALSE FALSE TRUE
COOKS<-cooks.distance(mlr_full_smoker_transform)
COOKS[COOKS>qf(0.5,p,n-p)]
```

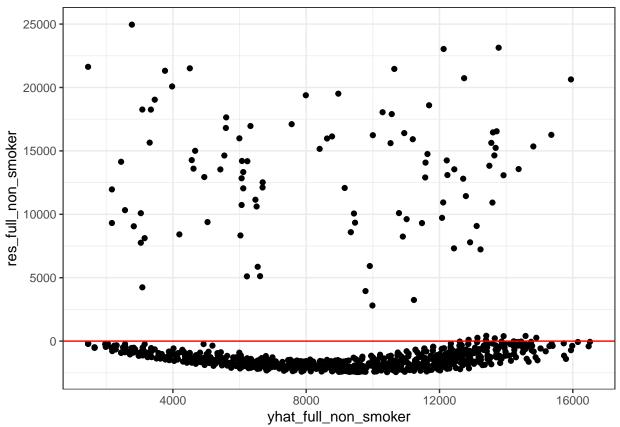
# Non Smokers

## named numeric(0)

```
mlr_full_non_smoker = lm(formula = charges ~ age + children + region + sex, data = non_smokers)
```

```
summary(mlr_full_non_smoker)
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smokers)
## Residuals:
               1Q Median
##
                                3Q
## -2441.2 -1870.1 -1380.6 -673.9 24954.7
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                  -1695.87
                               520.71 -3.257 0.001162 **
## (Intercept)
## age
                    265.53
                                10.01 26.524 < 2e-16 ***
## children
                    589.06
                                115.67
                                        5.093 4.18e-07 ***
## regionnorthwest -550.17
                               401.17 -1.371 0.170544
## regionsoutheast -913.18
                               398.99 -2.289 0.022293 *
## regionsouthwest -1372.97
                               401.23 -3.422 0.000646 ***
## sexmale
                   -521.01
                                281.62 -1.850 0.064585 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4589 on 1057 degrees of freedom
## Multiple R-squared: 0.417, Adjusted R-squared: 0.4137
                 126 on 6 and 1057 DF, p-value: < 2.2e-16
## F-statistic:
yhat_full_non_smoker <- mlr_full_non_smoker$fitted.values</pre>
res_full_non_smoker <- mlr_full_non_smoker$residuals
non_smokers %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
```

```
geom_point() +
theme_bw() +
geom_hline(yintercept = 0, color="red")
```



#### Transformation

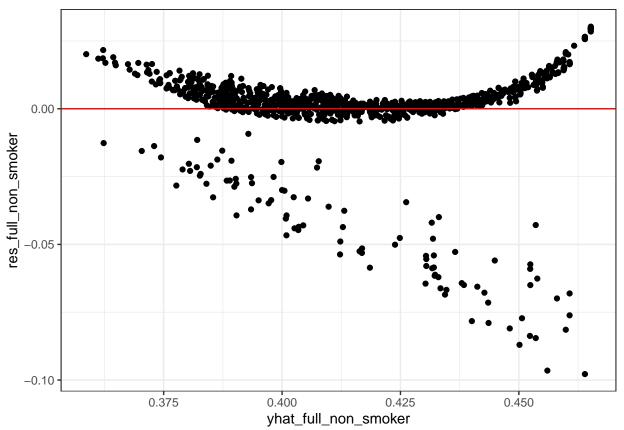
boxcox(mlr\_full\_non\_smoker, c(-0.5, 0.5, 0.1))

```
95%
     -2800
log-Likelihood
     -2850
     -2900
     -2950
                  -0.4
                                -0.2
                                                            0.2
                                              0.0
                                                                          0.4
                                               λ
non_smoker_transform <- non_smokers</pre>
non_smoker_transform$charges <- non_smoker_transform$charges^(-0.1)</pre>
mlr_full_non_smoker_transform = lm(formula = charges ~ age + children + region + sex, data = non_smoker
summary(mlr full non smoker transform)
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smoker_transform)
##
## Residuals:
         Min
##
                    1Q
                           Median
                                         3Q
                                                   Max
   -0.097790 -0.000251 0.002357 0.006879
##
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    4.853e-01 1.947e-03 249.214 < 2e-16 ***
## age
                   -1.762e-03 3.744e-05 -47.072 < 2e-16 ***
## children
                   -5.651e-03 4.326e-04 -13.065 < 2e-16 ***
## regionnorthwest
                   3.100e-03 1.500e-03
                                            2.066
                                                    0.0391 *
## regionsoutheast 7.149e-03 1.492e-03
                                            4.792 1.89e-06 ***
## regionsouthwest 7.667e-03 1.500e-03
                                            5.110 3.82e-07 ***
## sexmale
                    4.482e-03 1.053e-03
                                            4.256 2.27e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
\#\# Residual standard error: 0.01716 on 1057 degrees of freedom
## Multiple R-squared: 0.7023, Adjusted R-squared: 0.7006
## F-statistic: 415.6 on 6 and 1057 DF, p-value: < 2.2e-16
yhat_full_non_smoker <- mlr_full_non_smoker_transform$fitted.values</pre>
res_full_non_smoker <- mlr_full_non_smoker_transform$residuals
```

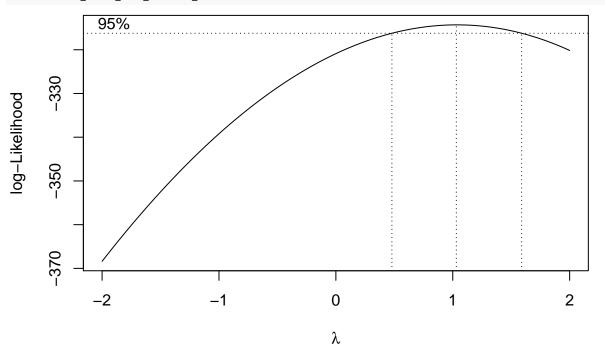
ggplot(aes(yhat\_full\_non\_smoker, res\_full\_non\_smoker)) +

non\_smokers %>%

```
geom_point() +
theme_bw() +
geom_hline(yintercept = 0, color="red")
```

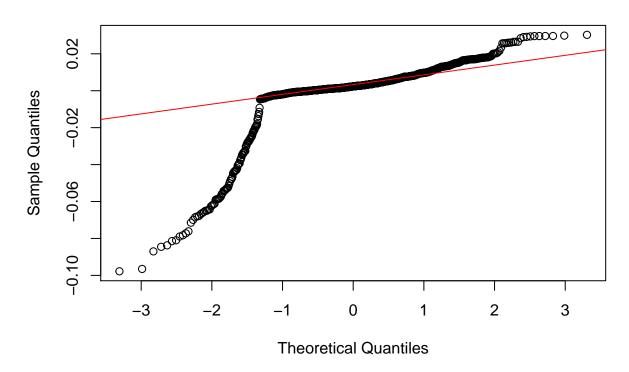


boxcox(mlr\_full\_non\_smoker\_transform)



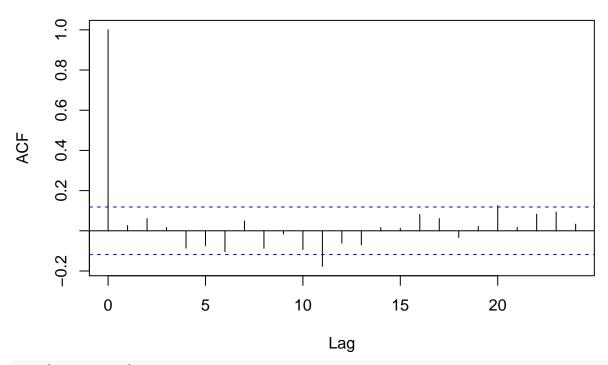
# QQPlot { qqnorm(mlr\_full\_non\_smoker\_transform\$residuals) qqline(mlr\_full\_non\_smoker\_transform\$residuals, col="red") }

## Normal Q-Q Plot

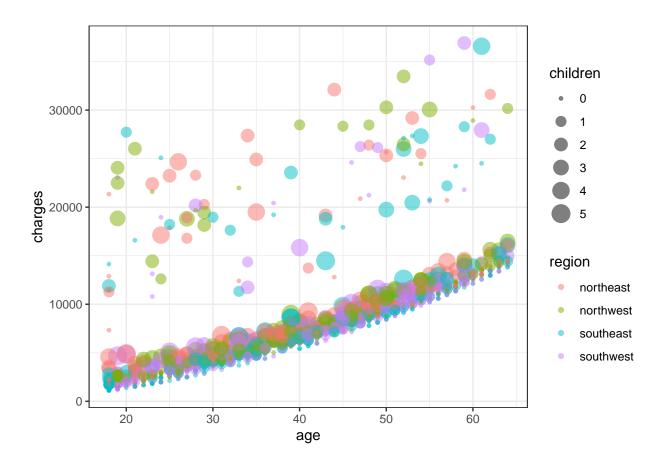


ACF
acf(mlr\_full\_smoker\_transform\$residuals, main="ACF")

## **ACF**



```
head(non_smokers)
                   bmi children smoker
                                          region
                                                    charges significant.charge
##
     age
            sex
## 2
           male 33.770
                                    no southeast
                                                  1725.552
                                                                         FALSE
     18
                              1
## 3
      28
           male 33.000
                              3
                                    no southeast
                                                  4449.462
                                                                         FALSE
           male 22.705
                                                                          TRUE
## 4
     33
                              0
                                    no northwest 21984.471
## 5
     32
           male 28.880
                              0
                                    no northwest
                                                  3866.855
                                                                         FALSE
## 6 31 female 25.740
                                    no southeast
                                                  3756.622
                                                                         FALSE
                              0
## 7 46 female 33.440
                                    no southeast
                                                  8240.590
                                                                         FALSE
                              1
# charges ~ age + children + region + sex
non_smokers %>%
  ggplot(aes(x=age, y=charges, color=region, size=children)) +
  theme_bw() +
  geom_point(alpha=0.5)
```



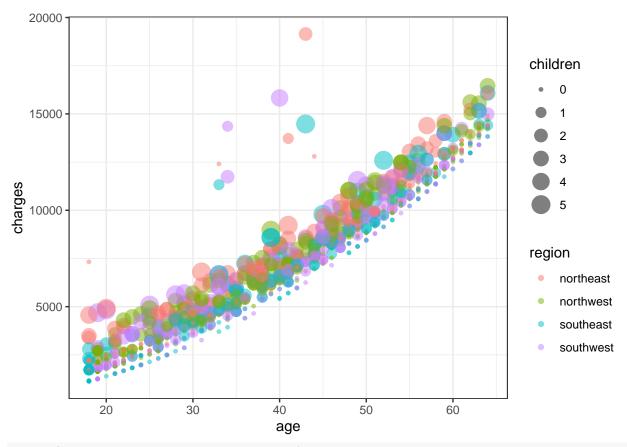
## Lets drop these outliers.

## regionsouthwest -656.634

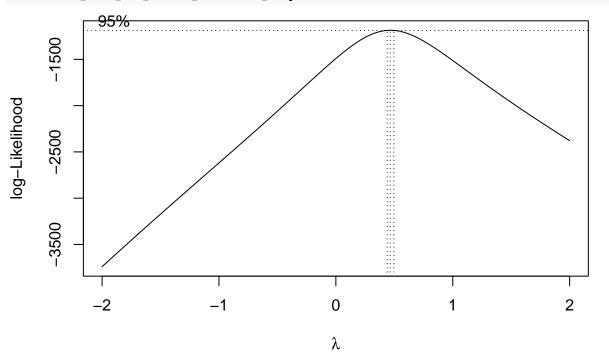
```
drop_outleirs <- non_smokers</pre>
DFFITS<-dffits(mlr_full_non_smoker)</pre>
want_drop = names(DFFITS[abs(DFFITS)>2*sqrt(5/1064)])
drop_outleirs = non_smokers[setdiff(rownames(non_smokers), want_drop),]
(dim(non_smokers)[1] - dim(drop_outleirs)[1]) / dim(non_smokers)[1]
## [1] 0.08364662
mlr_full_non_smoker_transform_drop = lm(formula = charges ~ region + age + children + sex, data = drop
summary(mlr_full_non_smoker_transform_drop)
##
## Call:
## lm(formula = charges ~ region + age + children + sex, data = drop_outleirs)
##
## Residuals:
##
      Min
              1Q Median
                            ЗQ
                                  Max
## -957.1 -528.9 -157.0 377.4 9979.3
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -3191.858
                                106.474 -29.978 < 2e-16 ***
## regionnorthwest -380.203
                                 81.624 -4.658 3.64e-06 ***
## regionsoutheast -693.456
                                 81.505 -8.508 < 2e-16 ***
```

81.119 -8.095 1.71e-15 \*\*\*

```
265.832
                                  2.041 130.242 < 2e-16 ***
## age
                     463.159
                                 23.342 19.842 < 2e-16 ***
## children
## sexmale
                    -461.038
                                 57.043 -8.082 1.88e-15 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 889.8 on 968 degrees of freedom
## Multiple R-squared: 0.9486, Adjusted R-squared: 0.9483
## F-statistic: 2979 on 6 and 968 DF, p-value: < 2.2e-16
yhat_full_non_smoker <- mlr_full_non_smoker_transform_drop$fitted.values</pre>
res_full_non_smoker <- mlr_full_non_smoker_transform_drop$residuals</pre>
drop_outleirs %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
  10000
   7500
res_full_non_smoker
   5000
   2500
                                 5000
                                                           10000
                                                                                    15000
                                      yhat_full_non_smoker
drop_outleirs %>%
  ggplot(aes(x=age, y=charges, color=region, size=children)) +
  theme_bw() +
  geom_point(alpha=0.5)
```

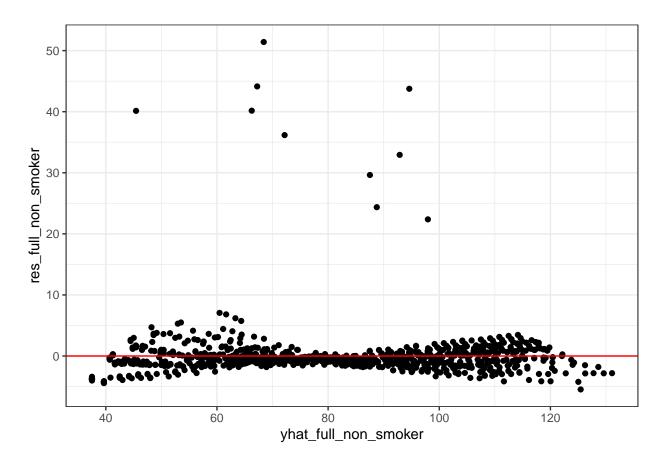


boxcox(mlr\_full\_non\_smoker\_transform\_drop)



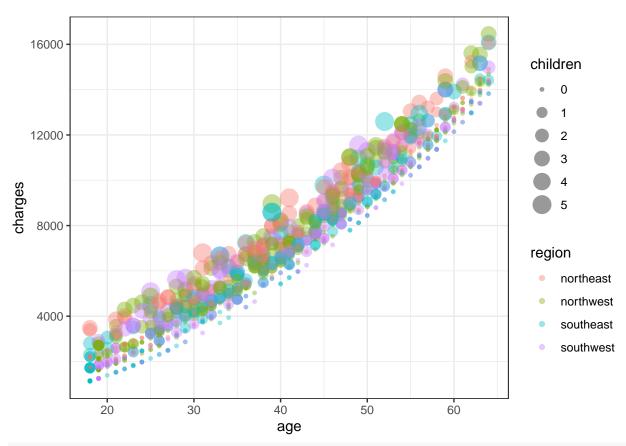
mlr\_full\_non\_smoker\_transform\_drop2 = lm(formula = (charges)^0.5 ~ age + children + region + sex, data summary(mlr\_full\_non\_smoker\_transform\_drop2)

```
##
## Call:
## lm(formula = (charges)^0.5 ~ age + children + region + sex, data = drop_outleirs)
## Residuals:
##
    Min
            1Q Median
                         3Q
## -5.473 -1.294 -0.488 0.603 51.411
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                 ## (Intercept)
                 1.666084 0.009543 174.593 < 2e-16 ***
## age
## children
                          0.109132 34.436 < 2e-16 ***
                  3.758067
## regionnorthwest -2.264117   0.381620   -5.933   4.14e-09 ***
## regionsouthwest -4.244789 0.379261 -11.192 < 2e-16 ***
## sexmale
                -3.195678
                          0.266695 -11.983 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.16 on 968 degrees of freedom
## Multiple R-squared: 0.9713, Adjusted R-squared: 0.9711
## F-statistic: 5462 on 6 and 968 DF, p-value: < 2.2e-16
yhat_full_non_smoker <- mlr_full_non_smoker_transform_drop2$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_transform_drop2$residuals
drop outleirs %>%
 ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
 geom_point() +
 theme_bw() +
 geom_hline(yintercept = 0, color="red")
```



## Second dropping

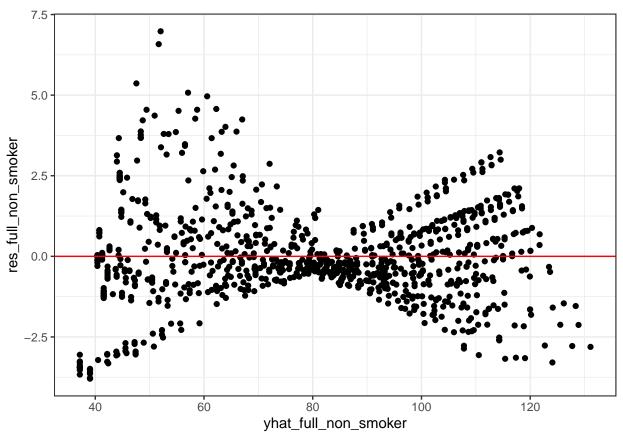
```
drop_outleirs2 <- drop_outleirs</pre>
DFFITS<-dffits(mlr_full_non_smoker_transform_drop2)</pre>
want_drop = names(DFFITS[abs(DFFITS)>2*sqrt(5/975)])
drop_outleirs2 = drop_outleirs[setdiff(rownames(drop_outleirs), want_drop),]
(dim(drop_outleirs)[1] - dim(drop_outleirs2)[1]) / dim(drop_outleirs)[1]
## [1] 0.01538462
(dim(non_smokers)[1] - dim(drop_outleirs2)[1]) / dim(non_smokers)[1]
## [1] 0.09774436
head(drop_outleirs2)
##
                  bmi children smoker
                                         region charges significant.charge
     age
            sex
                             1
                                                                       FALSE
## 2 18
           male 33.77
                                   no southeast 1725.552
           male 33.00
                             3
                                   no southeast 4449.462
                                                                       FALSE
## 3 28
           male 28.88
                                   no northwest 3866.855
                                                                       FALSE
## 5 32
                             0
     31 female 25.74
                             0
                                   no southeast 3756.622
                                                                       FALSE
## 6
## 7 46 female 33.44
                             1
                                   no southeast 8240.590
                                                                       FALSE
## 8 37 female 27.74
                                   no northwest 7281.506
                                                                       FALSE
drop_outleirs2 %>%
  ggplot(aes(x=age, y=charges, color=region, size=children)) +
  geom_point(alpha = 0.4) + theme_bw()
```



mlr\_full\_non\_smoker\_transform\_drop3 = lm(formula = (charges)^0.5 ~ region + age + children + sex, data
summary(mlr\_full\_non\_smoker\_transform\_drop3)

```
##
## Call:
## lm(formula = (charges)^0.5 ~ region + age + children + sex, data = drop_outleirs2)
##
## Residuals:
      Min
               1Q Median
## -3.7948 -0.7606 -0.1970 0.8076 6.9809
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                 ## (Intercept)
## regionnorthwest -1.388811 0.138855 -10.00
                                              <2e-16 ***
## regionsoutheast -4.108629 0.138912 -29.58
                                              <2e-16 ***
## regionsouthwest -3.918607
                            0.138610 -28.27
                                               <2e-16 ***
                            0.003466 484.30
## age
                  1.678697
                                               <2e-16 ***
## children
                 3.585316
                            0.040673
                                      88.15
                                               <2e-16 ***
                                              <2e-16 ***
## sexmale
                 -3.230049
                            0.096866 -33.34
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.499 on 953 degrees of freedom
## Multiple R-squared: 0.9962, Adjusted R-squared: 0.9962
## F-statistic: 4.199e+04 on 6 and 953 DF, p-value: < 2.2e-16
```

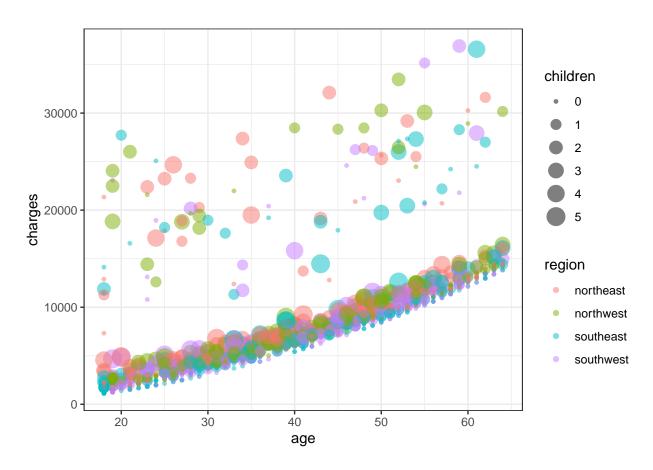
```
yhat_full_non_smoker <- mlr_full_non_smoker_transform_drop3$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_transform_drop3$residuals
drop_outleirs2 %>%
    ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



## **Next Steps**

We need to find for non smokers what is causing some data points to be more charges...?

```
non_smokers %>%
  ggplot(aes(x=age, y=charges, size=children, color=region)) +
  theme_bw() +
  geom_point(alpha=0.5)
```



## Try checking log of age?

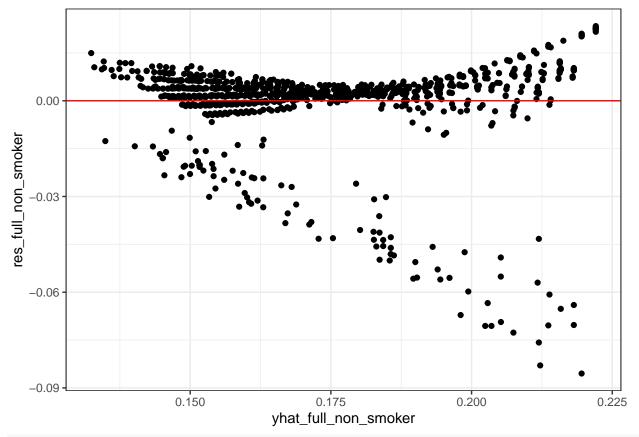
```
mlr_full_non_smoker_log_age = lm(formula = (charges)^(-0.2) ~ log(age) + children + region + sex, data
summary(mlr_full_non_smoker_log_age)
##
## Call:
## lm(formula = (charges)^(-0.2) \sim log(age) + children + region +
##
       sex, data = non_smokers)
##
```

```
## Residuals:
##
                          Median
        Min
                    1Q
                                        3Q
                                                 Max
## -0.085480 -0.000036 0.002798 0.005271 0.023402
```

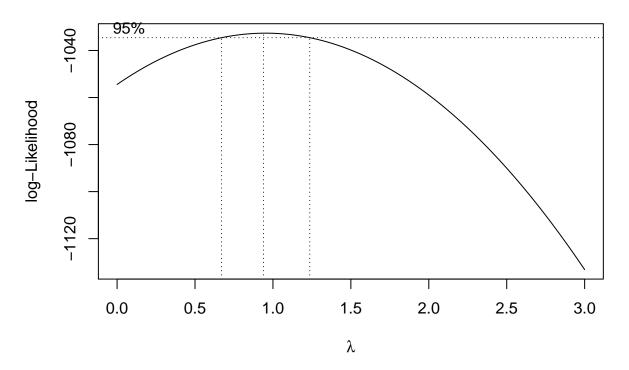
##

```
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   0.3701217  0.0040794  90.730  < 2e-16 ***
## log(age)
                  -0.0547231 0.0011007 -49.717 < 2e-16 ***
                  -0.0041158  0.0003533  -11.650  < 2e-16 ***
## children
## regionnorthwest
                  0.0027735 0.0012218
                                          2.270
                                                  0.0234 *
## regionsoutheast 0.0062215 0.0012152
                                          5.120 3.63e-07 ***
## regionsouthwest 0.0066586 0.0012221
                                          5.449 6.32e-08 ***
## sexmale
                   0.0039021 0.0008578
                                          4.549 6.01e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
## Residual standard error: 0.01398 on 1057 degrees of freedom
## Multiple R-squared: 0.7255, Adjusted R-squared: 0.724
## F-statistic: 465.7 on 6 and 1057 DF, p-value: < 2.2e-16
yhat_full_non_smoker <- mlr_full_non_smoker_log_age$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_log_age$residuals
non_smokers %>%
    ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



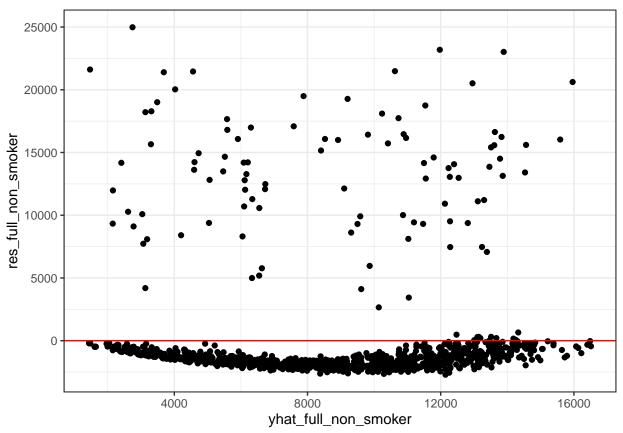
boxcox(mlr\_full\_non\_smoker\_log\_age, c(0,3,0.1))



#### Interaction age and region?

```
mlr_full_non_smoker_region_inter = lm(formula = charges ~ (age)*bmi + region + children + sex, data = n
summary(mlr_full_non_smoker_region_inter)
##
## Call:
  lm(formula = charges ~ (age) * bmi + region + children + sex,
##
       data = non_smokers)
##
## Residuals:
                10 Median
                                3Q
  -2709.7 -1866.9 -1359.3 -677.6 24979.9
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              2129.9278
                                         -0.564 0.572731
                   -1201.7270
## age
                     238.4680
                                 51.6271
                                           4.619 4.33e-06 ***
                                 68.4291
                                          -0.202 0.839749
## bmi
                     -13.8407
## regionnorthwest
                    -544.8748
                                401.4481
                                          -1.357 0.174985
## regionsoutheast
                    -985.7698
                                412.2071
                                          -2.391 0.016957 *
## regionsouthwest -1400.7248
                                402.5979
                                          -3.479 0.000523 ***
## children
                     586.8693
                                115.7543
                                           5.070 4.70e-07 ***
## sexmale
                    -531.6770
                                282.0645
                                          -1.885 0.059711 .
## age:bmi
                                  1.6427
                                           0.514 0.607489
                       0.8441
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 4592 on 1055 degrees of freedom
## Multiple R-squared: 0.4175, Adjusted R-squared: 0.4131
## F-statistic: 94.51 on 8 and 1055 DF, p-value: < 2.2e-16
```

```
yhat_full_non_smoker <- mlr_full_non_smoker_region_inter$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_region_inter$residuals
non_smokers %>%
    ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
    geom_point() +
    theme_bw() +
    geom_hline(yintercept = 0, color="red")
```



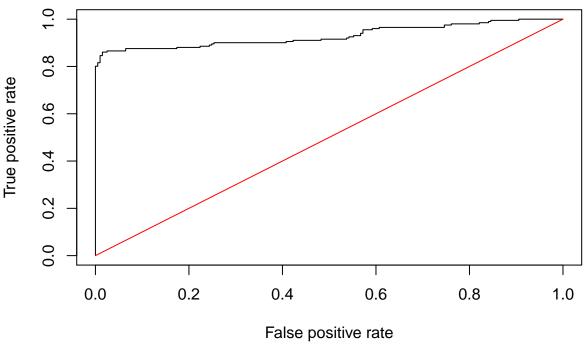
## Logistic

##

```
set.seed(6021) ##for reproducibility
sample<-sample.int(nrow(data), floor(.70*nrow(data)), replace = F)</pre>
train<- data[sample, ] ##training data frame</pre>
test<-data[-sample, ] ##test data frame</pre>
result <-glm(significant.charge ~ age + bmi + children + smoker + region, family="binomial", data=train)
summary(result)
##
## glm(formula = significant.charge ~ age + bmi + children + smoker +
       region, family = "binomial", data = train)
##
##
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                    3Q
                                            Max
## -1.5958 -0.3482 -0.0324
                              0.3666
                                         3.3946
```

```
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
                -9.34931 0.89151 -10.487 < 2e-16 ***
## (Intercept)
                   ## age
                                      1.831 0.06709 .
## bmi
                   0.03621 0.01978
## children
                   ## smokeryes
                  22.65853 598.12679 0.038 0.96978
## regionnorthwest -0.45803 0.31756 -1.442 0.14921
## regionsoutheast -0.86352 0.33350 -2.589 0.00962 **
## regionsouthwest -0.50195 0.32102 -1.564 0.11791
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1297.57 on 935 degrees of freedom
## Residual deviance: 507.03 on 928 degrees of freedom
## AIC: 523.03
## Number of Fisher Scoring iterations: 18
library(ROCR)
## Warning: package 'ROCR' was built under R version 4.0.2
##predicted survival rate for test data based on training data
preds<-predict(result,newdata=test, type="response")</pre>
##transform the input data into a format that is suited for the
##performance() function
rates<-prediction(preds, test$significant.charge)</pre>
##store the true positive and false positive rates
roc_result<-performance(rates,measure="tpr", x.measure="fpr")</pre>
##plot ROC curve and overlay the diagonal line for random guessing
plot(roc_result, main="ROC Curve")
lines(x = c(0,1), y = c(0,1), col="red")
```

## **ROC Curve**



```
##compute the AUC
auc<-performance(rates, measure = "auc")</pre>
auc@y.values
## [[1]]
## [1] 0.9299522
Matrix
table(test$significant.charge, preds>0.5)
##
##
           FALSE TRUE
              180
##
     FALSE
                    21
##
     TRUE
               25
                   176
Threshold value manipulation
table(test$significant.charge, preds>0.25)
```

Doesn't play a huge role in decreasing the False Positive Rate. We want to make sure that when someone signs up for a plan that they don't get charged significantly given their condition.

```
test<-data.frame(test,preds)
ggplot(test,aes(x=preds))+
geom_density()+
labs(title="Density Plot of Predicted Probs") + theme_bw()</pre>
```

## Density Plot of Predicted Probs

