

Project

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11/11/2021

```
## Data Processing
library(tidyverse)

## Warning: package 'tidyverse' was built under R version 4.0.2
## -- Attaching packages -----
## v ggplot2 3.3.2    v purrr   0.3.4
## v tibble  3.0.1    v dplyr  1.0.2
## v tidyr   1.1.2    v stringr 1.4.0
## v readr   1.4.0    v forcats 0.5.0
## Warning: package 'ggplot2' was built under R version 4.0.2
## Warning: package 'tidyr' was built under R version 4.0.2
## Warning: package 'readr' was built under R version 4.0.2
## Warning: package 'dplyr' was built under R version 4.0.2
## Warning: package 'stringr' was built under R version 4.0.2
## Warning: package 'forcats' was built under R version 4.0.2
## -- Conflicts -----
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()
library(dplyr)
library(MASS)

## Warning: package 'MASS' was built under R version 4.0.2
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##      select
library(leaps)

## Warning: package 'leaps' was built under R version 4.0.2
setwd("/Users/maxryoo/Documents/MSDS/STAT6021/Project2")
data <- read.csv("data/insurance.csv")
head(data)

##   age    sex    bmi children smoker   region  charges
## 1  19 female 27.900         0    yes southwest 16884.924
```

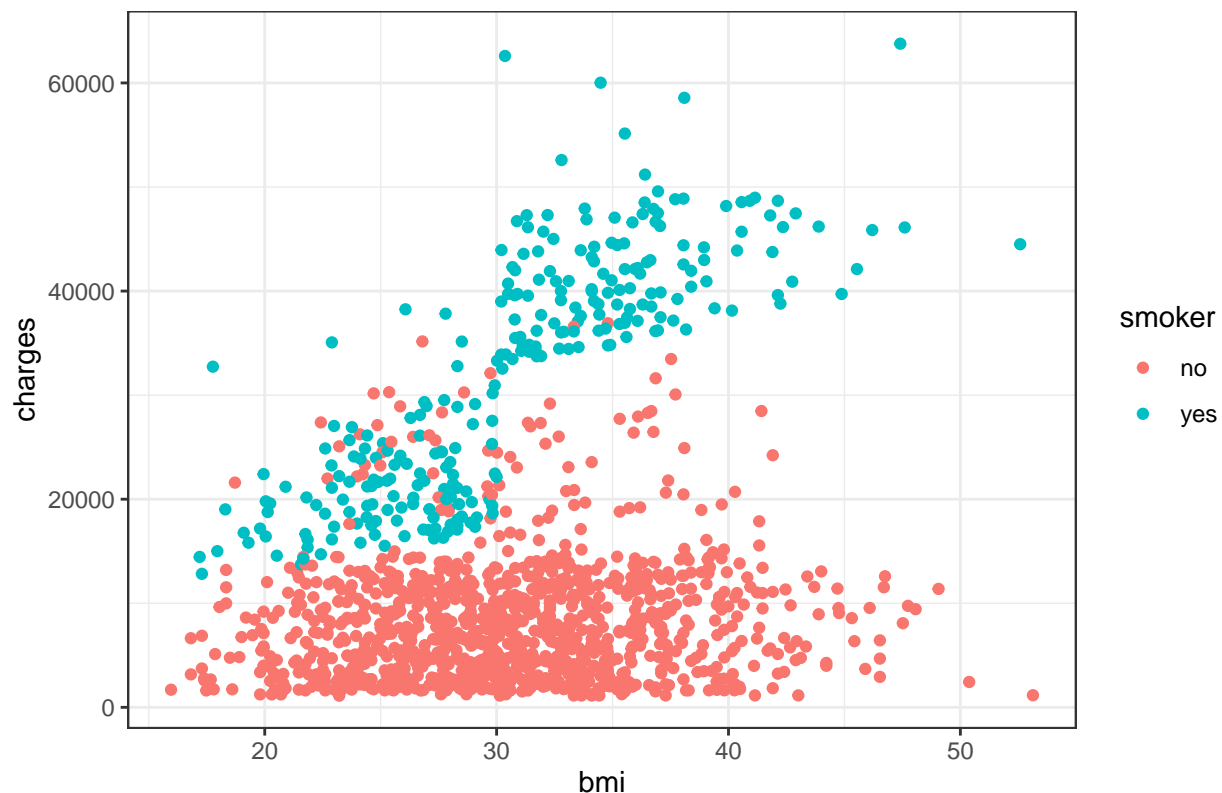
```
## 2  18  male 33.770      1    no southeast 1725.552
## 3  28  male 33.000      3    no southeast 4449.462
## 4  33  male 22.705      0    no northwest 21984.471
## 5  32  male 28.880      0    no northwest 3866.855
## 6  31 female 25.740      0    no southeast 3756.622
```

```
data$significant.charge = as.factor(data$charges > median(data$charges))
data$smoker = as.factor(data$smoker)
data$region = as.factor(data$region)
head(data)
```

```
##   age  sex   bmi children smoker   region   charges significant.charge
## 1  19 female 27.900      0    yes southwest 16884.924           TRUE
## 2  18  male 33.770      1    no southeast 1725.552           FALSE
## 3  28  male 33.000      3    no southeast 4449.462           FALSE
## 4  33  male 22.705      0    no northwest 21984.471           TRUE
## 5  32  male 28.880      0    no northwest 3866.855           FALSE
## 6  31 female 25.740      0    no southeast 3756.622           FALSE
```

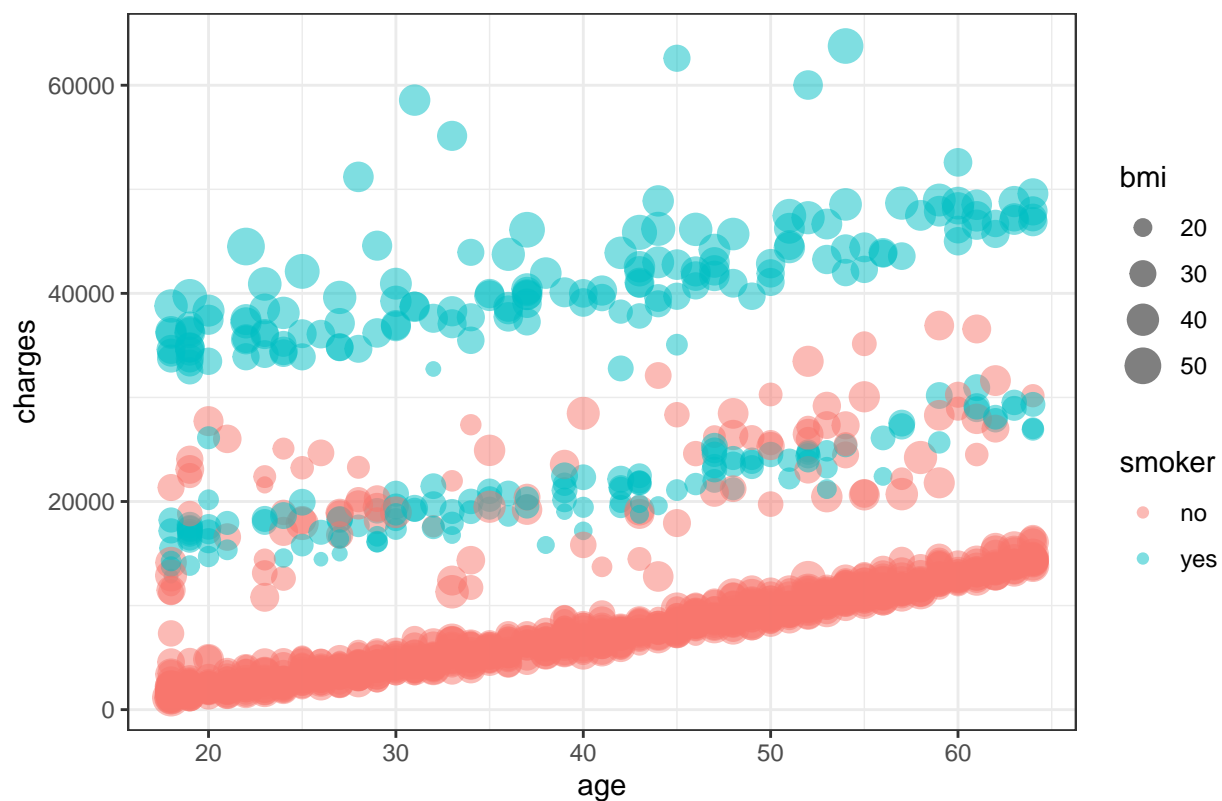
```
ggplot(aes(x=bmi, y=charges, color=smoker), data=data) +
  labs(title="Scatter Plot of Charges vs BMI by Smoker Status") +
  theme_bw() +
  geom_point()
```

Scatter Plot of Charges vs BMI by Smoker Status



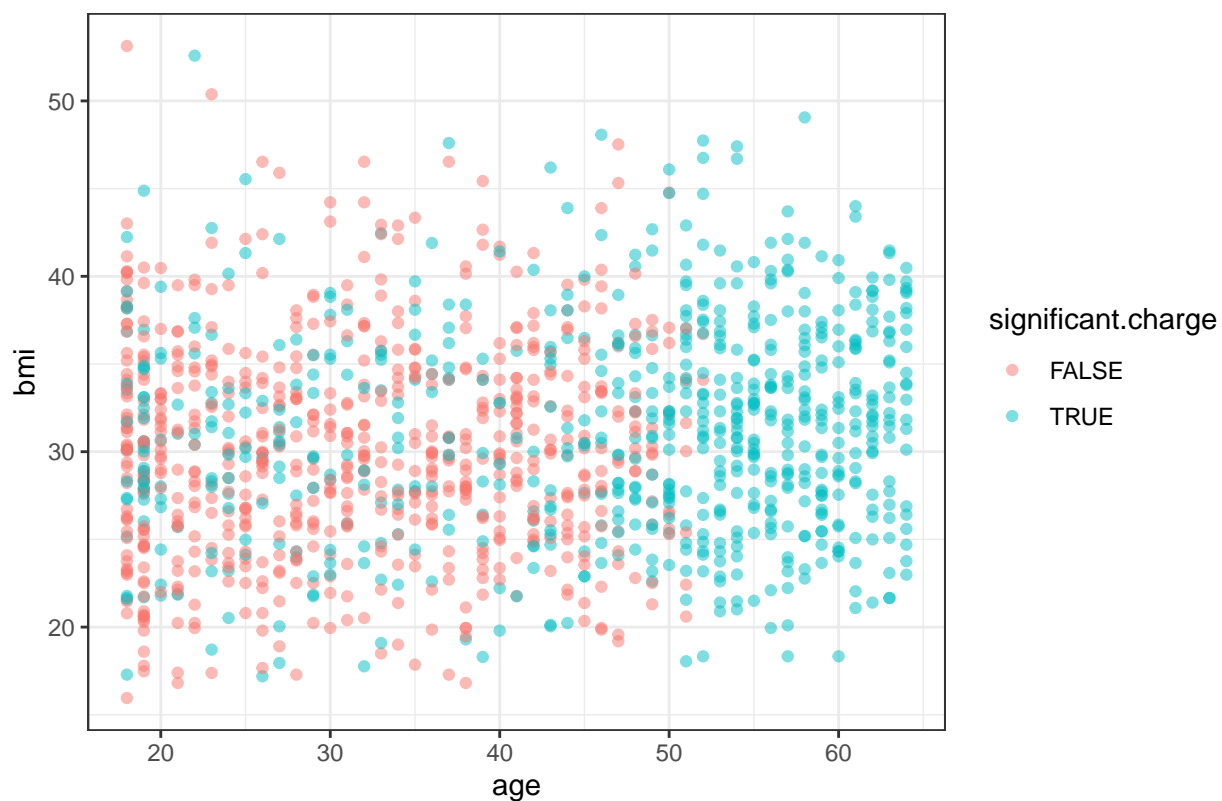
```
ggplot(aes(x=age,y=charges, color=smoker, size=bmi), data=data) +
  labs(title="Scatter plot of Charges vs Age by BMI and Smoker Status") +
  theme_bw() +
  geom_point(alpha=0.5)
```

Scatter plot of Charges vs Age by BMI and Smoker Status

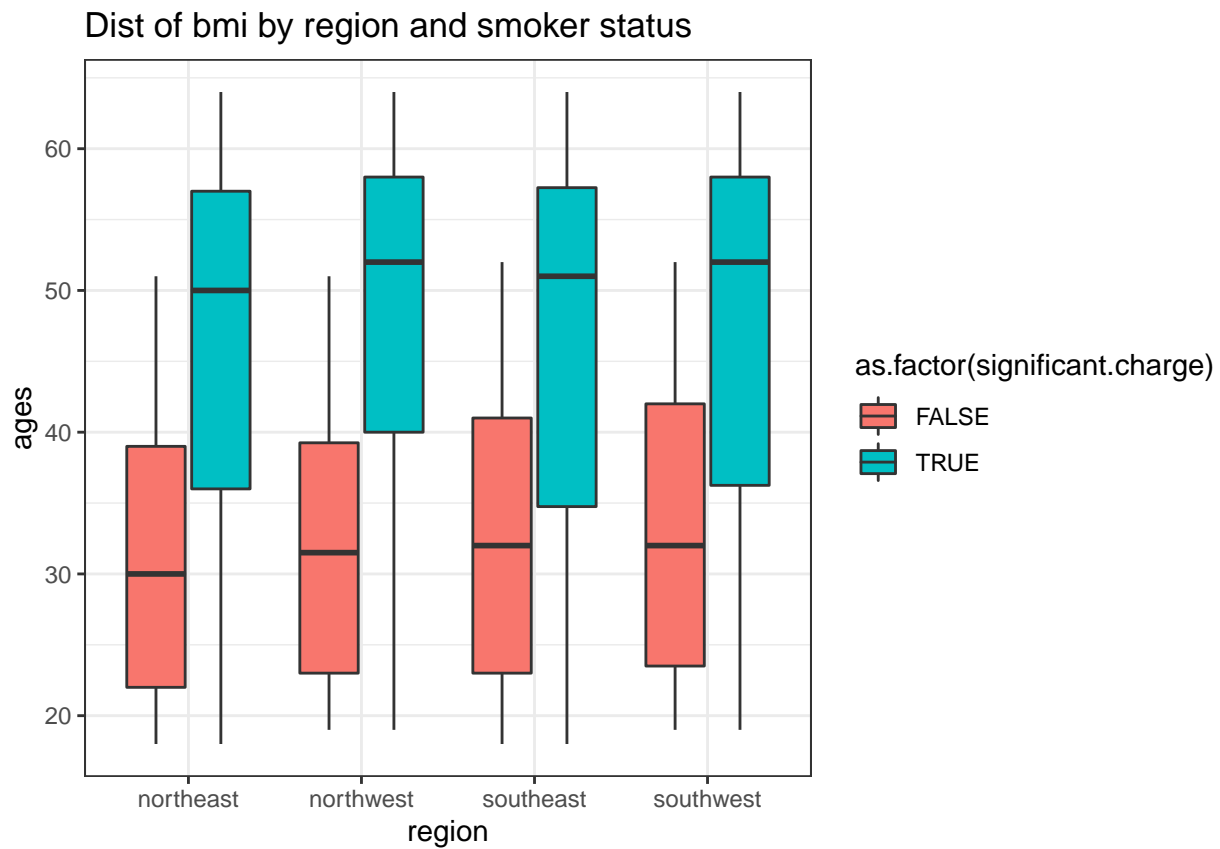


```
ggplot(aes(x=age,y=bmi, color=significant.charge), data=data) +  
  labs(title="Scatter plot of Charges vs Age by BMI and Smoker Status") +  
  theme_bw() +  
  geom_point(alpha=0.5)
```

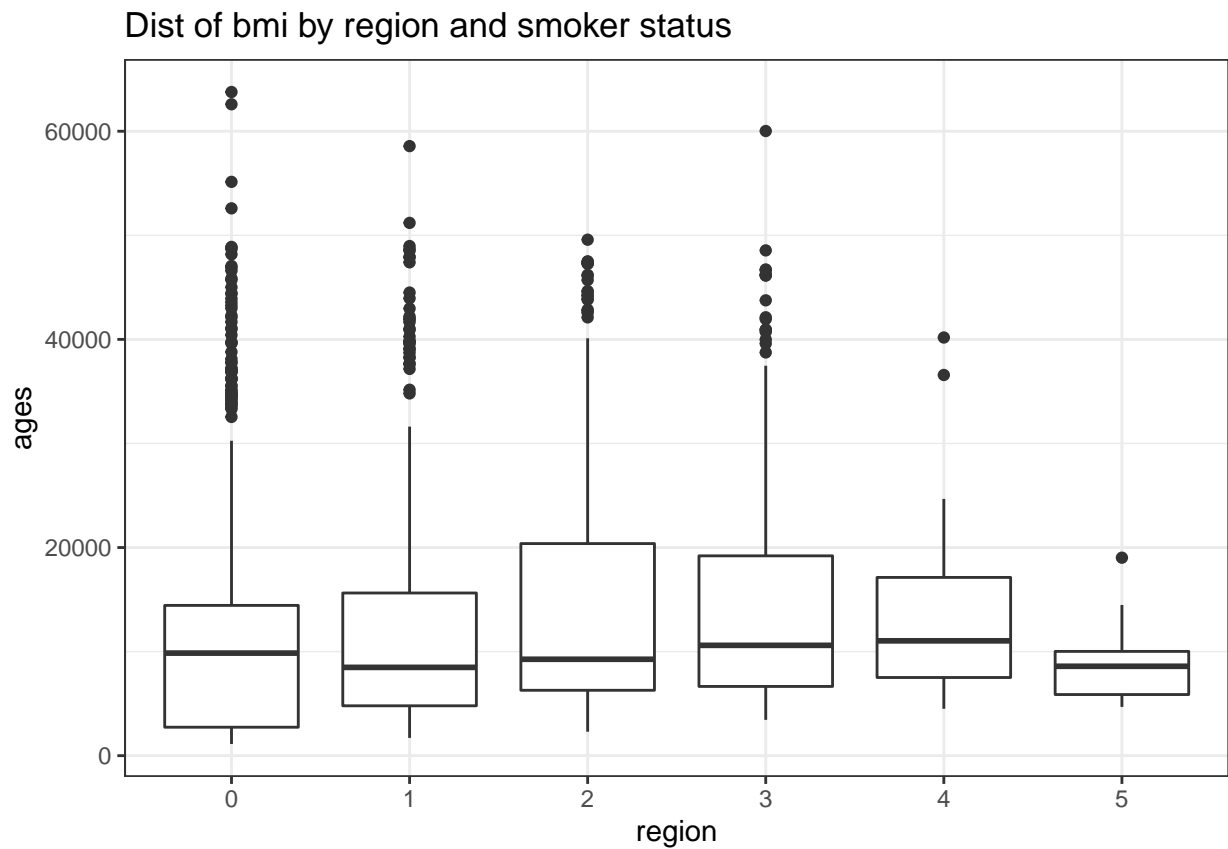
Scatter plot of Charges vs Age by BMI and Smoker Status



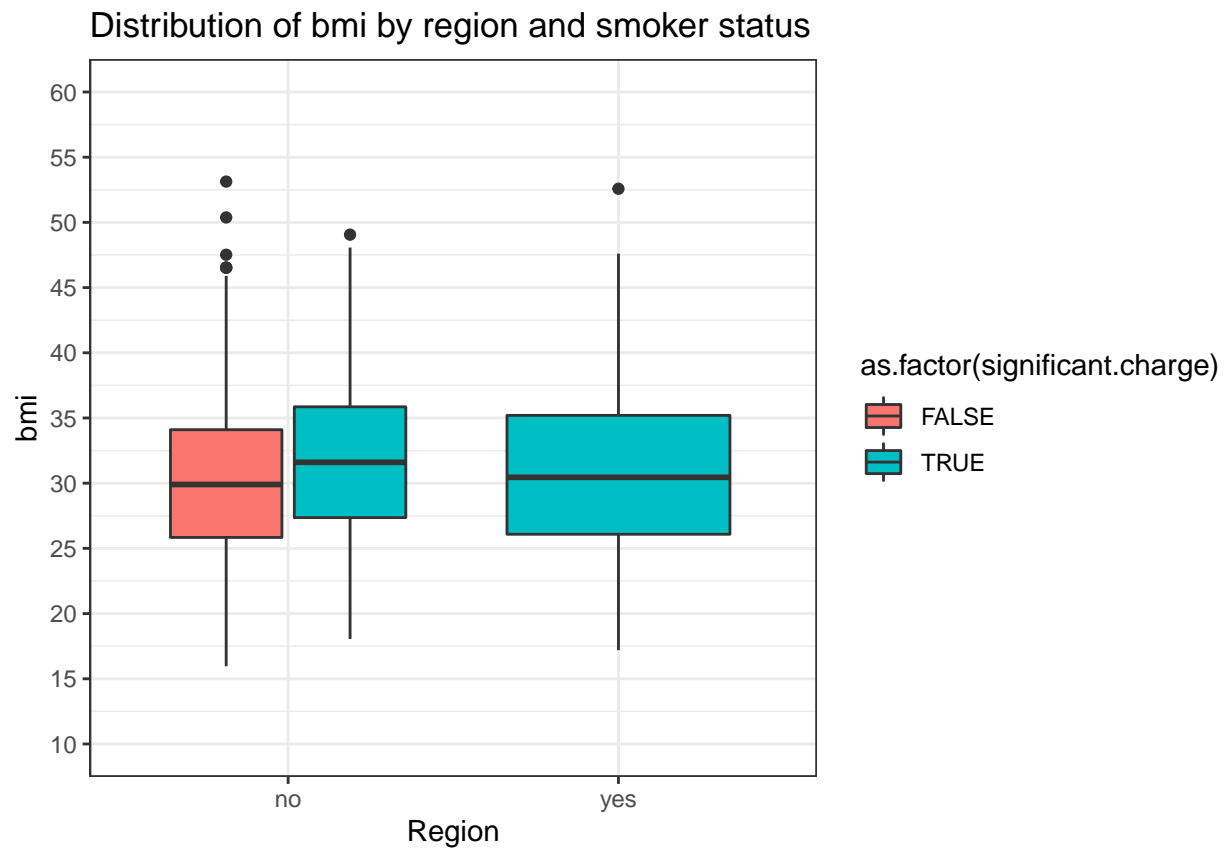
```
ggplot(data, aes(x=region, y=age, fill=as.factor(significant.charge)))+  
  geom_boxplot() +  
  theme_bw() +  
  labs(x="region", y="ages", title="Dist of bmi by region and smoker status")
```



```
ggplot(data, aes(x=as.factor(children), y=charges))+  
  geom_boxplot() +  
  theme_bw() +  
  labs(x="region", y="ages", title="Dist of bmi by region and smoker status")
```

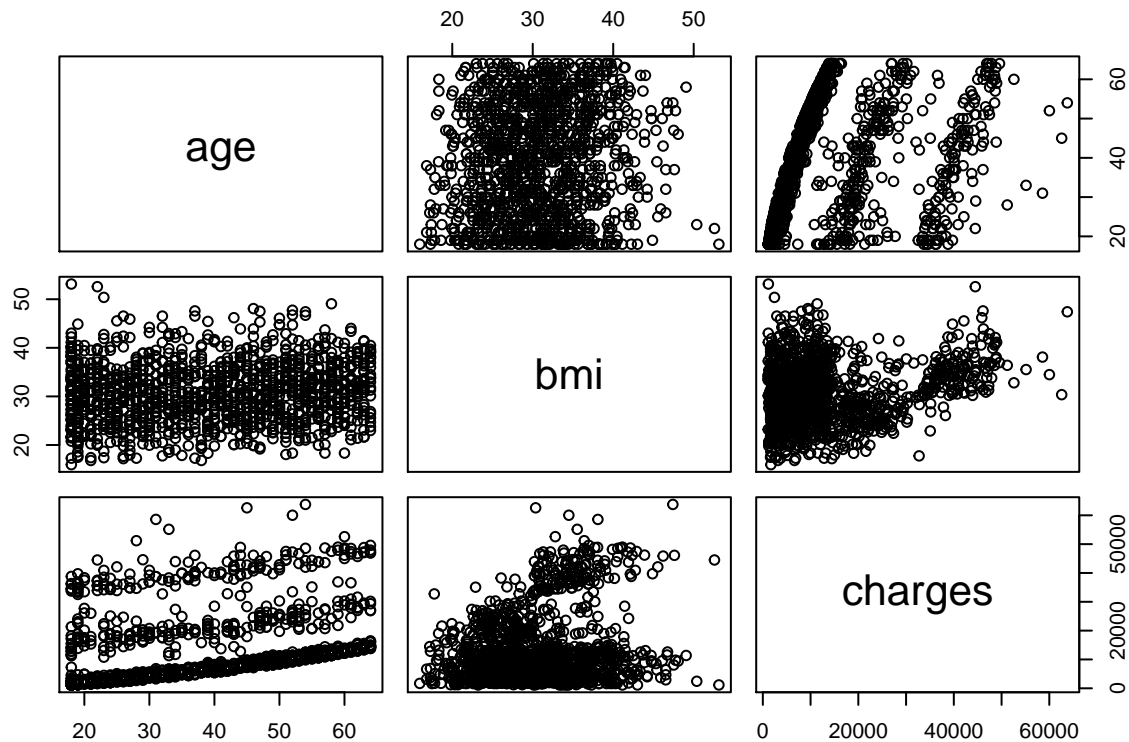


```
ggplot(data, aes(x=smoker, y=bmi, fill=as.factor(significant.charge)))+
  geom_boxplot() +
  theme_bw() +
  labs(x="Region", y="bmi", title="Distribution of bmi by region and smoker status") + scale_y_continuous
```



Correlation

```
pairs(data[c("age", "bmi", "charges")])
```



```
round(cor(data[c("age", "bmi", "charges")]),4)
```

```
##           age    bmi charges
## age      1.0000 0.1093 0.2990
## bmi      0.1093 1.0000 0.1983
## charges 0.2990 0.1983 1.0000
```

All possible regressions and pull based on adjusted R square, mallow, and BIC

```
no_class_predictor = data[1:7]
allreg2 <- regsubsets(charges ~ ., data=no_class_predictor, nbest=2)
summary(allreg2)
```

```
## Subset selection object
## Call: regsubsets.formula(charges ~ ., data = no_class_predictor, nbest = 2)
## 8 Variables (and intercept)
##              Forced in Forced out
## age                FALSE      FALSE
## sexmale            FALSE      FALSE
## bmi                FALSE      FALSE
## children           FALSE      FALSE
## smokeryes          FALSE      FALSE
## regionnorthwest    FALSE      FALSE
## regionsoutheast    FALSE      FALSE
## regionsouthwest    FALSE      FALSE
## 2 subsets of each size up to 8
## Selection Algorithm: exhaustive
##           age sexmale bmi children smokeryes regionnorthwest regionsoutheast
## 1  ( 1 ) " " " " " " " " " " " " " " " " " " " " " " " " " " " "
## 1  ( 2 ) "*" " " " " " " " " " " " " " " " " " " " " " " " " " " "
```



```
## 2 ( 1 ) "*" " " " " " " "*" " " " "
## 2 ( 2 ) " " " " "*" " " "*" " " " "
## 3 ( 1 ) "*" " " "*" " " "*" " " " "
## 3 ( 2 ) "*" " " " " "*" "*" "*" " " " "
## 4 ( 1 ) "*" " " "*" "*" "*" " " " "
## 4 ( 2 ) "*" " " "*" " " "*" " " "*"
## 5 ( 1 ) "*" " " "*" "*" "*" " " "*"
## 5 ( 2 ) "*" " " "*" "*" "*" " " " "
## 6 ( 1 ) "*" " " "*" "*" "*" " " "*"
## 6 ( 2 ) "*" "*" "*" "*" "*" " " "*"
## 7 ( 1 ) "*" " " "*" "*" "*" "*" "*"
## 7 ( 2 ) "*" "*" "*" "*" "*" " " "*"
## 8 ( 1 ) "*" "*" "*" "*" "*" "*" "*"
##      regionsouthwest
## 1 ( 1 ) " "
## 1 ( 2 ) " "
## 2 ( 1 ) " "
## 2 ( 2 ) " "
## 3 ( 1 ) " "
## 3 ( 2 ) " "
## 4 ( 1 ) " "
## 4 ( 2 ) " "
## 5 ( 1 ) " "
## 5 ( 2 ) "*"
## 6 ( 1 ) "*"
## 6 ( 2 ) " "
## 7 ( 1 ) "*"
## 7 ( 2 ) "*"
## 8 ( 1 ) "*"

```

Best for Adjusted R square

```
coef(allreg2, which.max(summary(allreg2)$adjr2))
```

```
##      (Intercept)          age          bmi      children      smokeryes
##      -12165.3824      257.0064      338.6413      471.5441      23843.8749
## regionsoutheast regionsouthwest
##      -858.4696      -782.7452

```

Best for Mallows

```
coef(allreg2, which.min(summary(allreg2)$cp))
```

```
##      (Intercept)          age          bmi      children      smokeryes
##      -12165.3824      257.0064      338.6413      471.5441      23843.8749
## regionsoutheast regionsouthwest
##      -858.4696      -782.7452

```

Best for BIC

```
coef(allreg2, which.min(summary(allreg2)$bic))
```

```
## (Intercept)          age          bmi      children      smokeryes
## -12102.7694      257.8495      321.8514      473.5023      23811.3998

```

Forward Selection

```
##intercept only model
regnull <- lm(charges~1, data=no_class_predictor)
##model with all predictors
regfull <- lm(charges ~ . , data=no_class_predictor)
```

Forward Selection

```
step(regnull, scope=list(lower=regnull, upper=regfull), direction="forward")
```

```
## Start:  AIC=25160.18
## charges ~ 1
##
##           Df Sum of Sq      RSS   AIC
## + smoker    1 1.2152e+11 7.4554e+10 23868
## + age        1 1.7530e+10 1.7854e+11 25037
## + bmi         1 7.7134e+09 1.8836e+11 25108
## + children    1 9.0660e+08 1.9517e+11 25156
## + region      3 1.3008e+09 1.9477e+11 25157
## + sex         1 6.4359e+08 1.9543e+11 25158
## <none>                1.9607e+11 25160
##
## Step:  AIC=23868.38
## charges ~ smoker
##
##           Df Sum of Sq      RSS   AIC
## + age        1 1.9928e+10 5.4626e+10 23454
## + bmi         1 7.4856e+09 6.7069e+10 23729
## + children    1 7.5272e+08 7.3802e+10 23857
## <none>                7.4554e+10 23868
## + sex         1 1.4213e+06 7.4553e+10 23870
## + region      3 1.0752e+08 7.4447e+10 23872
##
## Step:  AIC=23454.24
## charges ~ smoker + age
##
##           Df Sum of Sq      RSS   AIC
## + bmi         1 5112896646 4.9513e+10 23325
## + children    1 459283727 5.4167e+10 23445
## <none>                5.4626e+10 23454
## + sex         1 2225509 5.4624e+10 23456
## + region      3 138426748 5.4488e+10 23457
##
## Step:  AIC=23324.76
## charges ~ smoker + age + bmi
##
##           Df Sum of Sq      RSS   AIC
## + children    1 434769398 4.9078e+10 23315
## + region      3 232012208 4.9281e+10 23324
## <none>                4.9513e+10 23325
## + sex         1 3942912 4.9509e+10 23327
##
## Step:  AIC=23314.96
## charges ~ smoker + age + bmi + children
```

```
##
##           Df Sum of Sq          RSS   AIC
## + region  3 233200844 4.8845e+10 23315
## <none>                4.9078e+10 23315
## + sex      1   5486063 4.9073e+10 23317
##
## Step: AIC=23314.58
## charges ~ smoker + age + bmi + children + region
##
##           Df Sum of Sq          RSS   AIC
## <none>                4.8845e+10 23315
## + sex      1   5716429 4.8840e+10 23316
##
## Call:
## lm(formula = charges ~ smoker + age + bmi + children + region,
##     data = no_class_predictor)
##
## Coefficients:
##      (Intercept)          smokeryes             age             bmi
##      -11990.3           23836.3           257.0           338.7
##      children regionnorthwest regionsoutheast regionsouthwest
##           474.6           -352.2           -1034.4           -959.4

(Intercept)          age             bmi      children      smokeryes regionsoutheast
-12165.3824      257.0064      338.6413      471.5441      23843.8749      -858.4696
regionsouthwest -782.7452
```

Backwards

```
step(regfull, scope=list(lower=regnull, upper=regfull), direction="backward")
```

```
## Start: AIC=23316.43
## charges ~ age + sex + bmi + children + smoker + region
##
##           Df Sum of Sq          RSS   AIC
## - sex      1 5.7164e+06 4.8845e+10 23315
## <none>                4.8840e+10 23316
## - region    3 2.3343e+08 4.9073e+10 23317
## - children  1 4.3755e+08 4.9277e+10 23326
## - bmi       1 5.1692e+09 5.4009e+10 23449
## - age       1 1.7124e+10 6.5964e+10 23717
## - smoker    1 1.2245e+11 1.7129e+11 24993
##
## Step: AIC=23314.58
## charges ~ age + bmi + children + smoker + region
##
##           Df Sum of Sq          RSS   AIC
## <none>                4.8845e+10 23315
## - region    3 2.3320e+08 4.9078e+10 23315
## - children  1 4.3596e+08 4.9281e+10 23324
## - bmi       1 5.1645e+09 5.4010e+10 23447
## - age       1 1.7151e+10 6.5996e+10 23715
## - smoker    1 1.2301e+11 1.7186e+11 24996
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + region,
##     data = no_class_predictor)
##
## Coefficients:
##      (Intercept)          age          bmi      children
##      -11990.3         257.0         338.7         474.6
##      smokeryes regionnorthwest regionsoutheast regionsouthwest
##      23836.3         -352.2         -1034.4         -959.4
```

Based on forward and backward

We get the same model for forward and backward

Let's first make a multiple linear regression model with all the predictors.

```
mlr_full = lm(charges ~ age + bmi + children + smoker + region, data=data)
summary(mlr_full)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + region,
##     data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11367.2  -2835.4   -979.7   1361.9  29935.5
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -11990.27    978.76  -12.250 < 2e-16 ***
## age           256.97     11.89   21.610 < 2e-16 ***
## bmi           338.66     28.56   11.858 < 2e-16 ***
## children      474.57     137.74    3.445 0.000588 ***
## smokeryes     23836.30    411.86   57.875 < 2e-16 ***
## regionnorthwest -352.18    476.12   -0.740 0.459618
## regionsoutheast -1034.36    478.54   -2.162 0.030834 *
## regionsouthwest -959.37    477.78   -2.008 0.044846 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6060 on 1330 degrees of freedom
## Multiple R-squared:  0.7509, Adjusted R-squared:  0.7496
## F-statistic: 572.7 on 7 and 1330 DF,  p-value: < 2.2e-16
```

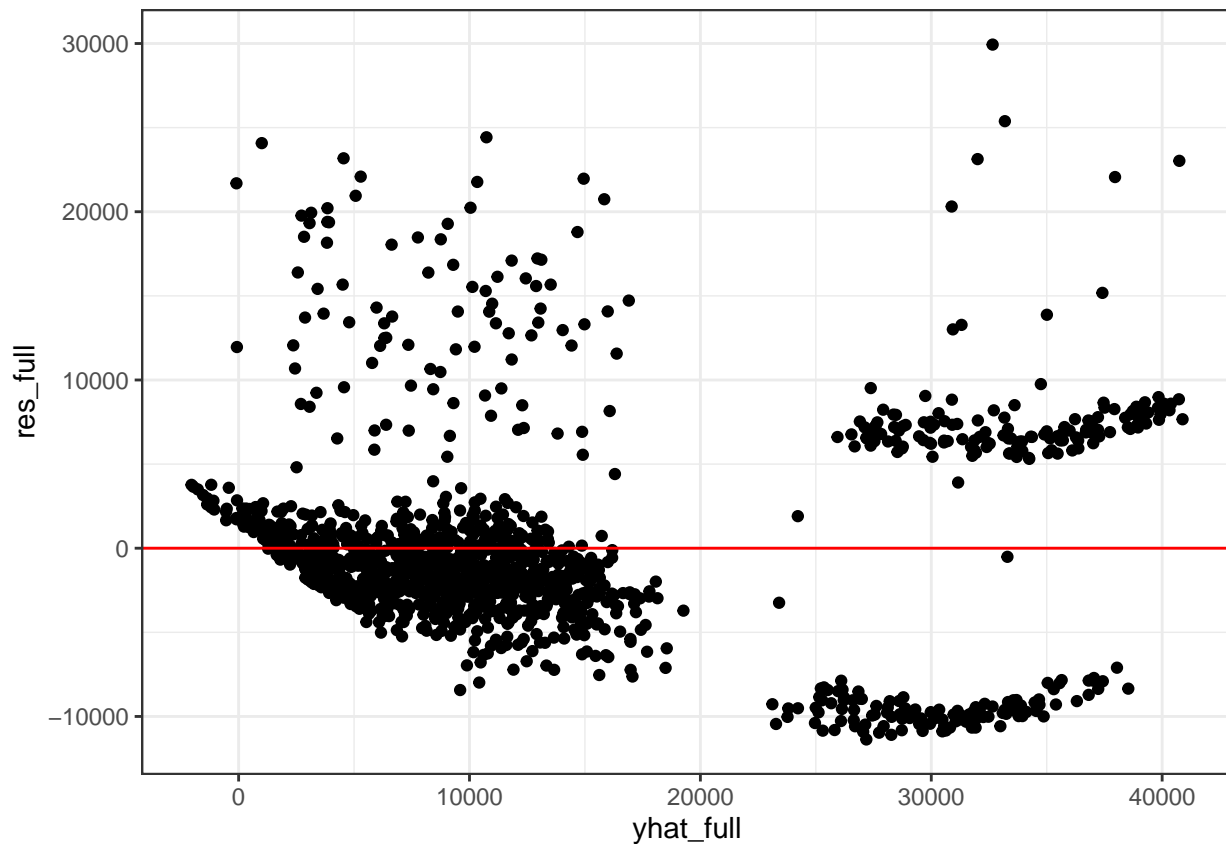
The full regression is as follows.

$$\hat{y} = -11938.5 + 256.9\text{age} - 131.3I_1 + 339.2\text{bmi} + 475.5\text{children} + 23848.5I_2 - 353.0I_3 - 1035.0I_4 - 960.0I_5$$

I_1 indicates whether the sex of the client is male. The value will be 0 for females. I_2 indicates whether that a client smokes. The value will be 0 for non smokers. I_3 indicates that the client is in the northwest region. I_4 indicates that the client is located in the southeast. I_5 indicates that the client is located in the southwest. If the client is in the northeast I_3, I_4, I_5 will be zero, since this is the reference class.

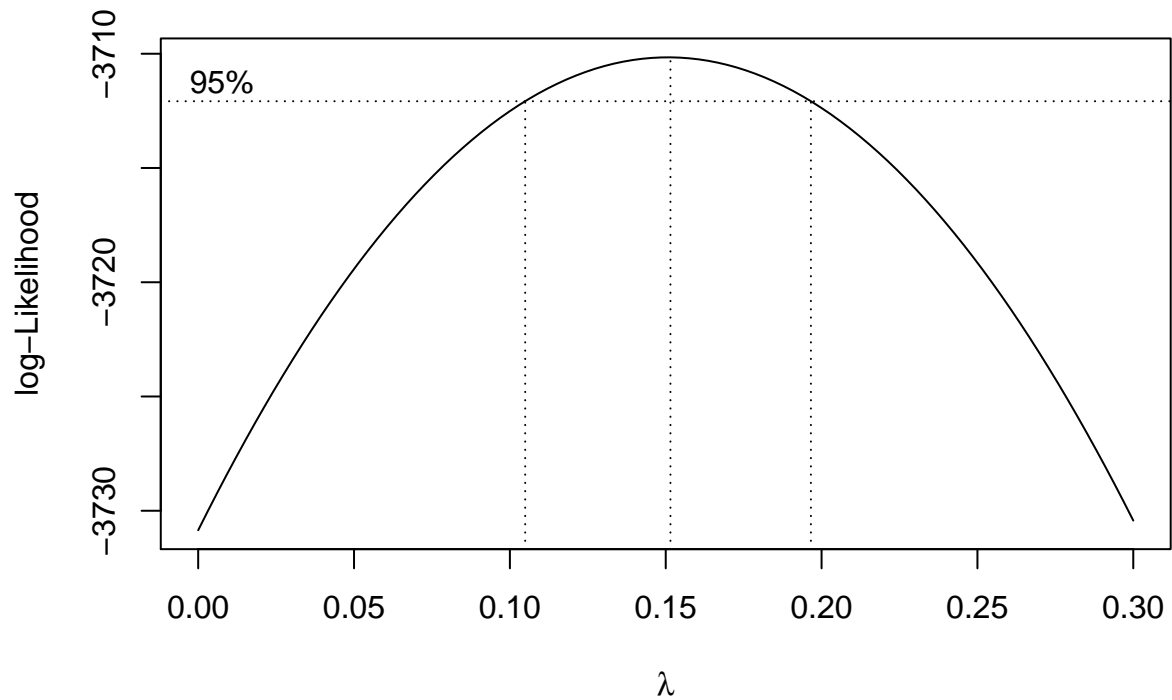
Assumption Check of Full Model

```
yhat_full <- mlr_full$fitted.values  
res_full <- mlr_full$residuals  
data %>%  
  ggplot(aes(yhat_full, res_full)) +  
  geom_point() +  
  theme_bw() +  
  geom_hline(yintercept = 0, color="red")
```



The residuals are obviously not evenly scattered, which then we can utilize the boxcox method to give us information about transformation.

```
boxcox(mlr_full, lambda=seq(0,0.3, 0.01))
```

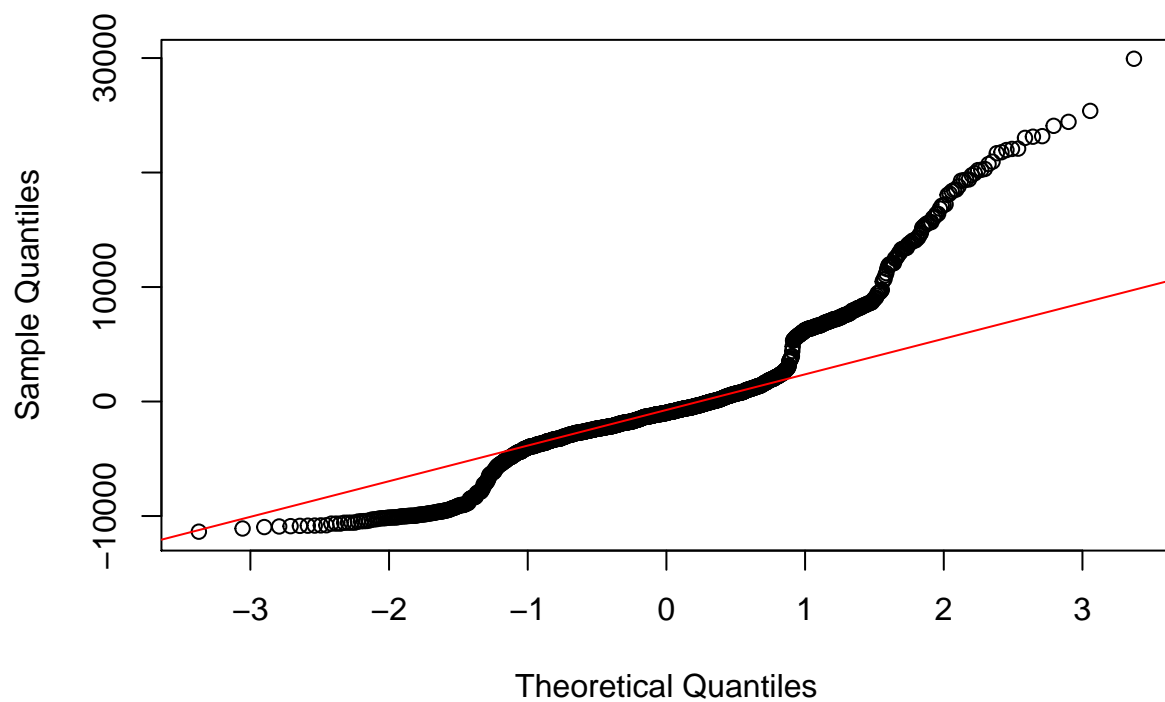


From the boxcox we can try a lambda value of 0.15 for transformation.

QQPlot

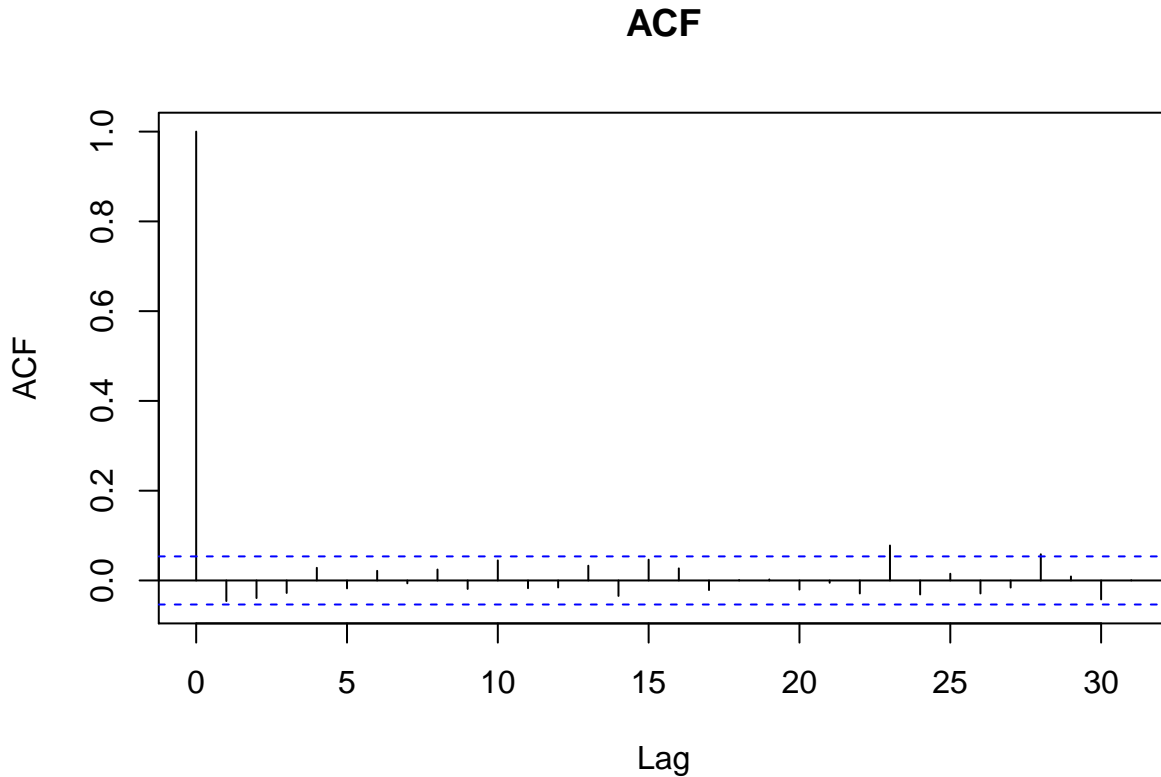
```
{
  qqnorm(mlr_full$residuals)
  qqline(mlr_full$residuals, col="red")
}
```

Normal Q-Q Plot



ACF

```
acf(mlr_full$residuals, main="ACF")
```



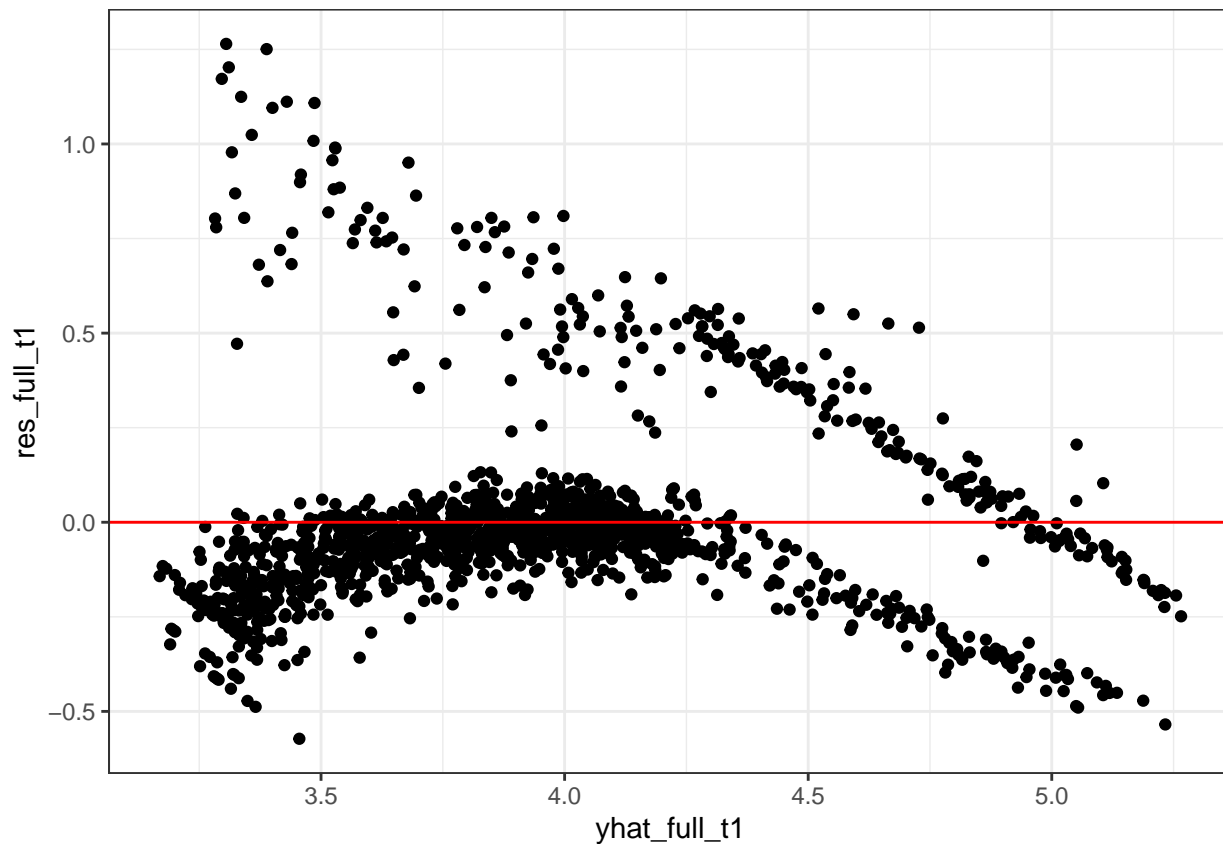
```
first_transformation_full <- data
first_transformation_full$charges <- first_transformation_full$charges^0.15
mlr_transform_first <- lm(charges ~ age + bmi + children + smoker + region, data=first_transformation_f
summary(mlr_transform_first)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + region,
##     data = first_transformation_full)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.57232 -0.12513 -0.04165  0.03000  1.26454
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   2.7239709   0.0416239   65.443 < 2e-16 ***
## age           0.0191744   0.0005057   37.916 < 2e-16 ***
## bmi           0.0088624   0.0012145    7.297 5.04e-13 ***
## children      0.0524721   0.0058577    8.958 < 2e-16 ***
## smokeryes     0.9560821   0.0175151   54.586 < 2e-16 ***
## regionnorthwest -0.0345277  0.0202480   -1.705  0.0884 .
## regionsoutheast -0.0845268  0.0203508   -4.153 3.48e-05 ***
## regionsouthwest -0.0708940  0.0203185   -3.489  0.0005 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.2577 on 1330 degrees of freedom
## Multiple R-squared:  0.7754, Adjusted R-squared:  0.7742
## F-statistic: 655.9 on 7 and 1330 DF,  p-value: < 2.2e-16
```

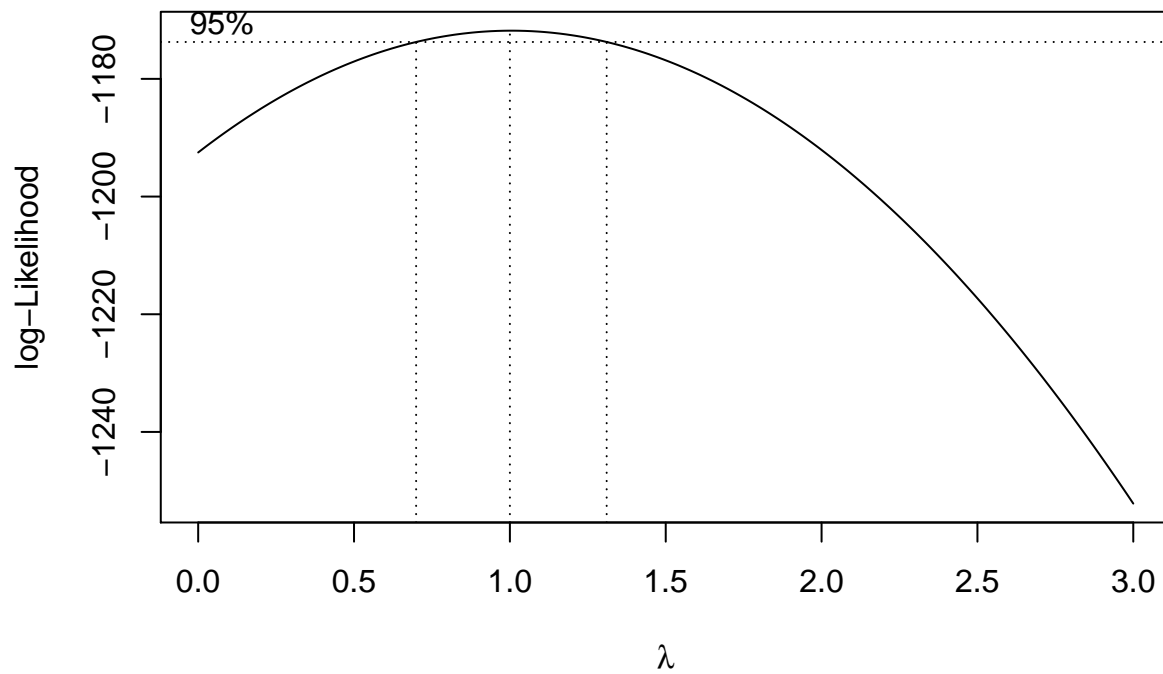
Residual Plot of the transformed model.

```
yhat_full_t1 <- mlr_transform_first$fitted.values
res_full_t1 <- mlr_transform_first$residuals
data %>%
  ggplot(aes(yhat_full_t1, res_full_t1)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



Violation in constant variance

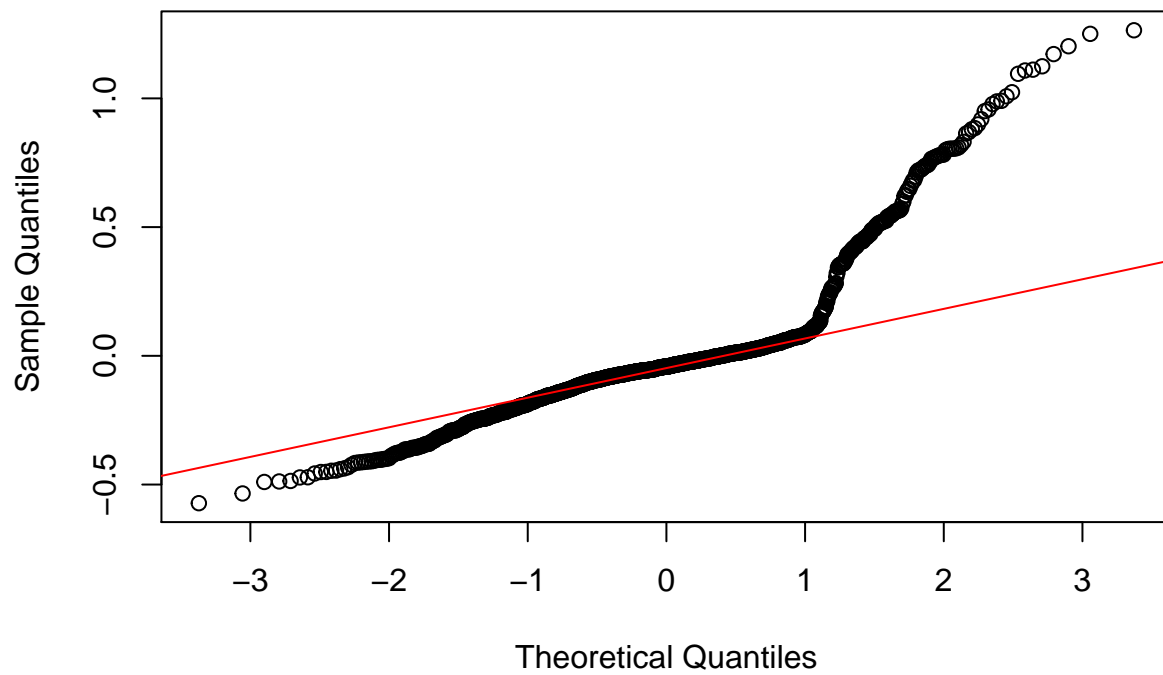
```
boxcox(mlr_transform_first, lambda=seq(0,3, 0.01))
```

QQPLOT

```
{
  qqnorm(mlr_transform_first$residuals)
  qqline(mlr_transform_first$residuals, col="red")
}
```

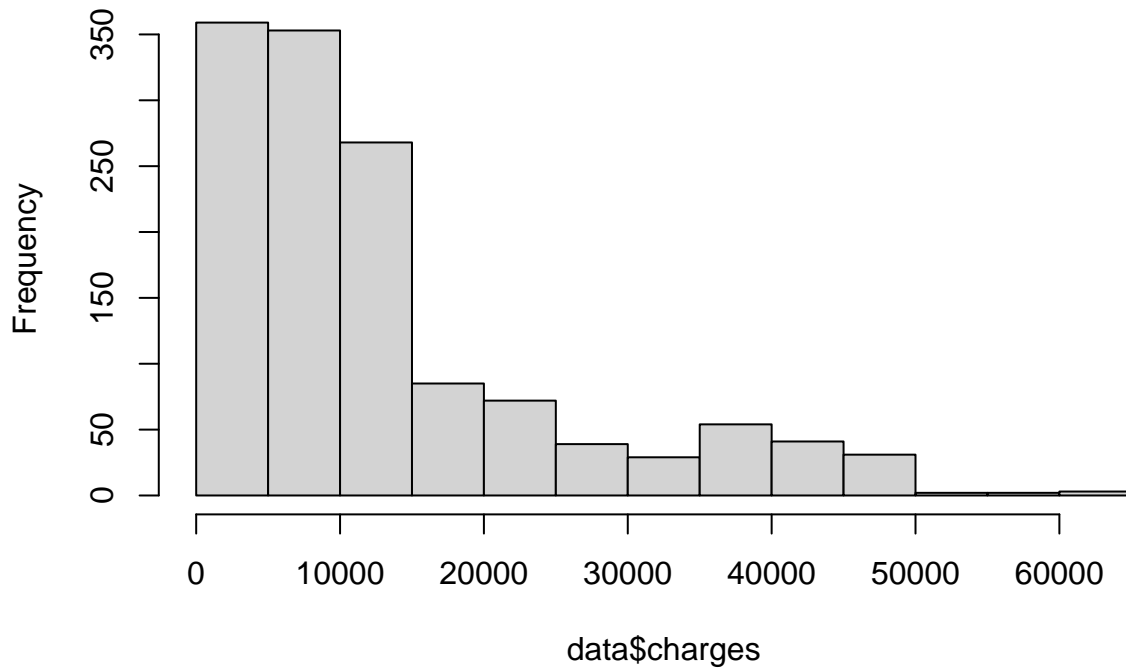
Normal Q-Q Plot



Why is this happening? Is there some weird behavior in the response variable?

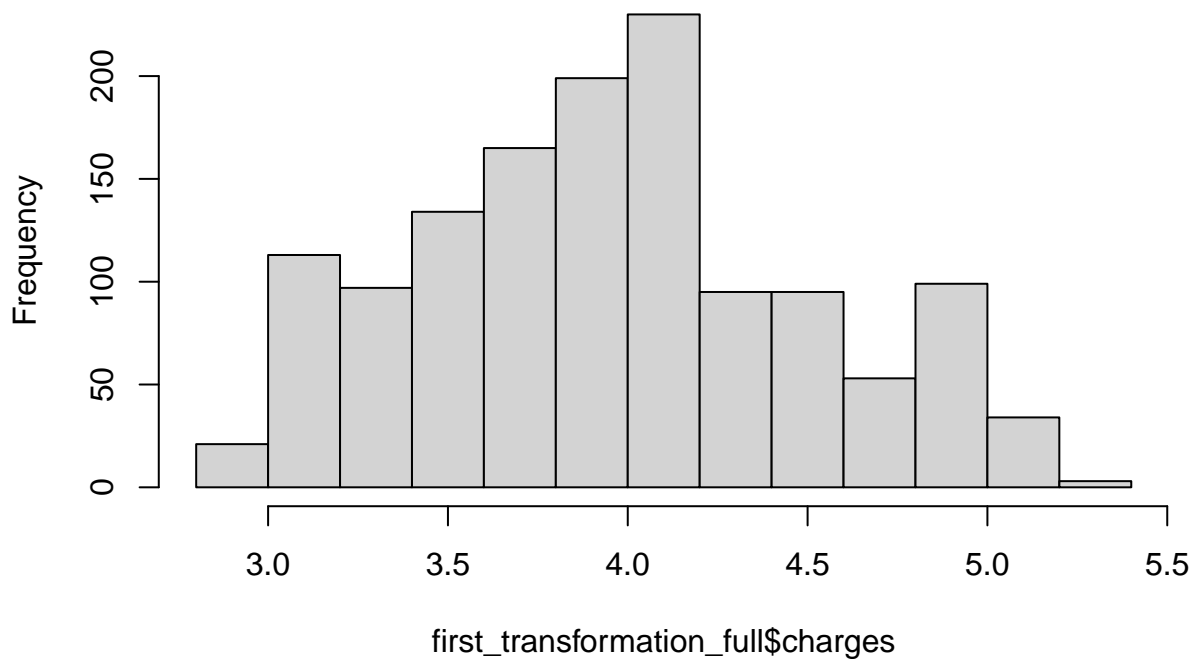
```
hist(data$charges)
```

Histogram of data\$charges



```
hist(first_transformation_full$charges)
```

Histogram of first_transformation_full\$charges



Trial of other predictors to fulfill the linearity assumption.

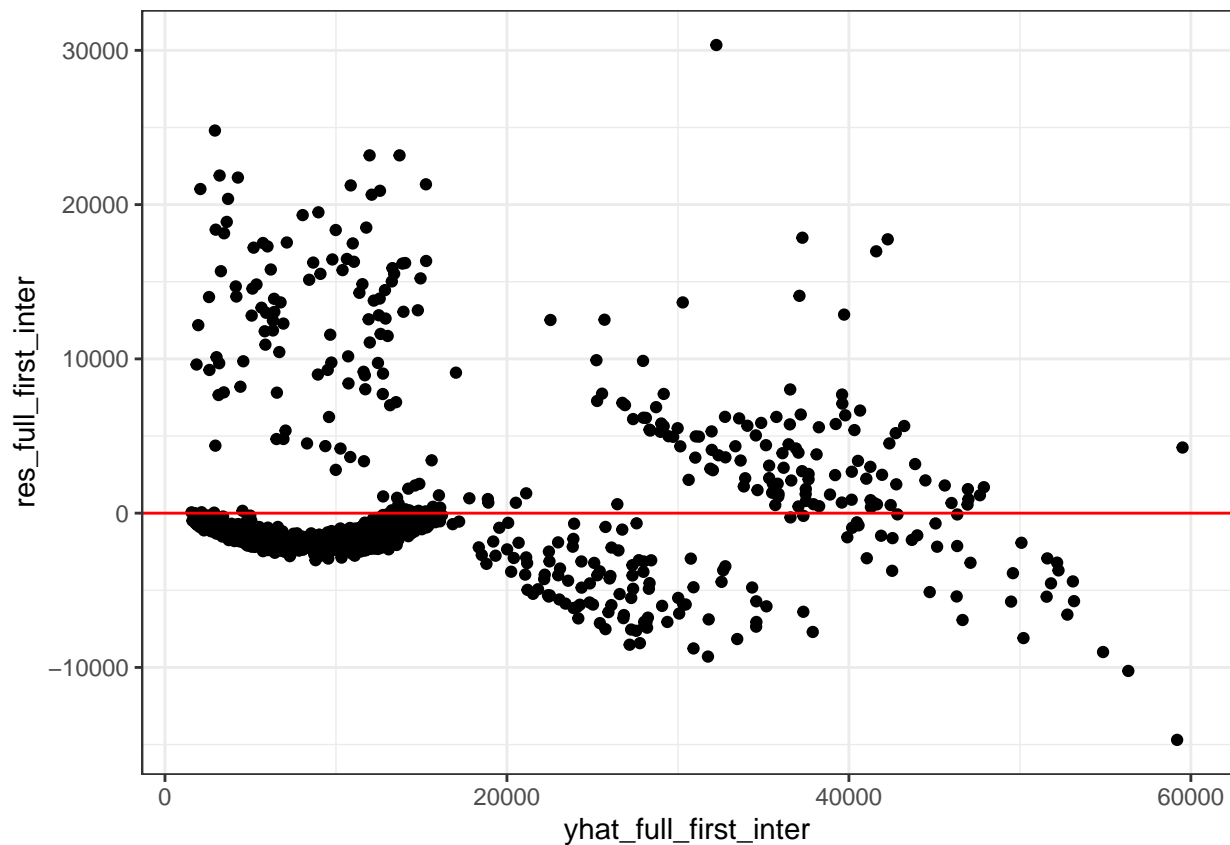
Maybe we can add some interaction terms to the model to see if we can fix the linearity assumption.

```
interaction_age_bmi_with_smoker = lm(charges ~ age*smoker + bmi*smoker + children + region, data=data)
summary(interaction_age_bmi_with_smoker)
```

```
##
## Call:
## lm(formula = charges ~ age * smoker + bmi * smoker + children +
##     region, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14695.2  -1918.6  -1316.2   -480.3   30345.6
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -2469.101     870.166  -2.838  0.00462 **
## age             264.558      10.672   24.791 < 2e-16 ***
## smokeryes     -20223.654    1831.889  -11.040 < 2e-16 ***
## bmi             22.444       25.679    0.874  0.38228
## children       512.956      110.331    4.649 3.66e-06 ***
## regionnorthwest -581.232      381.383  -1.524  0.12774
## regionsoutheast -1205.652      383.462  -3.144  0.00170 **
## regionsouthwest -1228.623      382.837  -3.209  0.00136 **
## age:smokeryes   -2.542       23.711  -0.107  0.91464
## smokeryes:bmi   1438.525       52.793   27.249 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4853 on 1328 degrees of freedom
## Multiple R-squared:  0.8405, Adjusted R-squared:  0.8394
## F-statistic: 777.5 on 9 and 1328 DF,  p-value: < 2.2e-16
```

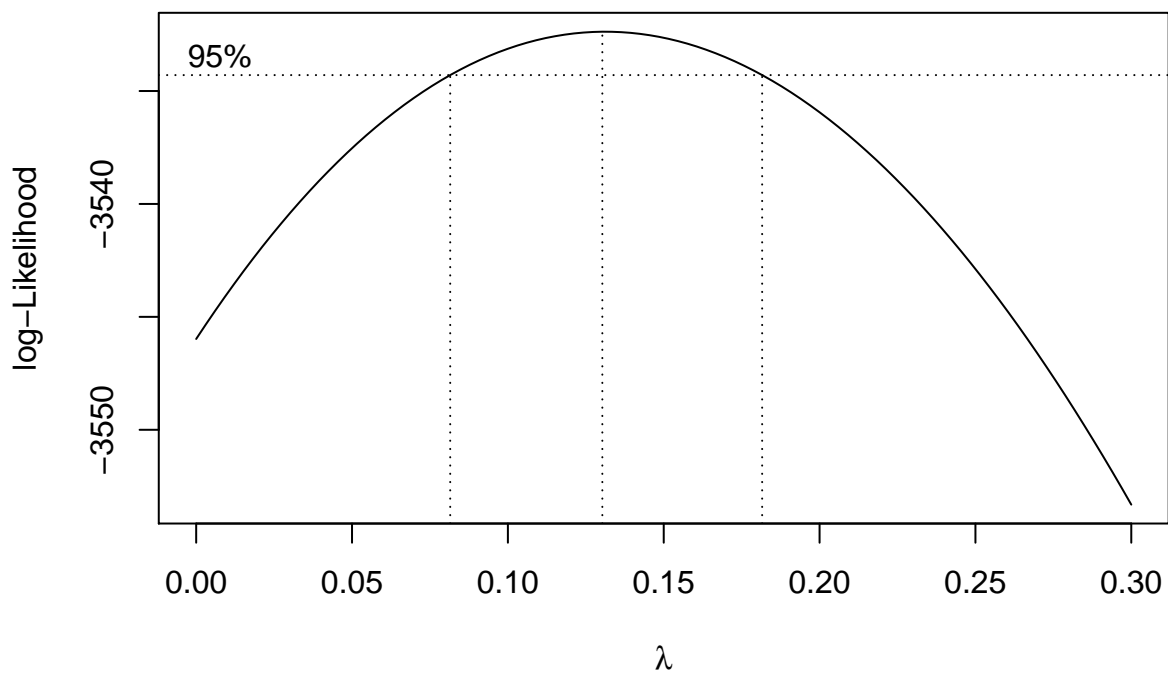
Residual Plot

```
yhat_full_first_inter <- interaction_age_bmi_with_smoker$fitted.values
res_full_first_inter <- interaction_age_bmi_with_smoker$residuals
data %>%
  ggplot(aes(yhat_full_first_inter, res_full_first_inter)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



This residual plot is a little better, lets see if we can transform the response with this new equation.

```
boxcox(interaction_age_bmi_with_smoker, lambda=seq(0,0.3, 0.01))
```



Maybe we can use a lambda value of 0.125

```

interaction_transform <- data
interaction_transform$charges <- interaction_transform$charges^0.125
mlr_interaction_tranform <- lm(charges ~ age*smoker + bmi*smoker + children + region, data=interaction_transform)
summary(mlr_interaction_tranform)

```

```

##
## Call:
## lm(formula = charges ~ age * smoker + bmi * smoker + children +
##     region, data = interaction_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.23325 -0.05925 -0.03216 -0.00578  0.89638
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.3898138   0.0268794   88.909 < 2e-16 ***
## age             0.0152818   0.0003296   46.358 < 2e-16 ***
## smokeryes       0.3867297   0.0565870    6.834 1.25e-11 ***
## bmi             0.0004622   0.0007932    0.583  0.5602
## children        0.0371914   0.0034081   10.913 < 2e-16 ***
## regionnorthwest -0.0243318   0.0117809   -2.065  0.0391 *
## regionsoutheast -0.0531652   0.0118451   -4.488 7.80e-06 ***
## regionsouthwest -0.0559589   0.0118258   -4.732 2.46e-06 ***
## age:smokeryes   -0.0115120   0.0007324  -15.717 < 2e-16 ***
## smokeryes:bmi    0.0223756   0.0016308   13.721 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1499 on 1328 degrees of freedom
## Multiple R-squared:  0.827, Adjusted R-squared:  0.8259
## F-statistic: 705.6 on 9 and 1328 DF, p-value: < 2.2e-16

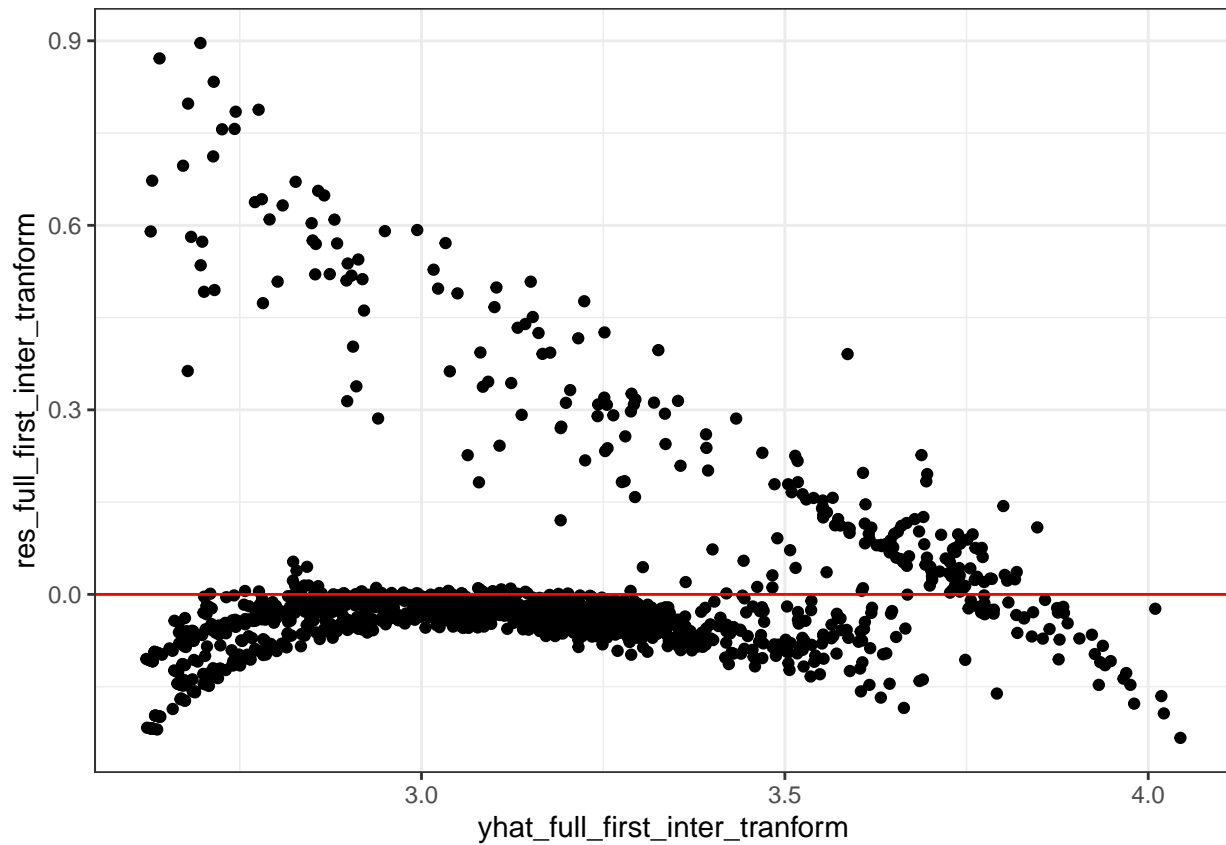
```

Recheck Residual Plot

```

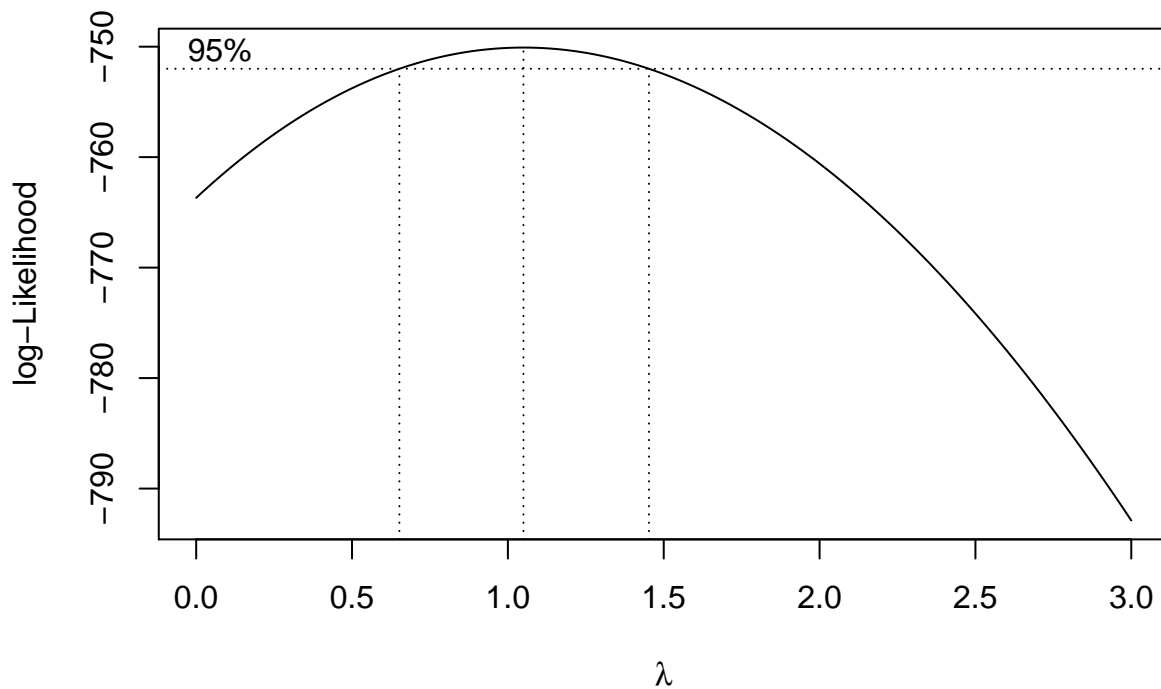
yhat_full_first_inter_tranform <- mlr_interaction_tranform$fitted.values
res_full_first_inter_tranform <- mlr_interaction_tranform$residuals
data %>%
  ggplot(aes(yhat_full_first_inter_tranform, res_full_first_inter_tranform)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")

```



Still see the same without adding the interaction terms.

```
boxcox(mlr_interaction_transform, lambda=seq(0,3, 0.01))
```



Still no luck. We retried this many times, but weren't lucky.

Partial F test of the interaction vs simple model after two transformation of response variable

```
full <- mlr_interaction_tranform
reduced <- lm(charges ~ age + bmi + children + smoker + region, data=interaction_transform)
anova(reduced, full)
```

```
## Analysis of Variance Table
##
## Model 1: charges ~ age + bmi + children + smoker + region
## Model 2: charges ~ age * smoker + bmi * smoker + children + region
##   Res.Df    RSS Df Sum of Sq    F    Pr(>F)
## 1     1330 38.959
## 2     1328 29.842  2     9.1174 202.87 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

We can't drop the interaction terms.

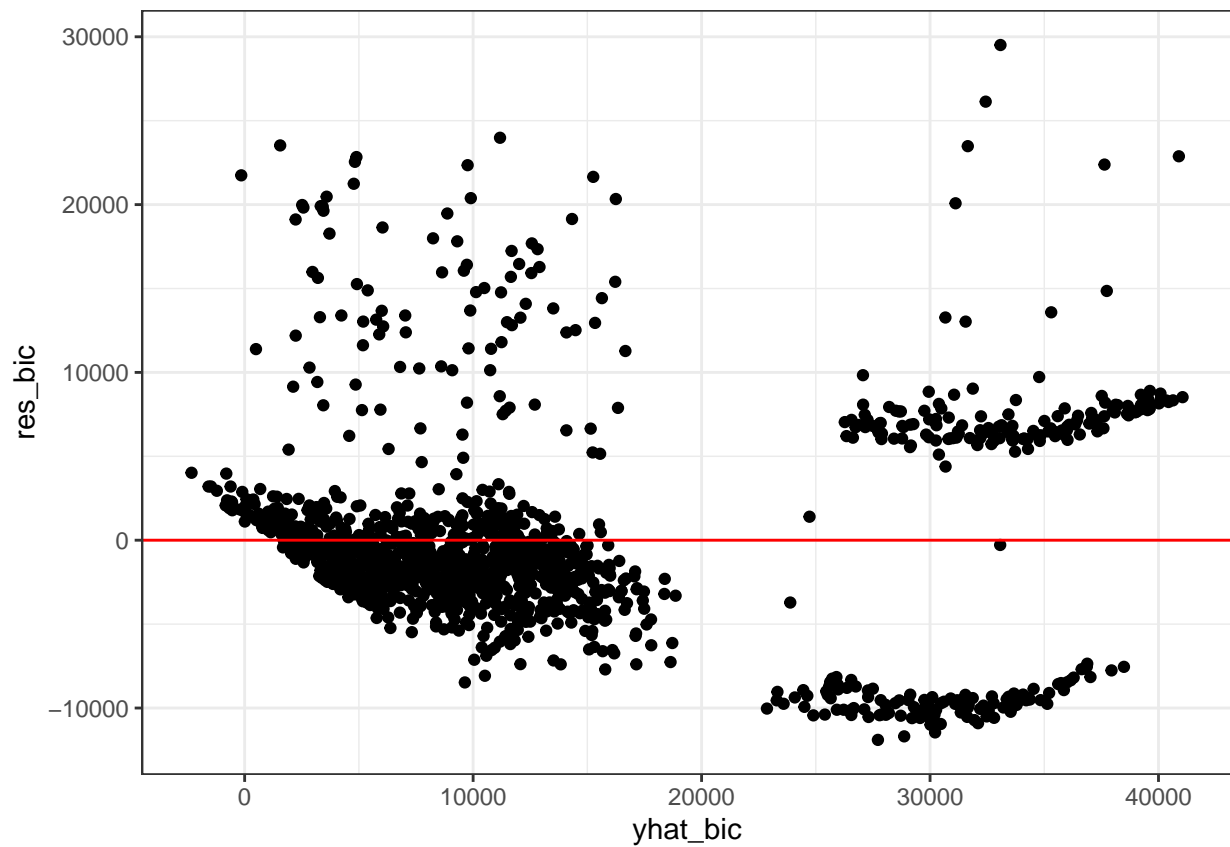
BIC Model selection model might be better

```
bic_selection_model = lm(charges ~ age + bmi + children + smoker, data=data)
summary(bic_selection_model)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11897.9  -2920.8   -986.6   1392.2  29509.6
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -12102.77     941.98  -12.848 < 2e-16 ***
## age           257.85       11.90   21.675 < 2e-16 ***
## bmi           321.85       27.38   11.756 < 2e-16 ***
## children      473.50       137.79    3.436 0.000608 ***
## smokeryes     23811.40     411.22   57.904 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6068 on 1333 degrees of freedom
## Multiple R-squared:  0.7497, Adjusted R-squared:  0.7489
## F-statistic: 998.1 on 4 and 1333 DF, p-value: < 2.2e-16
```

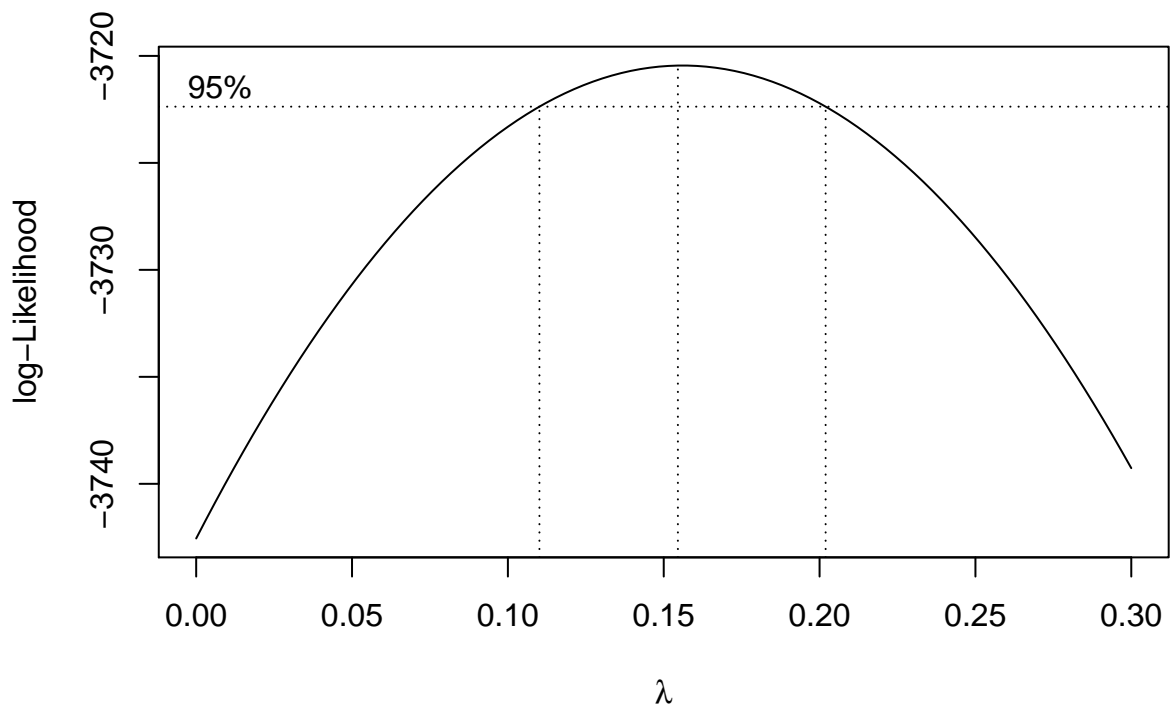
Residual Plot

```
yhat_bic <- bic_selection_model$fitted.values
res_bic <- bic_selection_model$residuals
data %>%
  ggplot(aes(yhat_bic, res_bic)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



We see a similar plot. Transformation?

```
boxcox(bic_selection_model, lambda=seq(0,0.3, 0.01))
```



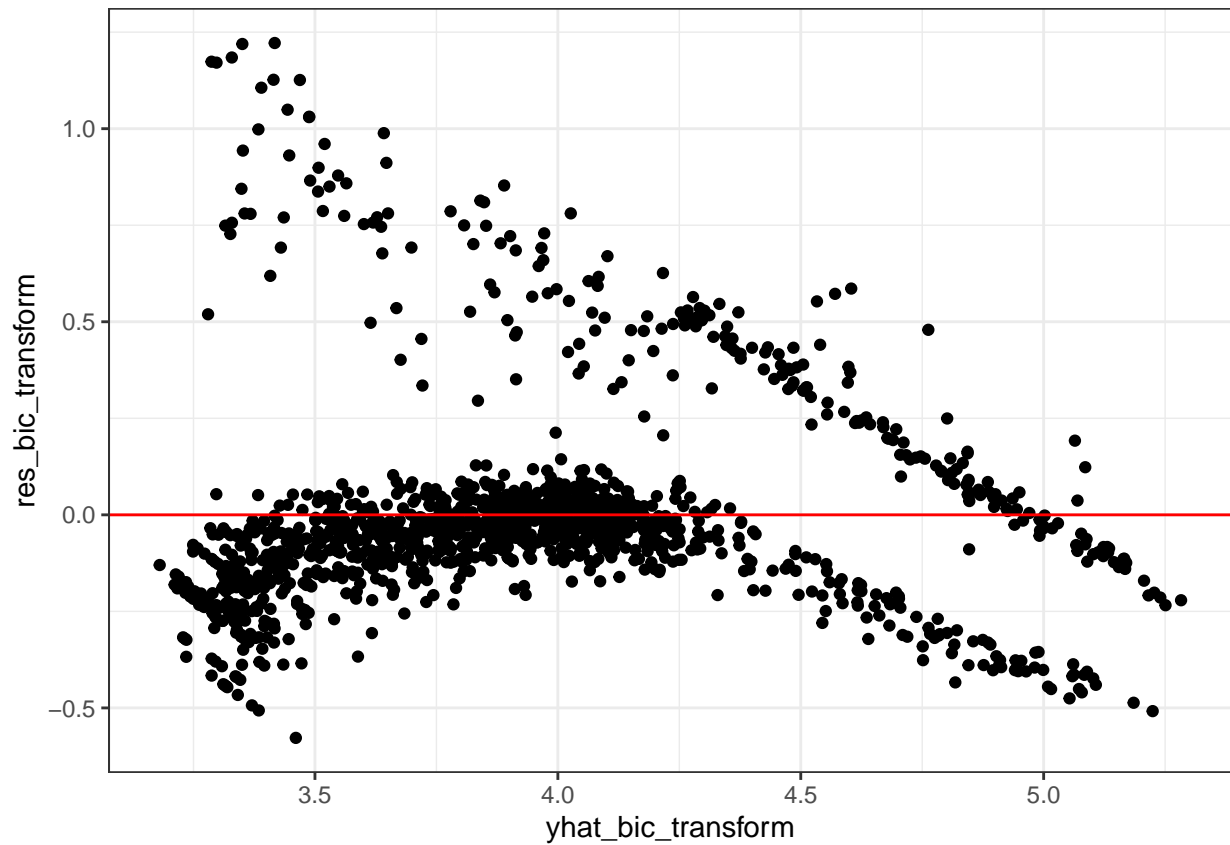
Again lambda of 0.15


```
bic_transform <- data
bic_transform$charges <- bic_transform$charges^(0.15)
bic_selection_model_transform = lm(charges ~ age + bmi + children + smoker, data=bic_transform)
summary(bic_selection_model_transform)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker, data = bic_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.57755 -0.12028 -0.03776  0.03505  1.22187
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.7136331  0.0402741  67.379  < 2e-16 ***
## age          0.0192458  0.0005086  37.839  < 2e-16 ***
## bmi          0.0075402  0.0011705   6.442 1.65e-10 ***
## children     0.0523899  0.0058912   8.893  < 2e-16 ***
## smokeryes    0.9539751  0.0175815  54.260  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2594 on 1333 degrees of freedom
## Multiple R-squared:  0.7719, Adjusted R-squared:  0.7712
## F-statistic: 1128 on 4 and 1333 DF,  p-value: < 2.2e-16
```

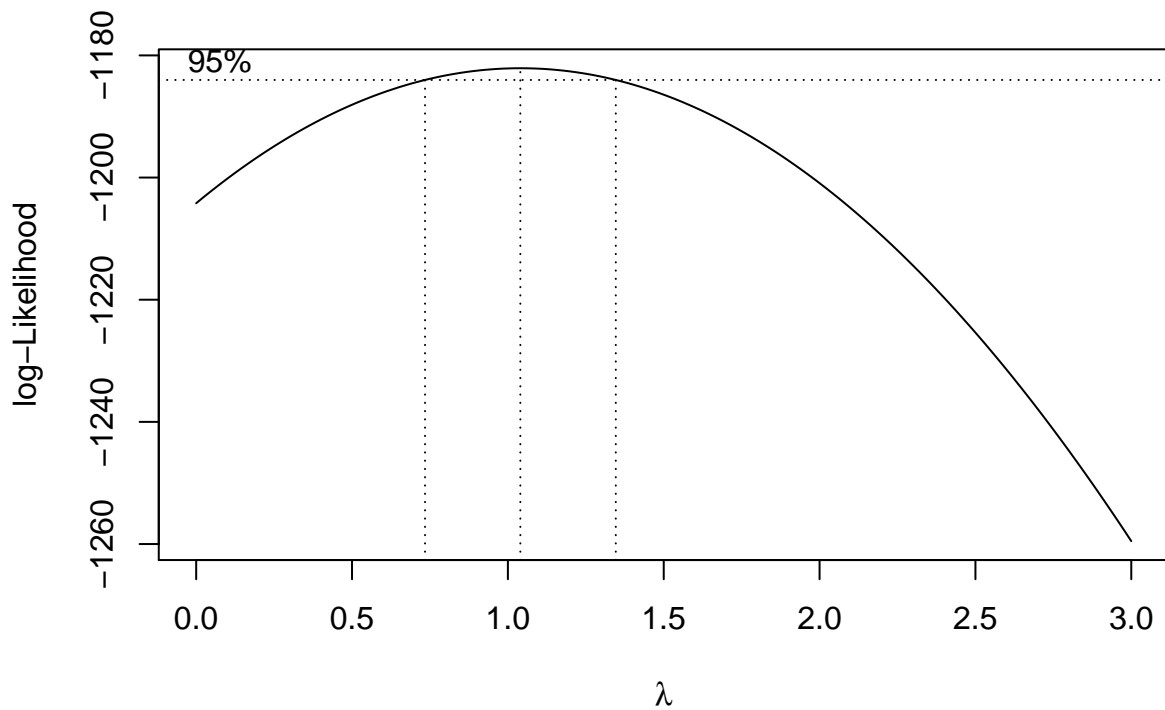
Residual Plot

```
yhat_bic_transform <- bic_selection_model_transform$fitted.values
res_bic_transform <- bic_selection_model_transform$residuals
data %>%
  ggplot(aes(yhat_bic_transform, res_bic_transform)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



Same Stuff happening.

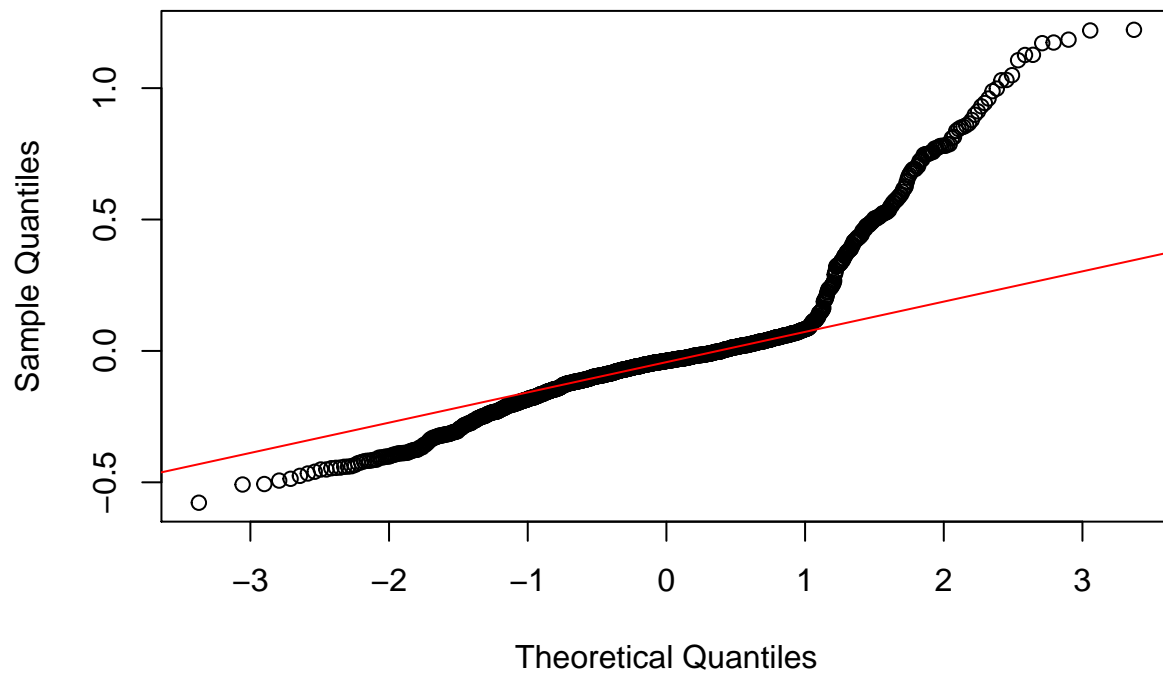
```
boxcox(bic_selection_model_transform, lambda=seq(0,3, 0.01))
```



QQPlot

```
{
  qqnorm(bic_selection_model_transform$residuals)
  qqline(bic_selection_model_transform$residuals, col="red")
}
```

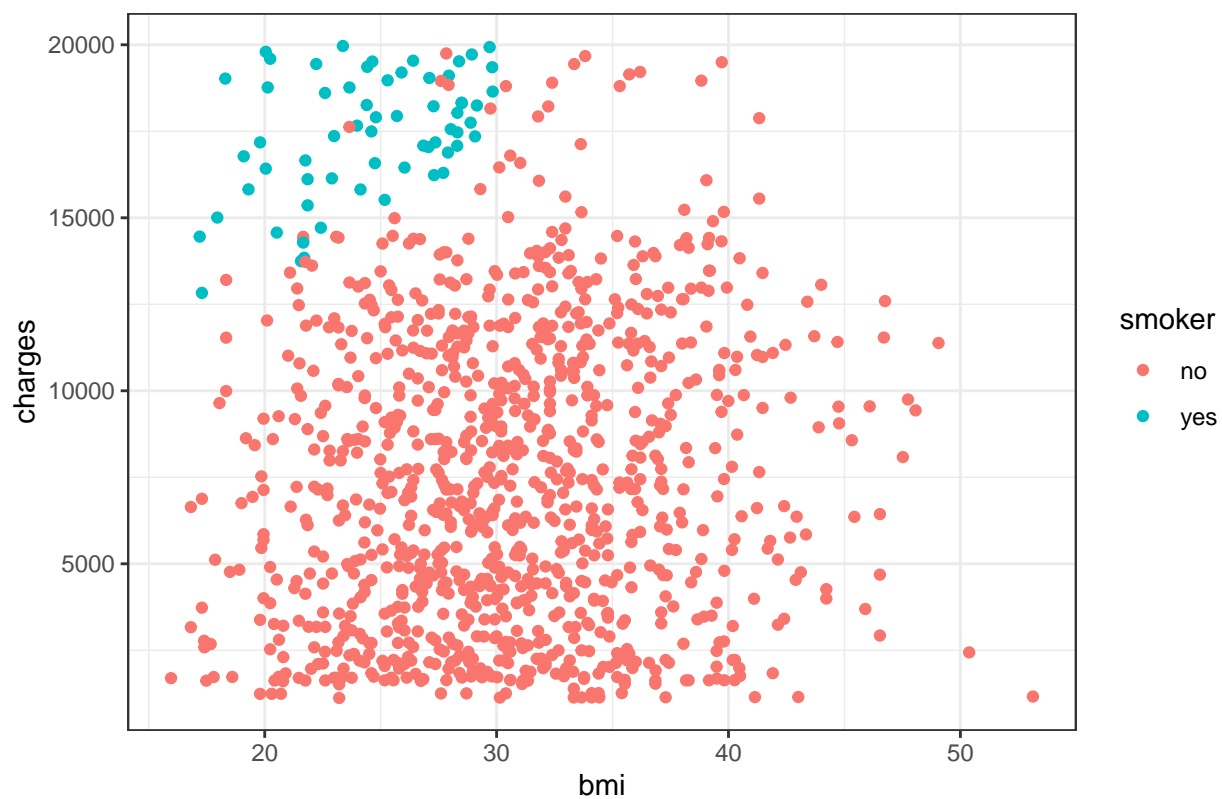
Normal Q-Q Plot



Change the data split the data ?

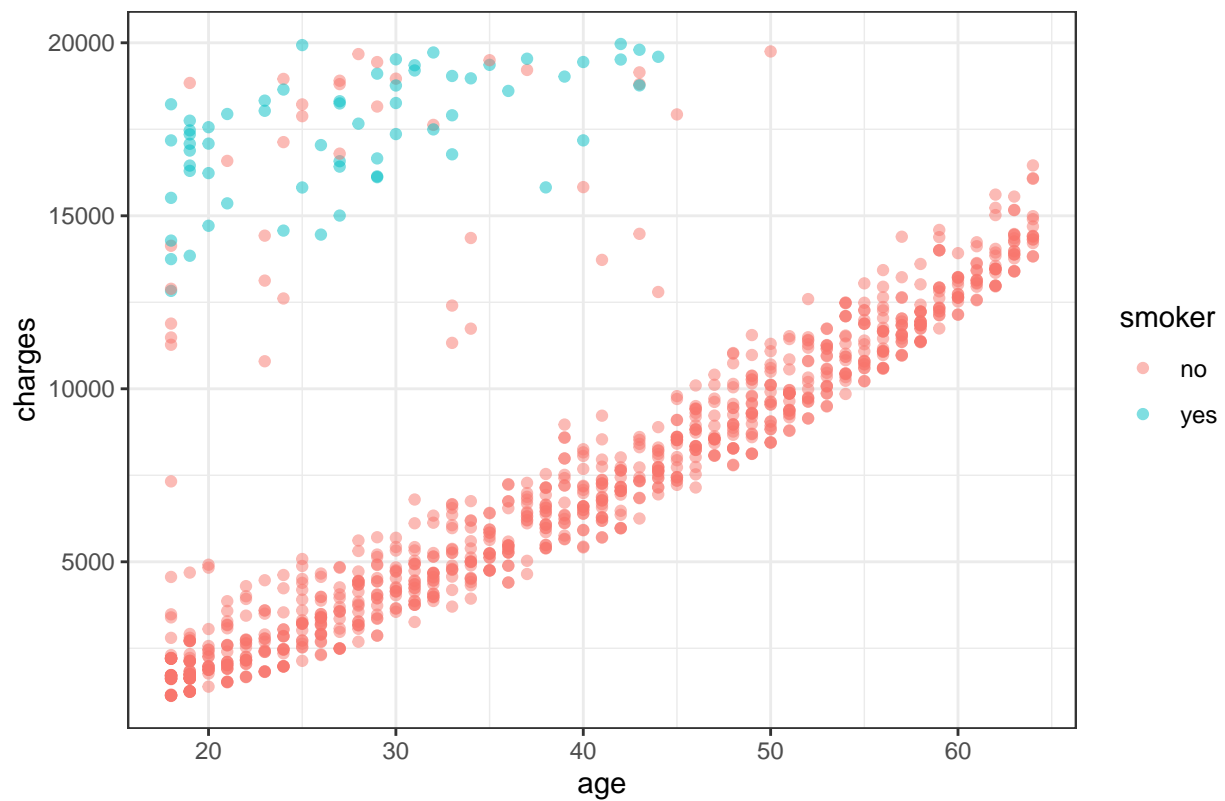
```
less_charge <- data[data$charges < 20000,]
more_change <- data[data$charges >= 20000, ]
library(tidyverse)
ggplot(aes(x=bmi, y=charges, color=smoker), data=less_charge) +
  labs(title="Scatter Plot of Charges vs BMI by Smoker Status for charges < 20,000") +
  theme_bw() +
  geom_point()
```

Scatter Plot of Charges vs BMI by Smoker Status for charges < 20,000



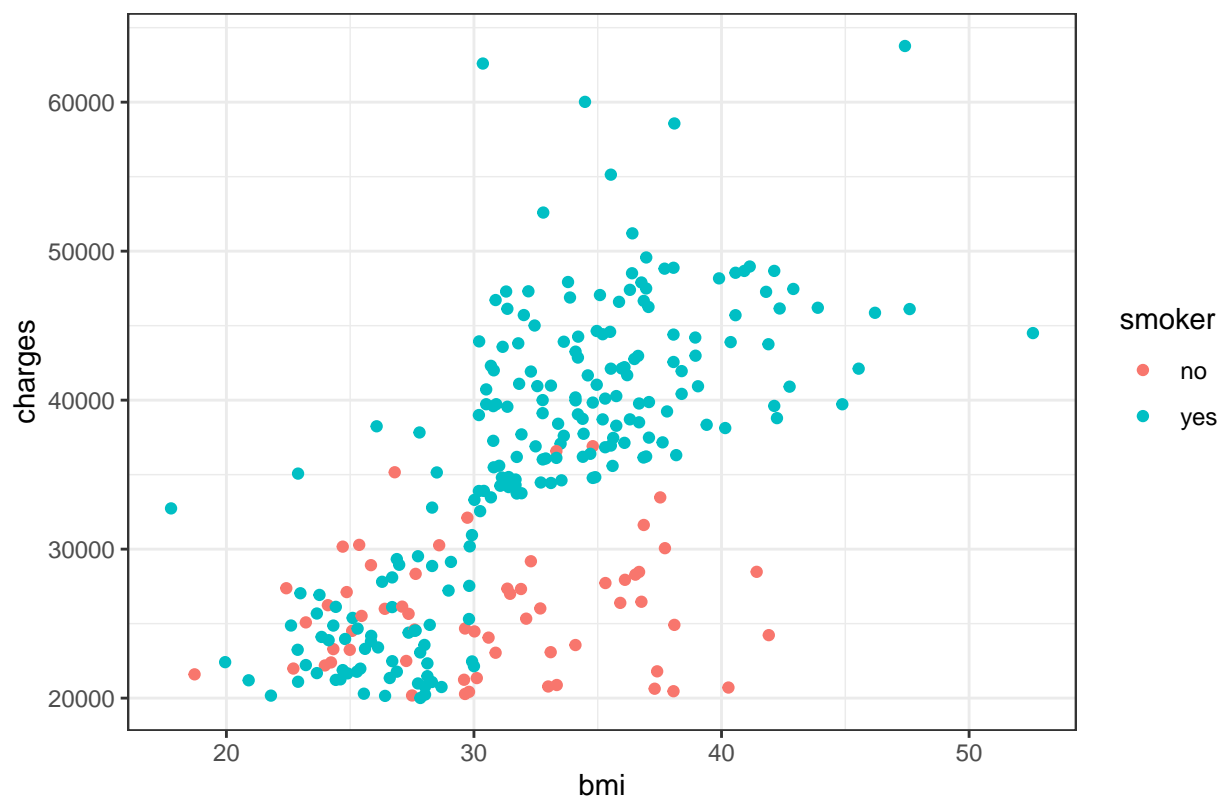
```
ggplot(aes(x=age,y=charges, color=smoker), data=less_charge) +  
  labs(title="Scatter plot of Charges vs Age by Smoker Status charges < 20,000") +  
  theme_bw() +  
  geom_point(alpha=0.5)
```

Scatter plot of Charges vs Age by Smoker Status charges < 20,000



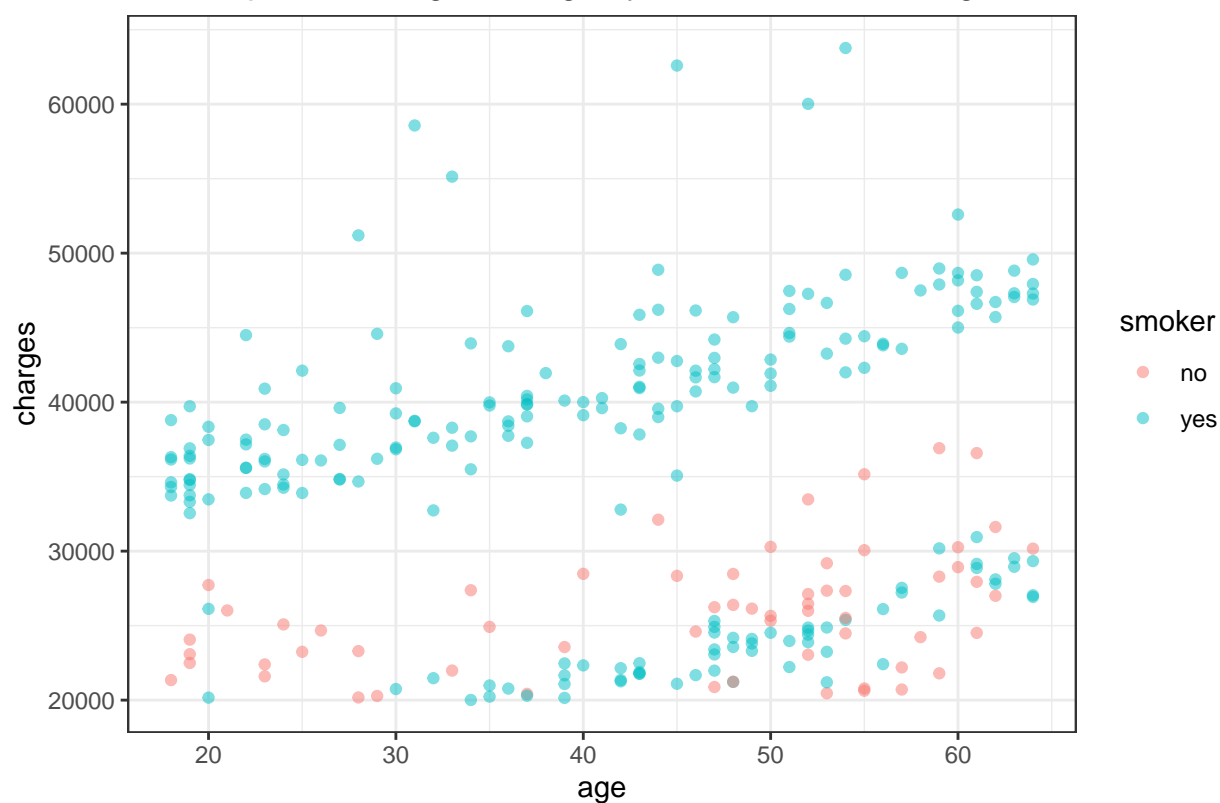
```
ggplot(aes(x=bmi, y=charges, color=smoker), data=more_change) +
  labs(title="Scatter Plot of Charges vs BMI by Smoker Status charges > 20,000") +
  theme_bw() +
  geom_point()
```

Scatter Plot of Charges vs BMI by Smoker Status charges > 20,000

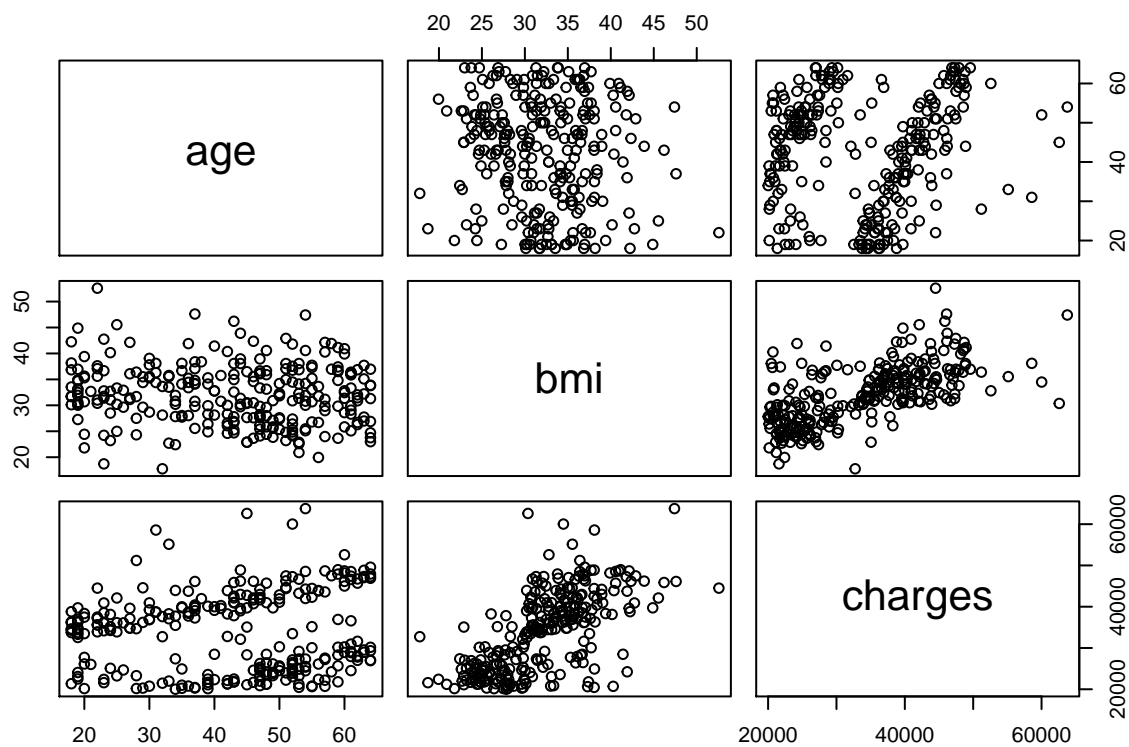


```
ggplot(aes(x=age,y=charges, color=smoker), data=more_change) +
  labs(title="Scatter plot of Charges vs Age by Smoker Status charges > 20,000") +
  theme_bw() +
  geom_point(alpha=0.5)
```

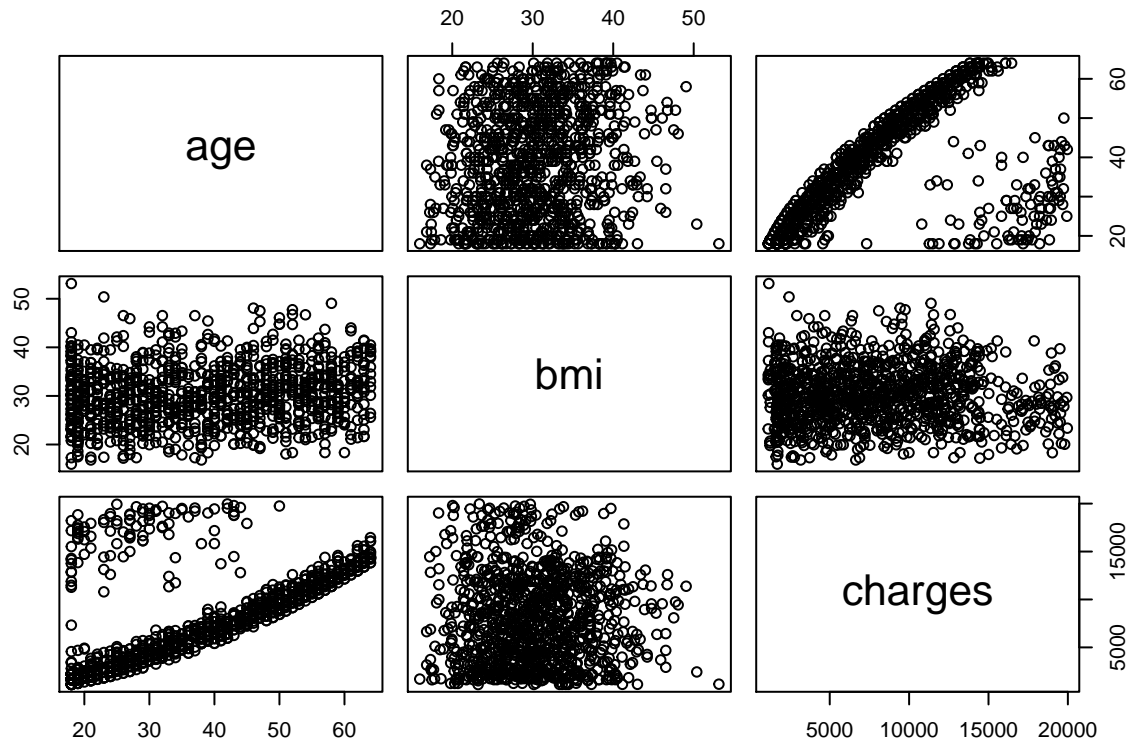
Scatter plot of Charges vs Age by Smoker Status charges > 20,000



```
pairs(more_change[c("age", "bmi", "charges")])
```



```
pairs(less_charge[c("age", "bmi", "charges")])
```



```
mlr_full_smoker = lm(charges ~ (age + bmi + children + region) * smoker, data=data)
summary(mlr_full_smoker)
```

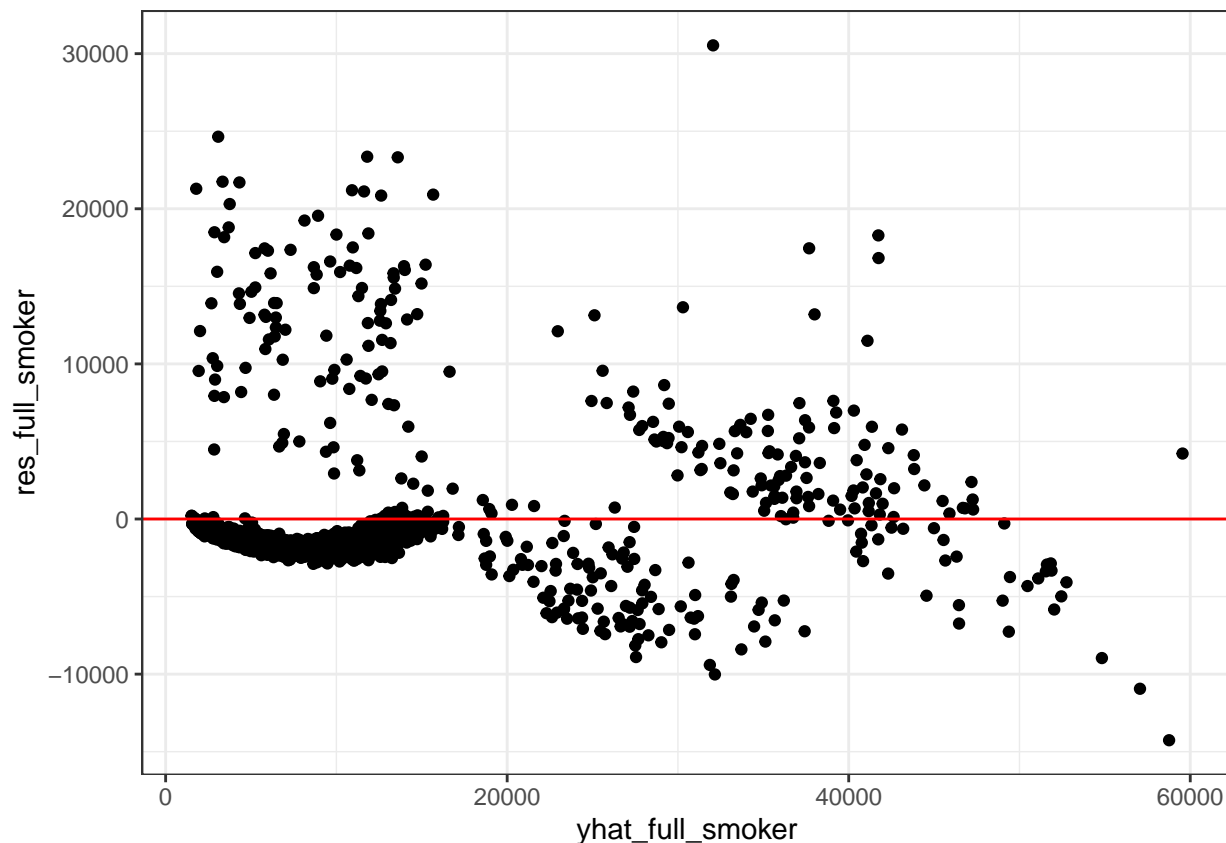
```
##
## Call:
## lm(formula = charges ~ (age + bmi + children + region) * smoker,
##     data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14260.4  -1922.0  -1299.4   -410.1   30534.4
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -2450.179    878.080  -2.790  0.00534 **
## age             264.947    10.671  24.828 < 2e-16 ***
## bmi             17.939    25.910   0.692  0.48883
## children       586.903    122.242   4.801 1.76e-06 ***
## regionnorthwest -552.249    423.912  -1.303  0.19289
## regionsoutheast -989.701    435.141  -2.274  0.02310 *
## regionsouthwest -1385.975    424.969  -3.261  0.00114 **
## smokeryes     -20310.836   1907.109 -10.650 < 2e-16 ***
## age:smokeryes    2.673     23.819   0.112  0.91067
## bmi:smokeryes   1453.239    55.209  26.323 < 2e-16 ***
## children:smokeryes -417.913    283.549  -1.474  0.14076
## regionnorthwest:smokeryes -105.947    969.919  -0.109  0.91303
## regionsoutheast:smokeryes -898.633    920.894  -0.976  0.32933
## regionsouthwest:smokeryes  935.973    977.752   0.957  0.33861
```



```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4850 on 1324 degrees of freedom
## Multiple R-squared:  0.8412, Adjusted R-squared:  0.8396
## F-statistic: 539.5 on 13 and 1324 DF,  p-value: < 2.2e-16
```

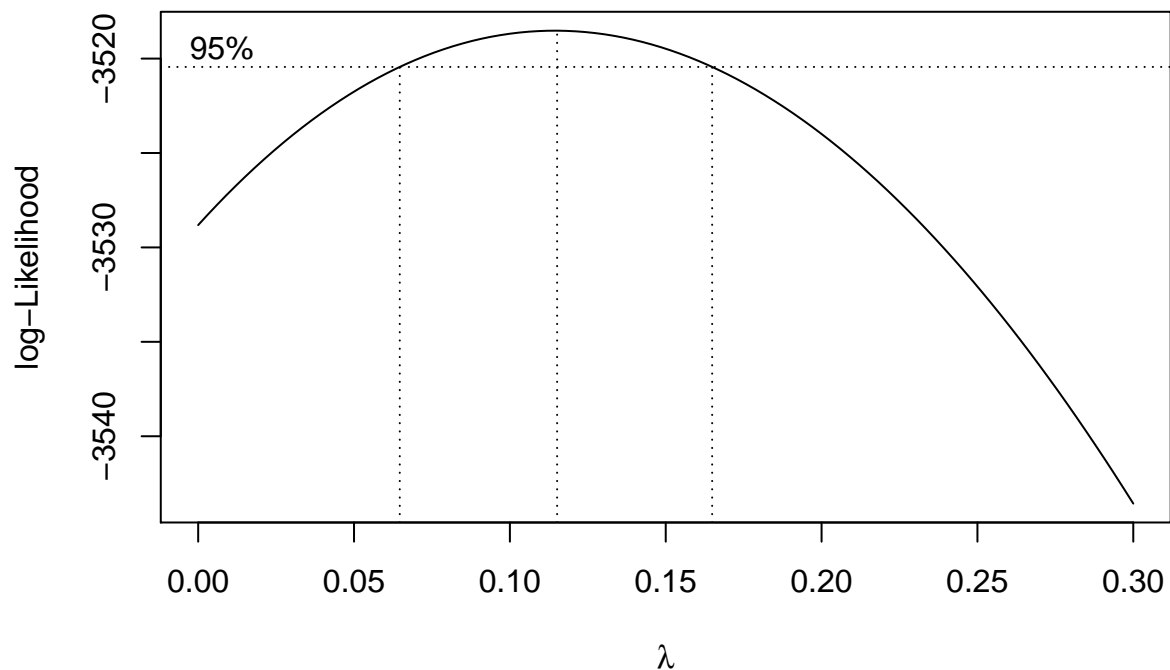
Assumption Check of Full Model

```
yhat_full_smoker <- mlr_full_smoker$fitted.values
res_full_smoker <- mlr_full_smoker$residuals
data %>%
  ggplot(aes(yhat_full_smoker, res_full_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



The residuals are obviously not evenly scattered, which then we can utilize the boxcox method to give us information about transformation.

```
boxcox(mlr_full_smoker, lambda=seq(0,0.3, 0.01))
```



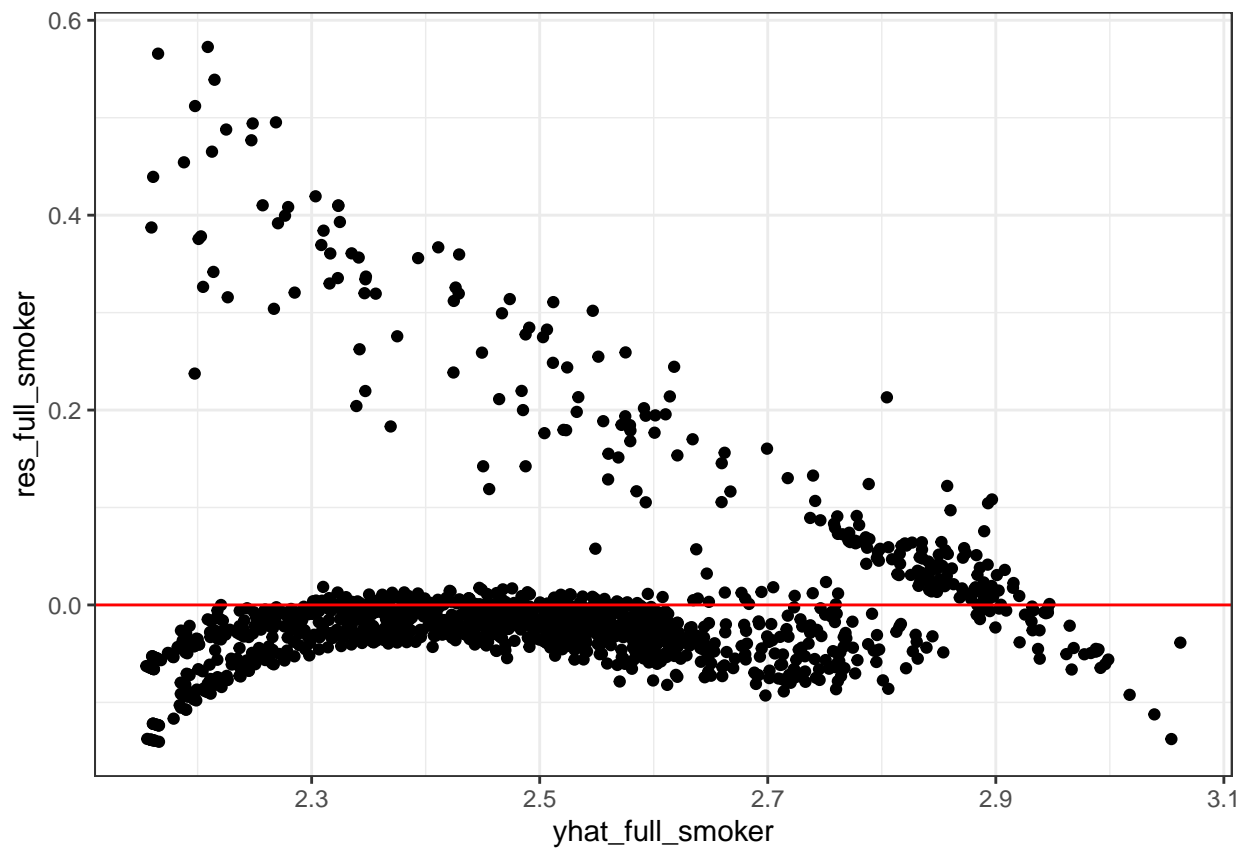
From the boxcox we can try a lambda value of 0.1 for transformation.

```
interaction_transform_smoker <- data
interaction_transform_smoker$charges <- interaction_transform_smoker$charges^0.1
mlr_interaction_tranform_smoker <- lm(charges ~ (age + bmi + children + region) * smoker, data=interaction_transform_smoker)
summary(mlr_interaction_tranform_smoker)
```

```
##
## Call:
## lm(formula = charges ~ (age + bmi + children + region) * smoker,
##     data = interaction_transform_smoker)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.14041 -0.03918 -0.01973 -0.00012  0.57262
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.0103535   0.0171453  117.254 < 2e-16 ***
## age             0.0098368   0.0002084   47.209 < 2e-16 ***
## bmi             0.0003437   0.0005059    0.679  0.4970
## children        0.0292642   0.0023869   12.260 < 2e-16 ***
## regionnorthwest -0.0180006   0.0082773   -2.175  0.0298 *
## regionsoutheast -0.0395694   0.0084965   -4.657 3.53e-06 ***
## regionsouthwest -0.0433088   0.0082979   -5.219 2.08e-07 ***
## smokeryes       0.2783934   0.0372380    7.476 1.39e-13 ***
## age:smokeryes   -0.0073089   0.0004651  -15.715 < 2e-16 ***
## bmi:smokeryes    0.0134167   0.0010780   12.446 < 2e-16 ***
## children:smokeryes -0.0273920   0.0055365   -4.947 8.48e-07 ***
## regionnorthwest:smokeryes 0.0142893   0.0189385    0.755  0.4507
## regionsoutheast:smokeryes 0.0237658   0.0179813    1.322  0.1865
## regionsouthwest:smokeryes 0.0413423   0.0190915    2.165  0.0305 *
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09469 on 1324 degrees of freedom
## Multiple R-squared:  0.83, Adjusted R-squared:  0.8283
## F-statistic: 497.3 on 13 and 1324 DF,  p-value: < 2.2e-16

yhat_full_smoker <- mlr_interaction_tranform_smoker$fitted.values
res_full_smoker <- mlr_interaction_tranform_smoker$residuals
data %>%
  ggplot(aes(yhat_full_smoker, res_full_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```

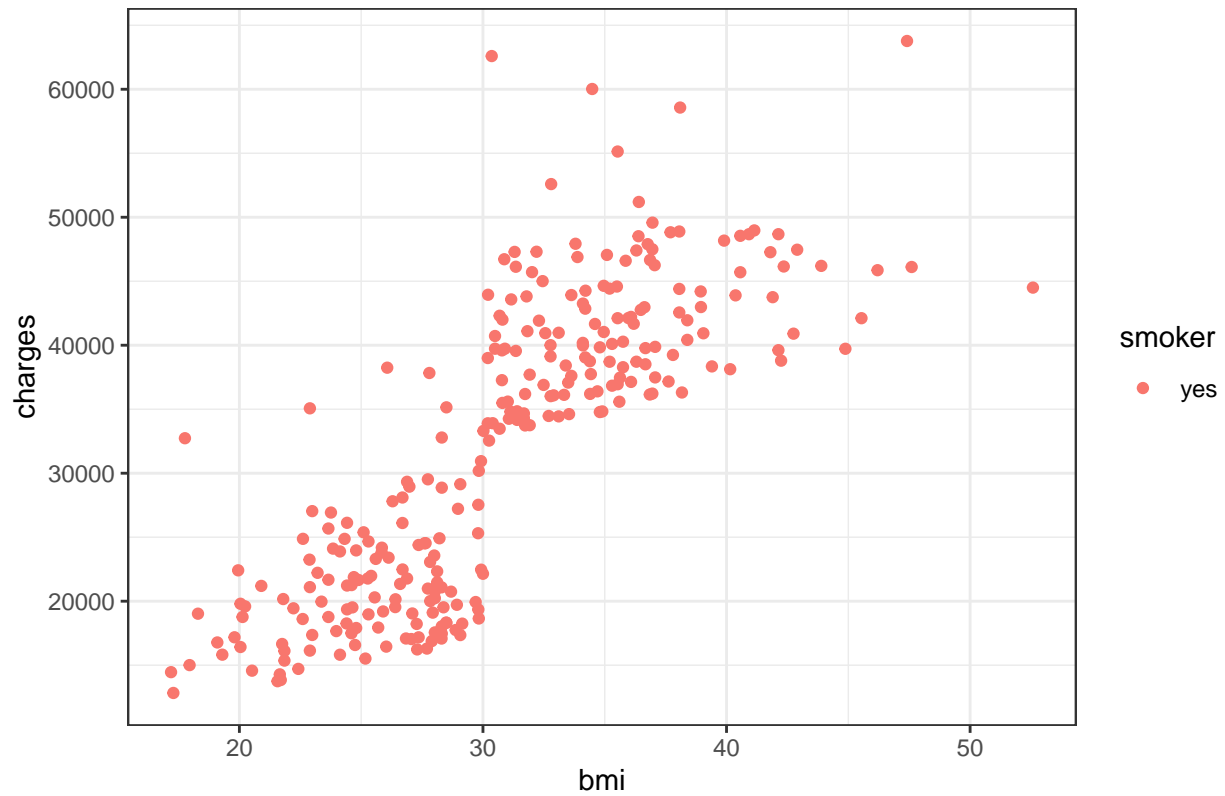


Lets SPLIT BY SMOKERS

```
smokers <- data[data$smoker == 'yes',]
non_smokers <- data[data$smoker != 'yes',]

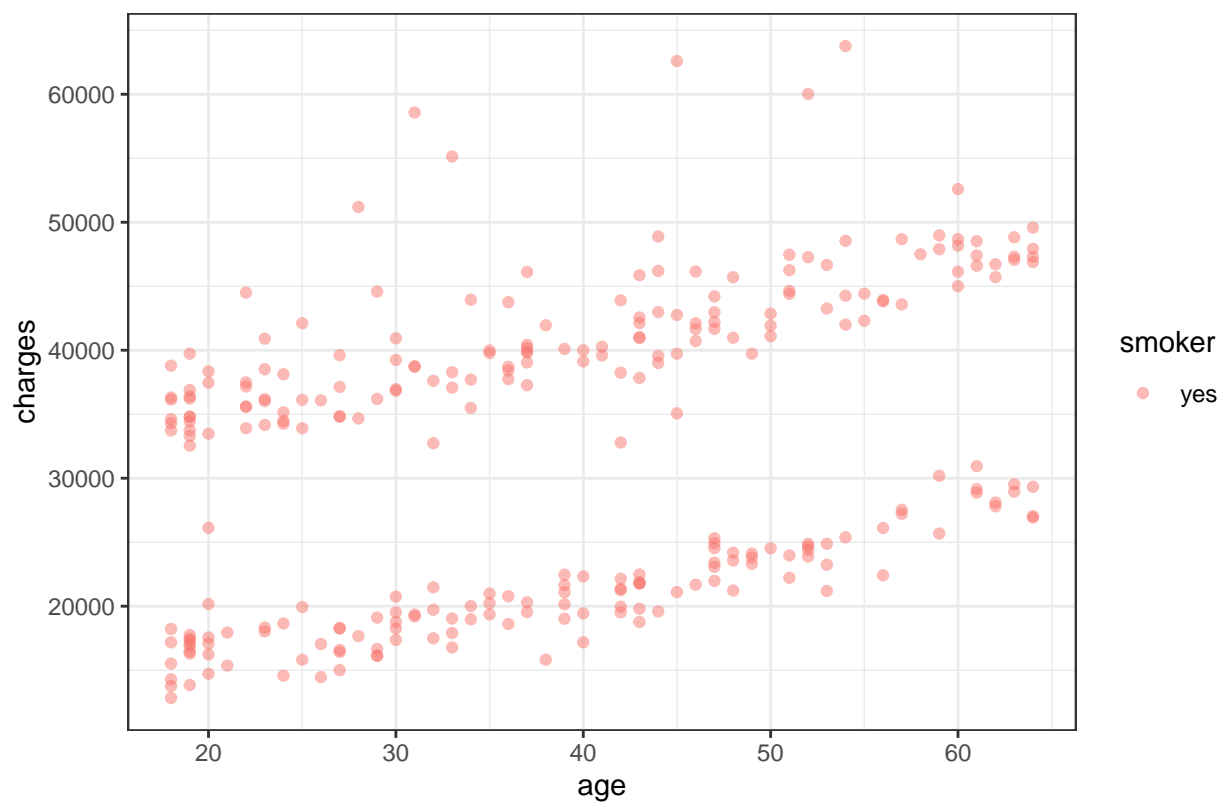
ggplot(aes(x=bmi, y=charges, color=smoker), data=smokers) +
  labs(title="Scatter Plot of Charges vs BMI For Smokers") +
  theme_bw() +
  geom_point()
```

Scatter Plot of Charges vs BMI For Smokers



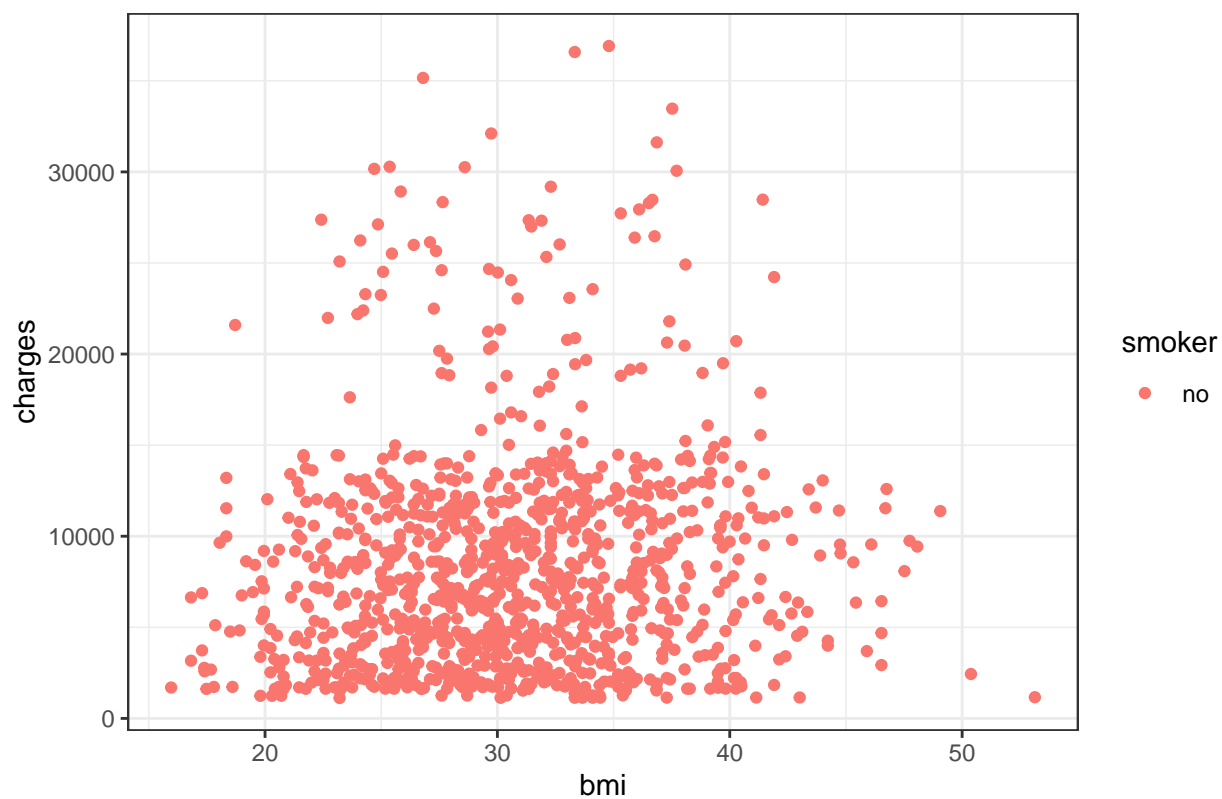
```
ggplot(aes(x=age,y=charges, color=smoker), data=smokers) +  
  labs(title="Scatter plot of Charges vs Age For Smokers") +  
  theme_bw() +  
  geom_point(alpha=0.5)
```

Scatter plot of Charges vs Age For Smokers



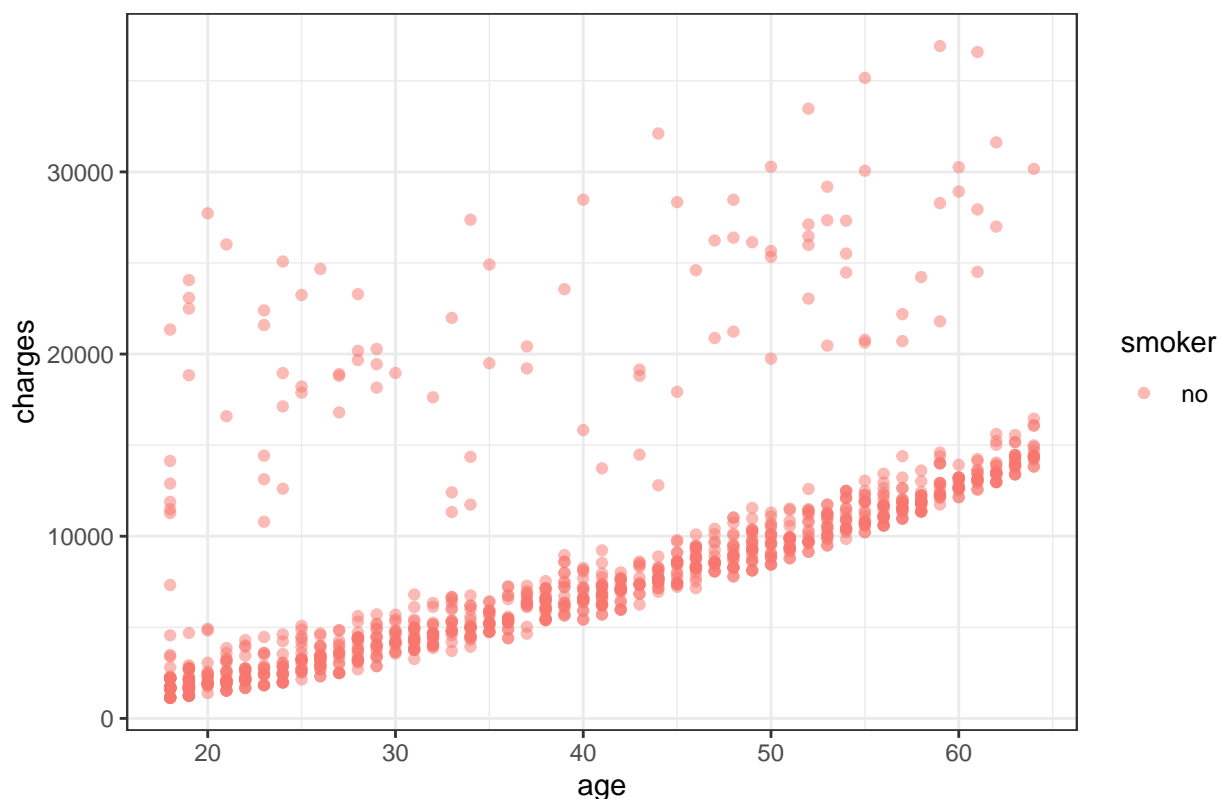
```
ggplot(aes(x=bmi, y=charges, color=smoker), data=non_smokers) +  
  labs(title="Scatter Plot of Charges vs BMI For Non_Smokers") +  
  theme_bw() +  
  geom_point()
```

Scatter Plot of Charges vs BMI For Non_Smokers



```
ggplot(aes(x=age,y=charges, color=smoker), data=non_smokers) +  
  labs(title="Scatter plot of Charges vs Age For Non_Smokers") +  
  theme_bw() +  
  geom_point(alpha=0.5)
```

Scatter plot of Charges vs Age For Non_Smokers



```
## Smokers
##intercept only model
regnull_smoker <- lm(charges~1, data=smokers)
##model with all predictors
regfull_smoker <- lm(charges ~ age + sex + bmi + children + region , data=smokers)
```

Forward Selection

```
step(regnull_smoker, scope=list(lower=regnull_smoker, upper=regfull_smoker), direction="forward")
```

```
## Start: AIC=5126.83
## charges ~ 1
##
##           Df Sum of Sq      RSS   AIC
## + bmi      1 2.3653e+10 1.2713e+10 4840.9
## + age      1 4.9308e+09 3.1435e+10 5088.9
## + region   3 1.2923e+09 3.5073e+10 5122.9
## + sex      1 3.7263e+08 3.5993e+10 5126.0
## <none>                      3.6366e+10 5126.8
## + children 1 4.6986e+07 3.6319e+10 5128.5
##
## Step: AIC=4840.86
## charges ~ bmi
##
##           Df Sum of Sq      RSS   AIC
## + age      1 3739448620 8.9736e+09 4747.4
## <none>                      1.2713e+10 4840.9
## + children 1 77371010 1.2636e+10 4841.2
```

```
## + sex      1  12609906 1.2700e+10 4842.6
## + region   3  112969895 1.2600e+10 4844.4
##
## Step:  AIC=4747.41
## charges ~ bmi + age
##
##           Df Sum of Sq      RSS      AIC
## <none>                8973564816 4747.4
## + region   3 149563719 8824001097 4748.8
## + children  1  14356763 8959208053 4749.0
## + sex      1   7002694 8966562122 4749.2
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers)
##
## Coefficients:
## (Intercept)          bmi          age
##    -22367.4         1438.1          266.3

#Non smokers
regnull_non_smokers <- lm(charges~1, data=non_smokers)
##model with all predictors
regfull_non_smokers <- lm(charges ~ age + sex + bmi + children + region , data=non_smokers)
```

Forward Selection

```
step(regnull_non_smokers, scope=list(lower=regnull_non_smokers, upper=regfull_non_smokers), direction="")
```

```
## Start:  AIC=18511.36
## charges ~ 1
##
##           Df Sum of Sq      RSS      AIC
## + age      1 1.5058e+10 2.3130e+10 17980
## + children  1 7.3709e+08 3.7452e+10 18493
## + bmi      1 2.6969e+08 3.7919e+10 18506
## + sex      1 1.2113e+08 3.8068e+10 18510
## + region   3 2.3153e+08 3.7957e+10 18511
## <none>                3.8189e+10 18511
##
## Step:  AIC=17979.87
## charges ~ age
##
##           Df Sum of Sq      RSS      AIC
## + children  1 531956489 2.2598e+10 17957
## + region   3 248975743 2.2881e+10 17974
## + sex      1  68342342 2.3062e+10 17979
## <none>                2.3130e+10 17980
## + bmi      1   1914187 2.3128e+10 17982
##
## Step:  AIC=17957.12
## charges ~ age + children
##
##           Df Sum of Sq      RSS      AIC
## + region   3 262141210 2.2336e+10 17951
## + sex      1  69429619 2.2529e+10 17956
```



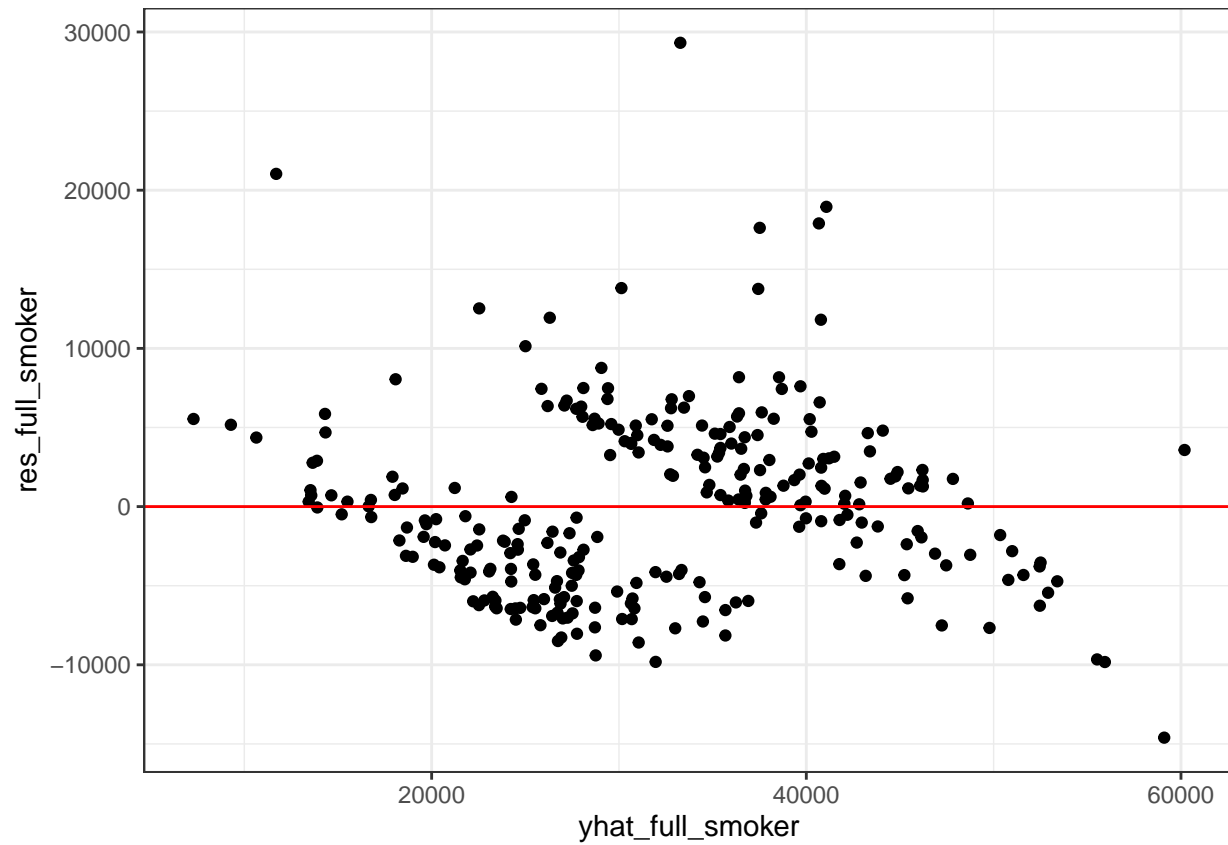
```
## <none>                2.2598e+10 17957
## + bmi      1    1065536 2.2597e+10 17959
##
## Step: AIC=17950.7
## charges ~ age + children + region
##
##      Df Sum of Sq      RSS   AIC
## + sex  1  72093470 2.2264e+10 17949
## <none>                2.2336e+10 17951
## + bmi  1  11274021 2.2325e+10 17952
##
## Step: AIC=17949.26
## charges ~ age + children + region + sex
##
##      Df Sum of Sq      RSS   AIC
## <none>                2.2264e+10 17949
## + bmi  1  12614493 2.2251e+10 17951
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smokers)
##
## Coefficients:
##      (Intercept)              age      children regionnorthwest
##          -1695.9             265.5             589.1           -550.2
## regionsoutheast regionsouthwest      sexmale
##          -913.2             -1373.0           -521.0
```

We get different models

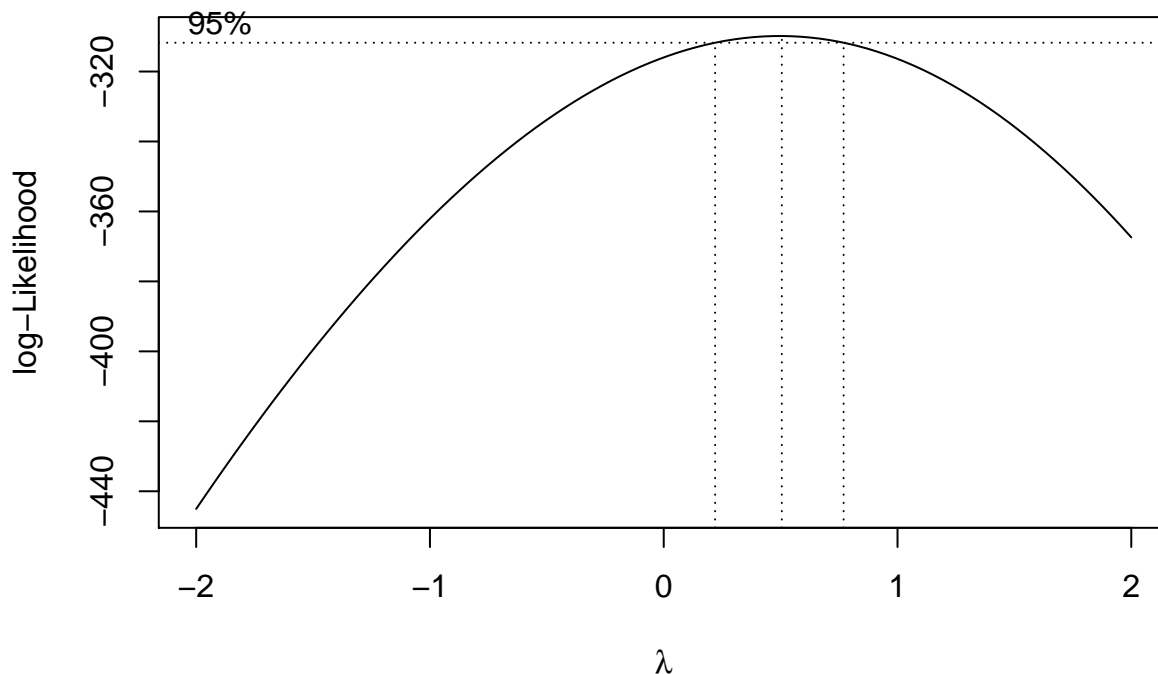
```
mlr_full_smoker = lm(charges ~ bmi+age , data=smokers)
summary(mlr_full_smoker)
```

```
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14604.4  -4315.1   -240.5   3638.0  29316.7
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -22367.45    1931.86  -11.58  <2e-16 ***
## bmi          1438.09     55.22    26.05  <2e-16 ***
## age          266.29      25.06    10.63  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5754 on 271 degrees of freedom
## Multiple R-squared:  0.7532, Adjusted R-squared:  0.7514
## F-statistic: 413.6 on 2 and 271 DF, p-value: < 2.2e-16
yhat_full_smoker <- mlr_full_smoker$fitted.values
res_full_smoker <- mlr_full_smoker$residuals
```

```
smokers %>%
  ggplot(aes(yhat_full_smoker, res_full_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



```
boxcox(mlr_full_smoker)
```



Rseponse needs to be transformed

```
smokers_transform <- smokers
smokers_transform$charges <- smokers_transform$charges^0.5
mlr_full_smoker_transform = lm(charges ~ bmi+age , data=smokers_transform)
mlr_full_smoker_transform_full = lm(charges ~ bmi+age + sex + region , data=smokers_transform)

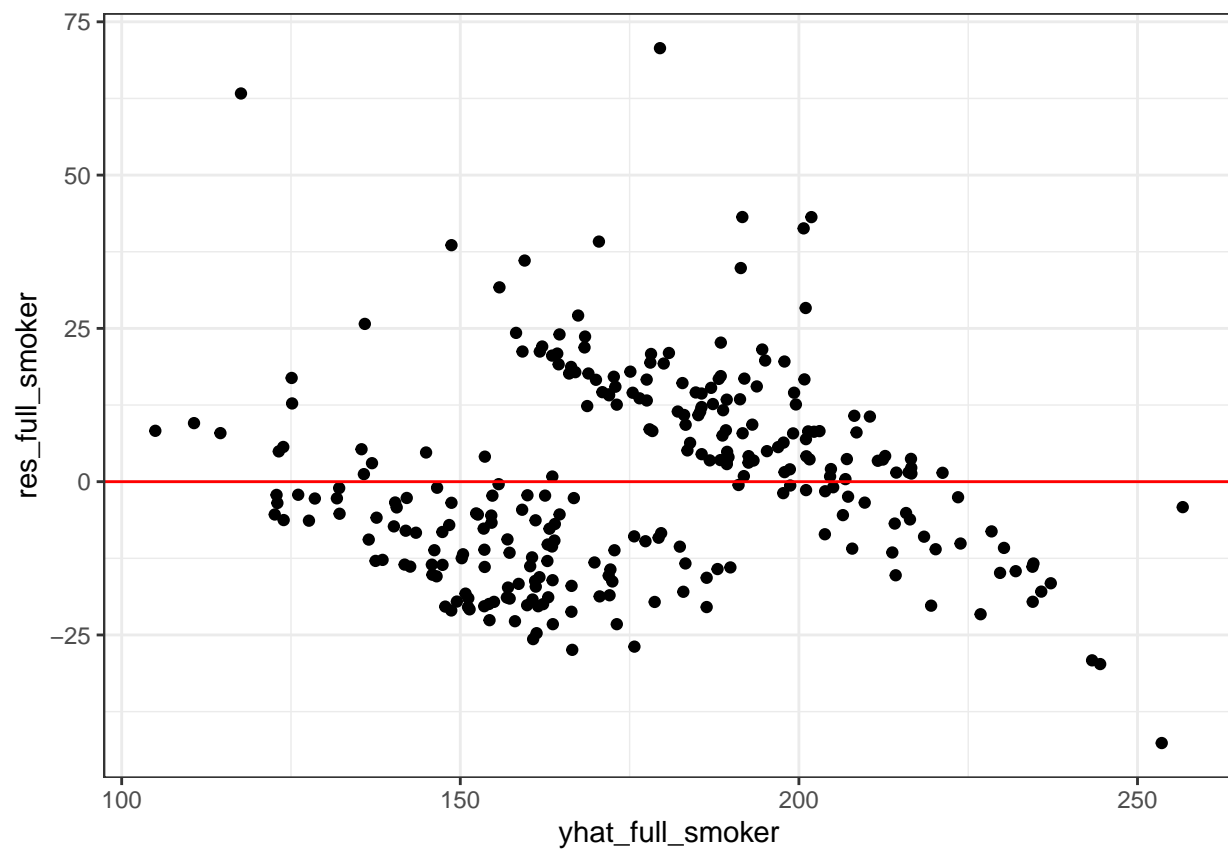
summary(mlr_full_smoker_transform)
```

```
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -42.622 -12.877  -1.715  10.868  70.699
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  19.9145     5.4586   3.648 0.000317 ***
## bmi           4.1245     0.1560  26.436 < 2e-16 ***
## age           0.7634     0.0708  10.781 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.26 on 271 degrees of freedom
## Multiple R-squared:  0.7587, Adjusted R-squared:  0.7569
## F-statistic: 426.1 on 2 and 271 DF, p-value: < 2.2e-16
```

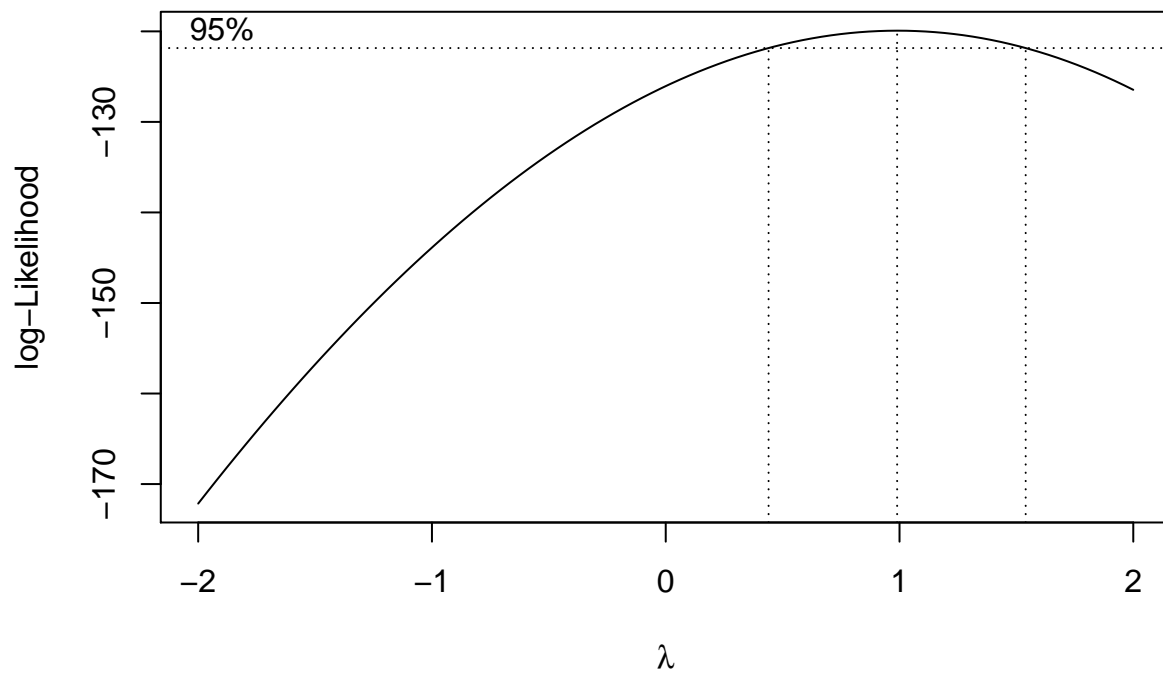
residual plot

```
yhat_full_smoker <- mlr_full_smoker_transform$fitted.values
res_full_smoker <- mlr_full_smoker_transform$residuals
smokers %>%
```

```
ggplot(aes(yhat_full_smoker, res_full_smoker)) +  
  geom_point() +  
  theme_bw() +  
  geom_hline(yintercept = 0, color="red")
```



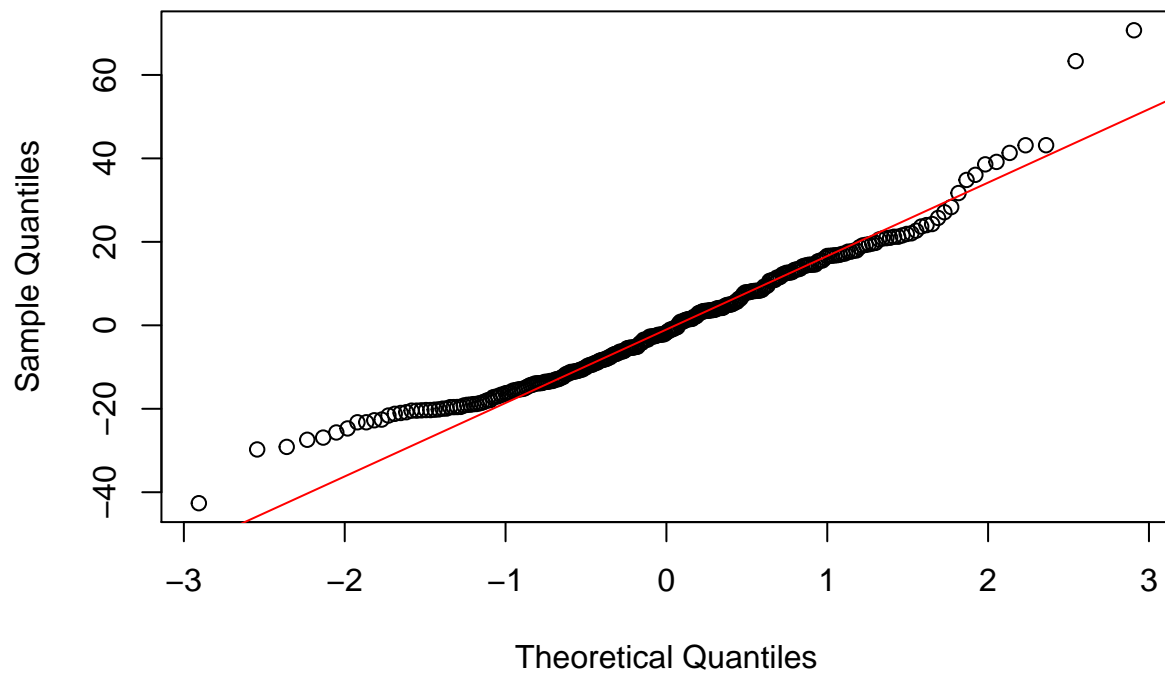
```
boxcox(mlr_full_smoker_transform)
```



QQPlot

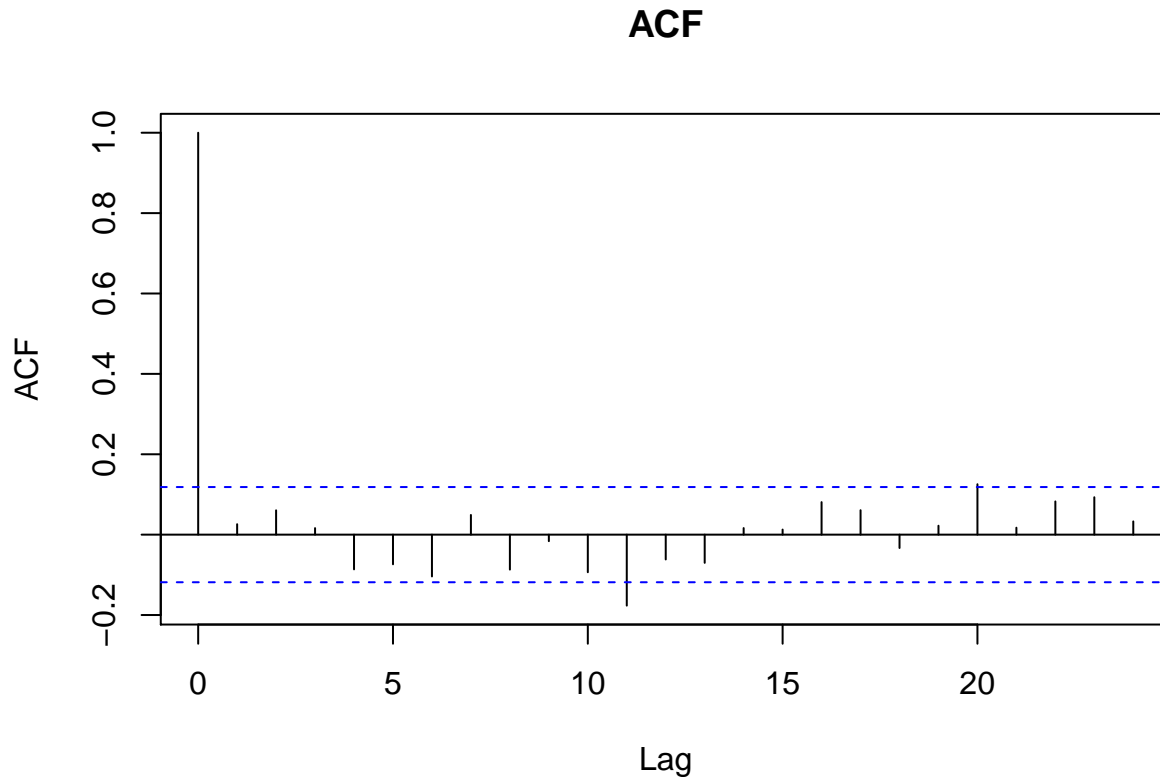
```
{
  qqnorm(mlr_full_smoker_transform$residuals)
  qqline(mlr_full_smoker_transform$residuals, col="red")
}
```

Normal Q-Q Plot



ACF

```
acf(mlr_full_smoker_transform$residuals, main="ACF")
```



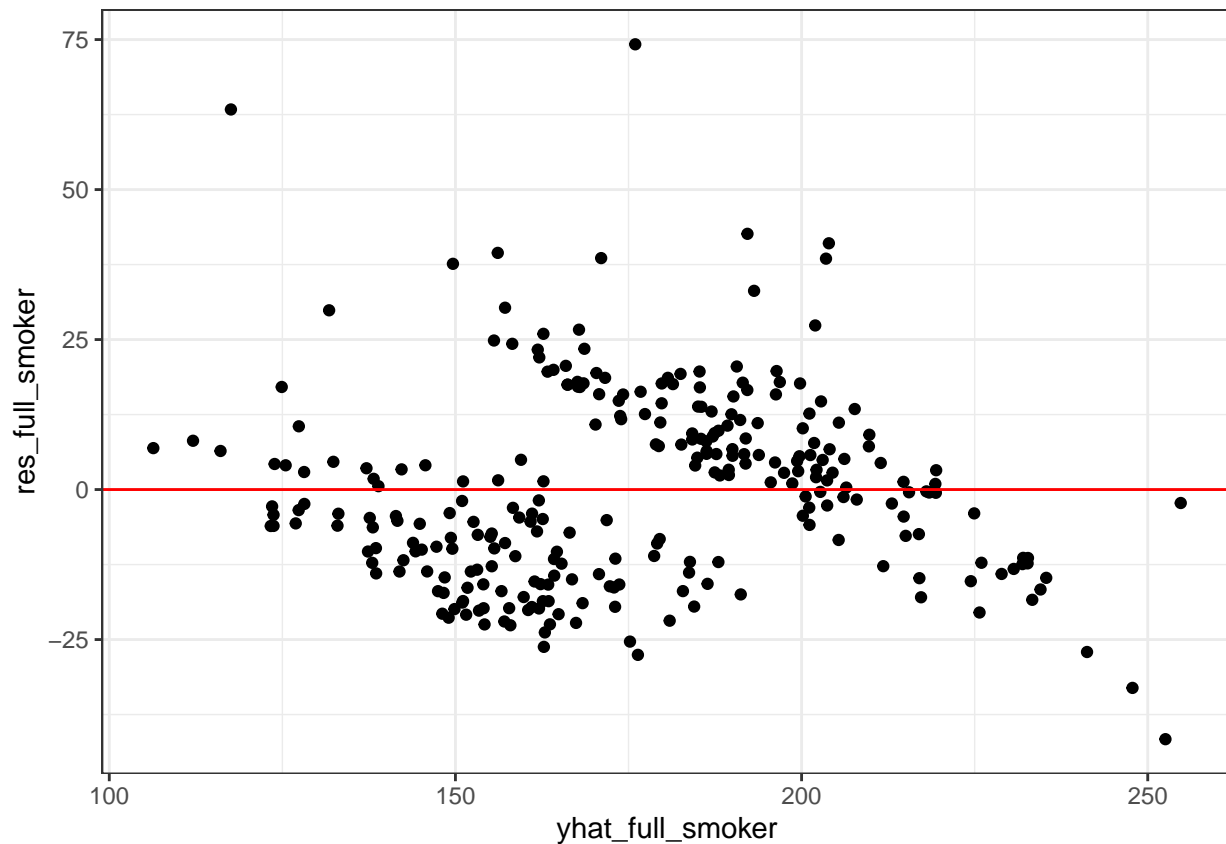
What about Region

```
mlr_full_smoker_full = lm(charges ~ bmi+age+children+region , data=smokers_transform)
summary(mlr_full_smoker_full)
```

```
##
## Call:
## lm(formula = charges ~ bmi + age + children + region, data = smokers_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -41.603 -12.339  -0.845   9.705  74.211
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   18.58918    5.66726   3.280  0.00118 **
## bmi           4.21653    0.16320  25.837 < 2e-16 ***
## age           0.76698    0.07129  10.759 < 2e-16 ***
## children      0.53142    0.85647   0.620  0.53547
## regionnorthwest -1.53030    2.92036  -0.524  0.60071
## regionsoutheast -5.14260    2.71691  -1.893  0.05946 .
## regionsouthwest -0.93879    2.94778  -0.318  0.75038
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.23 on 267 degrees of freedom
```

```
## Multiple R-squared:  0.763, Adjusted R-squared:  0.7577
## F-statistic: 143.3 on 6 and 267 DF,  p-value: < 2.2e-16
```

```
yhat_full_smoker <- mlr_full_smoker_full$fitted.values
res_full_smoker <- mlr_full_smoker_full$residuals
smokers %>%
  ggplot(aes(yhat_full_smoker, res_full_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



Residual Seems Fine, can we drop these predictors?

```
summary(mlr_full_smoker_transform)
```

```
##
## Call:
## lm(formula = charges ~ bmi + age, data = smokers_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -42.622 -12.877  -1.715  10.868  70.699
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   19.9145     5.4586   3.648 0.000317 ***
## bmi           4.1245     0.1560  26.436 < 2e-16 ***
## age           0.7634     0.0708  10.781 < 2e-16 ***
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.26 on 271 degrees of freedom
## Multiple R-squared:  0.7587, Adjusted R-squared:  0.7569
## F-statistic: 426.1 on 2 and 271 DF,  p-value: < 2.2e-16
```

```
anova(mlr_full_smoker_transform,mlr_full_smoker_transform_full )
```

```
## Analysis of Variance Table
##
## Model 1: charges ~ bmi + age
## Model 2: charges ~ bmi + age + sex + region
##   Res.Df  RSS Df Sum of Sq    F Pr(>F)
## 1      271 71645
## 2      267 70442  4    1202.7 1.1396 0.3382
```

We can drop these other predictors

Outliers

```
##critical value using Bonferroni procedure
n<-dim(smokers_transform)[1]
p<-3
crit<-qt(1-0.05/(2*n), n-1-p)
##externally studentized residuals
ext.student.res<-rstudent(mlr_full_smoker_transform)
##identify
ext.student.res[abs(ext.student.res)>crit]
```

```
##      129      1301
## 4.041989 4.510779
```

```
##leverages
lev<-lm.influence(mlr_full_smoker_transform)$hat
##identify
round(lev[lev>2*p/n],4)
```

```
##      251      293      413      544      550      665      804      861      1048      1125      1157
## 0.0268 0.0284 0.0226 0.0326 0.0258 0.0224 0.0251 0.0301 0.0547 0.0225 0.0307
```

```
DFFITS<-dffits(mlr_full_smoker_transform)
round(DFFITS[abs(DFFITS)>2*sqrt(p/n)],3)
```

```
##      129      293      550      578      820      861      918      1048      1157      1231      1301
## 0.569 -0.231 -0.297 0.260 0.218 -0.329 0.246 -0.656 -0.225 0.244 0.302
```

```
DFBETAS<-dfbetas(mlr_full_smoker_transform)
tempdfbetas = abs(DFBETAS)>2/sqrt(n)
tempdfbetas[(tempdfbetas[,1] == TRUE | tempdfbetas[,2] == TRUE | tempdfbetas[,3] == TRUE) ,]
```

```
##      (Intercept)  bmi   age
## 35             FALSE TRUE FALSE
## 95             FALSE FALSE TRUE
## 129            TRUE  TRUE FALSE
## 293            FALSE TRUE FALSE
## 477            FALSE FALSE TRUE
## 531            TRUE FALSE FALSE
## 550            TRUE  TRUE FALSE
```



```
## 578      FALSE TRUE FALSE
## 675      TRUE TRUE FALSE
## 820      FALSE TRUE FALSE
## 861      TRUE TRUE FALSE
## 918      TRUE TRUE FALSE
## 952      TRUE TRUE FALSE
## 1048     TRUE TRUE TRUE
## 1140     FALSE FALSE TRUE
## 1147     FALSE FALSE TRUE
## 1157     FALSE TRUE FALSE
## 1197     FALSE FALSE TRUE
## 1224     TRUE FALSE TRUE
## 1231     TRUE FALSE TRUE
## 1232     TRUE FALSE FALSE
## 1301     FALSE FALSE TRUE
## 1302     FALSE FALSE TRUE
```

```
COOKS<-cooks.distance(mlr_full_smoker_transform)
COOKS[COOKS>qf(0.5,p,n-p)]
```

```
## named numeric(0)
```

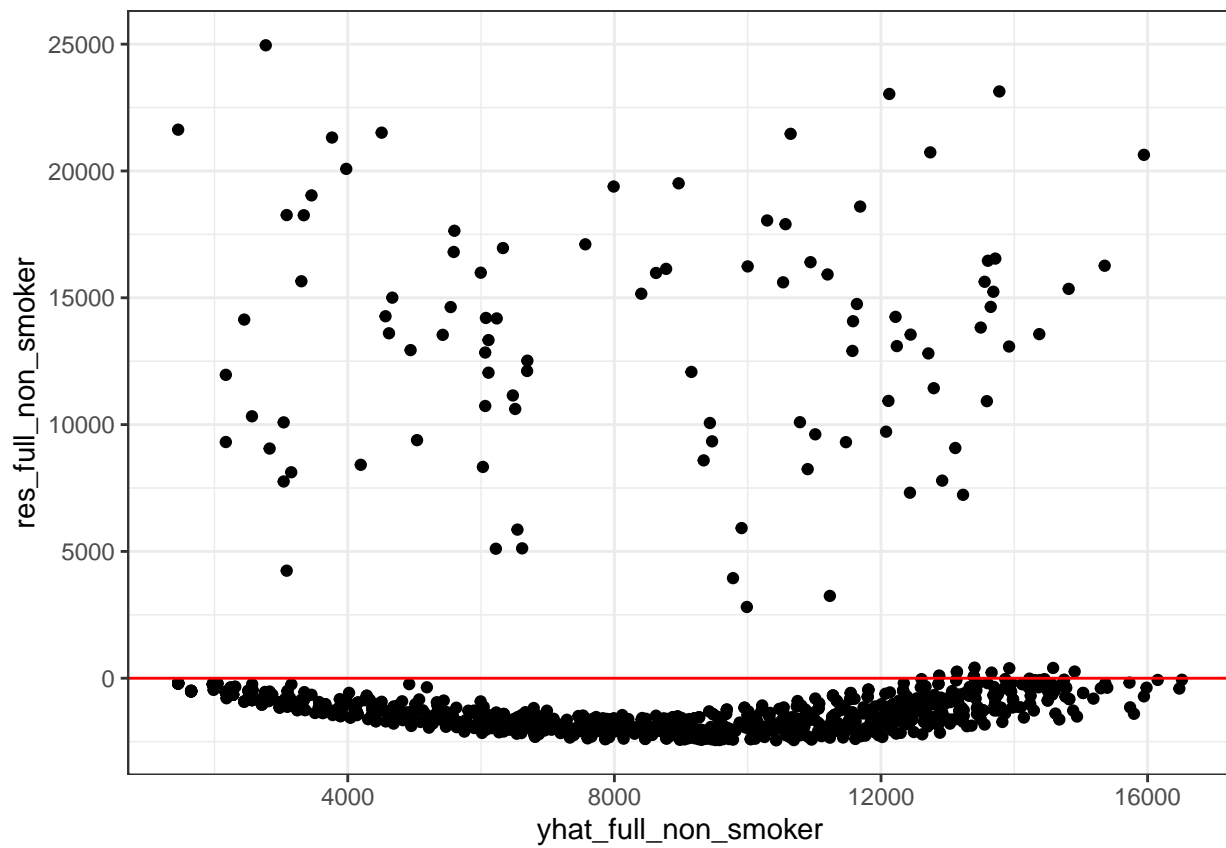
Non Smokers

```
mlr_full_non_smoker = lm(formula = charges ~ age + children + region + sex, data = non_smokers)
summary(mlr_full_non_smoker)
```

```
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smokers)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2441.2 -1870.1 -1380.6  -673.9 24954.7
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -1695.87     520.71  -3.257 0.001162 **
## age             265.53      10.01  26.524 < 2e-16 ***
## children       589.06      115.67   5.093 4.18e-07 ***
## regionnorthwest -550.17     401.17  -1.371 0.170544
## regionsoutheast -913.18     398.99  -2.289 0.022293 *
## regionsouthwest -1372.97     401.23  -3.422 0.000646 ***
## sexmale        -521.01     281.62  -1.850 0.064585 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4589 on 1057 degrees of freedom
## Multiple R-squared:  0.417, Adjusted R-squared:  0.4137
## F-statistic: 126 on 6 and 1057 DF, p-value: < 2.2e-16
```

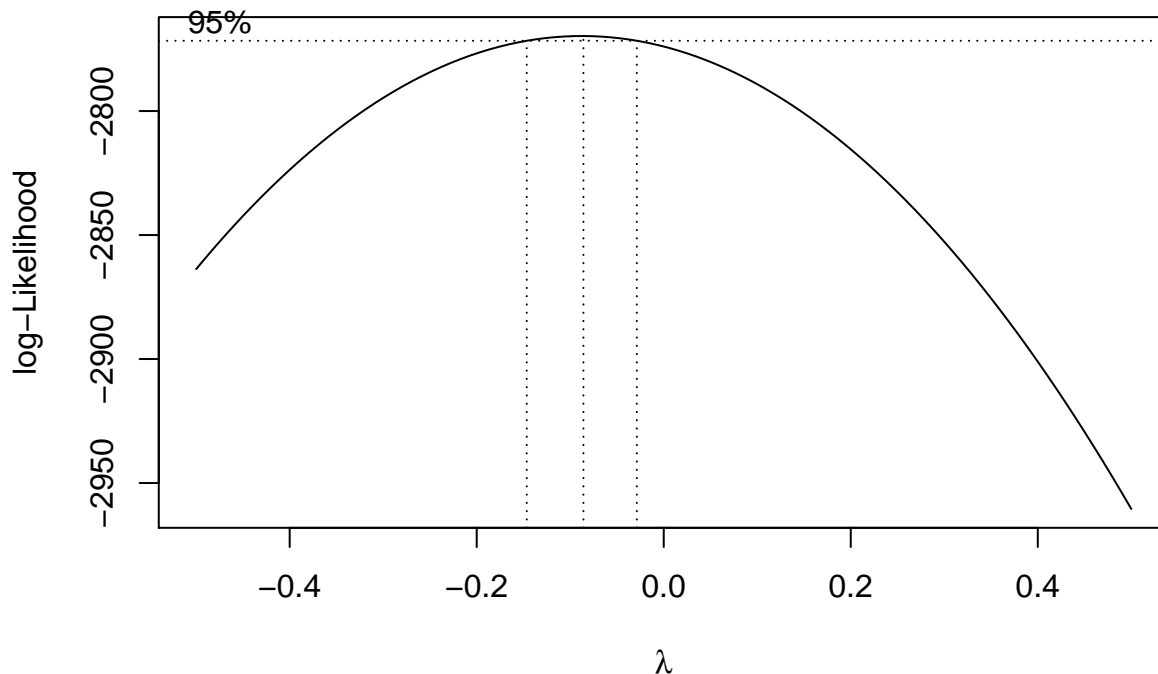
```
yhat_full_non_smoker <- mlr_full_non_smoker$fitted.values
res_full_non_smoker <- mlr_full_non_smoker$residuals
non_smokers %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
```

```
geom_point() +  
theme_bw() +  
geom_hline(yintercept = 0, color="red")
```



Transformation

```
boxcox(mlr_full_non_smoker, c(-0.5, 0.5, 0.1))
```

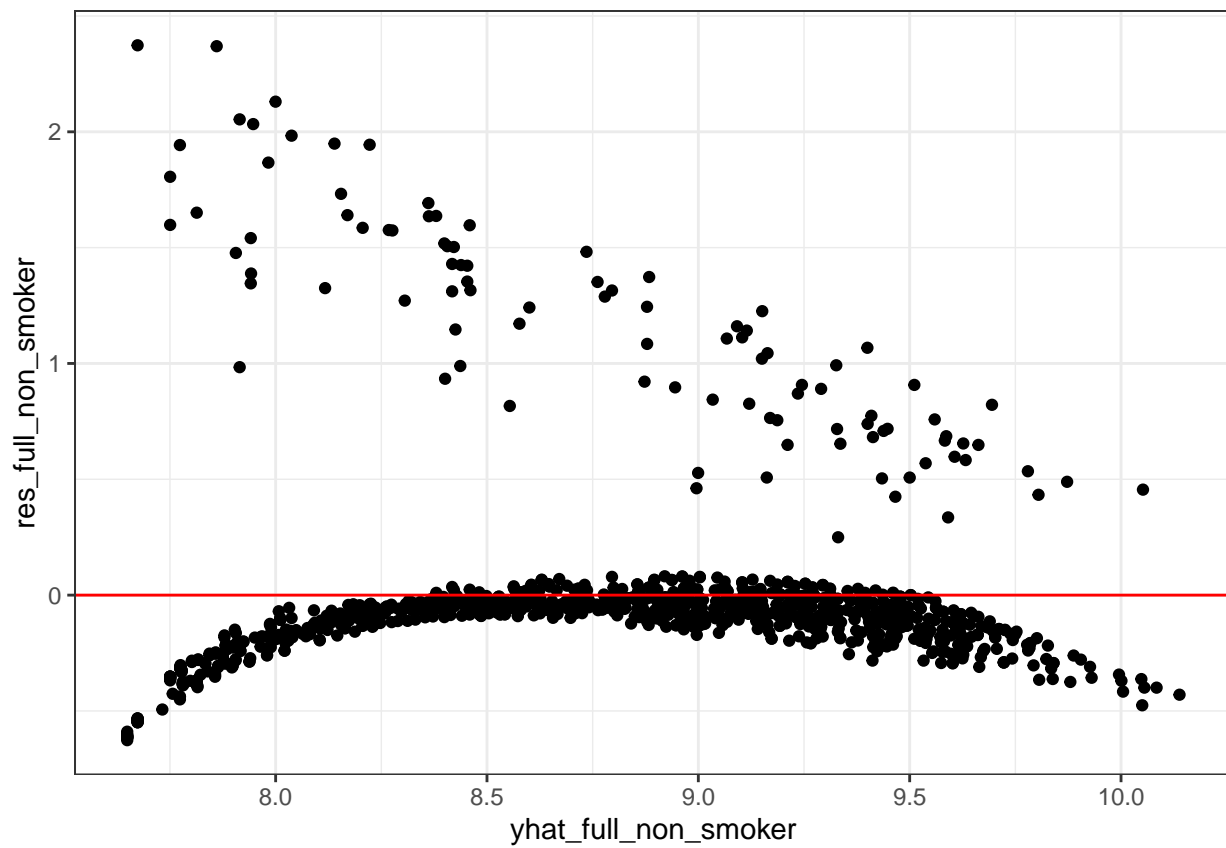


```
non_smoker_transform <- non_smokers
non_smoker_transform$charges <- log(non_smoker_transform$charges)
mlr_full_non_smoker_transform = lm(formula = charges ~ age + children + region + sex, data = non_smoker_transform)
summary(mlr_full_non_smoker_transform)
```

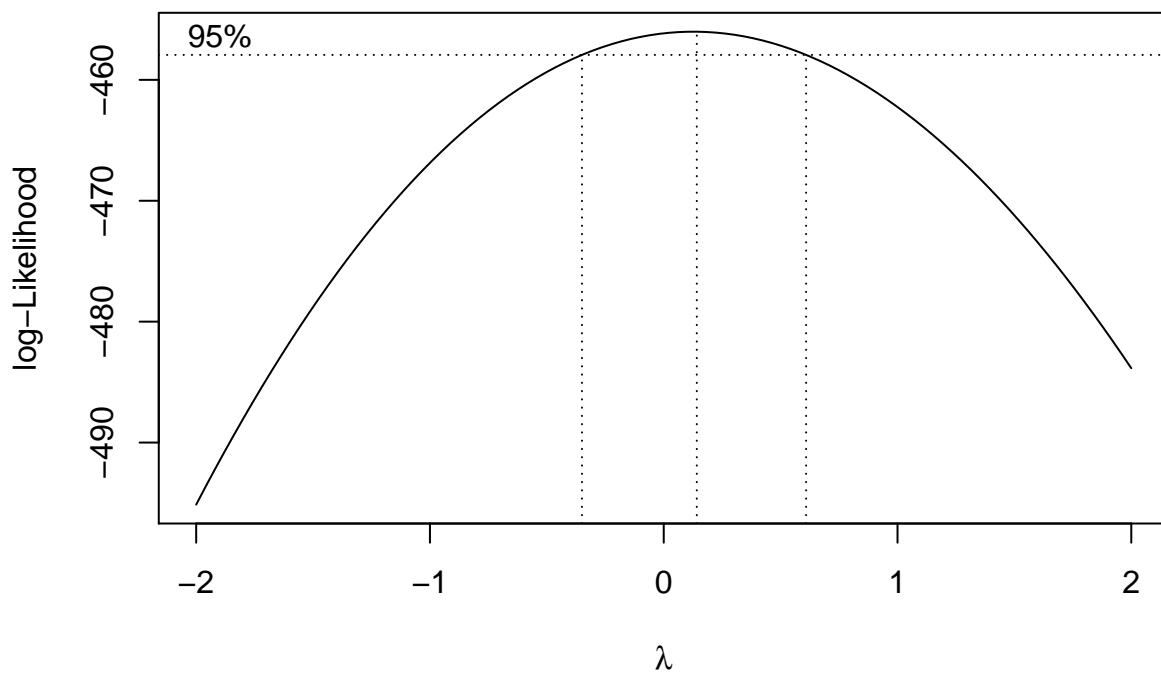
```
##
## Call:
## lm(formula = charges ~ age + children + region + sex, data = non_smoker_transform)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.62610 -0.16310 -0.07121 -0.01616  2.37346
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    7.1667168   0.0471819  151.896 < 2e-16 ***
## age             0.0415675   0.0009071   45.826 < 2e-16 ***
## children        0.1285244   0.0104807   12.263 < 2e-16 ***
## regionnorthwest -0.0742732   0.0363504    -2.043  0.0413 *
## regionsoutheast -0.1645062   0.0361529   -4.550 5.98e-06 ***
## regionsouthwest -0.1815336   0.0363559   -4.993 6.94e-07 ***
## sexmale        -0.1015747   0.0255178    -3.981 7.35e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4159 on 1057 degrees of freedom
## Multiple R-squared:  0.6895, Adjusted R-squared:  0.6878
## F-statistic: 391.3 on 6 and 1057 DF,  p-value: < 2.2e-16
```

```
yhat_full_non_smoker <- mlr_full_non_smoker_transform$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_transform$residuals
non_smokers %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
```

```
geom_point() +  
theme_bw() +  
geom_hline(yintercept = 0, color="red")
```



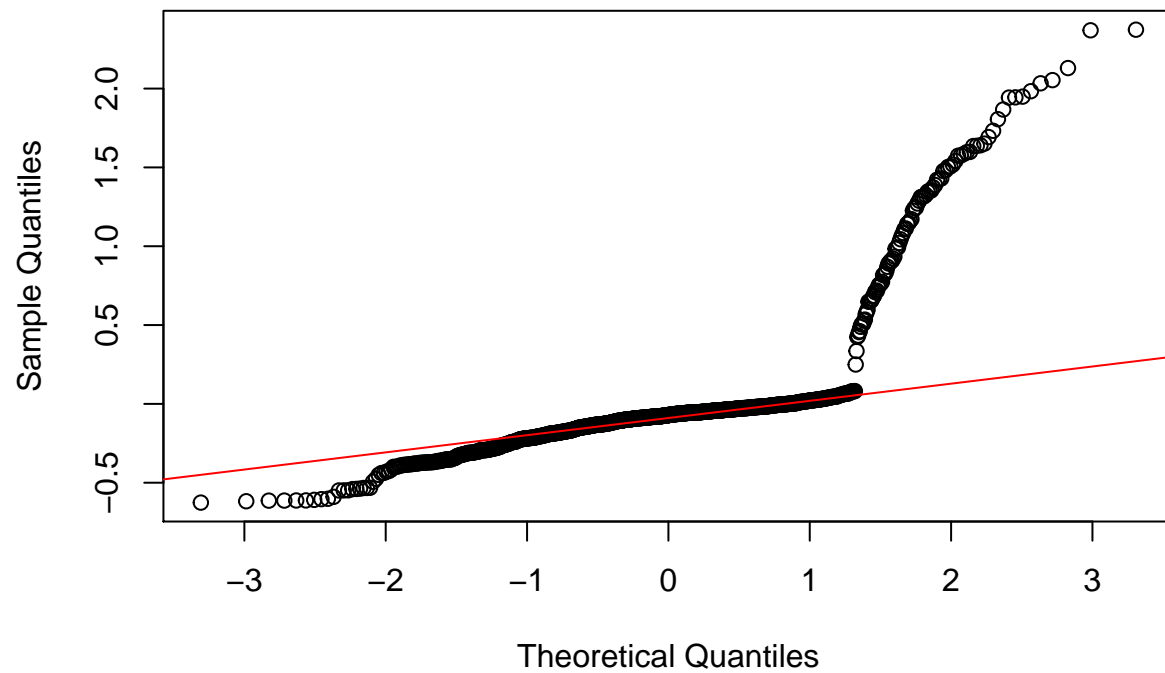
```
boxcox(mlr_full_non_smoker_transform)
```



QQPlot

```
{  
  qqnorm(mlr_full_non_smoker_transform$residuals)  
  qqline(mlr_full_non_smoker_transform$residuals, col="red")  
}
```

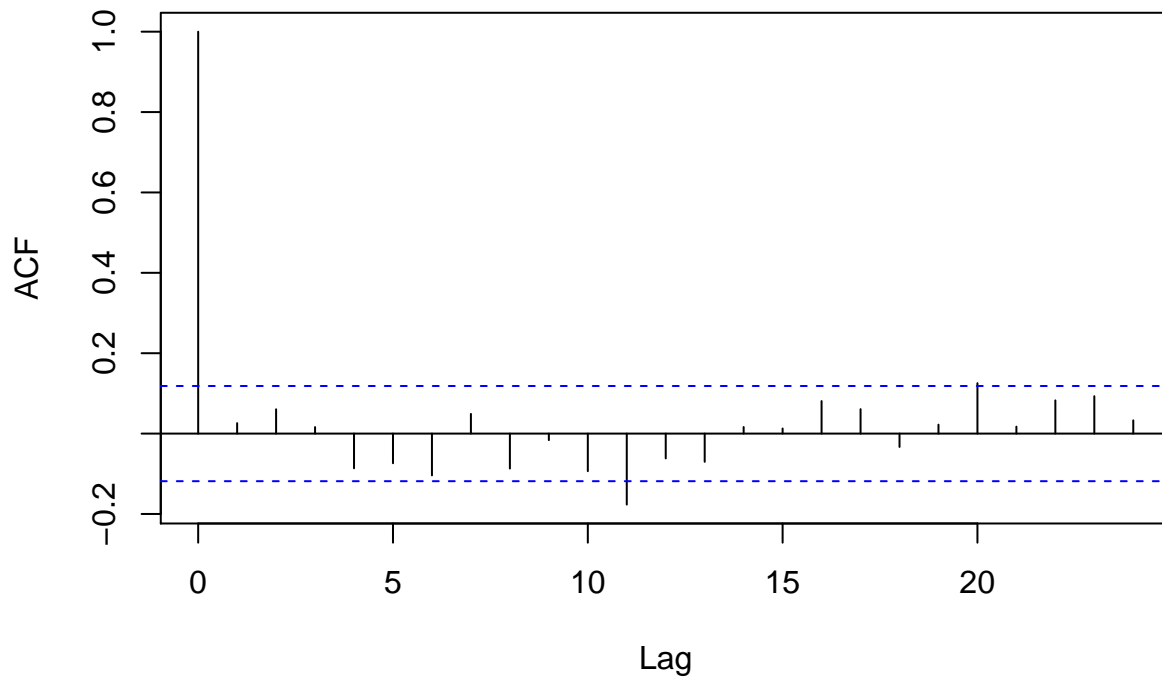
Normal Q-Q Plot



ACF

```
acf(mlr_full_smoker_transform$residuals, main="ACF")
```

ACF



```
head(non_smokers)
```

```
##   age    sex    bmi children smoker   region   charges significant.charge
## 2  18  male  33.770         1    no southeast  1725.552             FALSE
## 3  28  male  33.000         3    no southeast  4449.462             FALSE
## 4  33  male  22.705         0    no northwest 21984.471              TRUE
## 5  32  male  28.880         0    no northwest  3866.855             FALSE
## 6  31 female  25.740         0    no southeast  3756.622             FALSE
## 7  46 female  33.440         1    no southeast  8240.590             FALSE
```

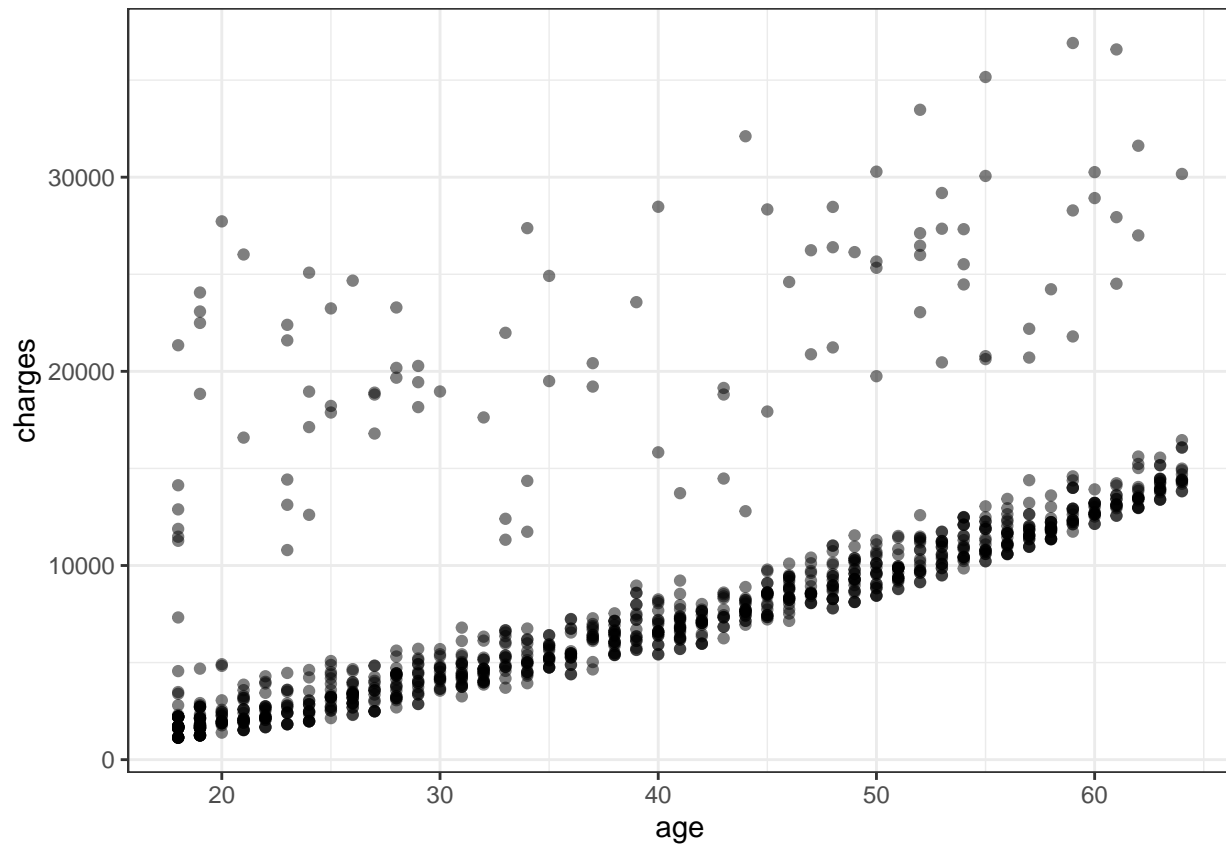
```
# charges ~ age + children + region + sex
```

```
non_smokers %>%
```

```
  ggplot(aes(x=age, y=charges)) +
```

```
  theme_bw() +
```

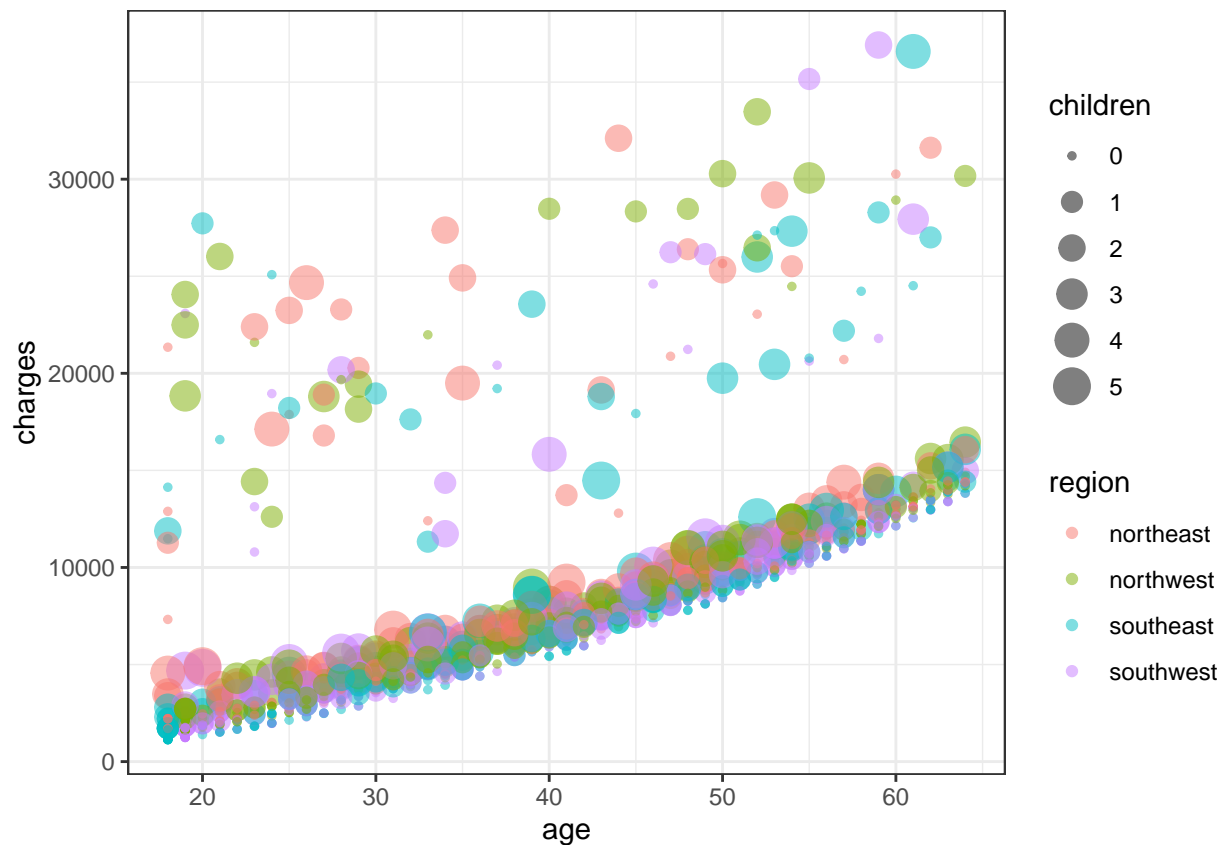
```
  geom_point(alpha=0.5)
```



Next Steps

We need to find for non smokers what is causing some data points to be more charges...?

```
non_smokers %>%  
  ggplot(aes(x=age, y=charges, size=children, color=region)) +  
  theme_bw() +  
  geom_point(alpha=0.5)
```



Try checking log of age?

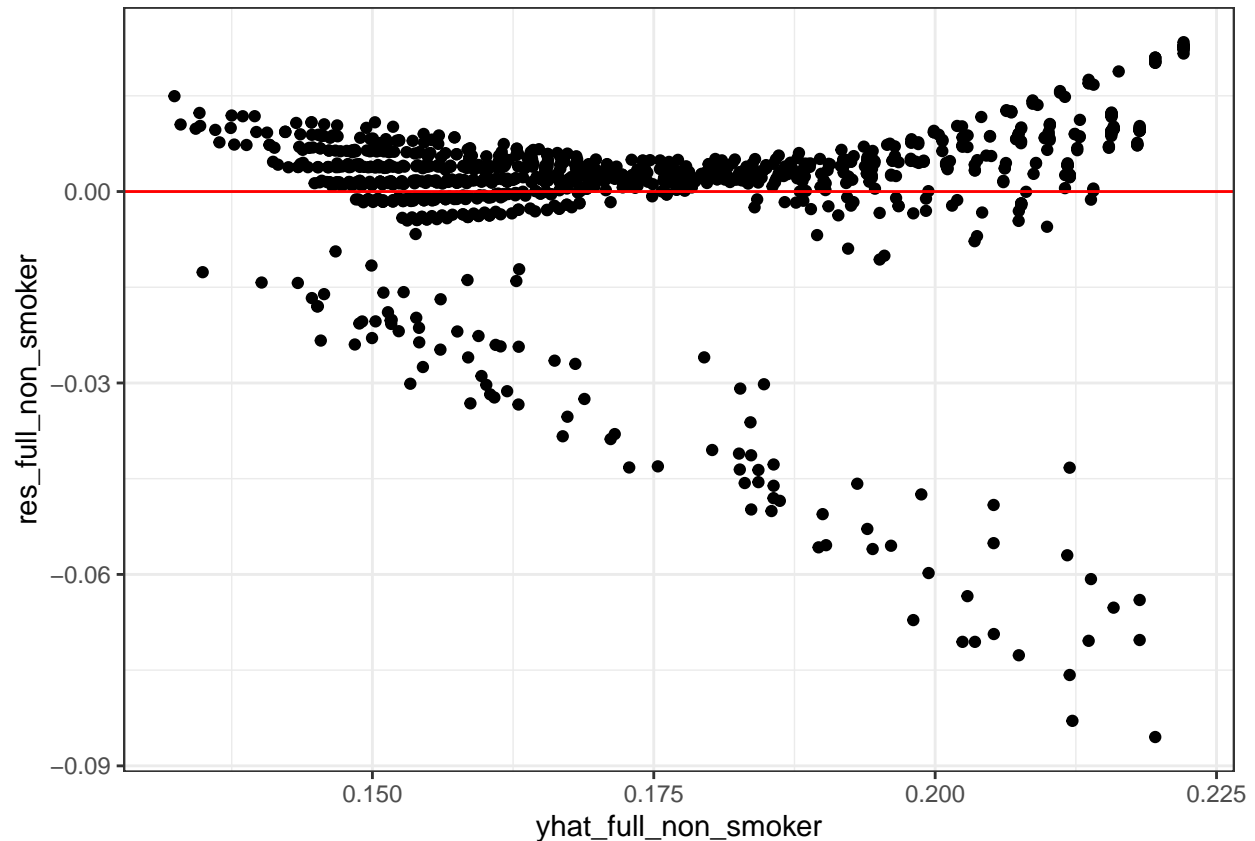
```
mlr_full_non_smoker_log_age = lm(formula = (charges)^(-0.2) ~ log(age) + children + region + sex, data = non_smokers)
summary(mlr_full_non_smoker_log_age)
```

```
##
## Call:
## lm(formula = (charges)^(-0.2) ~ log(age) + children + region +
##     sex, data = non_smokers)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.085480 -0.000036  0.002798  0.005271  0.023402
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   0.3701217  0.0040794  90.730 < 2e-16 ***
## log(age)      -0.0547231  0.0011007 -49.717 < 2e-16 ***
## children      -0.0041158  0.0003533 -11.650 < 2e-16 ***
## regionnorthwest 0.0027735  0.0012218   2.270  0.0234 *
## regionsoutheast 0.0062215  0.0012152   5.120 3.63e-07 ***
## regionsouthwest 0.0066586  0.0012221   5.449 6.32e-08 ***
## sexmale       0.0039021  0.0008578   4.549 6.01e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

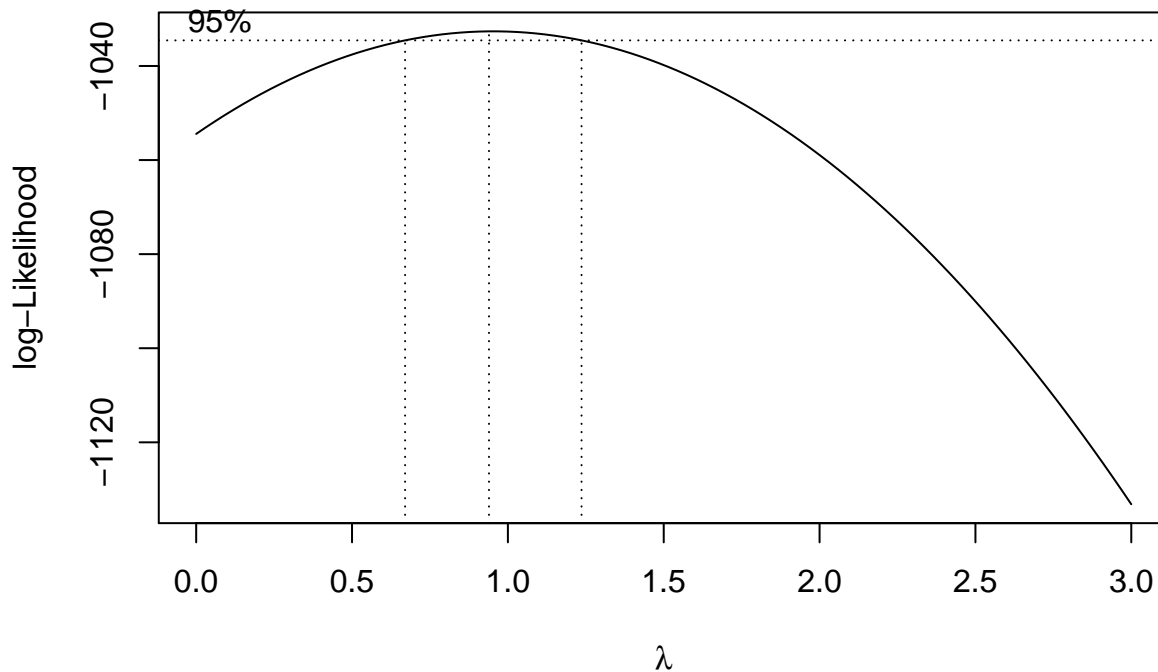


```
## Residual standard error: 0.01398 on 1057 degrees of freedom
## Multiple R-squared:  0.7255, Adjusted R-squared:  0.724
## F-statistic: 465.7 on 6 and 1057 DF,  p-value: < 2.2e-16

yhat_full_non_smoker <- mlr_full_non_smoker_log_age$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_log_age$residuals
non_smokers %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")
```



```
boxcox(mlr_full_non_smoker_log_age, c(0,3,0.1))
```



Interaction age and region?

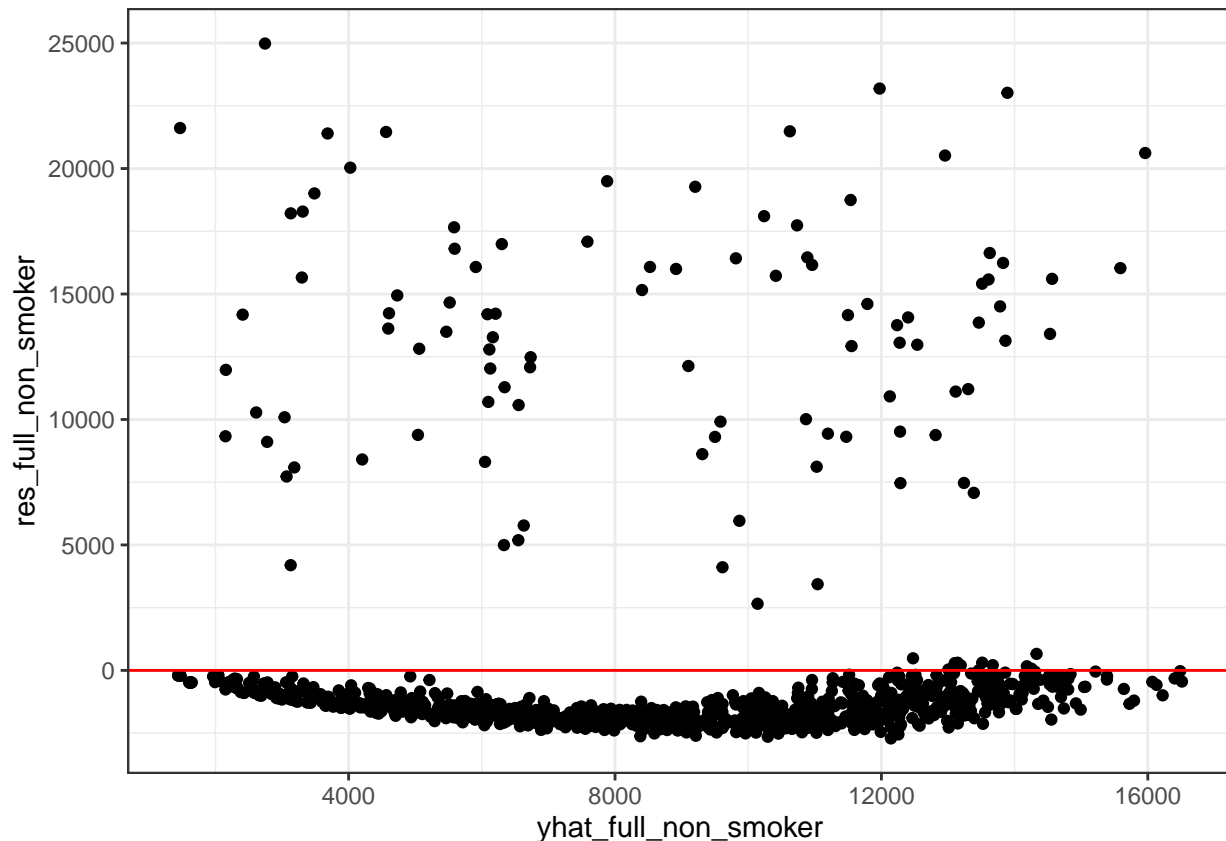
```
mlr_full_non_smoker_region_inter = lm(formula = charges ~ (age)*bmi + region + children + sex, data = non_smokers)
summary(mlr_full_non_smoker_region_inter)
```

```
##
## Call:
## lm(formula = charges ~ (age) * bmi + region + children + sex,
##     data = non_smokers)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2709.7 -1866.9 -1359.3  -677.6 24979.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -1201.727    2129.9278  -0.564  0.572731
## age             238.4680      51.6271   4.619 4.33e-06 ***
## bmi            -13.8407      68.4291  -0.202  0.839749
## regionnorthwest -544.8748     401.4481  -1.357  0.174985
## regionsoutheast -985.7698     412.2071  -2.391  0.016957 *
## regionsouthwest -1400.7248     402.5979  -3.479  0.000523 ***
## children        586.8693     115.7543   5.070 4.70e-07 ***
## sexmale        -531.6770     282.0645  -1.885  0.059711 .
## age:bmi          0.8441       1.6427   0.514  0.607489
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4592 on 1055 degrees of freedom
## Multiple R-squared:  0.4175, Adjusted R-squared:  0.4131
## F-statistic: 94.51 on 8 and 1055 DF, p-value: < 2.2e-16
```

```

yhat_full_non_smoker <- mlr_full_non_smoker_region_inter$fitted.values
res_full_non_smoker <- mlr_full_non_smoker_region_inter$residuals
non_smokers %>%
  ggplot(aes(yhat_full_non_smoker, res_full_non_smoker)) +
  geom_point() +
  theme_bw() +
  geom_hline(yintercept = 0, color="red")

```



Logistic

```

set.seed(6021) ##for reproducibility
sample<-sample.int(nrow(data), floor(.70*nrow(data)), replace = F)
train<- data[sample, ] ##training data frame
test<-data[-sample, ] ##test data frame
result<-glm(significant.charge ~ age + bmi + children + smoker + region, family="binomial", data=train)
summary(result)

```

```

##
## Call:
## glm(formula = significant.charge ~ age + bmi + children + smoker +
##      region, family = "binomial", data = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.5958  -0.3482  -0.0324   0.3666   3.3946
##

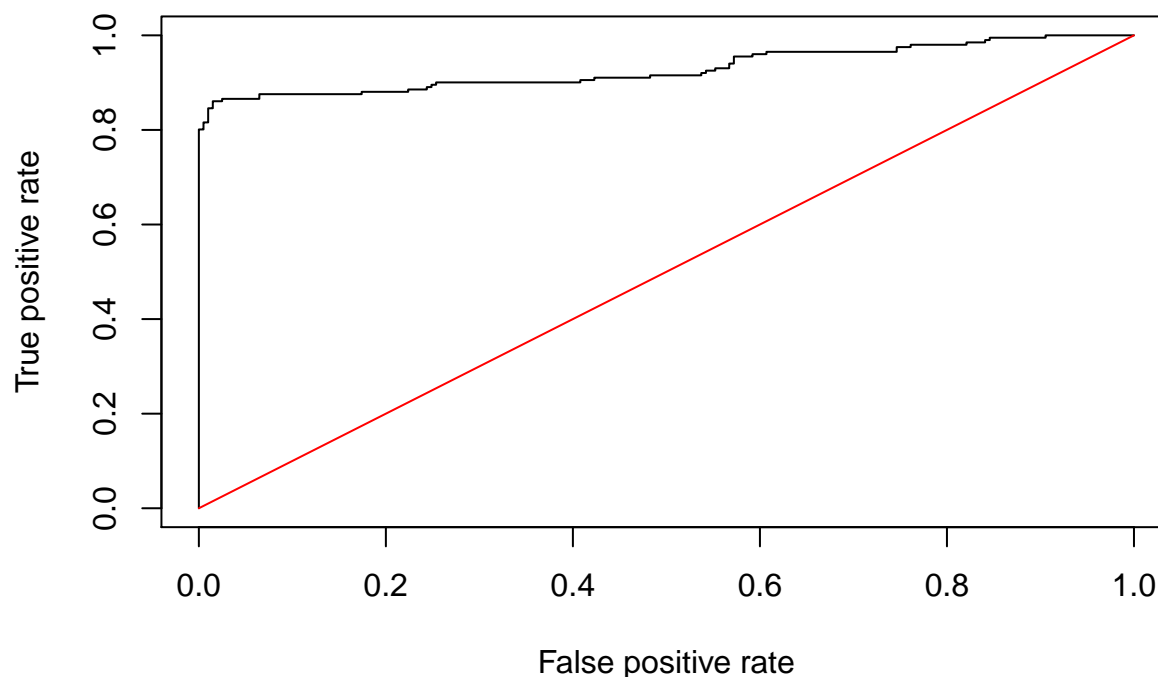
```

```
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -9.34931    0.89151 -10.487 < 2e-16 ***
## age            0.18315    0.01328  13.791 < 2e-16 ***
## bmi            0.03621    0.01978   1.831 0.06709 .
## children       0.18452    0.09189   2.008 0.04463 *
## smokeryes      22.65853   598.12679   0.038 0.96978
## regionnorthwest -0.45803    0.31756  -1.442 0.14921
## regionsoutheast -0.86352    0.33350  -2.589 0.00962 **
## regionsouthwest -0.50195    0.32102  -1.564 0.11791
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 1297.57  on 935  degrees of freedom
## Residual deviance:  507.03  on 928  degrees of freedom
## AIC: 523.03
##
## Number of Fisher Scoring iterations: 18
```

```
library(ROCR)
```

```
## Warning: package 'ROCR' was built under R version 4.0.2
##predicted survival rate for test data based on training data
preds<-predict(result,newdata=test, type="response")
##transform the input data into a format that is suited for the
##performance() function
rates<-prediction(preds, test$significant.charge)
##store the true positive and false positive rates
roc_result<-performance(rates,measure="tpr", x.measure="fpr")
##plot ROC curve and overlay the diagonal line for random guessing
plot(roc_result, main="ROC Curve")
lines(x = c(0,1), y = c(0,1), col="red")
```

ROC Curve



```
##compute the AUC
auc<-performance(rates, measure = "auc")
auc@y.values
```

```
## [[1]]
## [1] 0.9299522
```

Matrix

```
table(test$significant.charge, preds>0.5)
```

```
##
##      FALSE TRUE
## FALSE   180   21
## TRUE    25  176
```

Threshold value manipulation

```
table(test$significant.charge, preds>0.25)
```

```
##
##      FALSE TRUE
## FALSE   145   56
## TRUE    20  181
```

Doesn't play a huge role in decreasing the False Positive Rate. We want to make sure that when someone signs up for a plan that they don't get charged significantly given their condition.

```
test<-data.frame(test,preds)
ggplot(test,aes(x=preds))+
  geom_density()+
  labs(title="Density Plot of Predicted Probs") + theme_bw()
```

