

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Hands-on Machine Learning

Theoretical Overview

Marc Evrard

2022-2023

université
PARIS-SACLAY

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Section 1

Course information

People

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape
Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

Lectures and practical works:

Marc Evrard (marc.evrard@lisn.upsaclay.fr)

Practical works:

Yue Ma (yue.ma@lisn.upsaclay.fr)

Registration:

Alexandre Verrecchia
(alexandre.verrecchia@universite-paris-saclay.fr)

References

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

The **main references** for this class:

- Géron (2019) *Hands-on Machine Learning with Scikit-Learn, Keras, and Tensorflow: Concepts, Tools, and Techniques to Build Intelligent Systems*
- *Scikit-learn User Guide*:
https://scikit-learn.org/stable/user_guide.html
- VanderPlas (2017) *Python Data Science Handbook: Essential Tools for Working with Data*.

Great references for **machine learning algorithm** theory:

- Bishop (2006) *Pattern Recognition and Machine Learning*
- Russell and Norvig (2020) *Artificial Intelligence: A Modern Approach* (4th ed.)

Assessments (MCC)

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- Continuous assessment (CC): 100%
 - Weekly quizzes (40%)
 - Practical assignments: 2 challenges (60%)
 - Prepared on Jupyter Notebooks
 - By teams of 2 or 3

Quizzes with degrees of confidence[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- Need to give a **degree of confidence**:
Probability of the response you give is correct
- Self-assessing in a **realistic way** earns more points
- In general, the majority of students rate themselves well

Probability	Degree	Correct	Wrong
0 to 25%	0	+13	+4
25 to 50%	1	+16	+3
50 to 70%	2	+17	+2
70 to 85%	3	+18	0
85 to 95%	4	+19	-6
95 to 100%	5	+20	-20

[†]<http://smart.uliege.be>

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Section 2

The Machine Learning Landscape

What is Machine Learning?[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

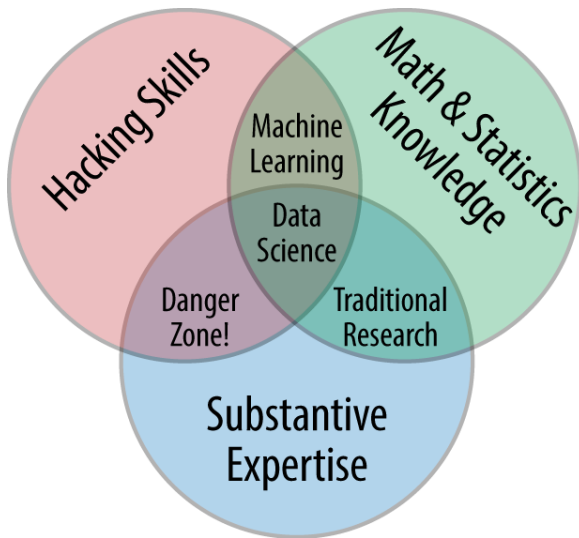
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]Drew Conway's Data Science Venn Diagram (from VanderPlas 2017)

What is Machine Learning?[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

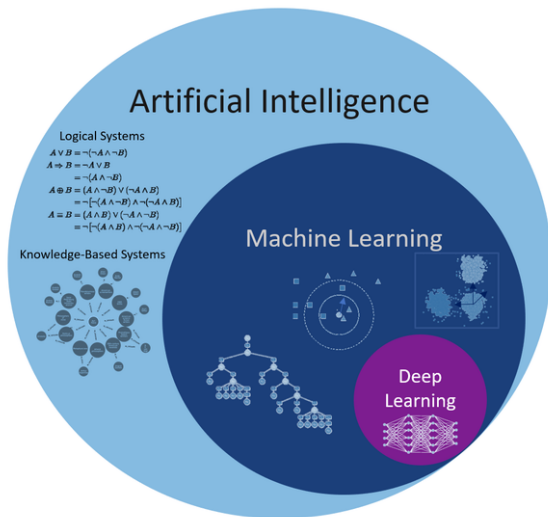
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†] Fig. from <https://www.quora.com/profile/Jens-Laufer>

What is Machine Learning?

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- *Machine Learning is the science (and art) of programming computers so they can learn from data.* (Géron 2019)
- More generally:
 - *It's the field of study that gives computers the ability to **learn without being explicitly programmed.*** (Samuel 1959)
- More formally:

A computer program is said to learn from experience E with respect to some task T and some performance measure P , if its performance on T (as measured by P) improves with experience E . (Mitchell 1997)

Spam filter example

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- ML program that can learn to flag spam given examples of:
 - Spam emails (e.g., flagged by users)
 - Regular (non-spam) emails
- **Training set:** The examples used by the system to learn
 - **Training instance (or sample):** Each training example
- In this case:
 - **Task T:** Flag spam for new emails
 - **Experience E:** Training data
 - **Performance measure P:**
E.g., the ratio of correctly classified emails (accuracy)

Use of ML

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

ML is great for:

- Problems **too complex** to be solved by explicitly programming them
 - Require **complex rules**
 - Requiring a lot of **hands tuning**
- **Fluctuating environments**, which need to constantly adapt to new data
- **Getting insights** on complex problems and large amounts of data (data mining)

ML, the magical pill?

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- The term *machine learning* is sometimes considered as a magical spell
 - *Apply ML to enough data, and any problems can be solved!*
- ML methods can be **extremely powerful**
 - But they are not equally capable of tackling all problems
- Several **issues** are highly likely to occur
 - Both on the data side and the ML methods side
 - **Bias** and **variance**, **overfitting** and **underfitting**, etc.

Types of ML Systems

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

According to the need for human supervision

Supervised:

The training data you feed to the algorithm includes the desired solutions (**labels**)

Unsupervised:

Modeling the variations of the features without reference to any labels

Semi-supervised:

Combines a small amount of labeled data with a large amount of unlabeled data during training

Reinforcement Learning:

Intelligent agents ought to take actions in an environment to maximize their cumulative reward

Supervised learning

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Supervised learning is further divided in:
 - **Classification** tasks
 - **Regression** tasks
- In a classification task the labels are **discrete categories**
 - Spam example: Predict the email tags (spam/ham)
- In a **regression** task the labels are **continuous quantities**:
Predicting a value according to a set of features
 - Price of a house (features: area, size, age, condition, etc.)
- Regression algorithms can also be used for **classification**:
 - **Logistic Regression** is commonly used for classification
 - It can output a probability of belonging to a given class (e.g., 80% chance of being spam)

Supervised learning algorithms (main ones)

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- **Classification**

- k-Nearest Neighbors
- Naive Bayes
- Logistic Regression
- Support Vector Machines (SVMs)
- Decision Trees and Random Forests

- **Regression**

- Linear Regression
- Regression Trees

- **Both** classification and regression

- Neural networks (NN)

Classification[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]Fig. from VanderPlas (2017)

Regression[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

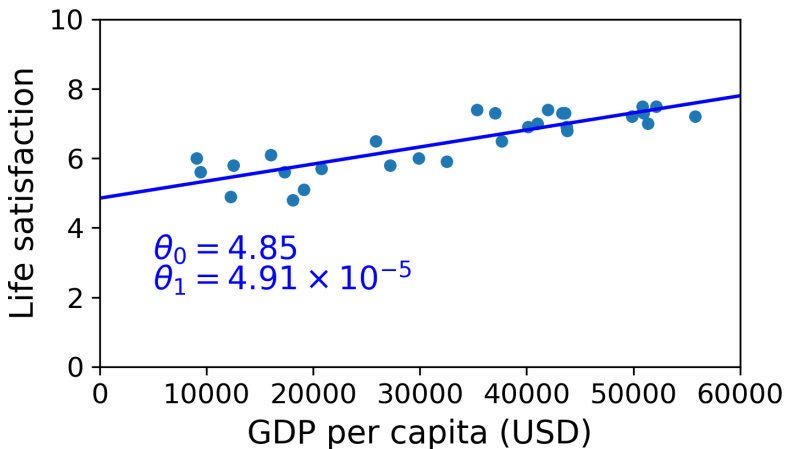
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]Fig. from Géron (2019)

Unsupervised learning algorithms (main ones)

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- **Clustering**

- K-Means
- Hierarchical Cluster Analysis (HCA)

- Visualization and **dimensionality reduction**

- Principal Component Analysis (PCA) — Kernel PCA
- t-distributed Stochastic Neighbor Embedding (t-SNE)

- **Self-supervised** (representation):

- DNN: Autoencoders
- Natural Language Processing (NLP):
 - Word embeddings
 - Transformers

Clustering I

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Example: Large data about blog's visitors

- Run a clustering algorithm to try to **detect groups** of similar visitors
- You don't need to tell the algorithm which group a visitor belongs to
 - It finds those connections on its own but grouping them according to their **feature similarities**
 - E.g., it might notice that:
 - 40% of visitors love comic books and generally read the blog in the evening
 - 20% are young sci-fi lovers who visit during the weekends
 - ...

Clustering II[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

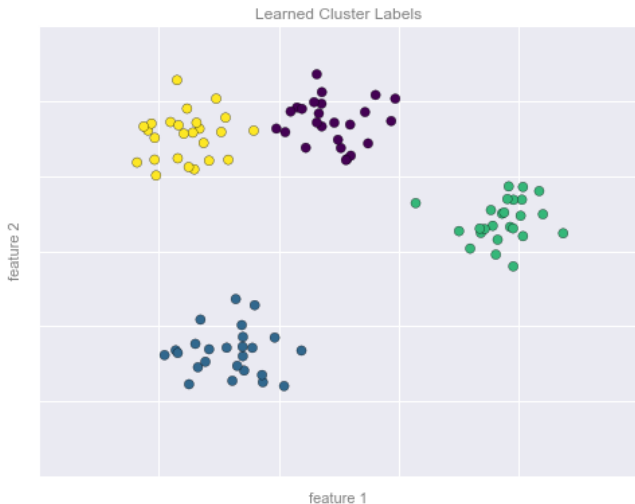
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]Fig. from VanderPlas (2017)

Visualization algorithms

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Input large and **complex sets of unlabeled data**
- Output a **2D or 3D representation** of your data to be plotted
- Trying to **preserve** the **global** and **local structure** of the data:
 - Keep separate clusters in the input space from **overlapping** in the visualization
 - Help to identify **unexpected patterns**

t-SNE[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

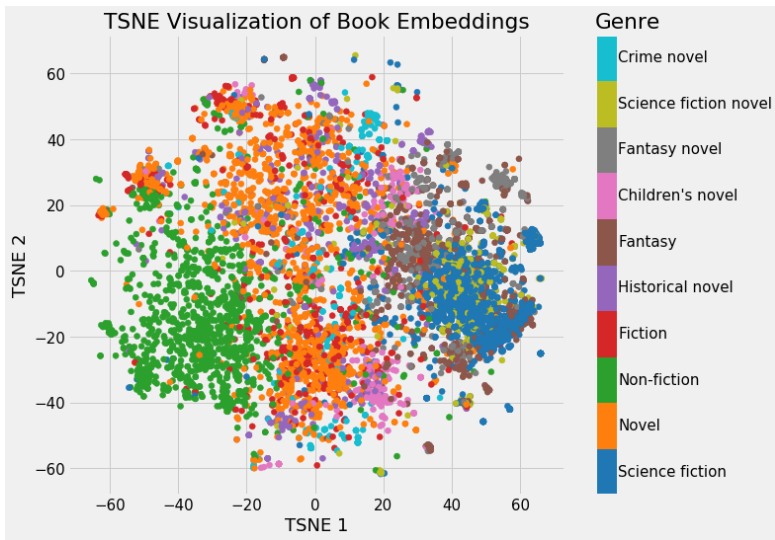
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]From <https://devopedia.org/word-embedding>

Dimension reduction

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Task related to **visualization**
- **Goal: Simplify the data** without losing too much information
- **Merge** several **correlated features** into one
 - E.g., a car's mileage may be very correlated with its age
 - Merge them into one feature: car's wear and tear
 - **Feature extraction**
- Often a good idea to reduce the dimension of your **training**
 - Before feeding it to another Machine Learning algorithm (e.g., supervised learning algorithm)
 - Train much **faster**
 - Data needs **less disk** and **memory** space
 - **Perform better** in some cases

Batch vs Online learning

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Whether or not the system can learn incrementally from a stream of incoming data

Batch learning

- **Not incremental:** Trained using all the available data
- Time and computing **resource-consuming:**
Need to be done offline
- System trained, then launched into production without learning anymore (**offline learning**)
- If new data needs to be included (e.g., new examples of spam), a new version must be **trained from scratch**

Batch vs Online learning

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

Online learning

- System trained **incrementally** by sequentially feeding data instances **individually** or by small groups: **Mini-batches**
- Each learning step is fast and cheap:
The system can learn new data **on the fly**
- Ideal for systems that receive data as a **continuous flow** (e.g., stock prices)
- Good option when **limited computing resources** are available (e.g., smartphone)
- Solution for **out-of-core learning** from huge datasets:
 - Loads part of the data
 - Runs a training step sequentially on the whole corpus

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

**Main
challenges**

Data issues

Algorithm issues

Evaluation

Bibliography

Section 3

Main challenges

Main challenges of ML

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- In short, tackling an ML problem supposes:
 - Selecting a **modeling algorithm**
 - That works best on **given data**
- The 2 main issues that thus can occur are:
 - **Algorithm** issues
 - **Data** issues
 - Insufficient **quantity** of training data
 - **Nonrepresentative** training data
 - Poor-**quality** data
 - Irrelevant **features**

Insufficient quantity of training data

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- To make a toddler learn what an apple is:
Point to an apple and say “apple” (possibly a few times)
 - Now the child is able to recognize apples in all sorts of colors and shapes
- ML algorithms need a lot more data to achieve such results
 - Simple problems typically require thousands of examples
 - Complex problems (e.g., image or speech recognition tasks) may require millions of examples

(Unless a semi-supervised approach is chosen or if an existing pretrained model is used through adaptation or fine-tuning)

The unreasonable effectiveness of data

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

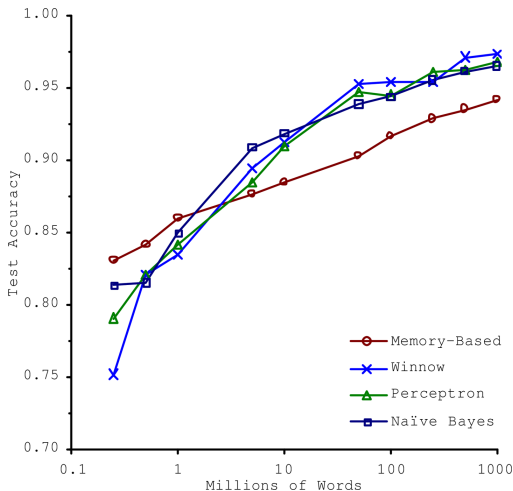
Algorithm issues

Evaluation

Bibliography

Microsoft researchers Banko and Brill (2001) showed (Fig.) that very **different algorithms** (including simple ones) performed almost **identically well** on complex problems provided **enough data** is given.

Further analyzed by Halevy, Norvig, and Pereira (2009) in *The unreasonable effectiveness of data*.



Nonrepresentative training data

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

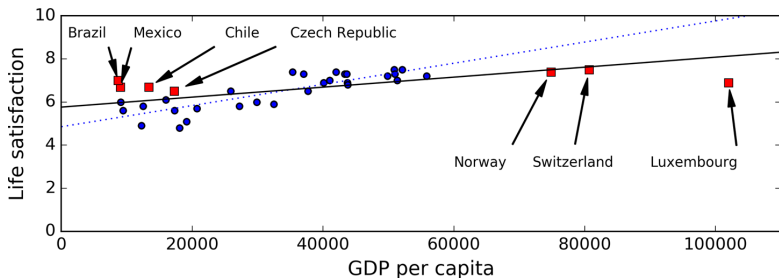
Data issues

Algorithm issues

Evaluation

Bibliography

- To **generalize well**: Training data must be **representative** of the **new cases**
- In the case of **linear regression**, some unseen data during training may not fit well with the predicted values
 - E.g., the GDP-Life Satisfaction (LS) relation:[†] It seems richest countries are not happier than moderately rich ones



[†]Fig. from Géron (2019)

Nonrepresentative training data: Sampling bias

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- If the sample is **too small** \Rightarrow sampling noise (i.e., high likelihood of nonrepresentative data)
- Even very large datasets can be nonrepresentative if the sampling method is biased
- Famous case of **sampling bias**:
 - US presidential election in 1936 (Landon vs Roosevelt)
 - Poll: **Mails** to about 10 million people (by Literary Digest)
 - They received 2.4 million answers:
 - Predicted Landon would win with 57%
 - Roosevelt won with 62% of the votes
 - Sampling issues:
 - **Exclusion bias**: subscribers, club membership lists, etc.
 - **Nonresponse bias** (25% answers)

Poor-quality data

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Plain errors: Outliers, and noise (e.g., from measurements)
- Important to **clean up** the training data
- **Significant part of the work** of researchers and data scientists
 - Remove **outliers**
 - If several instances are missing from some features:
 - Discard the attribute altogether
 - Ignore these instances
 - Fill in the missing values (e.g., with the median value)
 - A good idea is to **train multiple models** with the various possibilities and to compare their results

Irrelevant features

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- *Garbage in, garbage out*
- Too many irrelevant features will prevent the system from learning efficiently
- A critical part of ML projects: **Feature engineering**
- Choosing a good set of features
 - **Feature selection:** Selecting the most useful features
 - **Feature extraction:** Combining existing features to produce the most useful ones
(e.g., through dimensionality reduction like PCA)
 - Creating new features by gathering more data

Overfitting the training data

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

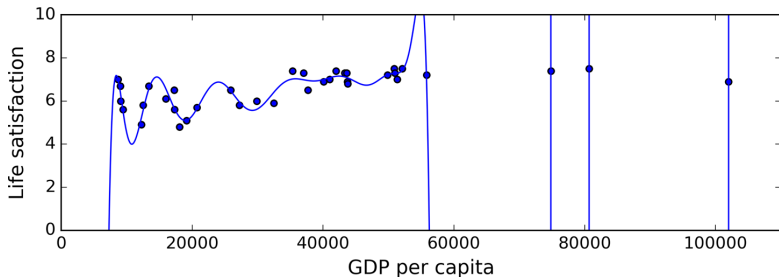
Data issues

Algorithm issues

Evaluation

Bibliography

- One of the most striking examples of overfitting is perhaps xenophobia
- Like xenophobia, **overfitting** is the process of **overgeneralizing assumptions** (to be euphemistic)
- In ML: The model **performs well** on the **training** data, but **not** in the **test** data (it does not generalize well)[†]



[†]Fig. from Géron (2019)

Overfitting the training data

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- **Overfitting** is when the **model is too complex** relative to:
 - The **amount** of training data
 - The level of **noise** in the data
- The possible **solutions** are:
 - For the **model**:
 - Simplify the model by selecting one with **fewer parameters** (e.g., a linear model vs high-degree polynomial model)
 - **Constraining** the model
 - For the **data**:
 - **Reducing** the number of **features** in the training data
 - Gather **more training data**
 - **Reduce the noise** in the training data

Overfitting: Regularization

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- **Regularization:** A way of **constraining** a model to make it less susceptible to overfitting
- E.g., The linear model: $LS = \theta_0 + \theta_1 \cdot GDP$
- It has 2 parameters: θ_0 and θ_1
 - 2 **degrees of freedom** to fit the model to the training data
 - Can adjust both the **height** (θ_0) and the **slope** (θ_1)
 - If we forced $\theta_1 = 0$: Only 1 degree of freedom
 - **Harder to fit** the data: Just a mean (very simple model indeed!)
 - If we force the model to keep it small:
To be *in between* 1 and 2 degrees of freedom.

Overfitting: Regularization

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

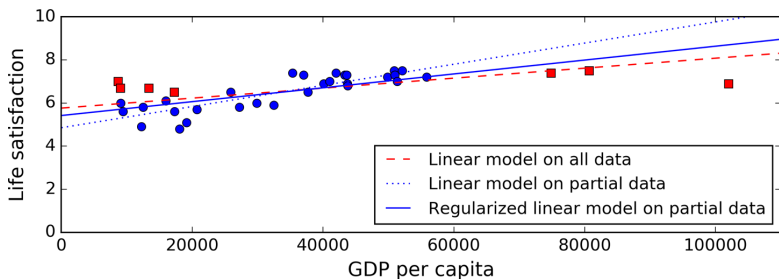
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



- **Regularization** forced the model to have a smaller slope[†]
 - Fits less well the training data
 - But allows generalizing better to new examples
- The amount of regularization to apply during learning can be controlled by a **hyperparameter**

[†]Fig. from Géron (2019)

Underfitting the training data

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- Underfitting occurs when your **model is too simple** to learn the underlying structure of the data
- E.g., the linear model of GDP-LS
- The possible **solutions** are:
 - Selecting a more powerful model (with more parameters)
 - **Feature engineering**
 - Reducing the constraints on the model (e.g., **reducing the regularization**)
- **Note:**
 - The previous slide illustrates the **overfitting** with the GDP-LS example \Rightarrow seems the **opposite!**
 - But a **reduced dataset** was given to the algorithm

Testing

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- How well a model will **generalize** to new cases?

Try on new cases

- Try in production: Bad idea
- Split the dataset into a **training** set and a **test** set
- Common values: 80% data for training and 20% for testing
- **Generalization error**: The error rate on new cases
 - If the **training error** is **low**
 - And the **testing error** is **high**
(High variance)
⇒ **Overfitting**

Validating

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

- If you want to test **multiple models** (e.g., a linear and polynomial model)
 - Train both and compare how they generalize on the test set
- You then want to apply some **regularization** to avoid overfitting
 - How do you choose the value of the regularization hyperparameter?
 - Train n different models using n different values for this hyperparameter
- Now the model and hyperparameters are the **best fit** for the test set
 - **Not likely to generalize** well on new data
 - Hold another set: The **validation set**

Cross-validation

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- If the dataset is too small for a training/validation/test split: Use **cross-validation**
- The training set is split into **complementary subsets**
 - Each model is trained against a **different combination** of these subsets
 - And validated against the remaining parts
- Once the **model type** and **hyperparameters** have been selected
 - A final model is trained using these hyperparameters on the **full training set**
 - And the generalized error is measured on the **test set**

Cross-validation[†]

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

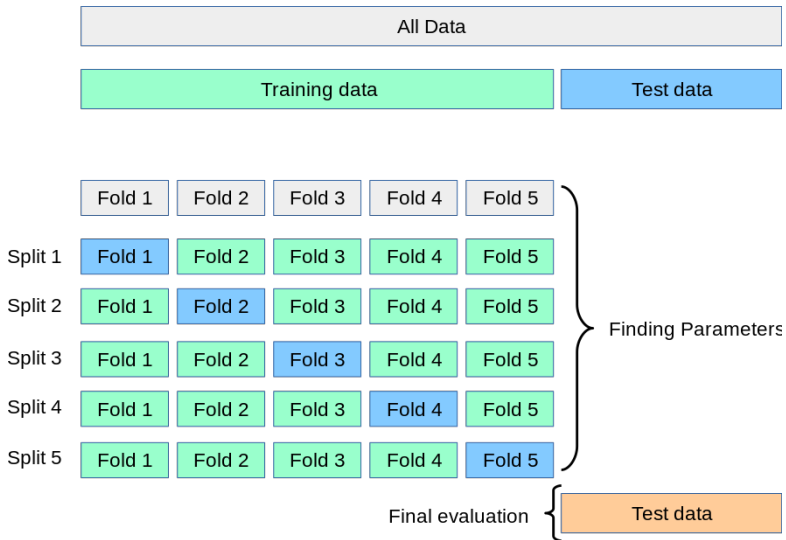
Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography



[†]From the Scikit-learn User Guide

No free lunch theorem

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

- A model is a **simplified version** of the observations
- The simplifications are meant to discard the superfluous details unlikely to generalize well
- **Assumptions** must be made to decide what data to discard/keep
- E.g., linear models suppose the assumption of **linearity** and that the rest is **noise**
- Wolpert and Macready (1997) demonstrated that:
*If you make absolutely **no assumption** about the data, then there is **no reason** to prefer one model over any other*
- **No model is a priori guaranteed to work better**

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Section 4

Bibliography

Bibliography I

HoML

Paris-Saclay
University

Course
information

References
Grading

The Machine
Learning
Landscape

Definition
Types of systems

Main
challenges

Data issues
Algorithm issues
Evaluation

Bibliography

Banko, Michele, and Eric Brill. 2001. "Scaling to Very Very Large Corpora for Natural Language Disambiguation." In *39th ACL*. Toulouse, France.

Bishop, Christopher M. 2006. *Pattern Recognition and Machine Learning*. Springer.

Géron, Aurélien. 2019. *Hands-on Machine Learning with Scikit-Learn, Keras, and TensorFlow: Concepts, Tools, and Techniques to Build Intelligent Systems*. 2nd ed. O'Reilly Media, Inc.

Halevy, Alon, Peter Norvig, and Fernando Pereira. 2009. "The Unreasonable Effectiveness of Data." *IEEE Intelligent Systems* 24 (2): 8–12.

Mitchell, Tom. 1997. "Machine Learning."

Russell, Stuart J, and Peter Norvig. 2020. *Artificial Intelligence: A Modern Approach*. 4th ed. Pearson Education.

Bibliography II

HoML

Paris-Saclay
University

Course
information

References

Grading

The Machine
Learning
Landscape

Definition

Types of systems

Main
challenges

Data issues

Algorithm issues

Evaluation

Bibliography

Samuel, Arthur L. 1959. "Some Studies in Machine Learning Using the Game of Checkers." *IBM Journal of Research and Development* 3 (3): 210–29.

VanderPlas, Jake. 2017. *Python Data Science Handbook: Essential Tools for Working with Data*. O'Reilly Media, Inc.

Wolpert, David H, and William G Macready. 1997. "No Free Lunch Theorems for Optimization." *IEEE Transactions on Evolutionary Computation* 1 (1): 67–82.