
Course Name: Web Information Retrieval

PageRank

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Content

- Background
- Basic Idea
- PageRank Algorithm
- HITS: Hyperlink-Induced Topic Search
- Further Reading

HITS: Hyperlink-Induced Topic Search,

referred from: [Pandu Nayak and Prabhakar Raghavan, Lecture 17: Link Analysis](#)

Background

- Example 1 submit a query in the search box

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Background

■ Example 2. a more complicate query, search in a moderate (million) scale document set

CNKI知识网络服务平台

术组($P<0.05$), 电针组心肌组织中TNF- α 及组胺含量低于模型组($P<0.05$); 肥大细胞脱颗粒率模型组明显高于假手术组, 电针组明显高于模型组($P<0.05$)。结论: 电针“内关”穴预处理促进心肌肥大细胞脱颗粒, 从而起到心肌保护作用。

【Abstract】 Objective To investigate the effects of “Neiguan” (PC 6)-electroacupuncture (EA) preconditioning on the myocardium and its mast cells in myocardial ischemia /reperfusion (MI/R) rats. Methods Eighteen male SD rats were randomly assigned to sham group,model (IR) group and EA group (n=6/group). MI/R model was established by occlusion of the descending anterior branch of the coronary artery. Blood samples were taken from the femoral vein before MI (T0),EA for 30 min (T1), 30 min after MI (T2), 30 min after MI/R (T3) and 120 min after MI/R (T4) for assaying serum tumor necrosis factor (TNF)- α and histamine contents by using ELISA. Serum lactate dehydrogenase (LDH) and creatinkinase isoenzyme (CK-MB) le-vels were measured at T0,T3 and T4 by using an automatic biochemistry analyzer. The infarct size was detected by Evan’s blue and tetrazolium chloride (TTC)

1	电针“内关”穴预处理对缺血再灌注大鼠心肌的保护作用	张江玲; 陈杰; 王祥瑞; 李玮伟; 王蓓蓓; 周洁	针刺研究 ?...	2010/03		
2	基于统计语言模型的信息检索演进探析	李进华; 周朴雄	图书情报知识	2010/03		15
3	缺血预处理影响兔肝缺血再灌注时细胞凋亡及调控基因Bcl-2/Bax表达的研究(英文)	苏松; 夏先明; 贺凯; 李波; 冯春红; 张孟愈	泸州医学院学报	2009/03		31
4	基于描述逻辑方法的VSM语义检索模型	张燕; 张睿	计算机工程与设计	2009/09		88
5	东疆天宇岩浆Cu-Ni矿床的铂族元素地球化学特征及其对岩浆演化、硫化物熔离的指示	唐冬梅; 秦克章; 孙赫; 漆亮; 肖庆华; 苏本勋	地质学报	2009/05	3	128

our expectation

Background

- Example 2. a more complicate query, search in a moderate (million) scale document set
 - Information retrieval models are required to find out relevant documents
 - Vector space model
 - Statistical language model
 - Probabilistic model
 -
 - Goal of IR models: increase search precision by
 - Understanding user's information needs
 - Providing techniques for computing relevance (or similarity) of query and documents

Background

■ Example specific



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Users
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[\[PDF\] A Graph-Based Information Retrieval Model](#)

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by O Sornil - [Related articles](#)

This decision usually depends upon similarity calculation intrinsic to the **information retrieval model** which attempts to establish an ordering of the ...

[conference.nida](#) [\[PDF\] Robust model estimation methods for information retrieval](#)

File Format: PDF/Adobe Acrobat

[Amazon.com](#) [\[PDF\] A Taxonomy of Information Retrieval Models and Tools](#)

\$31.58 - in stock File Format: PDF/Adobe Acrobat - Quick View

Amazon.com: S by G Canfora - 2004 - [Cited by 3](#) - [Related articles](#)

Human Language [www.lti.cs.cmu](#) Table 1. Vertical taxonomy of a set of **Information Retrieval Models**. space models of information retrieval with P-norm queries and multiple concept ...

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by D Valle Hidden Markov

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[citeseerx.ist.psu.edu/viewdoc/](#)

[Guest Post:](#)

4 Apr 2010 ... I

using a Bayesi

[themoisychann](#)

[\[PDF\] ICSM'00: Information Retrieval Models for Recovering Traceability ...](#)

File Format: PDF/Adobe Acrobat - Quick View

by G Antoniol - [Cited by 67](#) - [Related articles](#)

results of vector space and probabilistic **models** and formu- late hypotheses to explain the differences. 1. Introduction. Automated **Information Retrieval** ...

[www.sdml.info/library/Antoniol00b.pdf](#)

[\[PDF\] Term Feedback for Information Retrieval with Language Models](#)

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by B Tan - 2007 - [Cited by 15](#) - [Related articles](#)

H.3.3 [**Information Search and Retrieval**]: **Retrieval models**. General Terms. Algorithms. Keywords. Query expansion, interactive **retrieval**. 1. INTRODUCTION ...

[net.pku.edu.cn/~course/cs410/reading/sigir07-term.pdf](#)

[\[PDF\] An Object-Based Information Retrieval Model : Toward the ...](#)

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by JJ Han - [Cited by 4](#) - [Related articles](#)

In this paper, we propose an **information retrieval model**, where the ... Proposed in this paper is a new **information retrieval model** employing an ...

[ozzy.chonbuk.ac.kr/.../98_An%20Object-Based%20Information%20Retrieval%20Model.pdf](#)

[\[PDF\] The Dirichlet-Multinomial Model for Bayesian Information Retrieval](#)

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by IL Lu - [Cited by 1](#) - [Related articles](#)

to the development of a binary independence **model** for **information retrieval** (Robert- son and Sparck Jones 1976; van Rijsbergen 1979). ...

[interstat.statistik.uni-muenchen.de/YEAR/2007/articles/0710004.pdf](#) - [Similar](#)

Background

- Example 3. do the same search (with more specific keywords of Example 2) via Google
 - Now the critical problem becomes:
 - Which kind of documents should be presented on the 1st page?
 - It's not a question about relevant, rather than, it's a question about
 - Which document is more important?

Background

Document measures

Relevance, as conventionally defined, is binary (relevant or not relevant). It is usually estimated by the similarity between the terms in the query and each document: Boolean Model, Vector Space Model, Statistical Language Model, etc.

Importance measures documents by their likelihood of being useful to a variety of users. It is usually estimated by some measure of popularity.

Web search engines rank documents

by a combination of relevance and importance. The goal is to present the user with the most important of the relevant documents.

Then, how to compute the importance of a web document?

Basic Idea

- The question about “importance” also comes from the domain “Bibliometrics (文献计量学)”

Basic Idea

■ Bibliometrics (文献计量学):

- **Te** Convolutional neural network architectures for matching natural langu
- **sin**

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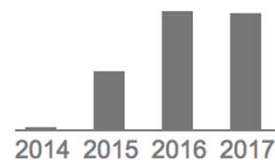
- two

■ Impa

- fre
- cite

- measure of “importance” of a journal

Authors	Baotian Hu, Zhengdong Lu, Hang Li, Qingcai Chen
Publication date	2014
Conference	Advances in Neural Information Processing Systems
Pages	2042-2050
Total citations	Cited by 238



Scholar articles [Convolutional neural network architectures for matching natural language sentences](#)
B Hu, Z Lu, H Li, Q Chen - Advances in neural information processing systems, 2014
Cited by 238 [Related articles](#) [All 18 versions](#)

been

Basic Idea

Basic philosophy implied in Impact Factor:

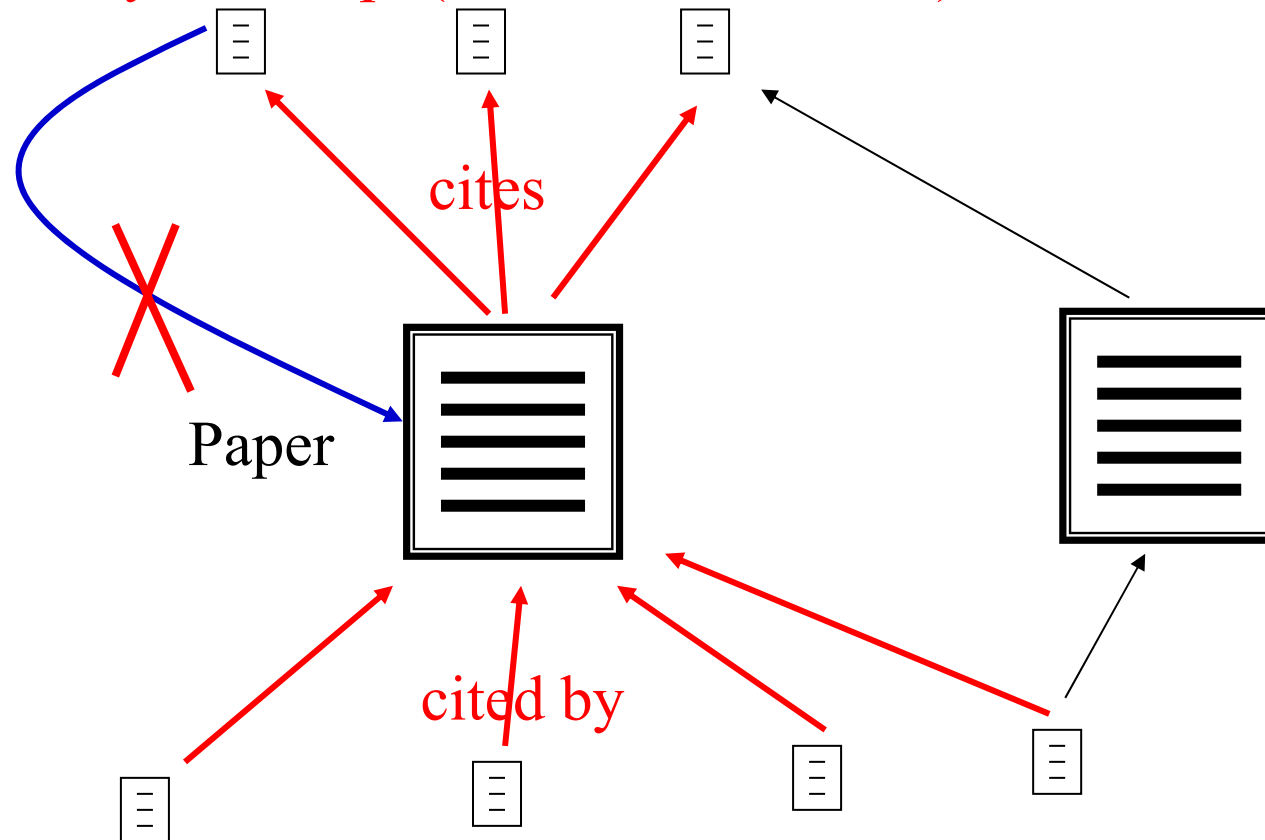
The importance of a journal or a paper is enhanced if more papers cite it.

Just those citations that come from important journals are counted.

Citation Graph - Visualization of Citations

Note that journal citations always refer to earlier work.

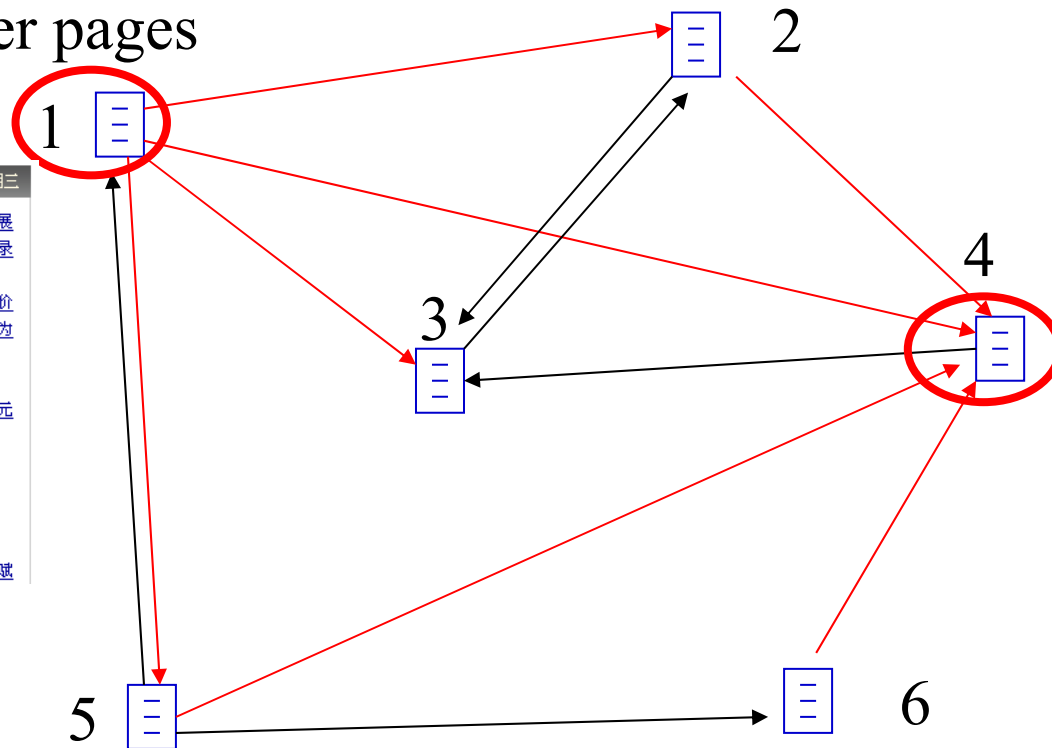
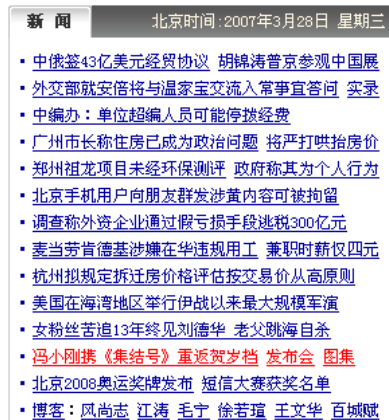
Directed Acyclic Graph(有向无环图, DAG)



Graphical Analysis of Hyperlinks on the Web

What's the difference between Hyperlink graph and Citation graph?

This page links to many other pages
(hub)



Many pages
link to this
page
(authority)

Matrix Representation

PageRank Algorithm

Used to estimate importance of documents.

Inspired by the Impact Factor.

Basic Concept:

1. The rank of a web page is higher if many pages link to it.
2. Links from highly ranked pages are given greater weight than links from less highly ranked pages.

Question:

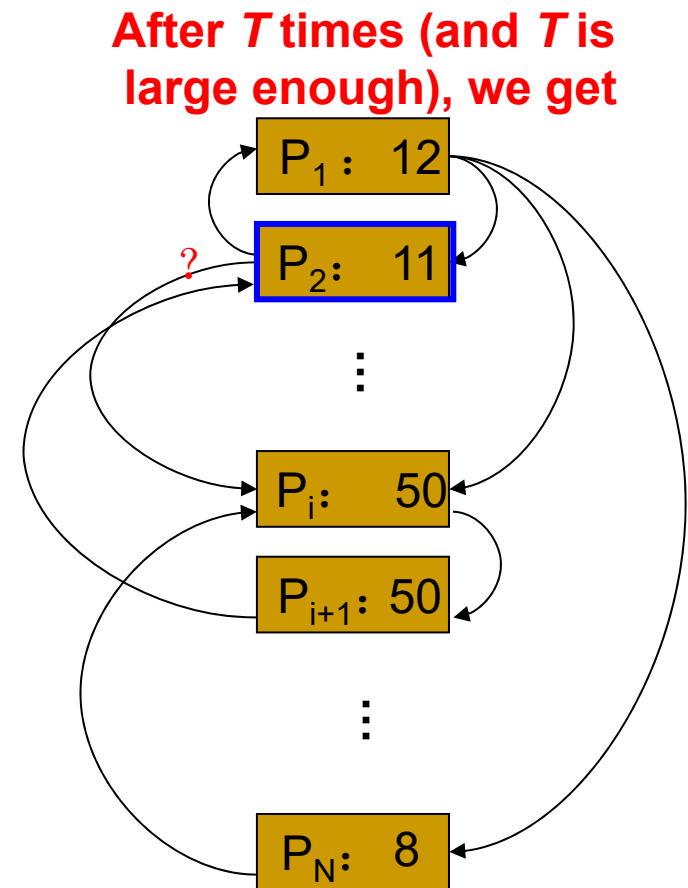
How do we know the rank of a web page that is linking to the web page under consideration?

Intuitive Model (no damping)

A user:

1. Starts at a random page on the web
2. Selects a random hyperlink from the current page and jumps to the corresponding page
3. Repeats Step 2 a very large number of times

Pages are ranked according to the relative frequency with which they are visited.



Then we can compute the rank (importance) of each webpage according to its visiting times

Intuitive Model (Probabilistic Model)

- It's a stochastic process
- To get a precise estimation of visiting times is not practicable
- Estimate the visiting probability of one webpage by the visiting probability of webpages **Link In** to it, for the example, we get:

$$\Pr(P_i) = \Pr(P_i | P_1) \Pr(P_1) + \Pr(P_i | P_2) \Pr(P_2) + \Pr(P_i | P_N) \Pr(P_N)$$

- We just want to get a relative importance (PageRank value), use w to replace the probability symbol "Pr", and get the matrix form:

$$w_i = \mathbf{Pr}_i \bullet \mathbf{w} \quad \text{or} \quad \mathbf{w} = \mathbf{B} \bullet \mathbf{w} \quad \text{for} \quad \mathbf{B} = [\mathbf{Pr}_1, \dots, \mathbf{Pr}_N]^T$$

$$\mathbf{Pr}_i = [\Pr(P_i | P_1), \Pr(P_i | P_2), \Pr(P_i | P_3), \dots, \Pr(P_i | P_N)]$$

$$\mathbf{w} = [w_1, w_2, w_3, \dots, w_N]^T \quad w_i \rightarrow \Pr(P_i)$$

$$\Pr(P_i | P_j) = \begin{cases} 0, & \text{If there is no hyperlink from } P_j \text{ to } P_i \\ 1/C(P_j), & \text{otherwise} \end{cases}$$

$C(P_j)$ is the **Link Out** of webpage P_j

Matrix Representation

The Citation Graph

		Citing page (from)						Number
		P ₁	P ₂	P ₃	P ₄	P ₅	P ₆	
Cited page (to)	P ₁					1		1
	P ₂	1	P ₂ cites P ₃					2
	P ₃	1	1		1			3
	P ₄	1	1			1	1	4
	P ₅	1						1
	P ₆					1		1
Number		4	2	1	1	3	1	

Basic Algorithm: Normalize by Number of Links from Page

		Citing page					
		P ₁	P ₂	P ₃	P ₄	P ₅	P ₆
Cited page	P ₁					0.33	
	P ₂	0.25		1			
	P ₃	0.25	0.5		1		
	P ₄	0.25	0.5			0.33	1
	P ₅	0.25					
	P ₆					0.33	
Number		4	2	1	1	3	1

= B
**Normalized
link matrix**

Basic Algorithm: Weighting of Pages

Initially all pages
have weight 1

$$\mathbf{w}_0 = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

Recalculate
weights

$$\mathbf{w}_1 = \mathbf{B}\mathbf{w}_0 =$$

$$\begin{bmatrix} 0.33 \\ 1.25 \\ 1.75 \\ 2.08 \\ 0.25 \\ 0.33 \end{bmatrix}$$

*Here the first iterating weight
for P1 is*

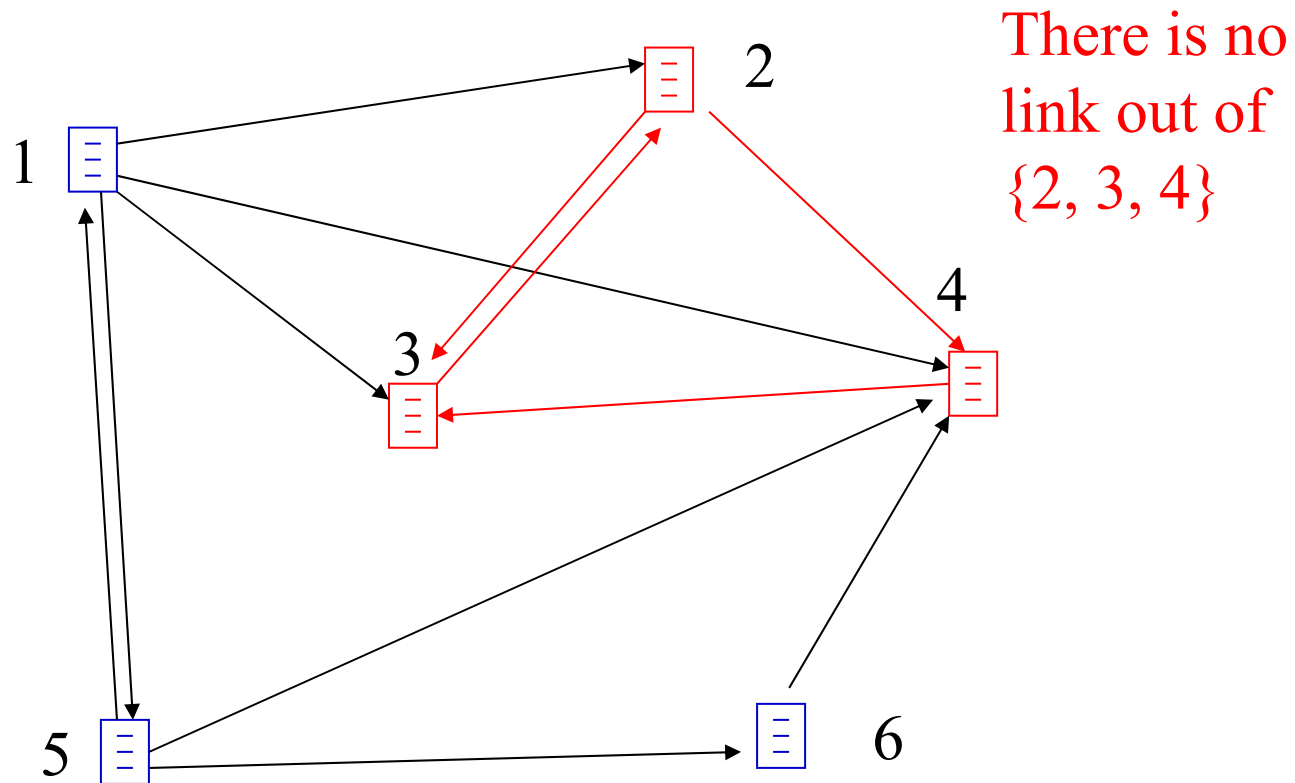
$$\begin{aligned} w_{11} &= \mathbf{B}_1 \bullet \mathbf{w}_0 \\ &= \mathbf{b}_{11} * \mathbf{w}_{01} + \dots + \mathbf{b}_{15} * \mathbf{w}_{05} + \dots \\ &= 0 * 1 + \dots + 0.33 * 1 + \dots \\ &= 0.33 \end{aligned}$$

Basic Algorithm: Iterate

Iterate: $\mathbf{w}_k = \mathbf{B}\mathbf{w}_{k-1}$

\mathbf{w}_0	\mathbf{w}_1	\mathbf{w}_2	\mathbf{w}_3	... converges to ...	\mathbf{w}
$\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 0.33 \\ 1.25 \\ 1.75 \\ 2.08 \\ 0.25 \\ 0.33 \end{bmatrix}$	$\begin{bmatrix} 0.08 \\ 1.83 \\ 2.79 \\ 1.12 \\ 0.08 \\ 0.08 \end{bmatrix}$	$\begin{bmatrix} 0.03 \\ 2.80 \\ 2.06 \\ 1.05 \\ 0.02 \\ 0.03 \end{bmatrix}$	$\begin{matrix} \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \end{matrix}$	$\begin{bmatrix} 0.00 \\ 2.39 \\ 2.39 \\ 1.19 \\ 0.00 \\ 0.00 \end{bmatrix}$

Graphical Analysis of Hyperlinks on the Web





Discussion:

How to deal with the issue of link loops?

Google PageRank with Damping

A user:

1. Starts at a random page on the web
- 2a. With probability d , selects any random page and jumps to it
- 2b. With probability $1-d$, selects a random hyperlink from the current page and jumps to the corresponding page
3. Repeats Step 2a and 2b a very large number of times

Pages are ranked according to the relative frequency with which they are visited.

Now, can we construct this new model?

The PageRank Iteration

The **basic method** iterates using the **normalized link matrix, \mathbf{B}** .

$$\mathbf{w}_k = \mathbf{B}\mathbf{w}_{k-1}$$

This \mathbf{w} is the high order eigenvector of \mathbf{B} (i.e., $\mathbf{w} = \mathbf{B}\mathbf{w}$)

PageRank iterates using a damping factor. The method iterates:

$$\mathbf{w}_k = d\mathbf{w}_0 + (1 - d)\mathbf{B}\mathbf{w}_{k-1}$$

\mathbf{w}_0 is a vector with every element equal to 1.

d is a constant found by experiment.

Iterate with Damping

Iterate: $\mathbf{w}_k = d\mathbf{w}_0 + (1-d)\mathbf{B}\mathbf{w}_{k-1}$ ($d = 0.3$)

\mathbf{w}_0	\mathbf{w}_1	\mathbf{w}_2	\mathbf{w}_3	... converges to ...	\mathbf{w}
$\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 0.53 \\ 1.18 \\ 1.53 \\ 1.76 \\ 0.48 \\ 0.53 \end{bmatrix}$	$\begin{bmatrix} 0.41 \\ 1.46 \\ 2.03 \\ 1.29 \\ 0.39 \\ 0.41 \end{bmatrix}$	$\begin{bmatrix} 0.39 \\ 1.80 \\ 1.78 \\ 1.26 \\ 0.37 \\ 0.39 \end{bmatrix}$	$\begin{matrix} \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \\ \rightarrow \end{matrix}$	$\begin{bmatrix} 0.38 \\ 1.68 \\ 1.87 \\ 1.31 \\ 0.37 \\ 0.38 \end{bmatrix}$

Google: PageRank

The Google PageRank algorithm is usually written with the following notation

If page A has pages T_i pointing to it.

- d : damping factor
- $C(T_i)$: number of links out of T_i
- n : number of pages pointing to A

Iterate until:

$$P(A) = (1 - d) + d \left(\sum_{i=1}^n \frac{P(T_i)}{C(T_i)} \right)$$

Information Retrieval Using PageRank

Simple Method

Consider all hits (i.e., all document vectors that share at least one term with the query vector) as equal.

Display the hits ranked by PageRank.

The disadvantage of this method is that it gives no attention to how closely a document matches a query

(i.e. No Relevance)

Combining Term Weighting with Reference Pattern Ranking

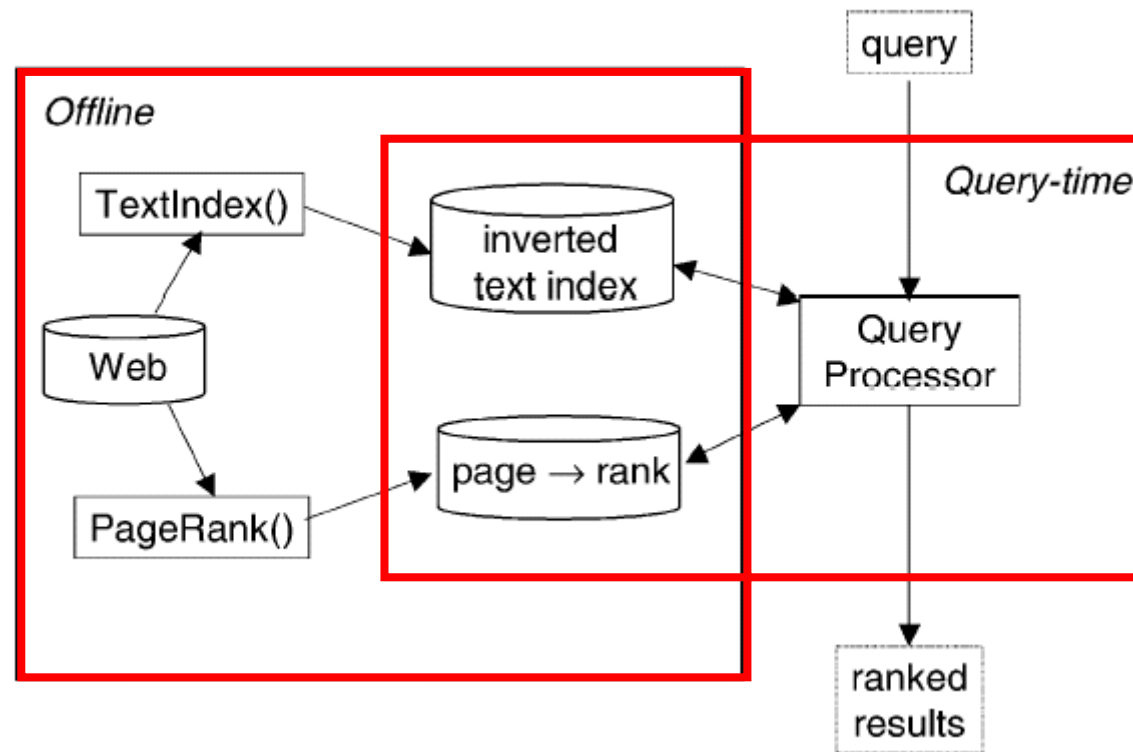
Combined Method

1. Find all documents that share a term with the query vector.
2. The similarity, using conventional term weighting, between the **query and document** j is s_j .
3. The rank of **document** j using PageRank or other reference pattern ranking is p_j .
4. Calculate a combined rank $c_j = \lambda s_j + (1 - \lambda)p_j$, where λ is a constant.
5. Display the hits ranked by c_j .

This method is used in several commercial systems but the details have not been published.

A standard search engine scheme by using PR

Haveliwala: Topic-sensitive Pagerank: A Context-sensitive Ranking Algorithm for Web Search





Topic sensitive PageRank

Topic sensitive PageRank

- Basic Idea:

- Once users random select one page to jump to, they may jump just among the webpages that belong to the same subject (or topic).

Topic Sensitive PageRank

Haveliwala: Topic-sensitive Pagerank: A Context-sensitive Ranking Algorithm for Web Search, 2003

- Assigns *multiple* a-priori “importance” estimates to pages
- One PageRank score per *basis topic*
 - Query specific rank score
 - Make use of context
 - Inexpensive at runtime
- Basis topics come from Yahoo, ODP (Open Directory Project <http://www.dmoz.org/>) etc.

Open Directory Project



Matrix form of PageRank

The main difference from our previous damping equation

Basic PageRank (in matrix form) $\mathbf{w}_k = d\mathbf{w}_0 + (1 - d)\mathbf{B}\mathbf{w}_{k-1}$

$$\vec{Rank} = (1 - \alpha)(M + D) \times \vec{Rank} + \alpha \vec{p}$$

- Here, if there is a link from page j to page i , then the matrix entry m_{ij} have the value $1/C(P_j)$, otherwise be 0.
- p be the n -dimensional column vector representing a uniform probability distribution over all nodes:

$$\vec{p} = \begin{bmatrix} 1 \\ n \end{bmatrix}_{n \times 1}$$

- \vec{d} be the n -dimensional column vector identifying the nodes with link-out 0:

$$d_i = \begin{cases} 1 & \text{if } \deg(i) = 0, \\ 0 & \text{otherwise.} \end{cases}$$

- and

$$D = \vec{p} \times \vec{d}^T$$

Why we need the matrix D ?

ODP-Biasing of PageRank

- Let T_j be the set of URLs in the ODP category c_j .
- computing the PageRank vector for topic c_j , in place of the uniform damping vector $\vec{p} = \left[\frac{1}{n}\right]_{n \times 1}$
- i.e. let $\vec{p} = \vec{v}_j$ and

$$v_{ji} = \begin{cases} \frac{1}{|T_j|} & i \in T_j, \\ 0 & i \notin T_j. \end{cases}$$

- The PageRank vector for topic c_j is given by $\vec{PR}(\alpha, \vec{v}_j)$ that can be computed by the basic PR algorithm

Query-Time Importance Score

Categorizing the query q

- Let q'_i be the i^{th} term in the query (or query context) q' . Then given the query q' , compute for each c_j the following:

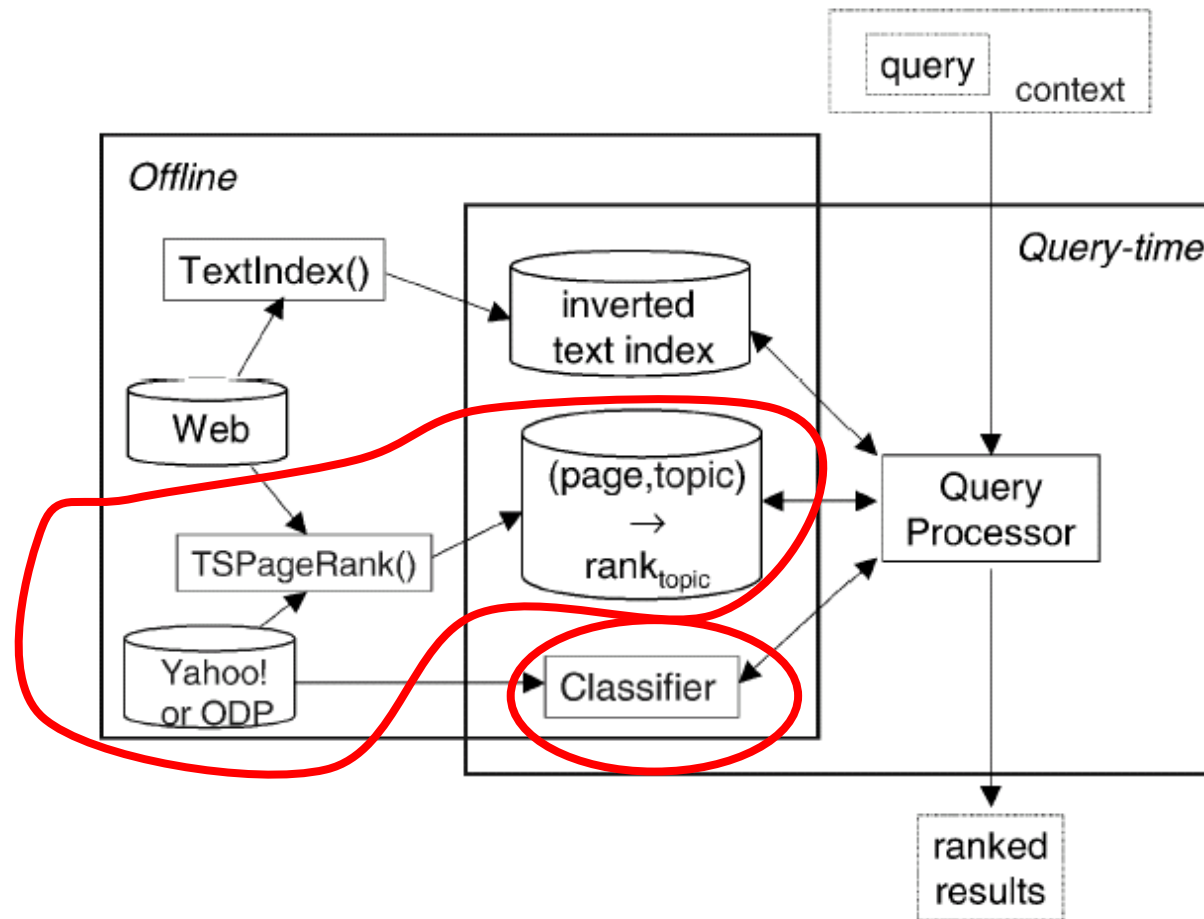
$$P(c_j|q') = \frac{p(c_j) \cdot P(q'|c_j)}{P(q')} \propto P(c_j) \cdot \prod_i P(q'_i|c_j)$$

Keep the
same for
all c_j

- Let r_{jd} be the rank of document d given by the rank vector $\vec{PR}(\alpha, \vec{v}_j)$, then for the Web document d , the query-sensitive importance score s_{qd} is computed as follows

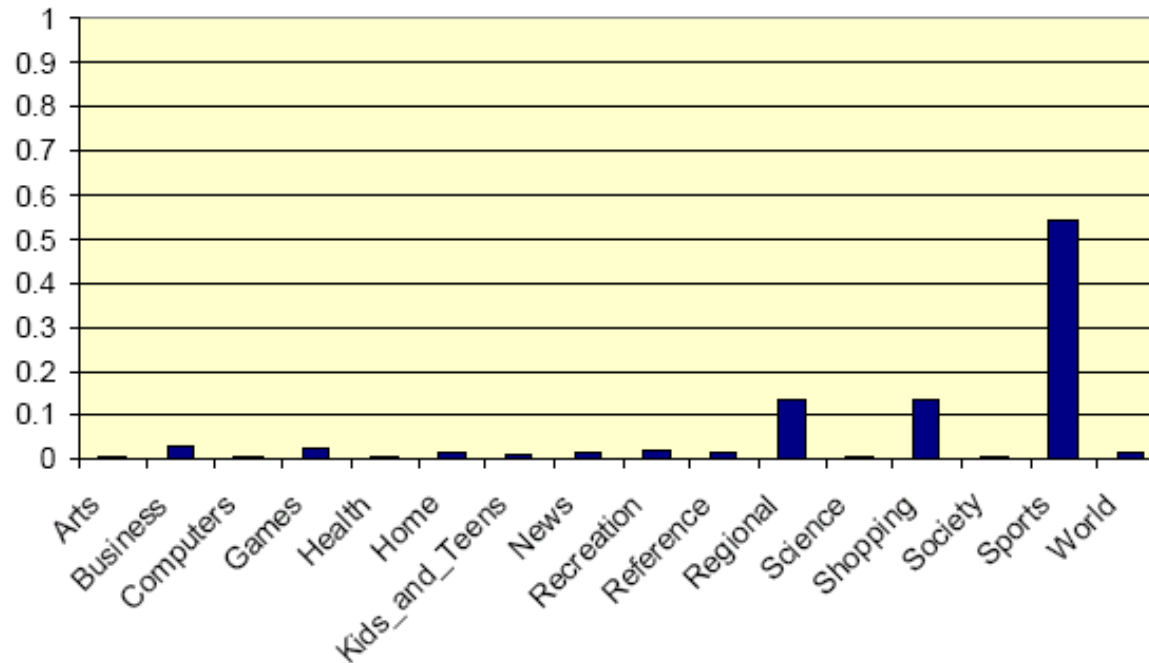
$$s_{qd} = \sum_j P(c_j|q') \cdot r_{jd}$$

SE System scheme with TS PageRank



Example Topic Distribution

- For the query 'golf', with no additional context the distribution of topic weights we would use is:



Experiment Results

TSPagerank vs. PageRank

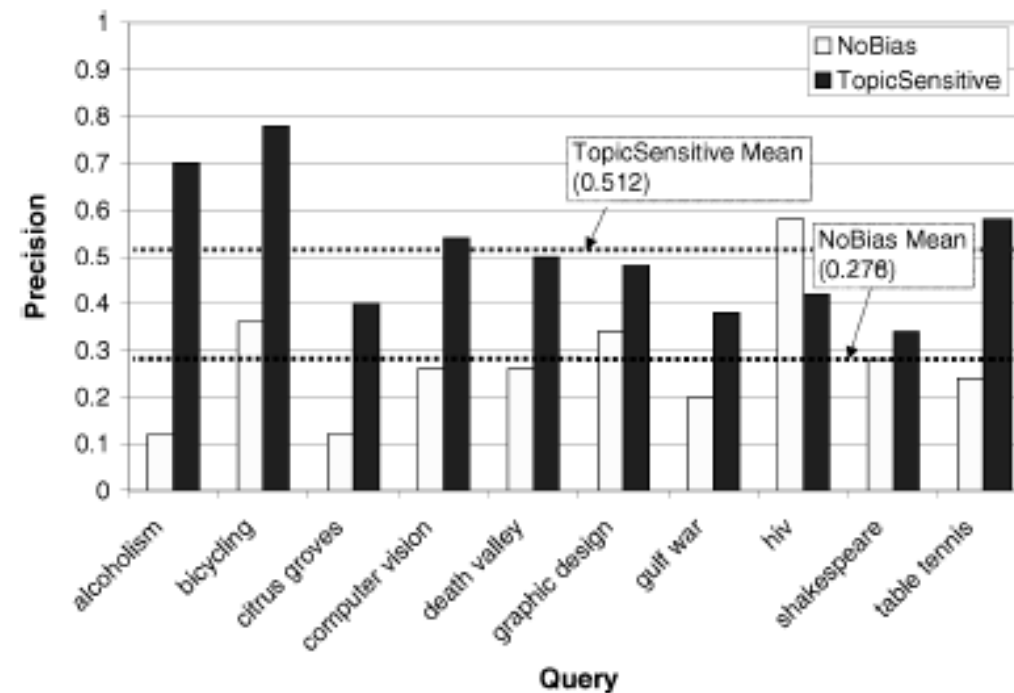


Fig. 3. Precision @ 10 results for our test queries. The average precision over the 10 queries is also shown.

From: Haveliwala, Topic-sensitive Pagerank: A Context-sensitive Ranking Algorithm for Web Search, 2003

Adaptive Search –Searching Context

- Rather than use query q itself, use the context of q to compute the topic distribution and PageRank values.
- The query context can be:
 - *The query history for the same user*
 - *The user provided text that contains the query terms*

Paper Discussion(Homework)

- Then, why is this paper named “topic-sensitive”?
- What’s the problem this paper was trying to address?
- What’s the role of matrix D ?
- Why we need the ODP or other similar project for the computing of multiple page ranks for a given page?

Content

- Background
- Basic Idea
- PageRank Algorithm
- **HITS: Hyperlink-Induced Topic Search**
- Further Reading

HITS: Hyperlink-Induced Topic Search,

referred from: [Pandu Nayak and Prabhakar Raghavan, Lecture 17: Link Analysis](#)

Hyperlink-Induced Topic Search (HITS)

- In response to a query, instead of an ordered list of pages each meeting the query, find two sets of inter-related pages:
 - *Hub pages* are good lists of links on a subject.
 - e.g., “Bob’s list of cancer-related links.”
 - *Authority pages* occur recurrently on good hubs for the subject.
- Best suited for “broad topic” queries rather than for page-finding queries.
- Gets at a broader slice of common *opinion*.

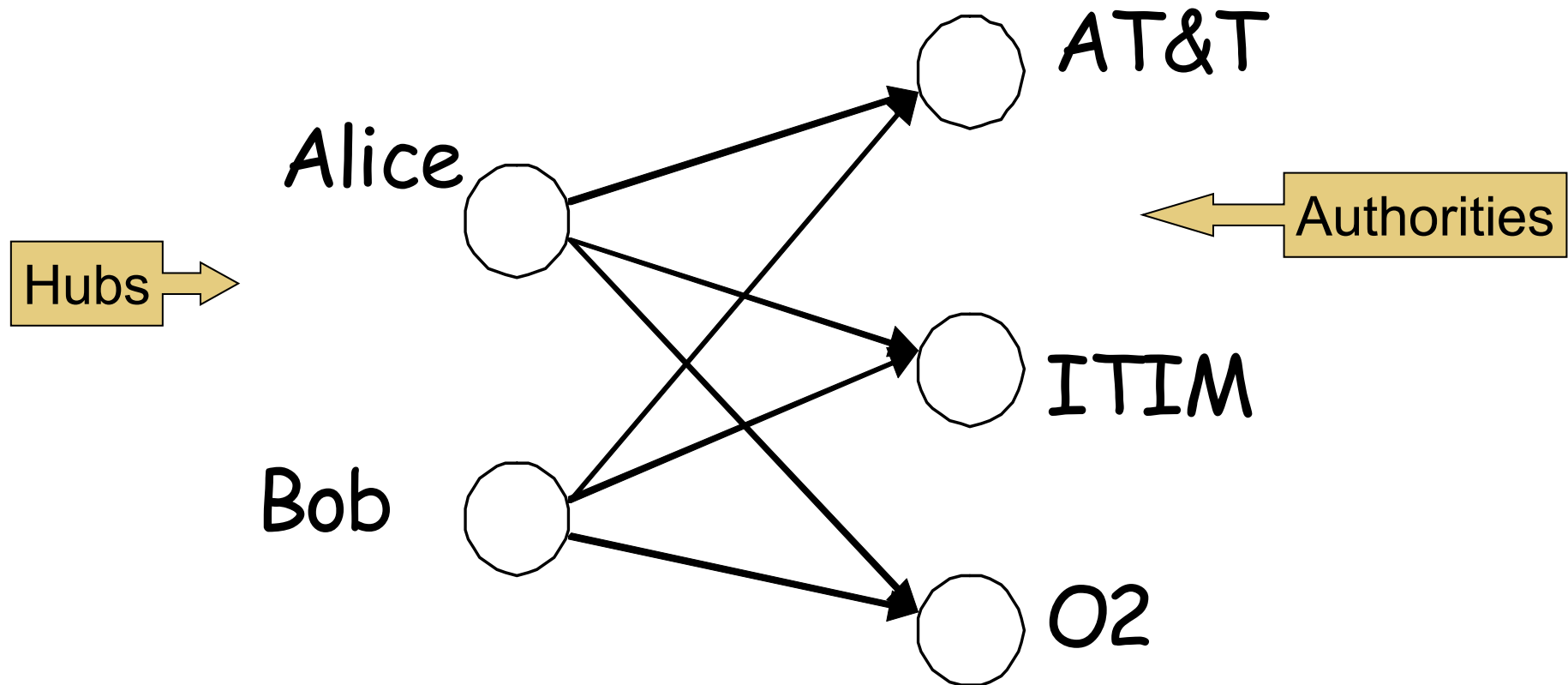
Hubs and Authorities

Basic Assumption

- A good hub page for a topic *points* to many authoritative pages for that topic.
- A good authority page for a topic is pointed to by many good hubs for that topic.

Circular definition - will turn this into an iterative computation

The hope



Mobile telecom companies

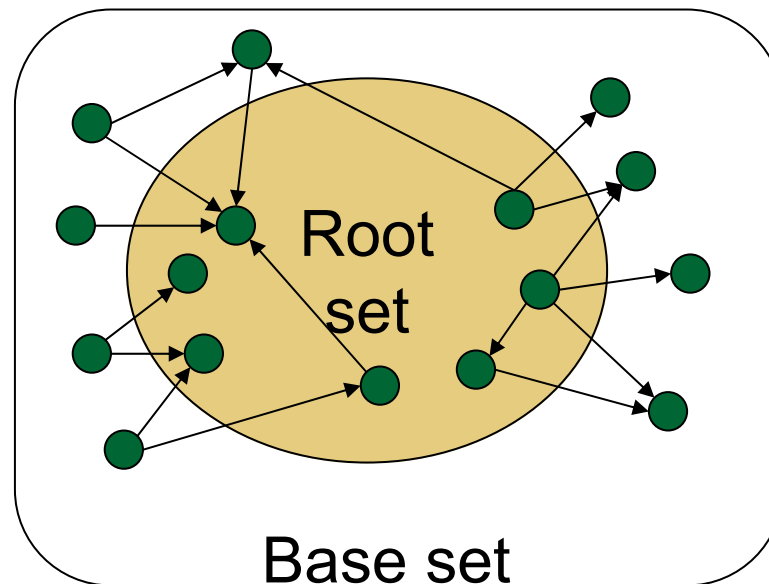
High-level scheme

- Extract from the web a base set of pages that *could* be good hubs or authorities.
- From these, identify a small set of top hub and authority pages
 - iterative algorithm

Base set


- Given text query (say **browser**), use a text index to get all pages containing **browser**.
 - Call this the root set of pages.
- Add in any page that either
 - points to a page in the root set, or
 - is pointed to by a page in the root set.
- Call this the base set.

Construct the Base Set



Get in-links (and out-links) from a *connectivity server*

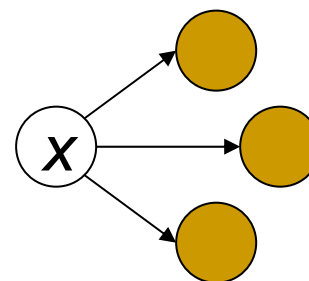
Distilling hubs and authorities

- Compute, for each page x in the base set, a hub score $h(x)$ and an authority score $a(x)$.
- Initialize: for all x , $h(x) \leftarrow 1$; $a(x) \leftarrow 1$
- Iteratively update all $h(x)$, $a(x)$  Key
- After iterations
 - output pages with highest $h()$ scores as top hubs
 - highest $a()$ scores as top authorities.

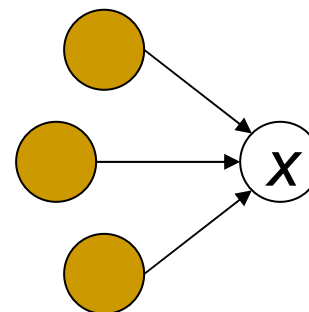
Iterative update

- Repeat the following updates, for all x :

$$h(x) \leftarrow \sum_{x \mapsto y} a(y)$$



$$a(x) \leftarrow \sum_{y \mapsto x} h(y)$$



Scaling

- To prevent the $h()$ and $a()$ values from getting too big, can scale down after each iteration
- Scaling factor doesn't really matter:
 - we only care about the *relative* values of the scores.

How many iterations?

- Claim: relative values of scores will converge after a few iterations:
 - in fact, suitably scaled, $h()$ and $a()$ scores settle into a steady state!
- In practice, ~5 iterations get you close to stability.

Things to note

- Pulled together good pages regardless of language of page content.
- Use *only* link analysis after base set assembled
 - iterative scoring is query-independent.
- Iterative computation after text index retrieval - significant overhead.

Content

- Background
- Basic Idea
- PageRank Algorithm
- HITS: Hyperlink-Induced Topic Search
- Further Reading

HITS: Hyperlink-Induced Topic Search,

referred from: [Pandu Nayak and Prabhakar Raghavan, Lecture 17: Link Analysis](#)

Further Reading

- **First publication that detail introduces Google's techniques by it's founders:**
- Brin, S. and Page, L., The Anatomy of a Large-Scale Hypertextual Web Search Engine. WWW 1998, April 14-18, 1998, Brisbane, Australia
- Lawrence Page, Sergey Brin, Rajeev Motwani, Terry Winograd, 'The PageRank Citation Ranking: Bringing Order to the Web', 1998
- Taher H. Haveliwala, 'Efficient Computation of PageRank', Stanford Technical Report, 1999
- **One of the important variations for PageRank:**
- Haveliwala T.H. Topic-sensitive Pagerank: A Context-sensitive Ranking Algorithm for Web Search, IEEE Trans. on Knowledge and Data Engineering, vol.15(4), 2003: 784-796
- **HITS:**
- Kleinberg, Jon (1999). "Authoritative sources in a hyperlinked environment". Journal of the ACM 46 (5): 604–632.