

Course: Data Structures

Student Name

Roll Number

Submission Date:

Exercise-1

Array Manipulation (Crush Problem) -

Problem Statement

Starting with a 1-indexed array of zeros and a list of operations, for each operation add a value to each array element between two given indices, inclusive. Once all operations have been performed, return the maximum value in the array.

Input and Output

Input:

- n: Integer, size of the array (1-indexed)
- m: Integer, number of operations
- queries: A list of m queries, each with three integers (a, b, k)

Output:

- A single integer: the maximum value after performing all operations.

Algorithm

1. Initialize the difference array:

- Create an array diff of size n + 2 (to handle boundaries).
- Set all elements of diff to 0.

2. Process each query efficiently:

- For each query (a, b, k) in queries:
 - Increment diff[a] by k.
 - Decrement diff[b + 1] by k.

3. Compute prefix sums and track the maximum:
 - Initialize maxVal = 0 and currentSum = 0.
 - For i from 1 to n:
 - Update currentSum = currentSum + diff[i].
 - If currentSum > maxVal, then set maxVal = currentSum.

4. Return the result:
 - Output maxVal as the maximum value in the array after all operations.

Exercise-2

Algorithm: Count Valid Array Pairs

Problem Description

Given an array arr of size n, count pairs (i, j) where $i < j$ and $arr[i] * arr[j] \leq \max(arr)$.

Algorithm Steps

Step 1: Read Input

- Input n → size of array
- Input array elements → arr[n]

Step 2: Find Maximum Value

- Initialize maxVal = arr[0]
- For each element x in arr:
 - If $x > \maxVal$, then $\maxVal = x$

Step 3: Sort the Array

- Sort arr in ascending order (Sorting helps us break early when condition fails and optimize searching.)

Step 4: Initialize Counter

- Set count = 0

Step 5: Iterate through Pairs

- For $i = 0$ to $n-2$:
 - For $j = i + 1$ to $n-1$:
 - If $arr[i] * arr[j] \leq \maxVal$:
 - Increment count
 - Else:
 - Break the inner loop (because further values will only be larger)

Step 6: Output Result

- Print count

