

Course: Data Structures

Student Name

Roll Number

Submission Date:

Exercise-1

Array Manipulation (Crush Problem) -

Problem Statement

Starting with a 1-indexed array of zeros and a list of operations, for each operation add a value to each array element between two given indices, inclusive. Once all operations have been performed, return the maximum value in the array.

Input and Output

Input:

- n: Integer, size of the array (1-indexed)
- m: Integer, number of operations
- queries: A list of m queries, each with three integers (a, b, k)

Output:

- A single integer: the maximum value after performing all operations.

Algorithm

1. Initialize the difference array:
 - Create an array diff of size $n + 2$ (to handle boundaries).
 - Set all elements of diff to 0.
2. Process each query efficiently:
 - For each query (a, b, k) in queries:
 - Increment $\text{diff}[a]$ by k.
 - Decrement $\text{diff}[b + 1]$ by k.

3. Compute prefix sums and track the maximum:
 - Initialize $\text{maxVal} = 0$ and $\text{currentSum} = 0$.
 - For i from 1 to n :
 - Update $\text{currentSum} = \text{currentSum} + \text{diff}[i]$.
 - If $\text{currentSum} > \text{maxVal}$, then set $\text{maxVal} = \text{currentSum}$.
4. Return the result:
 - Output maxVal as the maximum value in the array after all operations.

Exercise-2

Algorithm: Count Valid Array Pairs

Problem Description

Given an array arr of size n , count pairs (i, j) where $i < j$ and $\text{arr}[i] * \text{arr}[j] \leq \max(\text{arr})$.

Algorithm Steps

Step 1: Read Input

- Input $n \rightarrow$ size of array
- Input array elements $\rightarrow \text{arr}[n]$

Step 2: Find Maximum Value

- Initialize $\text{maxVal} = \text{arr}[0]$
- For each element x in arr :
 - If $x > \text{maxVal}$, then $\text{maxVal} = x$

Step 3: Sort the Array

- Sort arr in ascending order (Sorting helps us break early when condition fails and optimize searching.)

Step 4: Initialize Counter

- Set $\text{count} = 0$

Step 5: Iterate through Pairs

- For $i = 0$ to $n-2$:
 - For $j = i + 1$ to $n-1$:
 - If $\text{arr}[i] * \text{arr}[j] \leq \text{maxVal}$:
 - Increment count
 - Else:
 - Break the inner loop (because further values will only be larger)

Step 6: Output Result

- Print count

