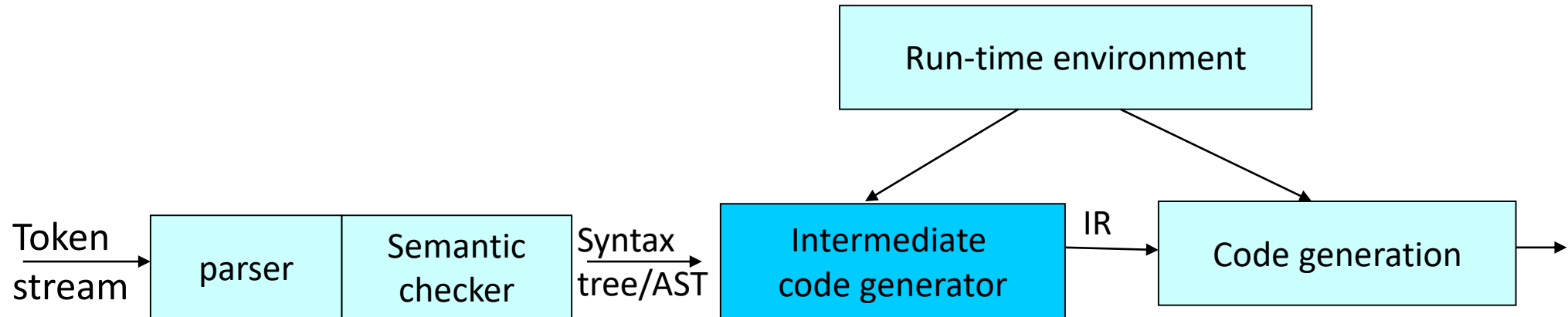


Intermediate Code Generation

- **Intermediate codes** are machine independent codes, but they are close to machine instructions
- The given program in a source language is converted to an **equivalent program** in an intermediate language by the intermediate code generator

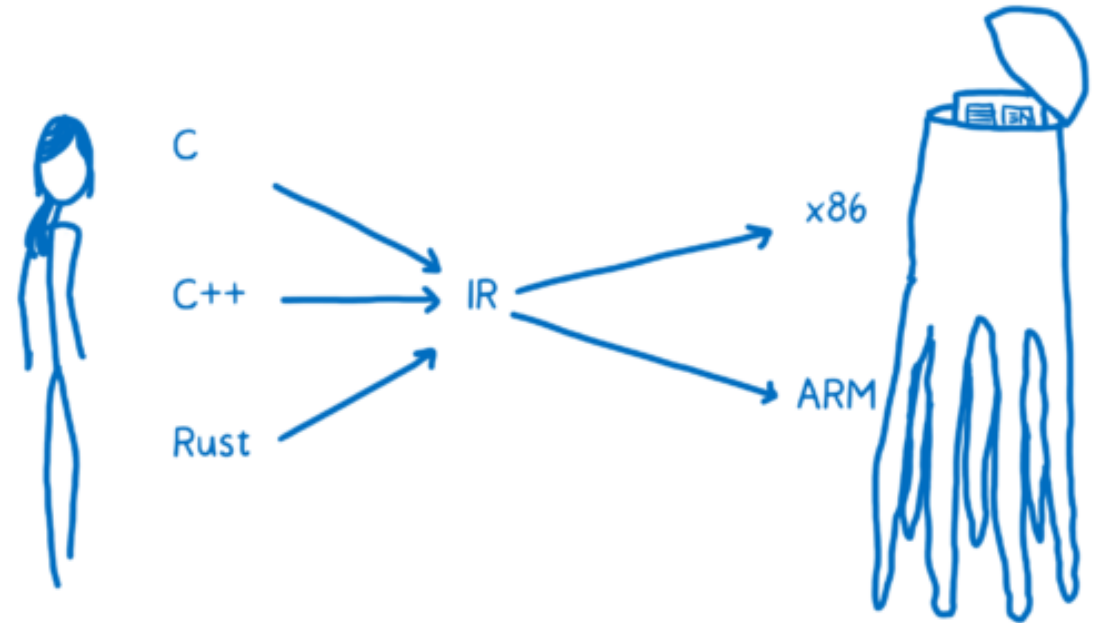


Basic Goals: Separation of Concerns

- Generate efficient code sequences for individual operations
- Keep it fast and simple: leave most optimizations to later phases
- Provide clean, easy-to-optimize code
- IR forms the basis for code optimization and target code generation

Intermediate language

- Goal: Translate AST to low-level machine-independent 3-address IR
- Two alternative ways:
 1. Bottom-up tree-walk on AST
 2. Syntax-Directed Translation



Three-Address Code (Quadraples)

- A quadraple is: $x := y \text{ op } z$
where x , y and z are names, constants or compiler-generated temporaries;
 op is any operator.
- But we may also use the following notation for quadraples (much better notation because it looks like a machine code instruction)
 $\text{op } x, y, z$
apply operator op to y and z , and store the result in x .
- We use the term “three-address code” because each statement usually contains three addresses (two for operands, one for the result).

Three-Address Statements

Binary Operator: `op result, y, z` or `result := y op z`

where `op` is a binary arithmetic or logical operator. This binary operator is applied to `y` and `z`, and the result of the operation is stored in `result`.

Ex: `add a, b, c`
 `addi a, b, c`
 `gt a, b, c`

Unary Operator: `op result, , y` or `result := op y`

where `op` is a unary arithmetic or logical operator. This unary operator is applied to `y`, and the result of the operation is stored in `result`.

Ex: `uminus a, , c`
 `not a, , c`
 `inttoreal a, , c`

Three-Address Statements (cont.)

Move Operator: `mov result, , y` or `result := y`

where the content of `y` is copied into `result`.

Ex:

```
mov    a, , c
movi   a, , c
movr   a, , c
```

Unconditional Jumps: `jmp , , L` or `goto L`

We will jump to the three-address code with the label `L`, and the execution continues from that statement.

Ex:

```
jmp    , , L1    // jump to L1
jmp    , , 7      // jump to the statement 7
```

Three-Address Statements (cont.)

Conditional Jumps: `jmprelop y, z, L` or `if y relop z goto L`

We will jump to the three-address code with the label `L` if the result of `y relop z` is true, and the execution continues from that statement. If the result is false, the execution continues from the statement following this conditional jump statement.

Ex:

<code>jmpgt</code>	<code>y, z, L1</code>	// jump to L1 if <code>y > z</code>
<code>jmpge</code>	<code>y, z, L1</code>	// jump to L1 if <code>y ≥ z</code>
<code>jmpeq</code>	<code>y, z, L1</code>	// jump to L1 if <code>y == z</code>
<code>jmpne</code>	<code>y, z, L1</code>	// jump to L1 if <code>y != z</code>

Our relational operator can also be a unary operator.

<code>jmpnz</code>	<code>y, , L1</code>	// jump to L1 if y is not zero
<code>jmpz</code>	<code>y, , L1</code>	// jump to L1 if y is zero
<code>jmpt</code>	<code>y, , L1</code>	// jump to L1 if y is true
<code>jmpf</code>	<code>y, , L1</code>	// jump to L1 if y is false

Three-Address Statements (cont.)

Procedure Parameters: param $x, ,$ or param x

Procedure Calls: call $p, n,$ or call p, n

where x is an actual parameter, we invoke the procedure p with n parameters.

Ex: param $x_1, ,$
... $\rightarrow p(x_1, \dots, x_n)$

param $x_n, ,$

call $p, n,$

$f(x+1, y) \rightarrow$ add $t1, x, 1$

param $t1, ,$

param $y, ,$

call $f, 2,$

Three-Address Statements (cont.)

Indexed Assignments:

move x, , y[i] or x := y[i]
move y[i], , x or y[i] := x

Address and Pointer Assignments:

moveaddr x, , y or x := &y
movecont x, , y or x := *y

Bottom-up tree-walk on AST

```
expr( node )
```

```
    int result, t1, t2, t3;
```

```
    switch( type of node )
```

```
    {
```

```
        case TIMES:
```

```
            t1 = expr( left child of node );
```

```
            t2 = expr( right child of node );
```

```
            result = new_name();
```

```
            emit( mov, result, t1, t2 );
```

```
            break;
```

```
        case PLUS:
```

```
            t1 = expr( left child of node );
```

```
            t2 = expr( right child of node );
```

```
            result = new_name();
```

```
            emit( add, result, t1, t2 );
```

```
            break;
```

```
        case ID:
```

```
            result = id.place;
```

```
            emit( "" )
```

```
            break;
```

```
        case NUM:
```

```
            result = node.val
```

```
            emit( "" )
```

```
            break;
```

```
    }
```

```
    return result;
```

Declarations

- A symbol table entry is created for every declared name
- Information includes name, type, relative address of storage, etc.
- Relative address consists of an offset:
 - Offset is from the base of the static data area for global
 - Offset is from the field for local data in an activation record for locals to procedures
- Types are assigned attributes type and width (size)
- Becomes more complex if we need to deal with nested procedures or records

Declarations

$$D \rightarrow T \text{ id} ; D \mid \varepsilon$$
$$T \rightarrow B C \mid \text{record } \{ \} D \{ \}$$
$$B \rightarrow \text{int} \mid \text{float}$$
$$C \rightarrow \varepsilon \mid [\text{num}] C$$

How to compute types via SDT?

SDT for Declarations

$D \rightarrow T \text{ id} ; D \mid \varepsilon$

$T \rightarrow B \ C \mid \text{record } \{ \text{' } D \text{' } \}$

$B \rightarrow \text{int} \mid \text{float}$

$C \rightarrow \varepsilon \mid [\text{num}] \ C$

$P \rightarrow \{ \text{offset} = 0; \text{top} = \text{new ST}(); \} D$

$D \rightarrow T \text{ id} ; \{ \text{top.enter}(\text{id.name}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$

$D \rightarrow \varepsilon$

$T \rightarrow B \{ C.t = B.\text{type} ; C.w = B.\text{width}; \} C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width} ; \}$

$B \rightarrow \text{int} \{ B.\text{type} = \text{integer}; B.\text{width} = 4; \}$

$B \rightarrow \text{float} \{ B.\text{type} = \text{float}; B.\text{width} = 8; \}$

$C \rightarrow \varepsilon \{ C.\text{type} = C.t ; C.\text{width} = C.w; \}$

$C \rightarrow [\text{num}] \{ C_1.t = C.t; C_1.w = C.w; \} C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type}); C.\text{width} = \text{num.val} * C_1.\text{width}; \}$

$T \rightarrow \text{record } \{ \{ \text{STStack.push}(\text{top}); \text{top} = \text{new ST}(\text{top}); \text{Stack.push}(\text{offset}); \text{offset} = 0 \}$

$\quad D \{ \{ T.\text{type} = \text{record}(\text{top}); T.\text{width} = \text{offset}; \text{offset} = \text{Stack.pop}(); \text{top} = \text{STStack.pop}(); \}$

Syntax-Directed Translation into Three-Address Code

- **Temporary names** are created for the interior nodes of a syntax tree
- The synthesized attribute **S.code** represents the code for the production S
- The nonterminal E has attributes:
 - **E.place** is the name that holds the value of E
 - **E.code** is a sequence of three-address statements evaluating E
- The function **newtemp()** returns a distinct name
- The function **newlabel()** returns a distinct label

Statements

$S \rightarrow \mathbf{id} := E$

$S \rightarrow \text{while } E \text{ do } S_1$

$S \rightarrow \text{if } E \text{ then } S_1 \text{ else } S_2$

$S \rightarrow S_1 S_2$

$E \rightarrow E_1 * E_2$

$E \rightarrow E_1 + E_2$

$E \rightarrow - E_1$

$E \rightarrow (E_1)$

$E \rightarrow \mathbf{id}$

Syntax-Directed Translation into Three-Address Code

```
S → id := E      { S.code = E.code || p = top.lookup(id.name);  
                    if p != NULL then gen('mov' p ',', E.place); else error ;}
```

```
E → E1 + E2      { E.place = newtemp();  
                        E.code = E1.code || E2.code || gen('add' E.place 'E1.place ' E2.place) ; }
```

```
E → E1 * E2    { E.place = newtemp();  
                      E.code = E1.code || E2.code || gen('mult' E.place ' ' E1.place ' ' E2.place); }
```

```
E → - E1      { E.place = newtemp();  
                  E.code = E1.code || gen('uminus' E.place ',', E1.place); }
```

$$E \rightarrow (E_1) \quad \{ E.place = E_1.place; \\ E.code = E_1.code; \}$$

```
E → id      { p = top.lookup(id.name);
               if p != NULL then E.place = id.place; else error;
               E.code = "" // null }
```

Syntax-Directed Definitions (cont.)

$S \rightarrow \text{if } E \text{ then } S_1 \text{ else } S_2$ `S.else = newlabel();`
 `S.after = newlabel();`
 `S.code = E.code ||`
 `gen('jmpf' E.place ',', S.else) || S1.code ||`
 `gen('jmp' ',', S.after) ||`
 `gen(S.else ':')` `|| S2.code ||`
 `gen(S.after ':')`

$S \rightarrow S_1 S_2$ `S1.code || S2.code`

Syntax-Directed Definitions (cont.)

$S \rightarrow \text{while } E \text{ do } S_1$

```
S.begin = newlabel();  
S.after = newlabel();  
S.code = gen(S.begin ":") || E.code ||  
           gen('jmpf' E.place ',', S.after) || S1.code ||  
           gen('jmp' ',', S.begin) ||  
           gen(S.after ':') }
```

Break and continue?

Syntax-Directed Definitions (cont.)

$S \rightarrow \text{while } E \text{ do } S_1$	$S_1.inbegin = \text{newlabel}(); S.begin = S_1.inbegin$ $S_1.inafter = \text{newlabel}(); S.after = S_1.inafter$ $S.code = \text{gen}(S.begin \text{ ":"}) \ \ E.code \ $ $\quad \text{gen}(\text{'jmpf' } E.place \text{ ',' } S.after) \ \ S_1.code \ $ $\quad \text{gen}(\text{'jmp' ',' } S.begin) \ $ $\quad \text{gen}(S.after \text{ ':'}) \}$
$S \rightarrow S_1 S_2$	$S_1.inbegin=S_2.inbegin=S.inbegin;$ $S_1.inafter=S_2.inafter=S.inafter;$ $S_1.code \ \ S_2.code$
$S \rightarrow \text{break}$	$\text{gen}(\text{'jmp' } S.inafter)$
$S \rightarrow \text{continue}$	$\text{gen}(\text{'jmp' } S.inbegin)$

Statements (cont.)

$D \rightarrow T \text{ id} ; D \mid \varepsilon$

$T \rightarrow B C \mid \text{record } \{ D \}$

$B \rightarrow \text{int} \mid \text{float}$

$C \rightarrow \varepsilon \mid [\text{num}] C$

$S \rightarrow \mathbf{id} := E$

$S \rightarrow \text{while } E \text{ do } S_1$

$S \rightarrow \text{if } E \text{ then } S_1 \text{ else } S_2$

$S \rightarrow S_1 S_2$

$E \rightarrow E_1 * E_2$

$E \rightarrow E_1 + E_2$

$E \rightarrow - E_1$

$E \rightarrow (E_1)$

$E \rightarrow \mathbf{id}$

$S \rightarrow \text{return } E$

$E \rightarrow \text{id (AP)}$

$AP \rightarrow \varepsilon \mid E, AP$

Function definitions and function calls

$D \rightarrow \text{fn } T \text{ id (FP) } \{ D; S \}$

$FP \rightarrow \varepsilon \mid T \text{ id, FP}$

Syntax-Directed Translation (cont.)

$D \rightarrow \text{fn } T \text{ id}$

(FP) '{ begin=newlabel(); gen(begin' :');

{ **STStack.push(top); top =new ST(top); Stack.push(offset); offset=0** }

D ; S}' {**offset=Stack.pop(); top=STStack.pop();**

top.enter(id.name,T.type, FP.types, begin)}

$FP \rightarrow \varepsilon \mid T \text{ id}, FP$ construct a list of types from FP

$S \rightarrow \text{return } E$ // introduced in runtime organization

$E \rightarrow \text{id (AP)}$ {p=top.lookup(id.name); AP.code || gen('call' p,n);}

$AP \rightarrow \varepsilon$

$AP \rightarrow E, AP_1$ {AP.code = E.code || gen('param' E.place) || AP₁.code}

Statements

$S \rightarrow \mathbf{id} := E$

$S \rightarrow \text{while } E \text{ do } S$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$E \rightarrow E * E$

$E \rightarrow E + E$

$E \rightarrow - E$

$E \rightarrow (E_1)$

$E \rightarrow \mathbf{id}$

$S \rightarrow L := E$

$E \rightarrow L$

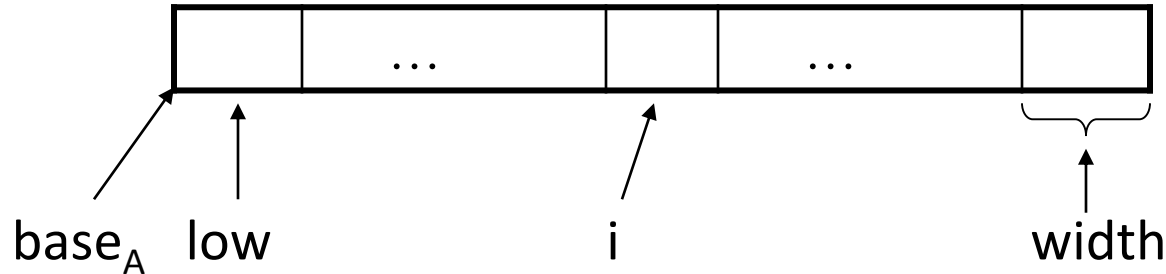
$L \rightarrow \mathbf{id} [E]$

$L \rightarrow L [E]$

Arrays

- Elements of arrays can be accessed quickly if the elements are stored in a block of consecutive locations.

A one-dimensional array **A**:



base_A is the address of the first location of the array **A**,

width is the width of each array element.

low is the index of the first array element

location of $A[i]$ \rightarrow $\text{base}_A + (i - \text{low}) * \text{width}$

Arrays (cont.)

$\text{base}_A + (i - \text{low}) * \text{width}$

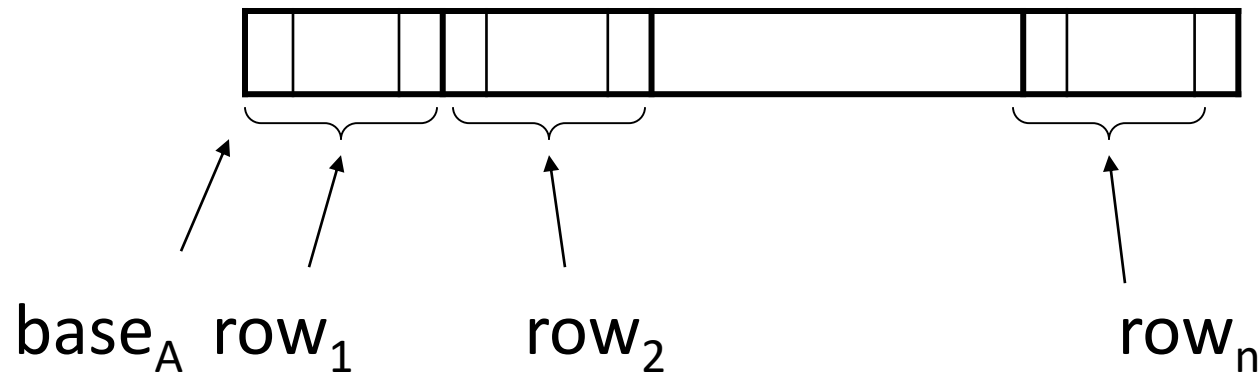
can be re-written as $\underbrace{i * \text{width}}_{\text{run-time}} + \underbrace{(\text{base}_A - \text{low} * \text{width})}_{\text{compile-time}}$

should be computed at **run-time** can be computed at **compile-time**

- So, the location of $A[i]$ can be computed at the run-time by evaluating the formula $i * \text{width} + c$ where c is $(\text{base}_A - \text{low} * \text{width})$ which is evaluated at compile-time.
- Intermediate code generator should produce the code to evaluate this formula $i * \text{width} + c$ (one multiplication and one addition operation).

Two-Dimensional Arrays

- A two-dimensional array can be stored in
 - either **row-major** (*row-by-row*)
 - or **column-major** (*column-by-column*).
- Most of the programming languages use **row-major** method.
- Row-major representation of a two-dimensional array:



Two-Dimensional Arrays (cont.)

- The location of $A[i_1][i_2]$ is: $\text{base}_A + ((i_1 - \text{low}_1) * n_2 + i_2 - \text{low}_2) * \text{width}$

base_A is the location of the array A.

low₁ is the index of the first row

low₂ is the index of the first column

n₂ is the number of elements in each row

width is the width of each array element

- Again, this formula can be re-written as

$$\underbrace{((i_1 * n_2) + i_2) * \text{width}}_{\text{run-time}} + \underbrace{(\text{base}_A - ((\text{low}_1 * n_2) + \text{low}_2) * \text{width})}_{\text{compile-time}}$$

should be computed at **run-time** can be computed at **compile-time**

Multi-Dimensional Arrays

- In general, the location of $A[i_1][i_2] \dots [i_k]$ is

$$((\dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k) * \text{width} + (\text{base}_A - ((\dots ((\text{low}_1 * n_2) + \text{low}_2) \dots) * n_k + \text{low}_k) * \text{width})$$

- So, the intermediate code generator should produce the codes to evaluate the following formula (to find the location of $A[i_1][i_2] \dots [i_k]$) :

$$((\dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k) * \text{width} + c$$

- To evaluate the $((\dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k) * \text{width}$ portion of this formula, we can compute

$$i_1 * \text{width} * n_2 * \dots * n_k + \dots + \underbrace{i_j * \text{width} * n_{j+1} * \dots * n_k}_{\text{width of the element at } i_j\text{-th DIM}} + \dots + i_k * \text{width}$$

$$= \text{width of the element at } i_j\text{-th DIM} = C_1.\text{width}$$

$C \rightarrow [\text{num}] \{ C_1.t = C.t; C_1.w = C.w; \} \quad C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type}); C.\text{width} = \text{num.val} * C_1.\text{width}; \}$

Syntax-Directed Translation into Three-Address Code

```
S → id := E      { S.code = E.code || p = top.lookup(id.name);  
                    if p != NULL then gen('mov' p ',', E.place); else error ; }
```

$$E \rightarrow E_1 * E_2 \quad \{ E.place = newtemp(); \\ E.code = E_1.code \parallel E_2.code \parallel gen('mult' E.place \text{ , } E_1.place \text{ , } E_2.place); \}$$

$S \rightarrow L := E \quad \{ S.code = E.code \mid \mid \text{gen('mov' L.array.base '[' L.place ']', , E.place); } \}$

$E \rightarrow L$ { E.place = newtemp(); gen('mov' E.place, , L.array.base '[' L.place '']); }

```
L → id [ E ] { L.code = E.code || L.array = top.lookup(id.name); L.type = L.array.type.elem;  
               L.place = newtemp(); gen('mult' L.place, E.place, L.type.width) ;}
```

```
L → L1 [ E ] { L.code = E.code || L1.type = L1.array.type.elem;  
                  L.place = newtemp(); t= newtemp();  
                  gen('mult' t, E.place, L1.type.width);  
                  gen('add' L.place, L1.place, t); }
```

Boolean Expressions

$E \rightarrow E_1 \text{ and } E_2$

{ E.code = E₁.code || E₂.code | E.place = newtemp(); gen('and' E.place ' ' E₁.place ' ' E₂.place; }

$E \rightarrow E_1 \text{ or } E_2$

{E.code = E₁.code || E₂.code | E.place = newtemp(); gen('or' E.place ' ' E₁.place ' ' E₂.place)}

$E \rightarrow \text{not } E_1$

{E.code = E₁.code | E.place = newtemp(); gen('not' E.place ' ' E₁.place) }

$E \rightarrow E_1 \text{ **relop** } E_2$

{E.code = E₁.code || E₂.code | E.place = newtemp(); gen(**relop**.code E.place ' ' E₁.place ' ' E₂.place) }

Three Address Codes - Example

```
x:=1;  
y:=x+10;  
while (x<y) {  
  x:=x+1;  
  if (x%2==1) then y:=y+1; →  
  else y:=y-2;  
}
```

```
01: mov  x,,1  
02: add  t1,x,10  
03: mov  y,,t1  
04: lt   t2,x,y  
05: jmpf t2,,17  
06: add  t3,x,1  
07: mov  x,,t3  
08: mod  t4,x,2  
09: eq   t5,t4,1  
10: jmpf t5,,14  
11: add  t6,y,1  
12: mov  y,,t6  
13: jmp  ,,16  
14: sub  t7,y,2  
15: mov  y,,t7  
16: jmp  ,,4  
17:
```

```
graph TD
    04((04)) -- blue --> 05((05))
    05 -- blue --> 06((06))
    06 -- blue --> 07((07))
    07 -- blue --> 08((08))
    08 -- blue --> 09((09))
    09 -- blue --> 10((10))
    10 -- red --> 14((14))
    10 -- blue --> 11((11))
    11 -- blue --> 12((12))
    12 -- blue --> 13((13))
    13 -- red --> 14
    13 -- blue --> 16((16))
    14 -- red --> 16
    14 -- blue --> 15((15))
    15 -- blue --> 16
    16 -- blue --> 04
    05 -- blue --> 17((17))
```

Classes

- Each class is regarded as a record
- All the **non-static attributes** are **fields** of the record
- All the **static attributes** are regarded as **global variables/functions**

Class C {	Record C {
int x;	int x;
fn T f(FP){	fn T f'(C& this, FP){
...	...
}	}
}	}
f(AP)	f'(this, AP)
c.f(AP)	f'(c, AP)
o.x	o.x
x	this.x

Inheritance

- How to handle methods may inherited from this parent classes?
- Naive approach: each class has its own Implementation?
- **Better approach:**
 - For each class, construct a **method table** including all the functions (**pointers to entry points of functions**) defined in this class as well as functions inherited from this parent classes
 - **method table:**
 1. **Copy inherited methods**
 2. **Overwrite overridden methods**
 3. **Append its own methods**
 - The record of the class includes all the data attributes defined in this class as well as inherited data attributes, in addition with **a pointer to this method table**

Exercise

Record {int x; float[3] y;} z; write ST?

$D \rightarrow T \text{ id ; } D \mid \varepsilon$

$T \rightarrow B \ C \mid \text{record } \{ \} D \{ \}$

$B \rightarrow \text{int} \mid \text{float}$

$C \rightarrow \varepsilon \mid [\text{num}] \ C$

$P \rightarrow \{ \text{offset} = 0; \text{top} = \text{new ST}(); \} D$

$D \rightarrow T \text{ id ; } \{ \text{top.enter(id.name, T.type, offset); offset} = \text{offset} + \text{T.width}; \} D_1$

$D \rightarrow \varepsilon$

$T \rightarrow B \{ C.t = B.type ; C.w = B.width; \} C \{ T.type = C.type; T.width = C.width ; \}$

$B \rightarrow \text{int} \{ B.type = \text{integer}; B.width = 4; \}$

$B \rightarrow \text{float} \{ B.type = \text{float}; B.width = 8; \}$

$C \rightarrow \varepsilon \{ C.type = C.t ; C.width = C.w; \}$

$C \rightarrow [\text{num}] \{ C_1.t = C.t; C_1.w = C.w; \} C_1 \{ C.type = \text{array}(\text{num.val}, C_1.type); C.width = \text{num.val} * C_1.width; \}$

$T \rightarrow \text{record } \{ \} \{ \text{STStack.push(top); top} = \text{new ST(top); Stack.push(offset); offset} = 0 \}$

$D \{ \} \{ T.type = \text{record(Top)}; T.width = \text{offset}; offset} = \text{Stack.pop()}; \text{top.STStack.pop()}; \}$