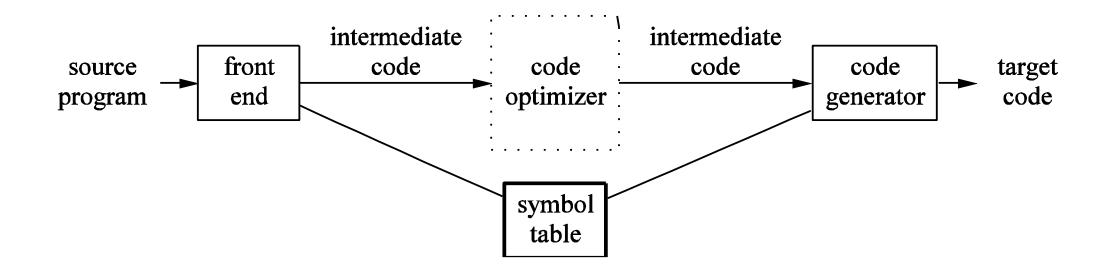
Code Optimization



Optimizations

```
[GCC/LLVM bugs: 1,622 (total) / 1,031 (fixed)]
[Reports: GCC (link1, link2, link3, link4, link5), LLVM (link1, link2, link3, link4, link5)]
[GCC/LLVM bugs: 1,634 (total) / 1,076 (fixed)]
[Reports: GCC (link1, link2, link3, link4, link5), LLVM (link1, link2, link3, link4, link5)]
[Recent CompCert bug reports: 31 (total) / 27 (fixed)]
[Reports: link]
[Recent Scala and Dotty bug reports: 42 (total) / 17 (fixed)]
[Reports: link]
[Recent ICC bug reports: 35 (total) / unknown (fixed)]
```

[Reports: link]

Optimizations

For languages like C and C++ there are three granularities of optimizations

Complexity

- 1. Local optimizations
 - Apply to a basic block in isolation
- 2. Global optimizations
 - Apply to a control-flow graph (method body) in isolation
- 3. Inter-procedural optimizations
- Apply across method boundaries

Most compilers do (1), many do (2), few do (3)

Cost of Optimizations

• In practice, a conscious decision is made not to implement the fanciest optimization known

Why?

- Some optimizations are hard to implement
- Some optimizations are costly in compilation time
- Some optimizations have low benefit, no theoretic guarantee
- Many fancy optimizations are all three!

Goal: Maximum benefit for minimum cost

Local Optimizations

- The simplest form of optimizations
- No need to analyze the whole procedure body
 - Just the basic block in question
- Techniques
 - 1. Algebraic Simplification
 - 2. Constant Folding
 - Dead Code Elimination
 - 4. Common Subexpression Elimination
 - 5. Copy Propagation
- Each local optimization does little by itself
- Typically optimizations interact, performing one optimization enables another
- Optimizing compilers repeat optimizations until no improvement is possible

Basic Blocks

- A basic block is a sequence of statements such that:
 - Flow of control enters at start
 - Flow of control leaves at end
 - No possibility of halting or branching except at end
- Each basic block has a first statement known as the "leader" of the basic block
- A name is "live" at a given point if its value will be used again in the program

Useful for local optimization

Transformations on Basic Blocks

- A basic block computes a set of expressions
 - The expressions are the values of names that are live on exit from the block
 - Two basic blocks are equivalent if they compute the same set of expressions
- Certain transformations can be applied without changing the computed expressions of a block
 - An optimizer uses such transformations to improve running time or space requirements of a program

Algebraic Simplification

Some statements can be deleted

```
x := x + 0x := x * 1
```

Some statements can be simplified

```
• x := x * 0 \Rightarrow x := 0

• x := x * 2 \Rightarrow x := x + x

• x := x * * 2 \Rightarrow x := x * x

• x := x * 8 \Rightarrow x := x << 3

• x := x * 15 \Rightarrow t := x << 4; x := t - x
```

(on some machines << is faster than *, and + is faster than *; but not on all!)

Constant Folding

- Operations on constants can be computed at compile time
 - If there is a statement $x := y \circ p z$ and y and z are constants
 - Then y op z can be computed at compile time

• Eg.

```
• x := 2+3 \Rightarrow x := 5
```

•
$$x := 2*3$$
 $\Rightarrow x := 6$

• if 2 < 0 jump L ⇒ if false jump L

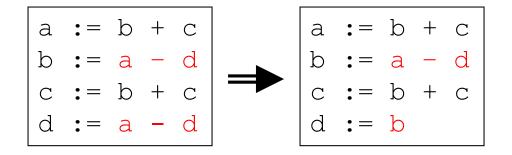
⇒ delete

Dead Code Elimination

- Eliminate unreachable basic blocks:
 - Code that is unreachable from the initial block
 - Is it possible?
- Removing unreachable code makes the program smaller
 - and sometimes also faster

Common Subexpression Elimination

Common subexpression elimination (DAG):



SSA form basic block without DAG

$$x := y + z$$
 $x := y + z$
... \Rightarrow ... no change of x,y,z
 $w := y + z$ $w := x$

Take care of points, array, function calls

Copy Propagation

- If w := x appears in a block, replace subsequent uses of w with uses
 of x
 - Assumes SSA form
- Example:

$$b := z + y$$

 $a := b$
 $x := 2 * a$
 $b := z + y$
 $a := b$
 $x := 2 * b$

- Only useful for enabling other optimizations
 - Constant folding
 - Dead code elimination

Examples

Copy Propagation and Constant Folding

$$a := 5$$
 $x := 2 * a$ \Rightarrow $x := 10$
 $y := x + 6$ $y := 16$
 $t := x * y$ $t := x << 4$

Copy Propagation and Dead Code Elimination and Algebraic Simplification

$$x := z + y$$
 $x := z + y$ $x := z + y$ $x := z + y$ \Rightarrow $x := z + x$ \Rightarrow $x := x + x$ \Rightarrow $x := x + x$ \Rightarrow $x := x + x$

Assume (a is not used anywhere else)

Applying Local Optimizations

- a := x * x b := 3
- c := x
- d := a

Dead code elimination

- Each local optimization does little by itself
- Typically optimizations interact, performing one optimization en $\frac{e}{f} := a + a$
- Optimizing compilers repeat optimizations until no improvemen g := 6 * f

a := x ** 2	a := x * x	a := x * x	a := x * x	a := x * x	a := x * x
b := 3	b := 3	b := 3	b := 3	b := 3	b := 3
c := x	c := x	c := x	c := x	c := x	c := x
d := c * c	d := c * c	d := x * x	d := x * x	d := a	d := a
e := b * 2	e := b << 1	e := 3 << 1	e := 6	e := 6	e := 6
f := a + d	f := a + d	f := a + d	f := a + d	f := a + d	f := a + a
g := e * f	g := e * f	g := e * f	g := e * f	g := e * f	g := 6 * f

Algebraic optimization

Copy propagation

Constant folding

Common subexpression elimination

Copy propagation

Review

- The simplest form of optimizations
- No need to analyze the whole procedure body
 - Just the basic block in question
- Techniques
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- Each local optimization does little by itself
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- Optimizing compilers repeat optimizations until no improvement is possible

Peephole Optimizations on Assembly Code

- These optimizations work on intermediate code
 - Target code
 - But they can be applied on IR
- Peephole optimization is effective for improving assembly code
 - The "peephole" is a short sequence of (usually contiguous) instructions
 - The optimizer replaces the sequence with another equivalent one (but faster

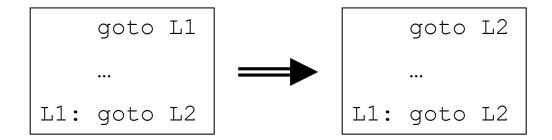
$$i_1, ..., i_n \rightarrow j_1, ..., j_m$$

Peephole Optimizations on Assembly Code

Eg. mov $a \b$, mov $b \a$ move $a \b$

if move \$b \$a is not the target of a jump

Flow-of-Control Optimizations



- If there are no other jumps to L1 and L1 is preceded by an unconditional jump, the statement at L1 can be eliminated
- Many of the basic block optimizations can be cast as peephole optimizations
- As for local optimizations, peephole optimizations must be applied repeatedly for maximum effect

Local Optimizations: Notes

Intermediate code is helpful for many optimizations

Many simple optimizations can still be applied on assembly language

- "Program optimization" is grossly misnamed
 - Code produced by "optimizers" is not optimal in any reasonable sense
 - "Program improvement" is a more appropriate term

Optimizations

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- 3. Inter-procedural optimizations
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Most compilers do (1), many do (2), few do (3)

Local vs. Global

- Local optimization involve statements within a single basic block
- All other optimizations are called global optimizations, e.g., peephole
- Local transformations are generally performed first
- Many types of transformations can be performed either locally or globally
- Global optimizations
 - ✓ Data-flow analysis
 - ✓ Intra-procedural analysis: across basic blocks, but not procedures
 - ✓ Inter-procedural analysis: across procedures

Global Optimization

- Global optimizations
 - 1. Global common subexpressions
 - 2. Copy Propagation
 - 3. Dead-code Elimination
 - 4. Code motion
 - 5. Induction Variables and Reduction in Strength

Quicksort in C

```
void quicksort(int m, int n) {
    int i, j, v, x;
    if (n <= m) return;</pre>
    /* Start of partition code */
    i = m-1; j = n; v = a[n];
    while (1) {
      do i = i+1; while (a[i] < v);
      do j = j-1; while (a[j] > v);
      if (i >= j) break;
      x = a[i]; a[i] = a[j]; a[j] = x;
    x = a[i]; a[i] = a[n]; a[n] = x;
    /* End of partition code */
    quicksort(m, j); quicksort(i+1, n);
```

Partition in Three-Address Code

```
(1) i := m-1
 (2) j := n
 (3) t1 := 4*n
 (4) v := a[t1]
 (5) i := i+1
 (6) t2 := 4*i
 (7) t3 := a[t2]
 (8) if t3 < v \text{ goto } (5)
 (9) j := j-1
(10) t4 := 4*j
(11) t5 := a[t4]
(12) if t5 > v goto (9)
(13) if i >= j goto (23)
(14) t6 := 4*i
(15) \times := a[t6]
```

```
(16) t7 := 4*i
(17) t8 := 4*j
(18) t9 := a[t8]
(19) a[t7] := t9
(20) t10 := 4*j
(21) a[t10] := x
(22) goto (5)
(23) t11 := 4*i
(24) \times := a[t11]
(25) t12 := 4*i
(26) t13 := 4*n
(27) t14 := a[t13]
(28) a[t12] := t14
(29) t15 := 4*n
(30) a[t15] := x
```

Control-flow graph

```
(1) i := m-1
                                          (13) if i >= j goto (23)
    (3) t1 := 4*n
    (4) v := a[t1]
                                                           (23) t11 := 4*i
                                  (14) t6 := 4*i
 (5) i := i+1
                                  (15) x := a[t6]
                                                           (24) x := a[t11]
 (6) t2 := 4*i
                                  (16) t7 := 4*i
                                                            (25) t12 := 4*i
 (7) t3 := a[t2]
                                  (17) t8 := 4*j
                                                            (26) t13 := 4*n
 (8) if t3 < v \text{ goto } (5)
                                  (18) t9 := a[t8]
                                                           (27) t14 := a[t13]
                                  (19) a[t7] := t9
                                                            (28) a[t12] := t14
                                  (20) t10 := 4*j
                                                           (29) t15 := 4*n
                                  (21) a[t10] := x
 (9) j := j-1
                                                           (30) a[t15] := x
                                  (22) goto (5)
(10) t4 := 4*j
(11) t5 := a[t4]
                            Local common-subexpression elimination and dead code
(12) if t5 > v goto (9)
```

elimination?

25

Local common-subexpression elimination and dead code elimination

```
(1) i := m-1
                                          (13) if i >= j goto (23)
    (3) t1 := 4*n
    (4) v := a[t1]
                                                            (23) t11 := 4*i
                                  (14) t6 := 4*i
 (5) i := i+1
                                  (15) x := a[t6]
                                                            (24) x := a[t11]
 (6) t2 := 4*i
                                  (17) t8 := 4*j
                                                            (26) t13 := 4*n
 (7) t3 := a[t2]
                                  (18) t9 := a[t8]
                                                            (27) t14 := a[t13]
 (8) if t3 < v \text{ goto } (5)
                                  (19) a[t6] := t9
                                                            (28) a[t11] := t14
                                  (21) a[t8] := x
                                                            (30) a[t13] := x
                                  (22) goto (5)
 (9) \ j := j-1
(10) t4 := 4*j
(11) t5 := a[t4]
                                    Global common-subexpression?
(12) if t5 > v goto (9)
                                                                                26
```

Global common-subexpression

```
(1) i := m-1
                                         (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
                                                          (23) t11 := 4*i
                                 (14) t6 := 4*i
 (5) i := i+1
                                 (15) x := t3
                                                           (24) x := t3
 (6) t2 := 4*i
                                 (17) t8 := 4*
                                                          (26) t13 := 4*n
 (7) t3 := a[t2]
                                 (18) t9 := a[t8]
                                                           (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                 (19) a[t2] := t5
                                                           (28) a[t2] := t14
                                 (21) a[t4] := x
                                                           (30) a[t1] := x
                                 (22) goto (5)
                                                        (27) t14 := v OK?
 (9) j := j-1
(10) t4 := 4*j
(11) t5 := a[t4]
                                    Copy Propagation?
(12) if t5 > v goto (9)
                                                                               27
```

Copy Propagation

```
(1) i := m-1
                                          (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
                                                           (23) t11 := 4*i
                                  (14) t6 := 4*i
 (5) i := i+1
                                  (15) x := t3
                                                            (24) x := t3
 (6) t2 := 4*i
                                  (17) t8 := 4*
                                                           (26) t13 := 4*n
 (7) t3 := a[t2]
                                  (18) t9 := a[t8]
                                                            (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                  (19) a[t2] := t5
                                                            (28) a[t2] := t14
                                  (21) a[t4] := t3
                                                            (30) a[t1] := t3
                                  (22) goto (5)
 (9) j := j-1
(10) t4 := 4*j
(11) t5 := a[t4]
                                       dead code elimination?
(12) if t5 > v goto (9)
```

Dead code elimination

```
(1) i := m-1
                                           (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
                                                            (23) t11 := 4*i
                                  (14) t6 := 4*i
 (5) i := i+1
                                  (15) \times := t3
                                                             (24) \times := t3
 (6) t2 := 4*i
                                  (17) t8 := 4*
                                                             (26) t13 := 4*n
 (7) t3 := a[t2]
                                  (18) t9 := a[t8]
                                                             (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                   (19) a[t2] := t5
                                                             (28) a[t2] := t14
                                   (21) a[t4] := t3
                                                             (30) a[t1] := t3
                                   (22) goto (5)
 (9) j := j-1
(10) t4 := 4*j
                                         Code motion?
(11) t5 := a[t4]
(12) if t5 > v goto (9)
                                         Move invariant to outside of loop
```

```
(1) i := m-1
                                           (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
                                  (14) t6 := 4*i
                                                             \frac{(23)}{(23)} t11 := 4*i
 (5) i := i+1
                                  (15) \times := t3
                                                             (24) x := t3
 (6) t2 := 4*i
                                  (17) t8 := 4*
                                                             (26) t13 := 4*n
 (7) t3 := a[t2]
                                  (18) t9 := a[t8]
                                                             (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                   (19) a[t2] := t5
                                                             (28) a[t2] := t14
                                   (21) a[t4] := t3
                                                             (30) a[t1] := t3
                                   (22) goto (5)
 (9) j := j-1
(10) t4 := 4*j
                                  (9) j := j-1
(11) t5 := a[t4]
                                  (10) t4 := 4*j => t4 :=t4-4
(12) if t5 > v goto (9)
                                  (5) i := i+1
                                   (6) t2 := 4*i => t2 :=t2+4
```

```
(1) i := m-1
                                           (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
       t4 : \div 4*j
       t2 := 4*i
                                   (14) t6 := 4*i
                                                             \frac{(23)}{(23)} t11 := 4*i
 (5) i := i+1
                                   (15) \times := t3
                                                             (24) x := t3
 (6) t2 := t2+4
                                   (17) t8 := 4*
                                                             (26) t13 := 4*n
 (7) t3 := a[t2]
                                   (18) t9 := a[t8]
                                                              (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                   (19) a[t2] := t5
                                                              (28) a[t2] := t14
                                   (21) a[t4] := t3
                                                              (30) a[t1] := t3
                                   (22) goto (5)
(9) j := j-1
(10) t4 := t4-4
                                   (9) j := j-1
(11) t5 := a[t4]
                                   (10) t4 := 4*j => t4 := t4-4
(12) if t5 > v goto (9)
                                  (5) i := i+1
                                                                                   31
                                  (6) t2 := 4*i => t2 :=t2+4
```

```
(1) i := m-1
                                            (13) if i >= j goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
       t4 : \( \pm 4 \times \)
       t2 := 4*i
                                   (14) t6 := 4*i
                                                              \frac{(23)}{(23)} t11 := 4*i
 (5) i := i+1
                                   (15) \times := t3
                                                              (24) \times := t3
 (6) t2 := t2+4
                                   (17) t8 := 4*
                                                              (26) t13 := 4*n
 (7) t3 := a[t2]
                                   (18) t9 := a[t8]
                                                               (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                    (19) a[t2] := t5
                                                               (28) a[t2] := t14
                                    (21) a[t4] := t3
                                                               (30) a[t1] := t3
                                    (22) goto (5)
 (9) j := j-1
(10) t4 := t4-4
                                   (10) t4 := 4*j => t4:=t4-4
(11) t5 := a[t4]
                                   (6) t2 := 4*i => t2 := t2+4
(12) if t5 > v goto (9)
                                                 i>=j iff t2>=t4
```

```
(1) i := m-1
                                           (13) if t2 >= t4 goto (23)
    (2) j := n
    (3) t1 := 4*n
    (4) v := a[t1]
       t4 : = 4*j
       t2 := 4*i
                                   (14) t6 := 4*i
                                                             \frac{(23)}{(23)} t11 := 4*i
 (5) i := i+1
                                   (15) \times := t3
                                                             (24) \times := t3
 (6) t2 := t2+4
                                   (17) t8 := 4*
                                                             (26) t13 := 4*n
 (7) t3 := a[t2]
                                   (18) t9 := a[t8]
                                                             (27) t14 := a[t1]
 (8) if t3 < v \text{ goto } (5)
                                   (19) a[t2] := t5
                                                             (28) a[t2] := t14
                                   (21) a[t4] := t3
                                                             (30) a[t1] := t3
                                   (22) goto (5)
(10) t4 := t4-4
                                   (10) t4 := 4*j => t4:=t4-4
(11) t5 := a[t4]
                                   (6) t2 := 4*i => t2 := t2+4
(12) if t5 > v goto (9)
                                                i>=j iff t2>=t4
```