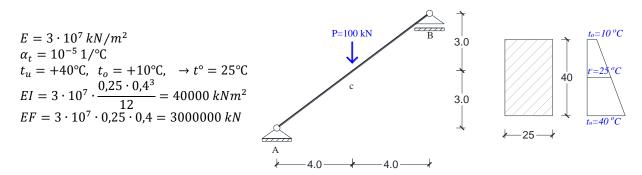
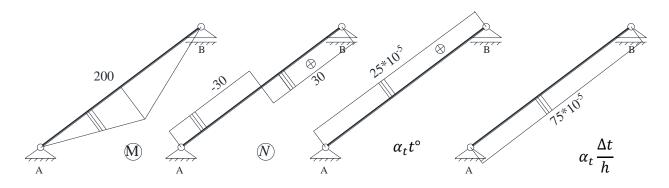
Zadatak: Za istovremeno dejstvo opterećenja i temperature odrediti dijagram pomeranja nosača sa slike u pravcu: a) ose štapa b) upravno na osu štapa c)vertikalno d)horizontalno Uticaj transverzalne sile na deformaciju se zanemaruje.



-Dijagrami presečnih sila i temperaturne promene u nosaču

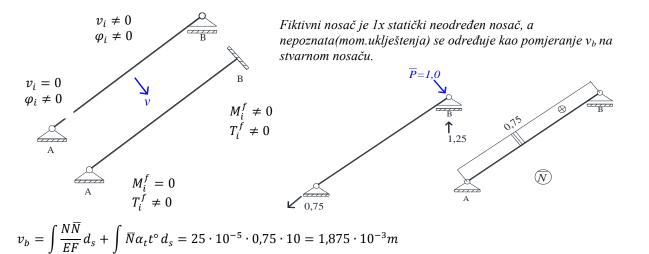


a) Pomeranje u pravcu ose štapa
$$\varepsilon = \frac{N}{EF} + \alpha_t t^\circ \to u_x = \int_0^x \varepsilon_\zeta \, d_\zeta + u_0$$

u₀- početno pomjeranje A podintegralne veličine su konstantne

$$\begin{split} u_c &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot 5 = \left(\frac{-30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot 5 = 1, 2 \cdot 10^{-3} m \\ u_B &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot 5 + u_c = \left(\frac{30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot 5 + u_c = 2, 5 \cdot 10^{-3} m \end{split}$$

b) Pomeranje upravno na osu štapa

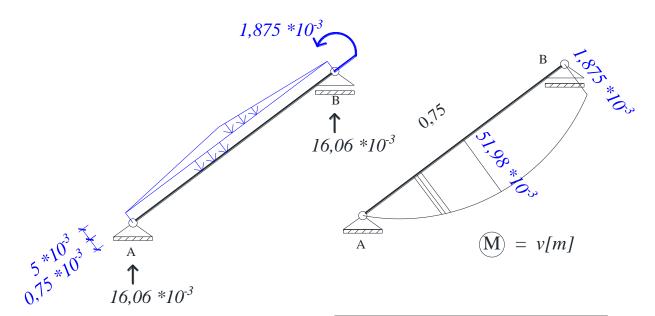


-Fiktivno opterećenje

$$m^f = \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot tg\alpha; \; \alpha = 0 \to m^f = 0$$

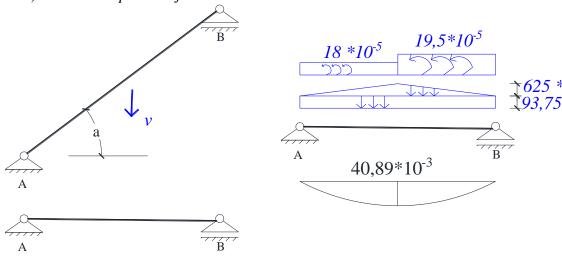
α- ugao između stvarnog i fiktivnog nosača

$$p^f = \left(\frac{M}{EI} + \alpha_t \frac{\Delta t}{h}\right) \frac{1}{\cos \alpha} = \left(\frac{200}{4 \cdot 10^4} + 75 \cdot 10^{-5}\right) \frac{1}{1} = 0,005 + 0,00075$$



c) Vertikalno pomeranje

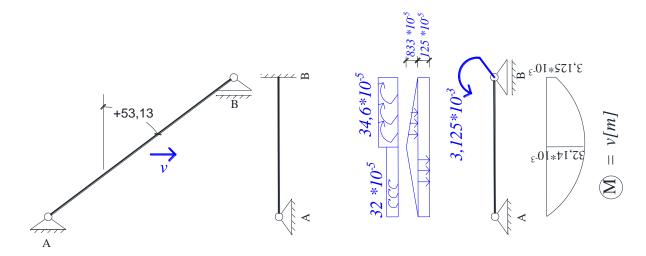
αje pozitivan ukoliko ide u smeru kazalike na satu.



 $arctg\alpha=6/8=36,\!87^\circ\rightarrow\alpha=-36,\!87^\circ$

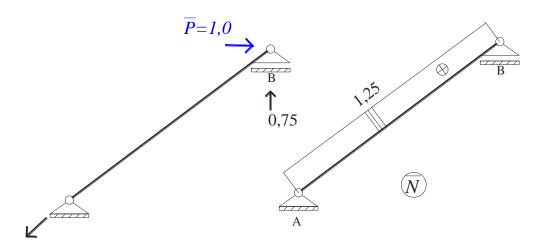
$$\begin{split} p^f &= \left(\frac{M}{EI} + \alpha_t \frac{\Delta t}{h}\right) \frac{1}{\cos \alpha} = \left(\frac{200}{4 \cdot 10^4} + 75 \cdot 10^{-5}\right) \frac{1}{0.8} = (625 + 93.75) 10^{-5} \\ a\text{-}c\text{:} \ m^f &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot tg\alpha = \left(\frac{-30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot (-0.75) = -18 \cdot 10^{-5} \\ c\text{-}b\text{:} \ m^f &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot tg\alpha = \left(\frac{30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot (-0.75) = -19.5 \cdot 10^{-5} \end{split}$$

d) Horizontalno pomjeranje



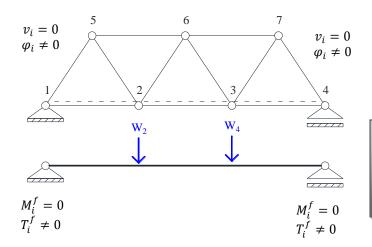
$$arctg\alpha = 8/6 = 53,13^{\circ} \rightarrow \alpha = +53,13^{\circ}$$

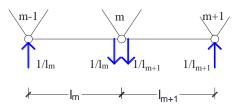
$$\begin{split} p^f &= \left(\frac{M}{EI} + \alpha_t \frac{\Delta t}{h}\right) \frac{1}{\cos \alpha} = \left(\frac{200}{4 \cdot 10^4} + 75 \cdot 10^{-5}\right) \frac{1}{0.6} = (833.3 + 125)10^{-5} \\ a\text{-}c\text{:} \ m^f &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot tg\alpha = \left(\frac{-30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot 1,333 = 32 \cdot 10^{-5} \\ c\text{-}b\text{:} \ m^f &= \left(\frac{N}{EF} + \alpha_t t^\circ\right) \cdot tg\alpha = \left(\frac{30}{3 \cdot 10^6} + 25 \cdot 10^{-5}\right) \cdot 1,333 = 34.6 \cdot 10^{-5} \end{split}$$



$$v_b = \int \frac{N\overline{N}}{EF} d_s + \int \overline{N} \alpha_t t^{\circ} d_s = 25 \cdot 10^{-5} \cdot 1,25 \cdot 10 = 3,125 \cdot 10^{-3} m$$

Dijagram pomeranja rešetkastih nosača





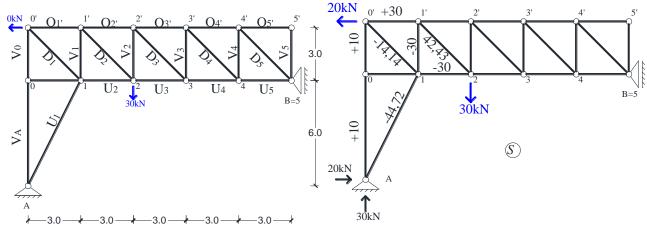
Izraz za elastične težine (razlika obrtanja štapova levo i desno od čvora):

$$W_m = \sum \frac{S \cdot \bar{S}}{EF} l + \sum \bar{S}_m \alpha_T t^{\circ} l$$

Zadatak: Za rešetkasti nosač sa slike nacrtati dijagram vertikalnog pomeranja gornjeg pojasa usled:

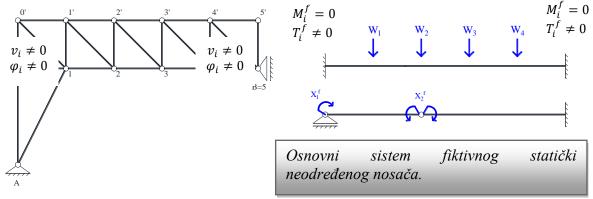
- a) Zadatog opterećenja sa slike
- b) Temperaturne promene u osama štapova gornjeg pojas $t^{\circ} = +25^{\circ}C$
- c) Pomeranja oslonca "A" u levo za 3cm

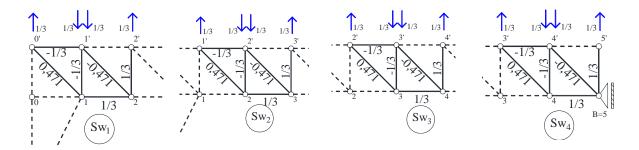
EF = const.



Redukovane dužine zbog EF=const su iste kao i stvarne dužine nosača $l'' = \frac{F_c}{F} d_s = l$.

-Fiktivni nosač i elastične težine





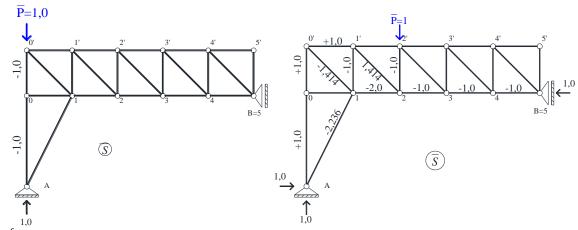
a) Usled zadatog opterećenja

$$\begin{split} EFW_1 &= \sum S \cdot \bar{S} \ l \\ &= 30 \cdot (-1/3) \cdot 3 + (-30) \cdot 1/3 \cdot 3 + (-30) \cdot (-1/3) \cdot 3 + (-14,14) \cdot 0,471 \\ &\cdot 4,243 + 42,43 \cdot (-0,471) \cdot 4,243 = -143,05 \end{split}$$

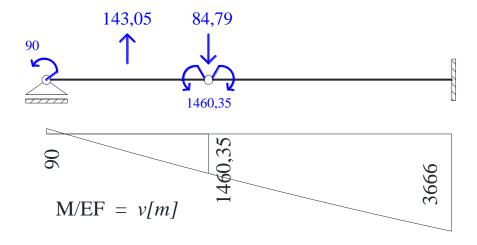
$$EFW_2 &= \sum S \cdot \bar{S} \ l = 42,43 \cdot 0,471 \cdot 4,243 = 84,79 \\ EFW_3 &= EFW_4 = 0 \end{split}$$

-fiktivne nepoznate

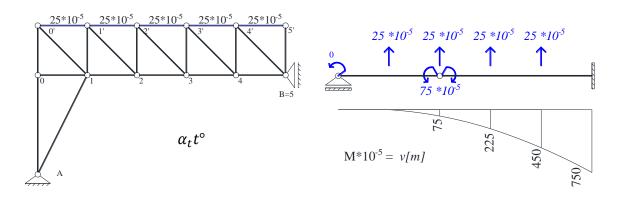
* $Stanje X_1^f = 1$



$$\begin{split} X_1^f &= EFv_0 = 10 \cdot (-1) \cdot 3 + 10 \cdot (-1) \cdot 6 = -90 \\ X_2^f &= EFv_2 = 10 \cdot 1 \cdot 6 + 10 \cdot 1 \cdot 3 + 30 \cdot 1 \cdot 3 + (-14,14) \cdot (-1,414) \cdot 4,243 + (-44,72) \cdot (-2,236) \\ & \cdot 6,708 + (-30) \cdot (-1) \cdot 3 + 42,43 \cdot 1,414 \cdot 4,243 + (-30) \cdot (-2) \cdot 3 = 1460,2 \end{split}$$



b) Usled temperaturne promene u osi štapova gornjeg pojasa



$$W_1 = W_2 = W_3 = W_4 = \sum \alpha_t t^{\circ} \cdot \bar{S} \cdot l = -25 \cdot 10^{-5} \cdot \frac{1}{3} \cdot 3 = -25 \cdot 10^{-5}$$

$$X_1^f = EFv_0 = 0$$

 $X_2^f = EFv_2 = 25 \cdot 10^{-5} \cdot 1 \cdot 3 = 75 \cdot 10^{-5}$

c) Usled pomeranja oslonca "A" za 3cm u levo

Sve elastične težine su jednake 0 zbog toga što pomeranje oslonaca ne izaziva sile u štapovima.

$$X_1^f = v_0 = 0$$

 $X_2^f = v_2 = -\sum \bar{C}_i \bar{c}_i \, 25 = -(-1) \cdot 0.03 = 0.03$

