12

СТАТИКА КОНСТРУКЦИЈА 1

Модул: Конструкције

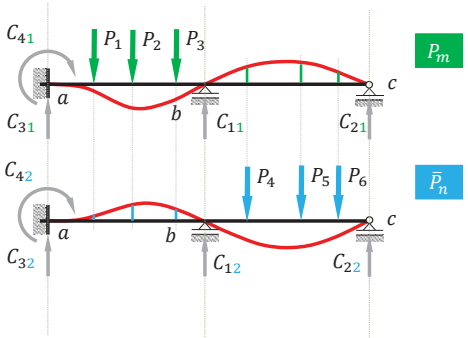
– материјал за вежбе –

2024.

Теореме о узајамности

20 Betti – јева теорема

$$\sum P_m \bar{\delta}_m + \sum C_i \bar{c}_i = \sum \bar{P}_n \delta_n + \sum \bar{C}_i c_i$$



Рад спољашњих сила P_m и C_i **првог** система при померањима која изазива **други** систем једнак је раду спољашњих сила $\bar{P}_n$ и $\bar{C}_i$ **другог** система при померањима који изазива **први** систем утицаја.

21 Maxwell – ова теорема

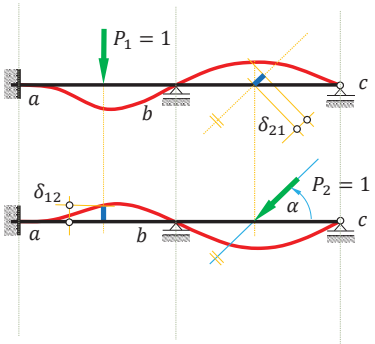
$$\sum P_m \bar{\delta}_m + \sum C_i \bar{c}_i = \sum \bar{P}_n \delta_n + \sum \bar{C}_i c_i$$

$P_m \Rightarrow P_1 = 1 \qquad \Rightarrow \quad \delta_n = \delta_{21}$

$\bar{P}_n \Rightarrow P_2 = 1 \qquad \Rightarrow \quad \bar{\delta}_m = \delta_{12}$

$$\sum 1 \cdot \bar{\delta}_{12} + \sum C_i \bar{c}_i = \sum 1 \cdot \delta_{21} + \sum \bar{C}_i c_i$$

$$1 \cdot \delta_{12} = 1 \cdot \delta_{21} \qquad \delta_{12} = \delta_{21}$$



Померање нападне тачке силе P_1 у правцу те силе услед силе P_2 једнако је померању нападне тачке силе P_2 у правцу силе P_2 услед силе P_1.

22 прва Rayleigh – јева теорема

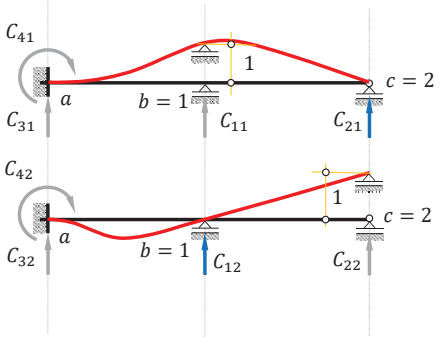
$$\sum P_m \bar{\delta}_m + \sum C_i \bar{c}_i = \sum \bar{P}_n \delta_n + \sum \bar{C}_i c_i$$

$P_m \Rightarrow P_1 = 0 \qquad c_i = c_1 = 1 \quad \Rightarrow \quad C_i = C_{12}$

$\bar{P}_n \Rightarrow P_2 = 0 \qquad \bar{c}_i = c_2 = 1 \quad \Rightarrow \quad \bar{C}_i = C_{21}$

$$\sum 0 \cdot \bar{\delta}_m + \sum C_i \bar{c}_i = \sum 0 \cdot \delta_n + \sum \bar{C}_i c_i$$

$$C_{12} \cdot 1 = C_{21} \cdot 1$$



Реакција ослонца 1 услед јединичног померања ослонца 2 једнака је реакцији ослонца 2 услед јединичног померања ослонца 1.

23 друга Rayleigh – јева теорема

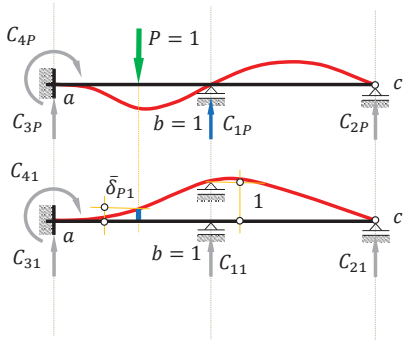
$$\sum P_m \bar{\delta}_m + \sum C_i \bar{c}_i = \sum \bar{P}_n \delta_n + \sum \bar{C}_i c_i$$

$P_m \Rightarrow P = 1 \qquad c_i = 0 \quad \Rightarrow \quad C_{1P}$

$\bar{P}_n \Rightarrow P = 0 \qquad \bar{c}_i = c_1 = 1 \quad \Rightarrow \quad \bar{\delta}_{P1}$

$$\sum 1 \cdot \bar{\delta}_{P1} + \sum C_{1P} \cdot 1 = \sum 0 \cdot \delta_n + \sum \bar{C}_{1P} \cdot 0$$

$$C_{1P} \cdot 1 = -\bar{\delta}_{P1} \cdot 1 \qquad C_{1P} = -\bar{\delta}_{P1}$$



Реакција ослонца **1** услед дејства јединичне силе **P** једнака је негативној вредности померања нападне тачке силе **P** у правцу те силе услед јединичног померања ослонца **1**.

DEFORMACIJA STATIČKI ODREĐENIH NOSAČA

$$\left.\begin{aligned} \varkappa &= \frac{M}{EJ} + \alpha_t \frac{\Delta t}{h} \\ \varepsilon &= \frac{N}{EF} + \alpha_t t^\circ \\ \varphi_T &= k \frac{T}{GF} \end{aligned}\right\} \rightarrow \Delta_{ik}, T_{ik}, T_{ki} \rightarrow C_{oi}, C_{ui} \Rightarrow u_i, v_i$$

→ princip virtuelni radova =

Princip: Algebarski zbir radova unutrašnji i spoljašnji jednog mogućeg stanja jeste jednak nuli

$$\underbrace{\Sigma \bar{F}_i + \Sigma \bar{Q} c_i}_{\delta} = \int_s (\bar{M}\varkappa + \bar{N}\varepsilon + \bar{T}\varphi_T)\, ds$$

$\bar{P}=1$

$\bar{M}=1$

$$\delta = \int_s (\bar{M}\varkappa + \bar{N}\varepsilon + \bar{T}\varphi_T)\, ds - \Sigma \bar{Q} c_i$$

$$\delta = \int_s \left(\frac{M\bar{M}}{EJ} + \frac{N\bar{N}}{EF} + k\frac{T\bar{T}}{GF} + \bar{M}\alpha_t \frac{\Delta t}{h} + \bar{N}\alpha_t t^\circ \right) ds - \Sigma \bar{Q} c_i$$

$$\delta_0 = \int_s \frac{M\bar{M}}{EJ} ds + \int_s \frac{N\bar{N}}{EF} ds + k \cdot \int \frac{T\bar{T}}{GF} ds \quad / EJ_c$$

$$\delta_t = \int_s \bar{M}\alpha_t \frac{\Delta t}{h} ds + \int_s \bar{N}\alpha_t t^\circ ds$$

$\delta_c = -\Sigma \bar{Q} c_i$ pom. oslonca

$$EJ_c \cdot \delta_0 = \int_s M\bar{M} \frac{J_c}{J} ds + \frac{J_c}{F_c} \int_s N\bar{N} \frac{F_c}{F} ds + (2+\mu) \frac{J_c}{F_c} \int_s T\bar{T} \frac{F_c}{F} ds$$

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$ds' = \frac{J_c}{J} ds$

$ds'' = \frac{F_c}{F} ds$

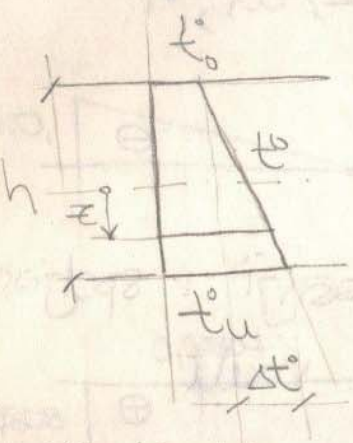
$ds''' =$

$$\boxed{EJ_c \delta_0 = \int_s M\bar{M} \frac{J_c}{J} ds + \frac{J_c}{F_c} \int_s N\bar{N} \frac{F_c}{F} ds}$$

usled spoljašnjeg opterećenja

$$EJ_c \cdot \delta_t = EJ_c \int_s \bar{M} \alpha_t \frac{\Delta t}{h} ds + EJ_c \int_s \bar{N} \alpha_t t^\circ \cdot ds$$

$$EJ_c \delta_c = -\sum \bar{C}_i c_i$$



$$t^\circ(z) = t^\circ_o + \Delta t \frac{z}{h}$$

$$\Delta t^\circ = t^\circ_u - t^\circ_o$$

$$t^\circ = \frac{t^\circ_u + t^\circ_o}{2}$$

tod rešetki 5

$$\delta = \int_s \bar{N} \varepsilon ds - \sum \bar{C}_i c_i$$

$$\delta = \sum_s \int_i^k \bar{N} \varepsilon ds - \sum \bar{C}_i c_i = \sum_s \bar{S} \Delta l - \sum \bar{C}_i c_i = \sum_s \frac{S\bar{S}}{EF} l + \sum \bar{S} \cdot \alpha_t t^\circ \cdot l - \sum \bar{C}_i c_i$$

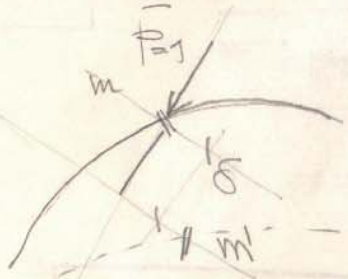
$$\int_i^k \bar{N} \varepsilon ds = \bar{N} \varepsilon \int_i^k ds = \bar{N} \cdot \underbrace{\varepsilon \cdot l}_{\Delta l} = \bar{S} \cdot \Delta l$$

$$\delta_o = \sum_s \frac{S\bar{S}}{EF} l \Big/ EF_c \rightarrow EF_c \cdot \delta_o = \sum \frac{S\bar{S}}{F} \cdot l$$

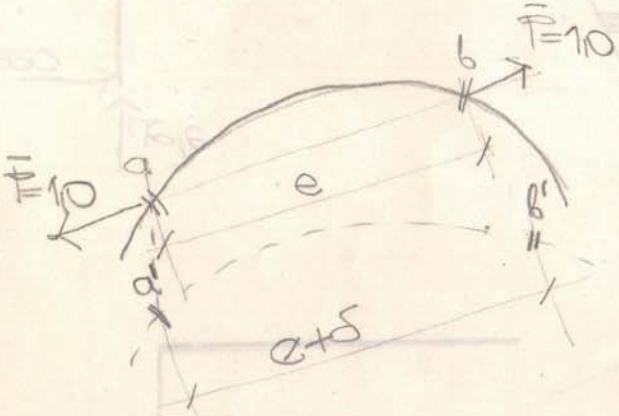
$$\delta_t = \sum_s \bar{S} \alpha_t t^\circ \cdot l \Big/ EF_c \rightarrow EF_c \cdot \delta_t = \sum \bar{S} \alpha_t t^\circ l E F_c$$

$$\delta_c = -\sum \bar{C}_i c_i \Big/ EF_c \qquad EF_c \delta_c = -EF_c \sum \bar{C}_i c_i$$

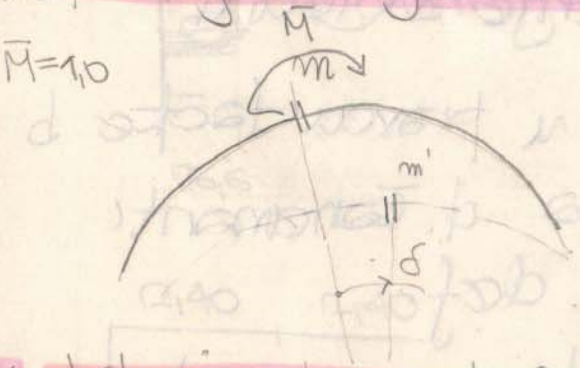
1. pom. tačke u određenom pravcu



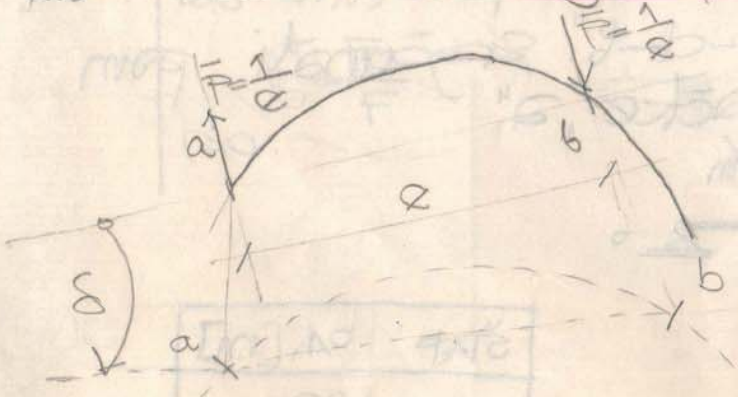
2. promjena odstojanja između dvije tačke



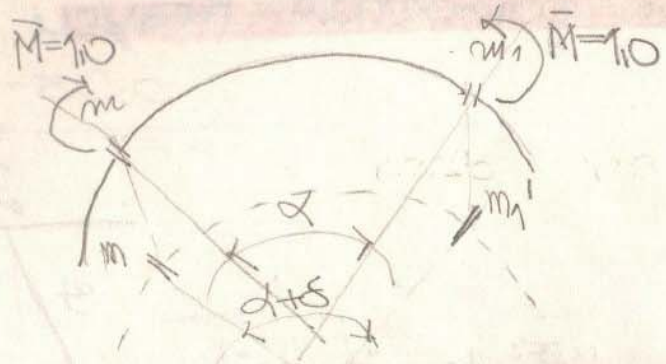
3. promjena ugla u presjeku



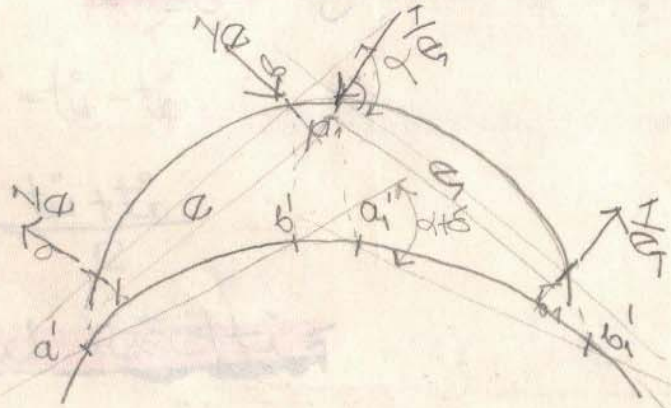
4 obrtanje prave koja prolazi kroz tačke A i B



5. promjena ugla između pravaca m i m_1

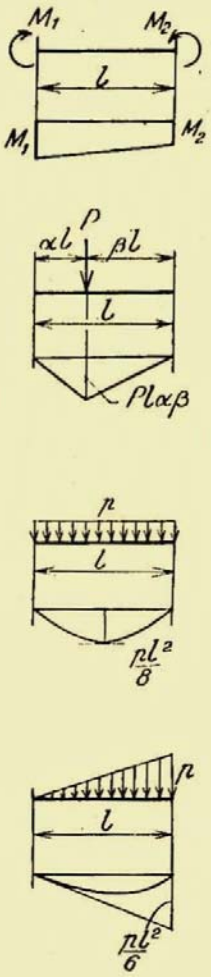


6. promjena ugla između dvije prave

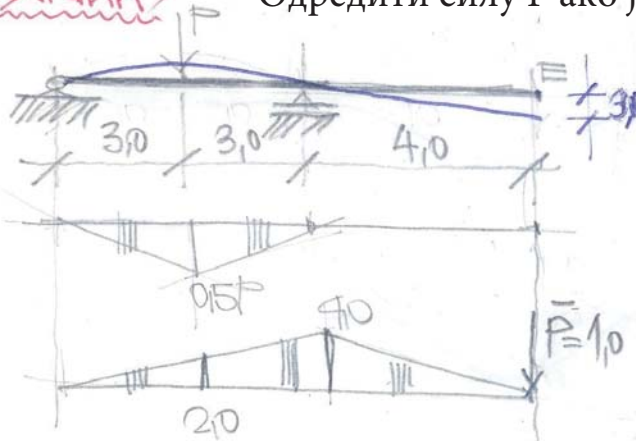


TABLICA 1

$\frac{1}{l}\frac{J_c}{J}\int M\bar{M}ds$	$\bar{i}$	$\bar{k}$	$\bar{i}$ $\bar{k}$	$\bar{m}$ αl βl	$\bar{m}$	$\bar{k}$
i	$i\bar{i}$	$\frac{1}{2}i\bar{k}$	$\frac{1}{2}i(\bar{i}+\bar{k})$	$\frac{1}{2}i\bar{m}$	$\frac{2}{3}i\bar{m}$	$\frac{1}{4}i\bar{k}$
k	$\frac{1}{2}k\bar{i}$	$\frac{1}{3}k\bar{k}$	$\frac{1}{6}k(\bar{i}+2\bar{k})$	$\frac{1}{6}k\bar{m}(1+\alpha)$	$\frac{1}{3}k\bar{m}$	$\frac{2}{15}k\bar{k}$
i	$\frac{1}{2}i\bar{i}$	$\frac{1}{6}i\bar{k}$	$\frac{1}{6}i(2\bar{i}+\bar{k})$	$\frac{1}{6}i\bar{m}(1+\beta)$	$\frac{1}{3}i\bar{m}$	$\frac{7}{60}i\bar{k}$
i k	$\frac{1}{2}(i+k)\bar{i}$	$\frac{1}{6}(i+2k)\bar{k}$	$\frac{1}{6}[i(2\bar{i}+\bar{k})+ +k(\bar{i}+2\bar{k})]$	$\frac{1}{6}[i(1+\beta)+ +k(1+\alpha)]\bar{m}$	$\frac{1}{3}(i+k)\bar{m}$	$\frac{1}{60}(7i+8k)\bar{k}$
$\bar{m}$ αl βl	$\frac{1}{2}m\bar{i}$	$\frac{1}{6}m\bar{k}(1+\alpha)$	$\frac{1}{6}m[\bar{i}(1+\beta)+ +\bar{k}(1+\alpha)]$	$\frac{1}{3}m\bar{m}$	$\frac{1}{3}m\bar{m}(1+\alpha\beta)$	$\frac{1}{20}m\bar{k}(1+\alpha)\times \times(\frac{7}{3}-\alpha^2)$
$\bar{m}$	$\frac{2}{3}m\bar{i}$	$\frac{1}{3}m\bar{k}$	$\frac{1}{3}m(\bar{i}+\bar{k})$	$\frac{1}{3}m\bar{m}(1+\alpha\beta)$	$\frac{8}{15}m\bar{m}$	$\frac{1}{5}m\bar{k}$
k	$\frac{1}{4}k\bar{i}$	$\frac{2}{15}k\bar{k}$	$\frac{1}{60}k(7\bar{i}+8\bar{k})$	$\frac{1}{20}k\bar{m}(1+\alpha)\times \times(\frac{7}{3}-\alpha^2)$	$\frac{1}{5}k\bar{m}$	$\frac{8}{105}k\bar{k}$
i	$\frac{1}{4}i\bar{i}$	$\frac{2}{60}i\bar{k}$	$\frac{1}{60}i(8\bar{i}+7\bar{k})$	$\frac{1}{20}i\bar{m}(1+\beta)\times \times(\frac{7}{3}-\beta^2)$	$\frac{1}{5}i\bar{m}$	$\frac{31}{420}i\bar{k}$



ЗАДАТАК: Одредити силу P ако је вертикално померање тачке "E" 3mm.



$v_E = 3{,}0\ mm$

$EJ = 10 \cdot 10^{-3}\ kNm^2$

(M) (kNm)

(M₁) (kNm)

$EJ v_E = -3{,}0P$

$10 \cdot 10^{-3} \cdot 0{,}003 = -3{,}0P$

$P = -10{,}00\ kN$

$EJ\, v_E = -\frac{1}{3} \cdot 0{,}5P \cdot 2 \cdot 3 - \frac{1}{6} 0{,}5P(4+2\cdot 2)\cdot 3 =$

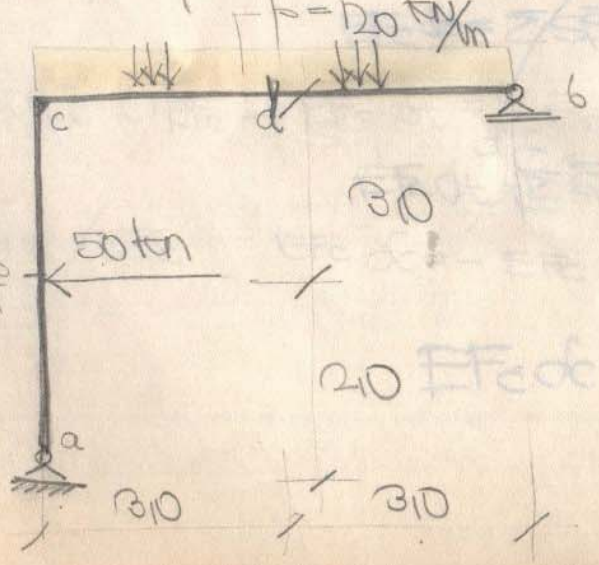
$= -1P - 2P = -3P$

Zadatak:

Za dati nosač i opterećenje odrediti:

1.
a) pomeranje tačke f u pravcu tačke b
b) obrtanje preseka d. Tenzoriti uticaj transf. sila na def.

2. Pri zadatoj promjeni temperature $t_0 = -5°C$, $t_u = 25°C$ duž štapa „c–d–b" sračunati pom. tačke „d" u pravcu tačke „2"



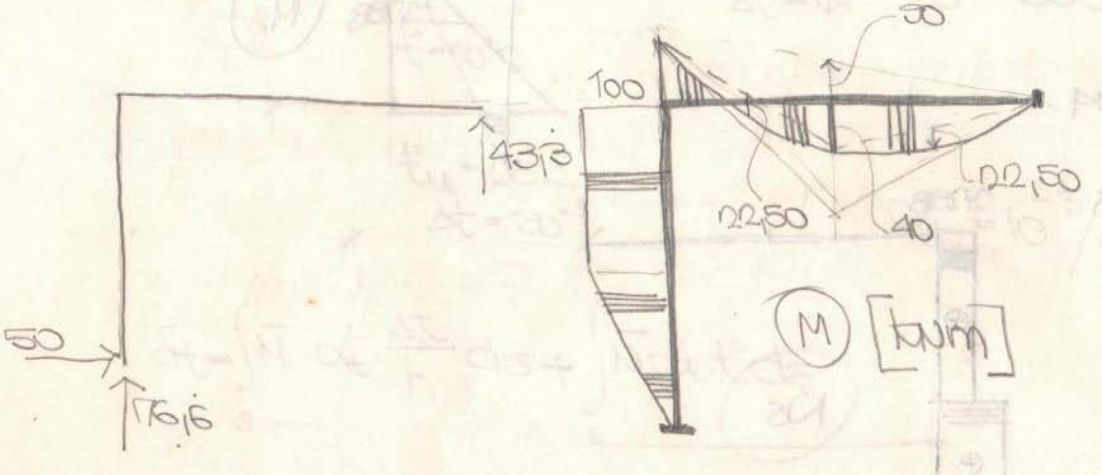
ŠTAP	b/h [m]	J (m⁴)
a–c	0,3/0,4	0,0016
c–b	0,3/0,5	0,003125

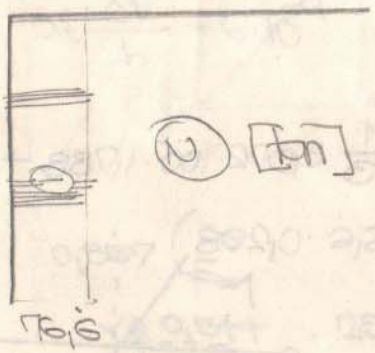
$E = 2 \cdot 10^7\ kN/m^2$

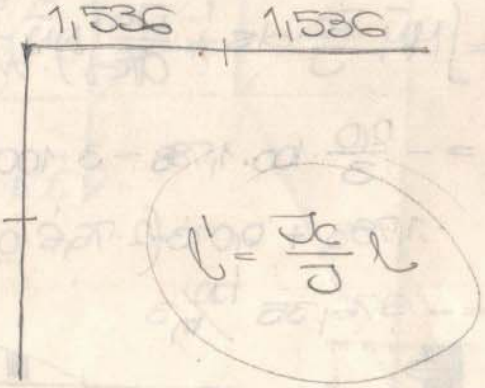
F (m²)
0,12
0,15

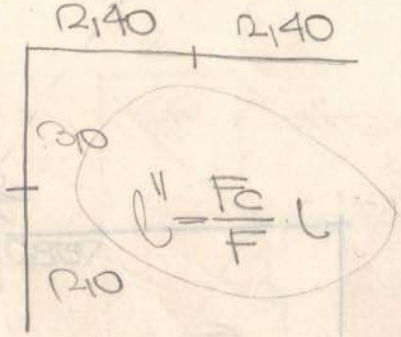
$F_c = 0{,}12\ m^2$ $\quad J_c = 0{,}0016\ m^4$ $\quad \frac{J_c}{F_c} = 0{,}0133\ m^2$

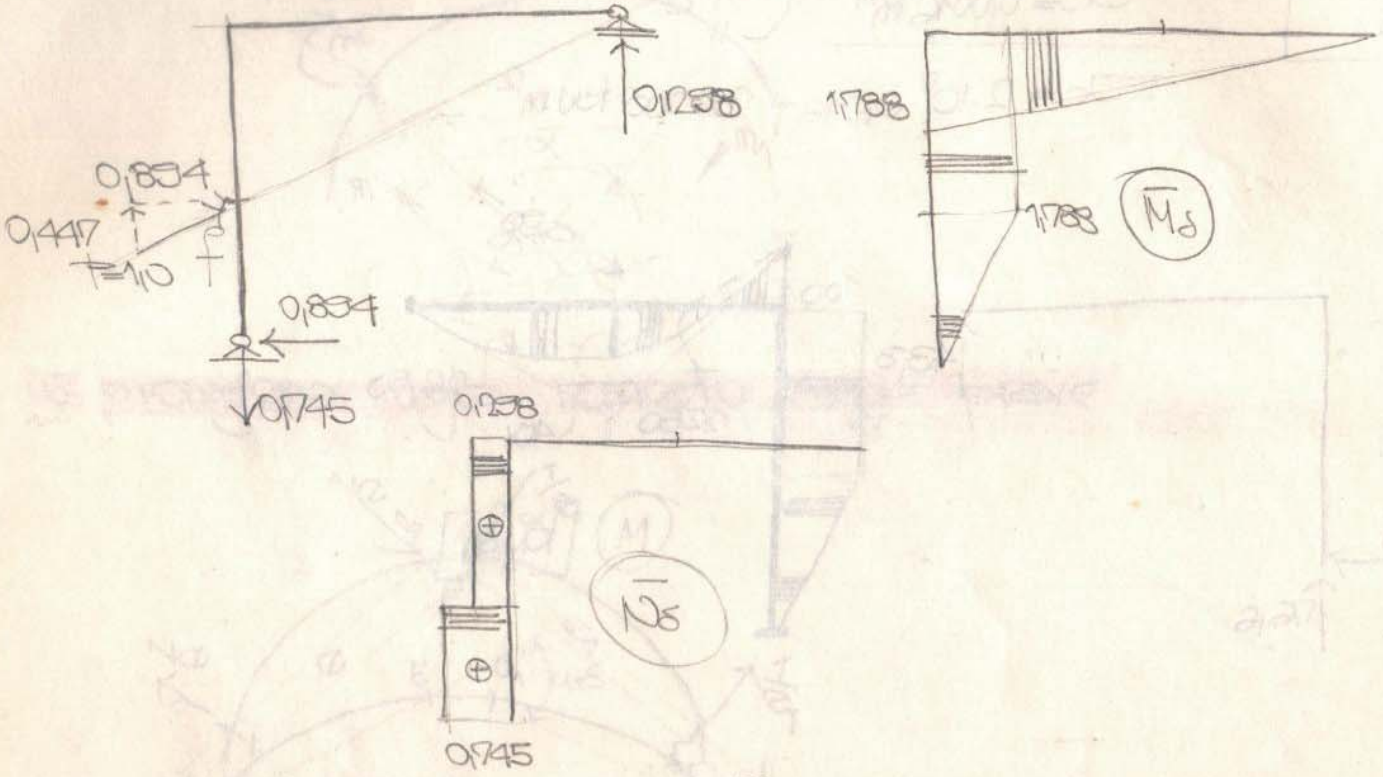
$EJ_c = 2 \cdot 10^7 \cdot 0{,}016 = 32000\ kNm^2$











$$EJ_c\delta = \int M\bar{M}\frac{J_c}{J}ds + \frac{J_c}{F_c}\int N\bar{N}\frac{F_c}{F}ds$$

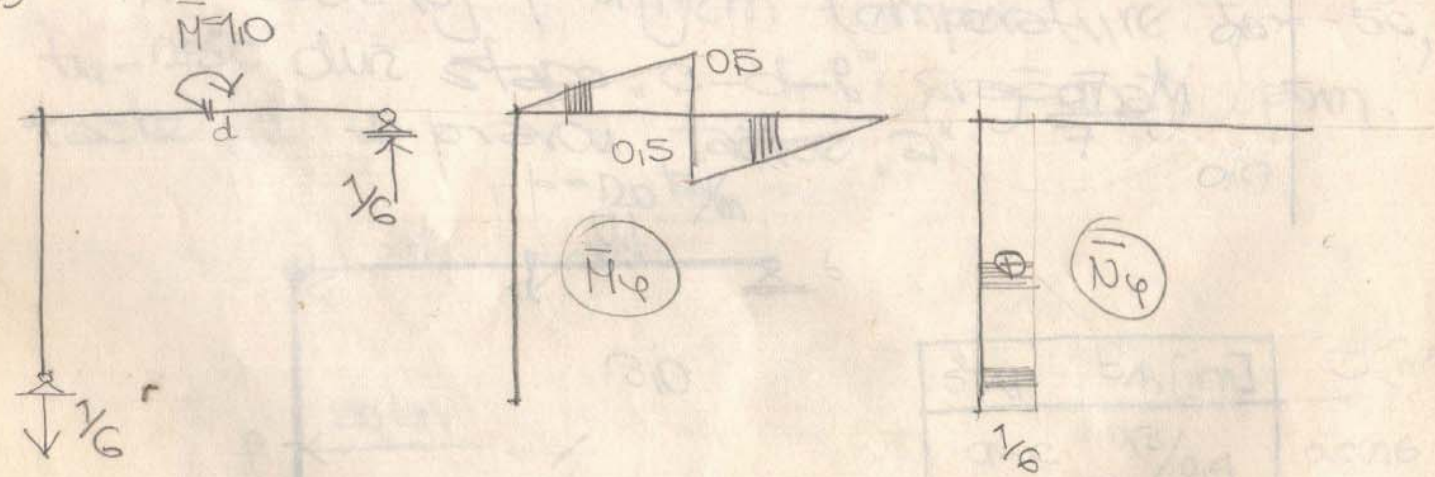
$$EJ_c\cdot\delta = -\frac{2,0}{3}\cdot 100\cdot 1,788 - 3\cdot 100\cdot 1,788 - \frac{1}{3}3,072\cdot 100\cdot 1,788 + \frac{1}{3}3,072\cdot 30\cdot$$

$$\cdot 1,788 + 0,013(2\cdot 76,6\cdot 0,1745 - 3\cdot 76,6\cdot 0,1298)$$

$$EJ_c\cdot\delta = -676,135\ tonm^3$$

$$\delta = -0,021\ m = -2,1\ cm$$

b)

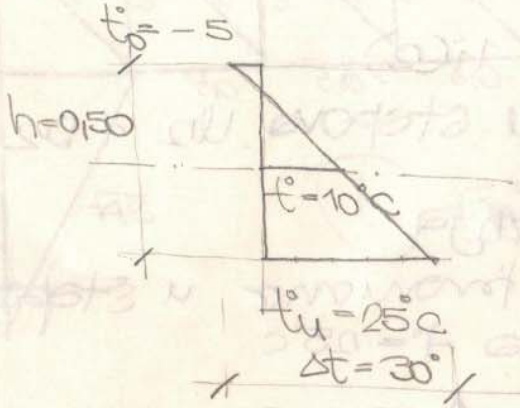


$$EJ_c\varphi = -\frac{1}{6}1,536\cdot 0,50(2\cdot 40 - 100) - \frac{1}{3}1,536\cdot 0,50\cdot 22,50 + \frac{1}{3}1,536\cdot 40\cdot 0,50 -$$

$$+\frac{1}{3}1,536\cdot 22,50\cdot 0,50 + 0,013\left(-50\cdot 76,6\cdot\frac{1}{6}\right) = 101,55\ tonm2$$

$\varphi = 0{,}0032$ rad.

(12.)

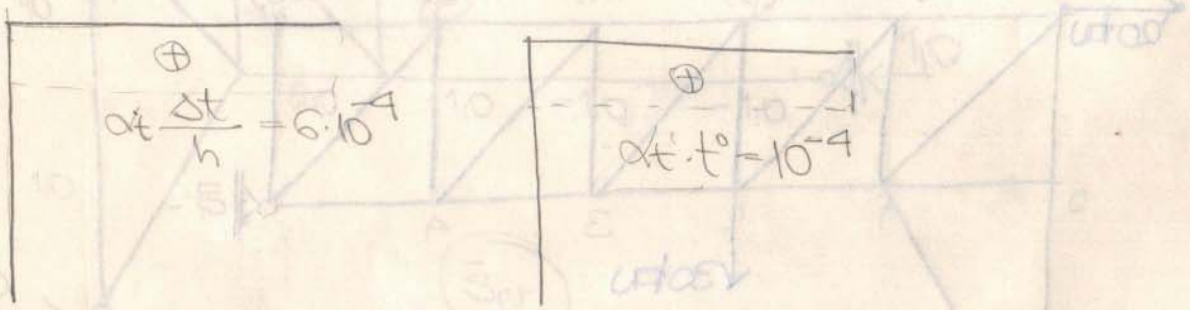


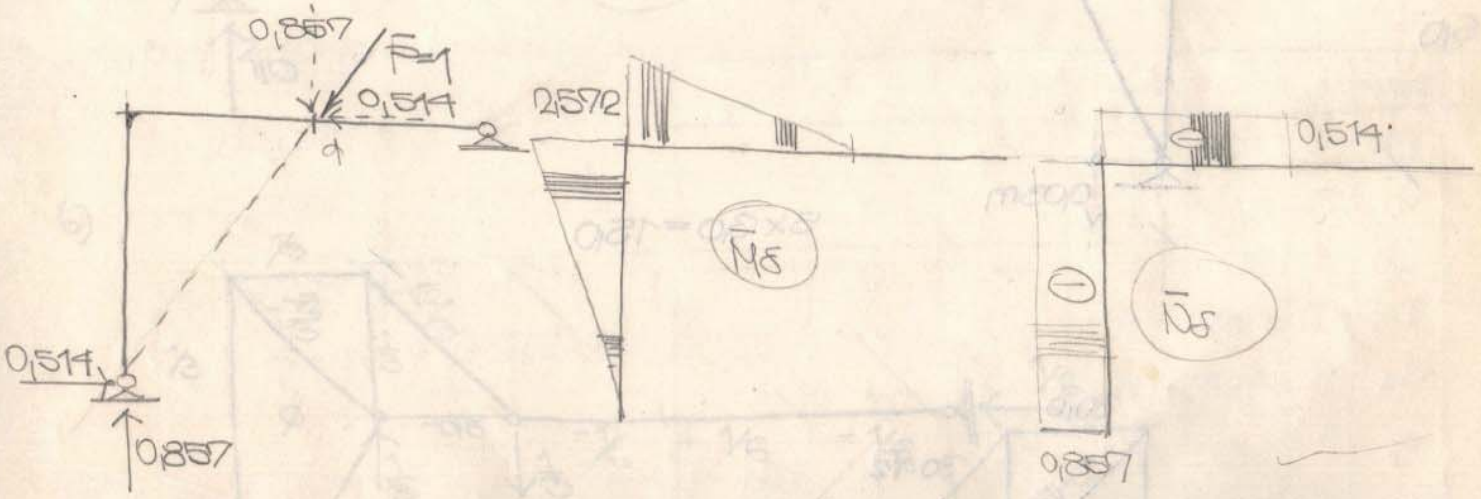
$$t° = \frac{t_u + t_b}{2} = 10°C$$

$$\Delta t = t_u - t_b = 30°C$$

$\alpha_t = 10^{-5}/°C$ - za beton

$$\delta_t = \int_s \bar{M} \cdot \alpha_t \frac{\Delta t}{h} ds + \int_s \bar{N} \alpha_t \cdot t° ds$$



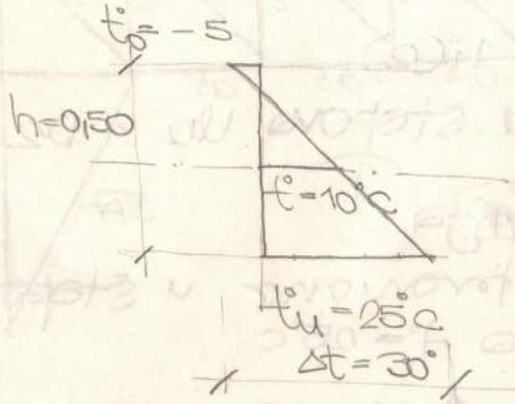


$$E_c \delta_t = \left(-\frac{1}{2} \cdot 3{,}0 \cdot 2{,}572 \cdot 6 \cdot 10^{-4} - 3 \cdot 0{,}514 \cdot 10^{-4}\right) \cdot E_c$$

$$\delta_t = -2{,}161 \cdot 10^{-3}\ m \rightarrow \delta = -2{,}16\ mm$$

$\varphi = 0{,}0032$ rad.

(2.)



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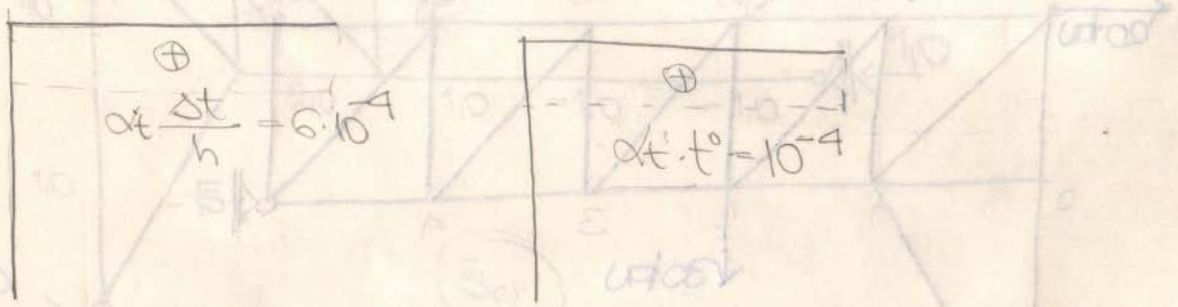
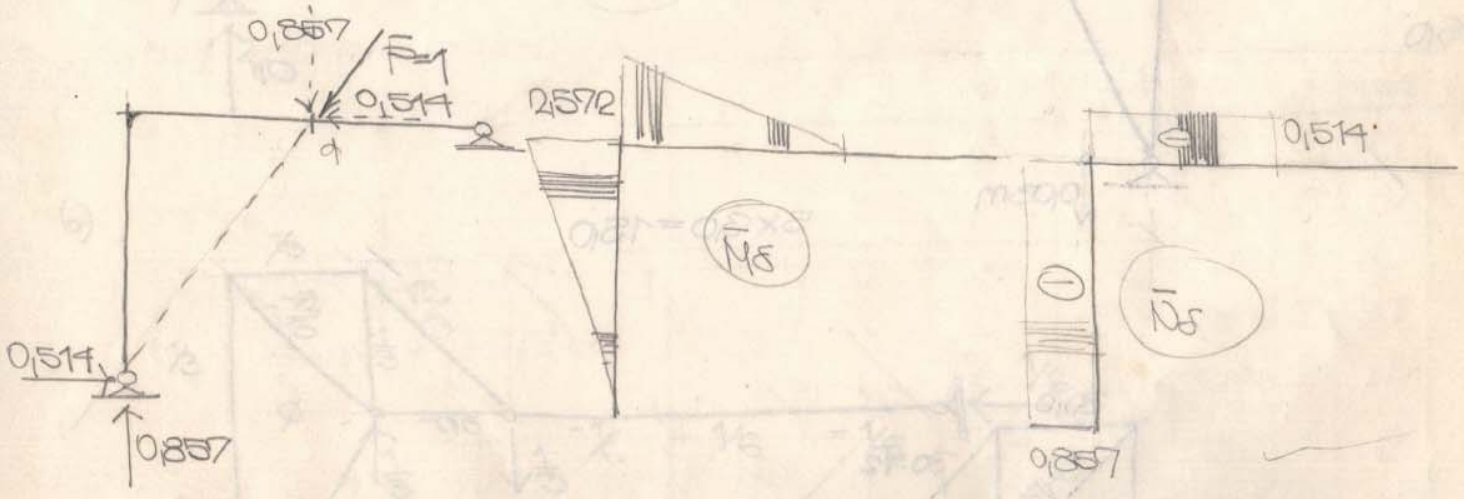




$$E J_c \delta_t = \left(-\frac{1}{2} \cdot 3{,}0 \cdot 2{,}572 \cdot 6 \cdot 10^{-4} - 3 \cdot 0{,}514 \cdot 10^{-4}\right) \cdot E J_c$$

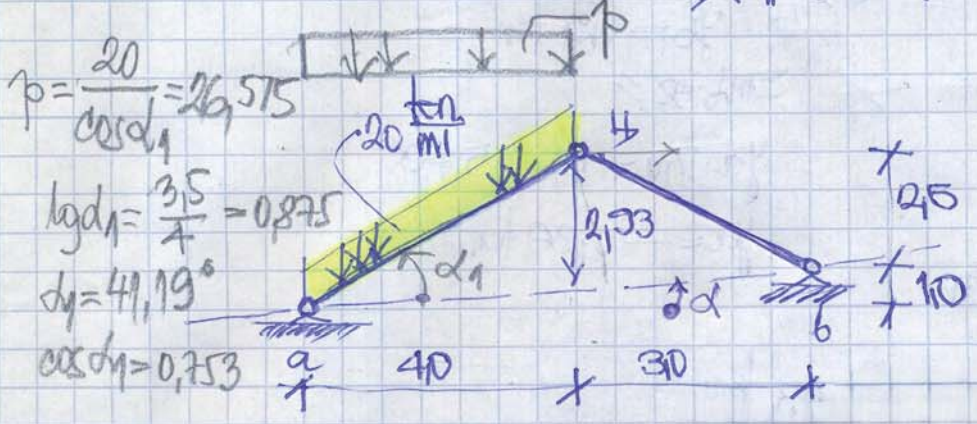
$$\delta_t = -2{,}161 \cdot 10^{-3} \text{ m} \rightarrow \delta = -2{,}16 \text{ mm}$$

ЗАДАЧА:

ЗА НОСАЧ НА СЛИКИ УСЛЕД ЗАДАТОГ ОПТЕРЕЋЕЊА ОДРЕДИТИ:

1° – ПРОМЕНУ УГЛА У „Ц"

2° – ХОРИЗОНТАЛНО ПОМЕРАЊЕ ЧВОРА „Ц" УСЛЕД ВЕРТИКАЛНОГ ПОМЕРАЊА ОСЛОНЦА „а" ЗА 0,01 m



$p = \frac{20}{\cos\alpha_1} = 26,575$

$\operatorname{tg}\alpha_1 = \frac{3,5}{4} = 0,875$

$\alpha_1 = 41,19°$

$\cos\alpha_1 = 0,753$

$E = 2 \cdot 10^7$

$J = 0,0072\ m$

$\operatorname{tg}\alpha = \frac{1}{7} = 0,14285 = 0,14$

$\alpha = 8,13°$

$\sum M_a = 0 \Rightarrow y_b \cdot 7,0 - 106,30 \cdot 2,0 = 0 \Rightarrow y_b = 30,37$ t

$\sum M_b = 0 \Rightarrow -y_a \cdot 7,0 + 106,30 \cdot 5,0 = 0 \Rightarrow y_a = 75,93$ t

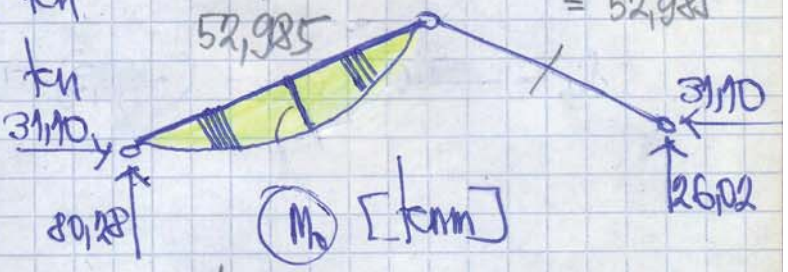
$H_a = \frac{1}{2,93}(75,93 \cdot 4,0 - 106,30 \cdot 2,0) \Rightarrow H_a = 31,10$ t

$H_b = \frac{1}{2,93}(30,37 \cdot 3,0) \Rightarrow H_b = 31,10$ t

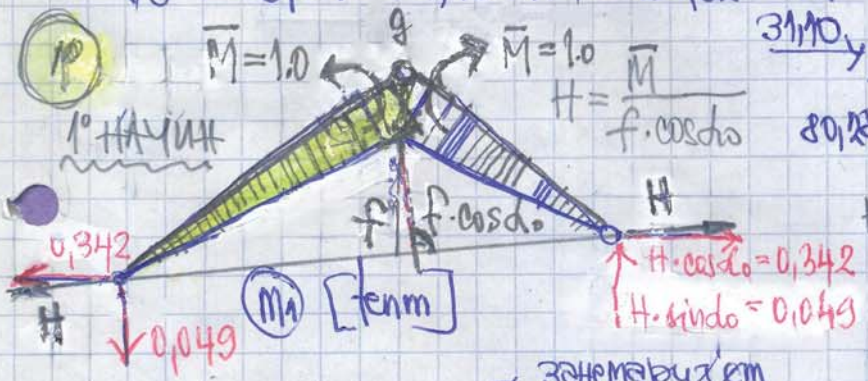
$V_a = 75,93 + 31,10 \cdot 0,14 = 80,28$ t

$V_B = 30,37 - 31,10 \cdot 0,14 = 26,02$ t

(p) $M = 80,28 \cdot 2 - 31,1 \cdot 0,5 \cdot 3,5 - 26,575 \cdot 2 \cdot 1 =$
$= 52,985$



1° НАЧИН



$H = \frac{\bar{M}}{f \cdot \cos\alpha_0}$

$H = \frac{1}{2,93 \cdot 0,9899} = 0,345$ t/m

$EI \cdot \delta_{11} = \int_S \frac{M_1 M_0}{EJ} ds + \int_S \frac{N_1 N_0}{EF} ds + \int_S \frac{T_1 T_0}{GF} ds$ (занемарујем)

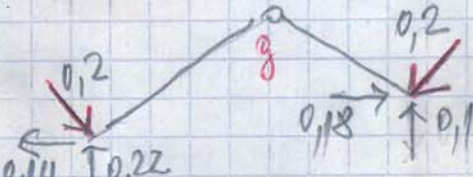
$EI \cdot \delta_{11} = -\frac{1}{3} \cdot 1 \cdot 52,985 \cdot 5 + 0 = 88,417$

$\delta_{11} = \frac{88,417}{2 \cdot 10^7 \cdot 0,0072}$

$\delta_{11} = 0,000614$ rad.

→ ПРОВЕРА СА 2° НАЧИНОМ.

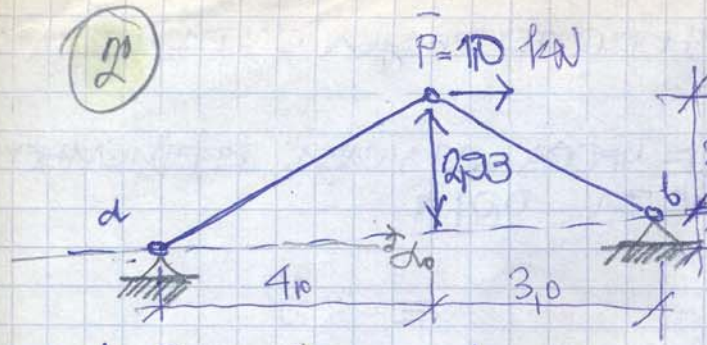
2° НАЧИН



$EI\,\delta_{11} = \frac{1}{3} \cdot 1 \cdot 52,985 \cdot 5 + 0 = 88,417$

$\delta_{11} = 0,000614$ rad.

2)



$\Sigma M_a = 0 =$

$y_b \cdot 7,0 - 1,0 \cdot 3,5 = 0$

$y_b = 0,5$ kN

$\Sigma M_b = 0 =$

$y_a \cdot 7,0 + 1,0 \cdot 2,5 = 0$

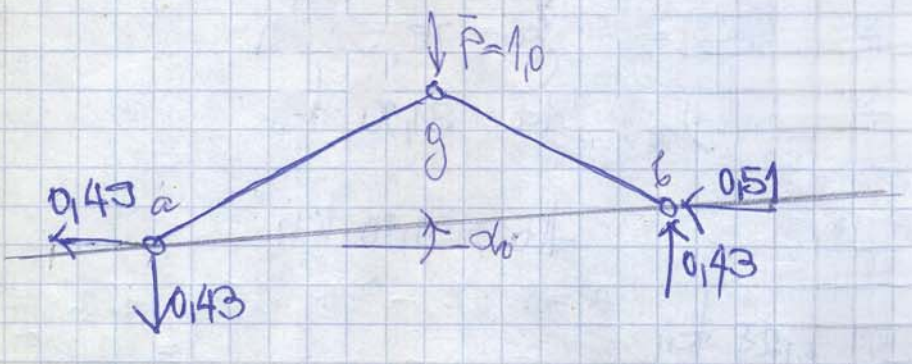
$y_a = -0,36$ kN

$H_b = \frac{1}{2,93}(0,5 \cdot 3,0) = 0,51$ kN

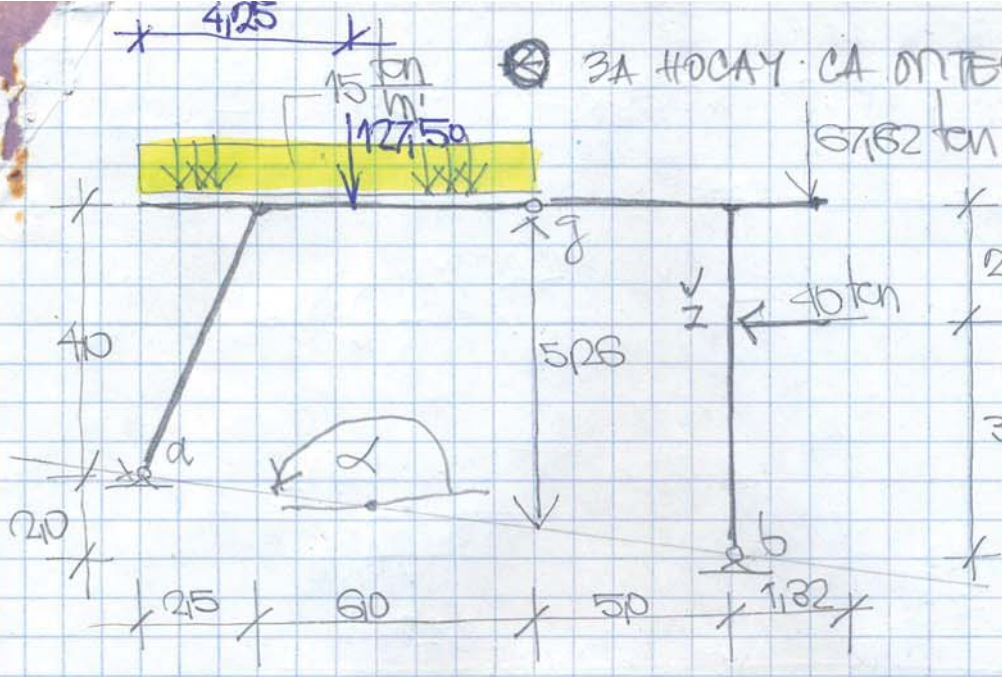
$H_a = \frac{1}{2,93}(-0,36 \cdot 4,0) = -0,49$ kN

$y_a = -0,36 + (-0,49) \cdot 0,14 = -0,43$ kN

$V_b = 0,5 - 0,51 \cdot 0,14 = 0,43$



$\delta_y = -\Sigma \bar{c}_i \cdot c_i = -(-0,43) \cdot 0,01 = \underline{0,0043 \text{ m.} = 4,3 \text{ mm}}$



За носач са оптерећењем на скици

1° Израчунати и накртати дијаграме пресечних сила.

2° Обртање пресека у чвору „2".

$E = 2 \cdot 10^7 \ kN/m^2$

$b/h = 0,2/0,4 \ m.$

$\Sigma M_a = 0:$ $\quad y_b \cdot 13,5 + 40 \cdot 1,8 - 67,62 \cdot 14,82 - 127,5 \cdot 4,25 = 0$

$$y_b = \frac{-40 \cdot 1,8 + 67,62 \cdot 14,82 + 127 \cdot 4,25}{13,5}$$

$y_b = 108,71 \ kn$

$\Sigma M_b = 0:$ $\quad -y_a \cdot 13,5 + 127,5 \cdot 9,25 + 40 \cdot 3,8 - 67,62 \cdot 1,32$

$$y_a = \frac{127,5 \cdot 9,25 + 40 \cdot 3,8 - 67,62 \cdot 1,32}{13,5}$$

$y_a = 92,00 \ kn.$

$\Sigma M_3^l = 0:$ $\quad -y_a \cdot 8,5 + 127,5 \cdot 4,25 + H_a \cdot 5,26 = 0$

$$H_a = \frac{92,0 \cdot 8,5 - 127,5 \cdot 4,25}{5,26}$$

$H_a = 45,65 \ kn$

$\Sigma M_5^d = 0:$ $\quad H_b \cdot 5,26 - y_b \cdot 5,0 + 40 \cdot 2,2 + 67,62 \cdot 6,32 = 0$

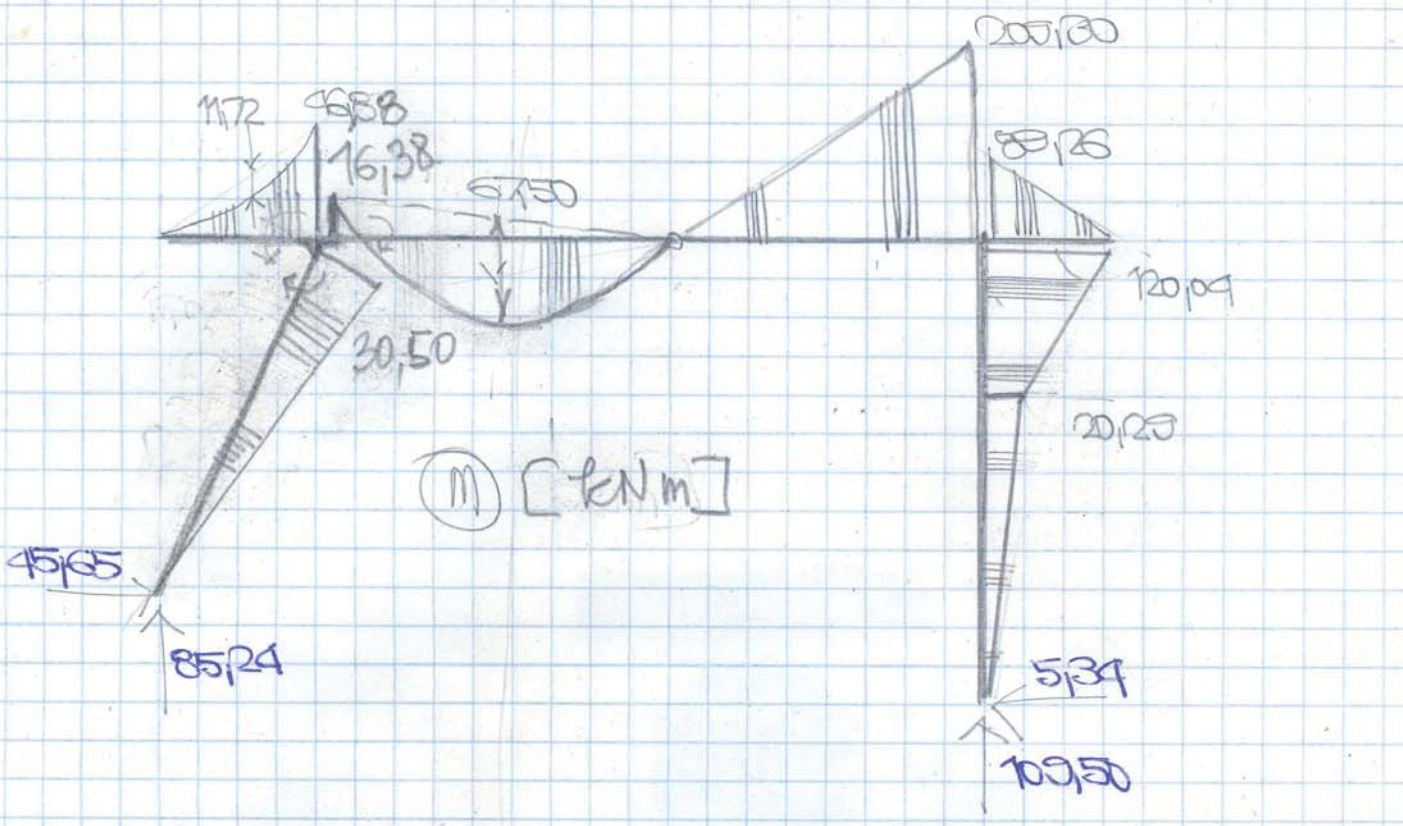
$$H_b = \frac{108,71 \cdot 5,0 - 40 \cdot 2,2 - 67,62 \cdot 6,32}{5,26}$$

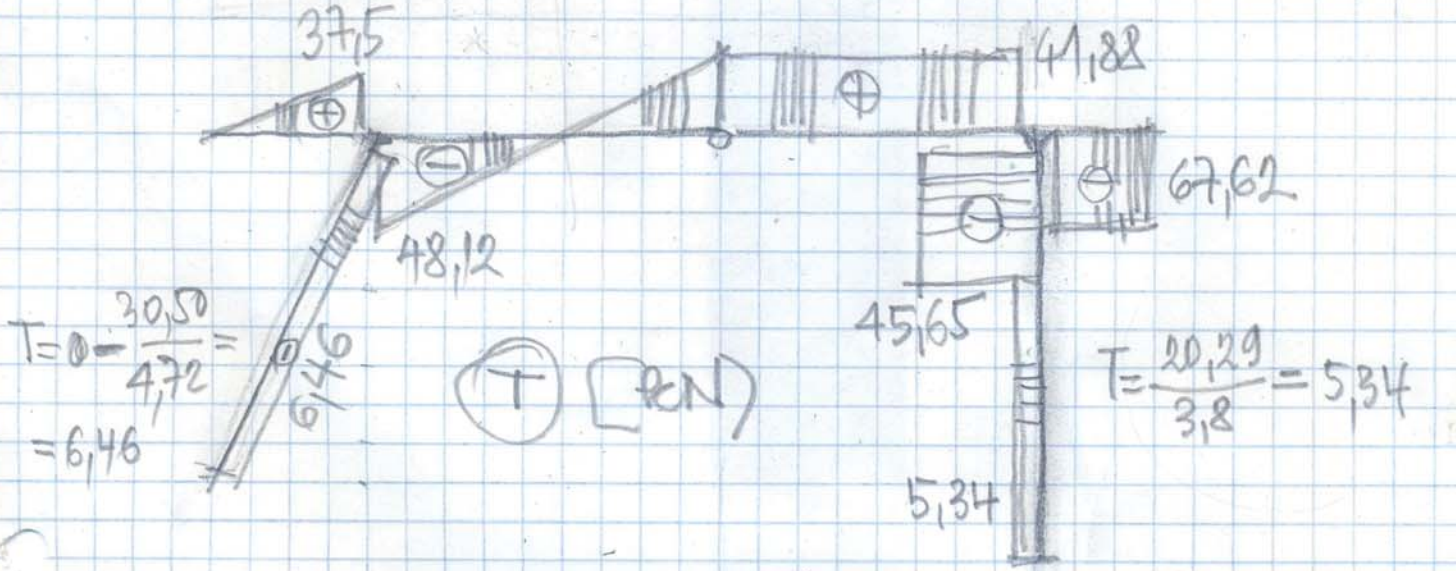
$H_b = 5,34 \ kn$

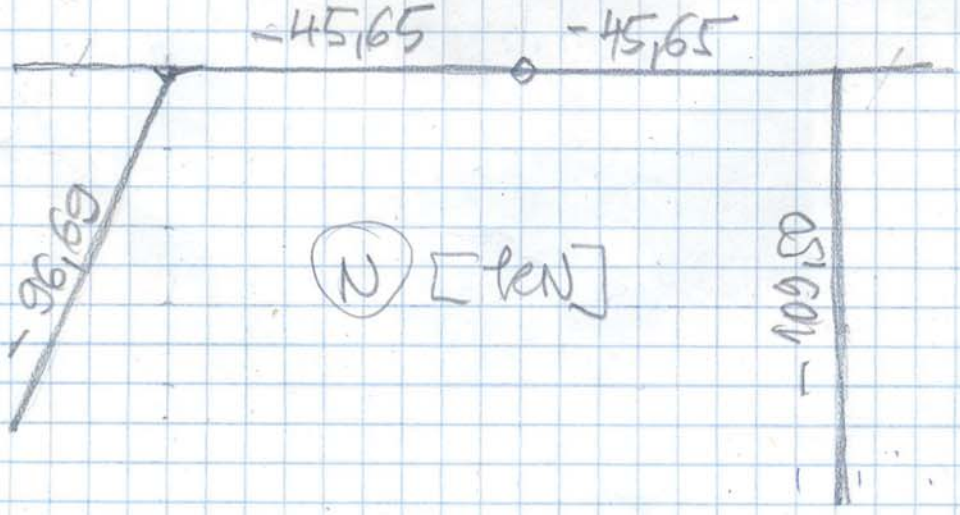
$\operatorname{tg}\alpha_b = -0,148$

$A = 92,00 + 45,65(-0,148) = 85,24 \ kn$

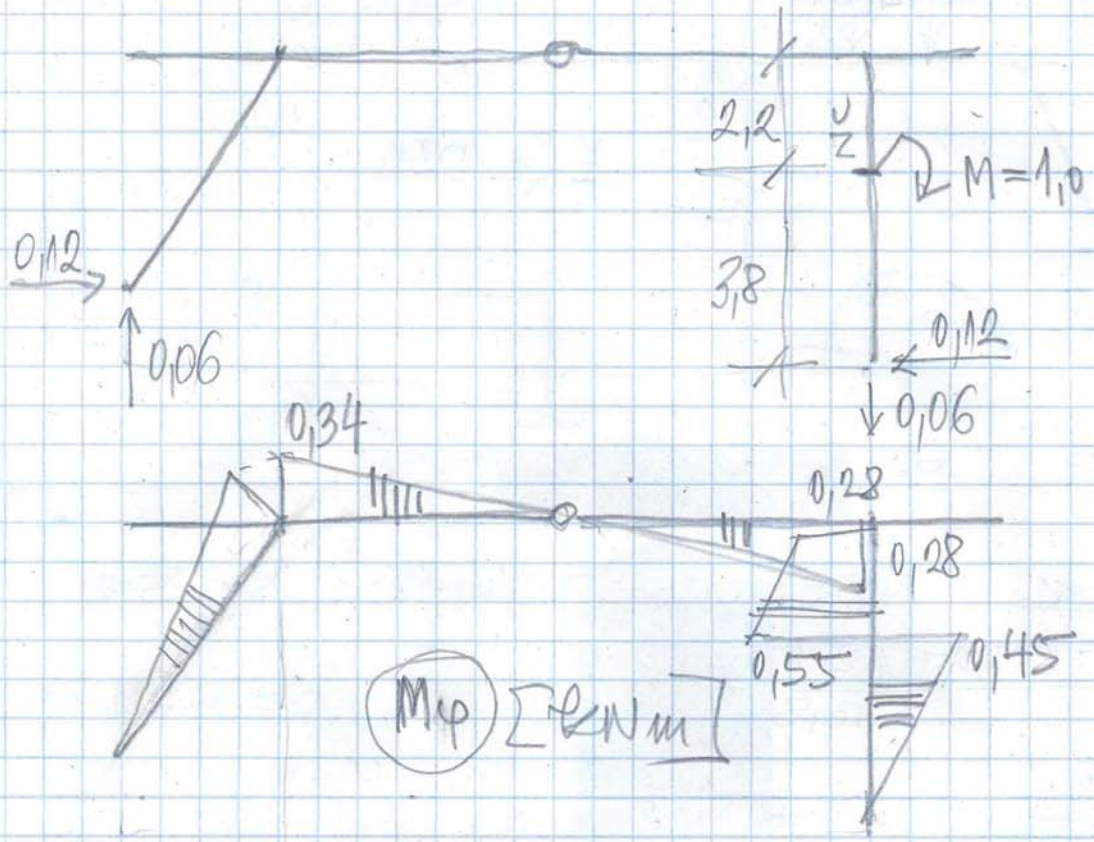
$B = 108,71 + 5,34 \cdot 0,148 = 109,50 \ kn.$


11,72
16,38
9,150
30,50
45,65
85,24
200,00
88,26
120,04
20,29
5,34
109,50
M [kN m]


37,5
41,88
48,12
67,62
45,65
5,34
T=0-30,50/4,72=
=6,46
6,46
T=20,29/3,8=5,34
T [kN]


-45,65
-45,65
-96,69
-109,03
N [kN]

*ОБРТАЊЕ ПОПРЕЧНОГ ПРЕСЕКА У ЧВОРУ „2"



$$EI\delta_\varphi = \int_S M \cdot M_\varphi \, ds =$$

$$= -\frac{1}{3} 30,5 \cdot 0,34 \cdot 4,72 +$$

$$+ \frac{1}{3} 0,34 \cdot 16,38 \cdot 6 - \frac{1}{3} \cdot 0,34 \cdot 67,5 \cdot 6 -$$

$$- \frac{1}{3} 209,30 \cdot 0,28 \cdot 5 =$$

$$- \frac{1}{6} \left[0,55 \cdot (2 \cdot 20,29 + 120,04) + 0,28 (20,29 + 2 \cdot 120,04) \cdot 2,2 + \right.$$

$$\left. + \frac{1}{3} 0,45 \cdot 20,29 \cdot 3,8 = -196,308 \right.$$

$$EI\delta_\varphi = -196,308$$

$$\delta_\varphi = -\frac{196,308}{3 \cdot 10^7 \cdot \frac{0,2 \cdot 0,4^3}{12}} = -\frac{196,308}{3,2 \cdot 10^4} =$$

$$\delta_\varphi = -0,006135 \text{ rad.}$$

ZADATAK: Za rešetku na slici sračunati

a) vertikalno pom. čvora (2)

b) dobanje štapa U2

c) razmicanje čvorova 1i(2)

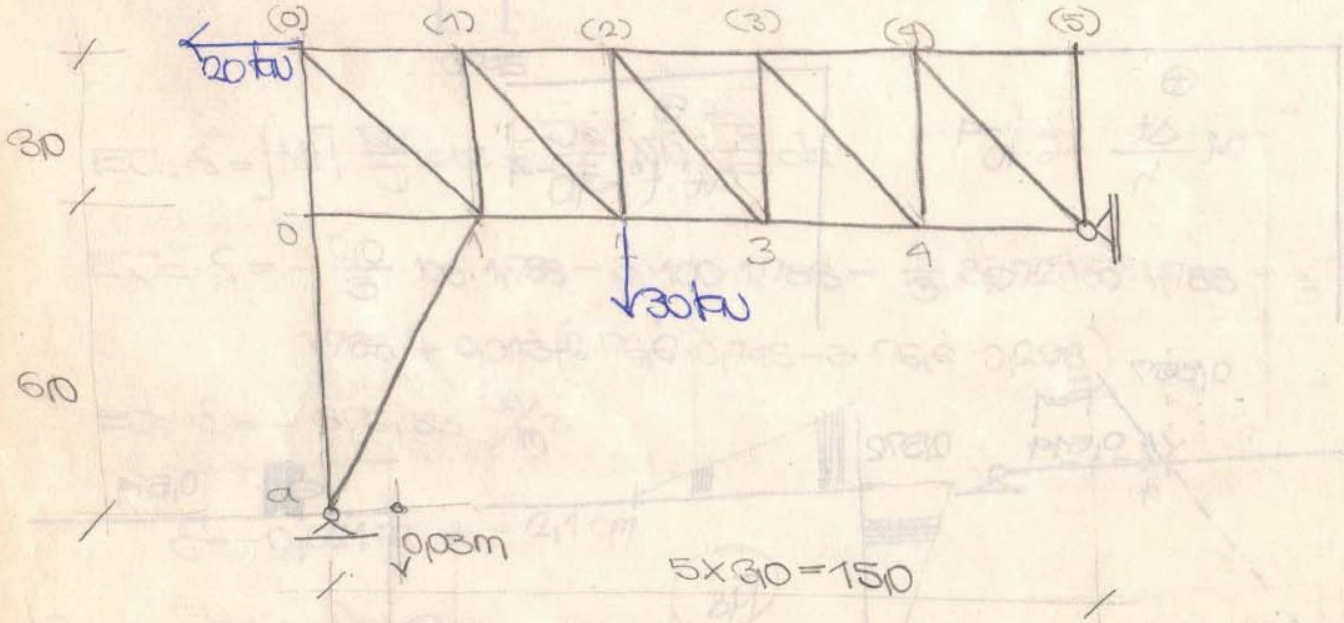
d) promena ugla između štapova U2 i D2

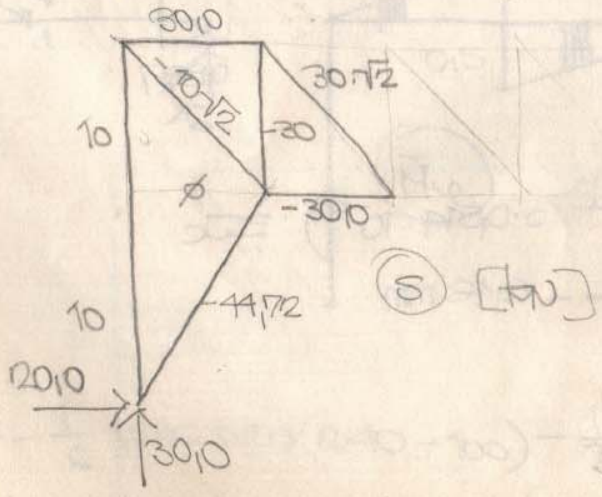
usled

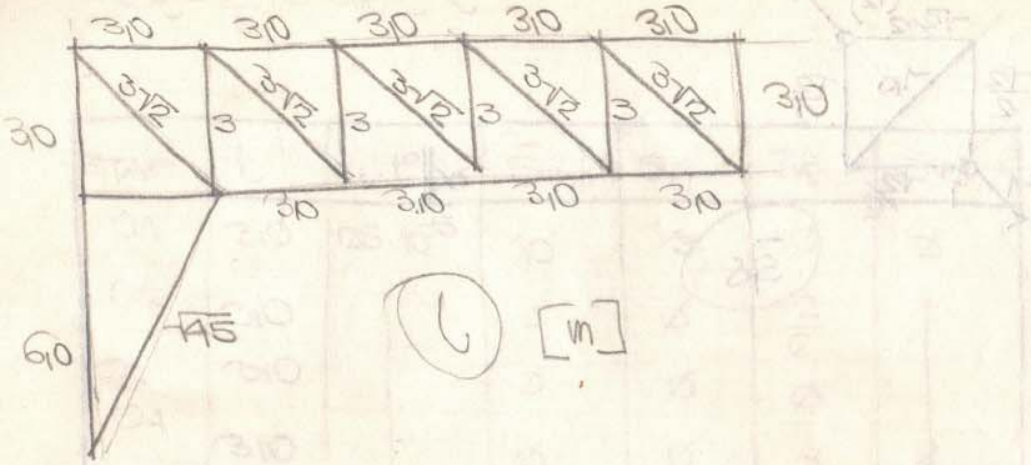
A - datog opterećenja

B - temperaturne promene u štapovima donjeg pojasa $t° = 25°C$

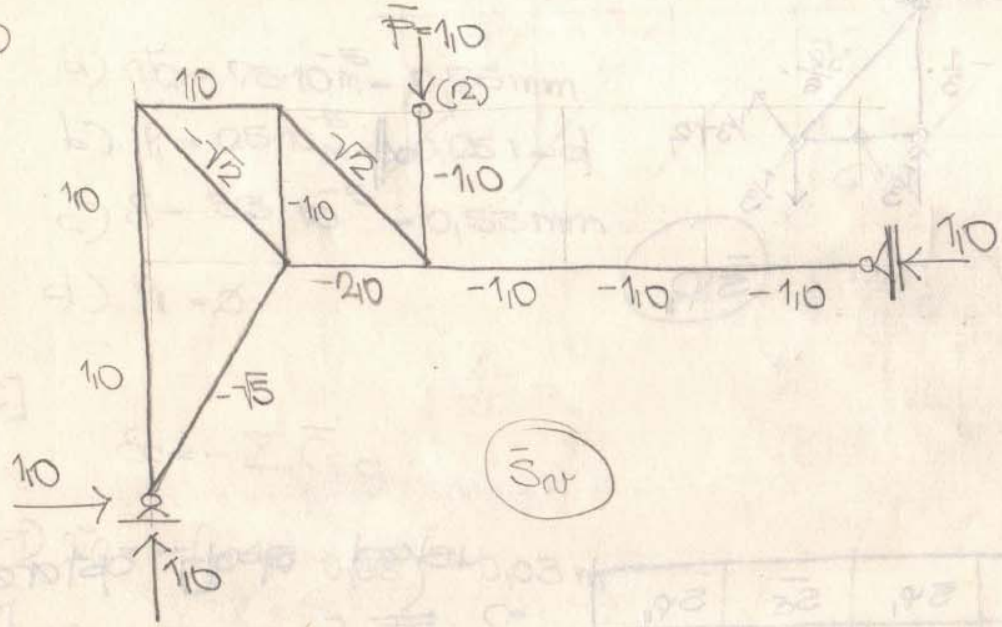
C - pom. oslonca A za 0,03m.



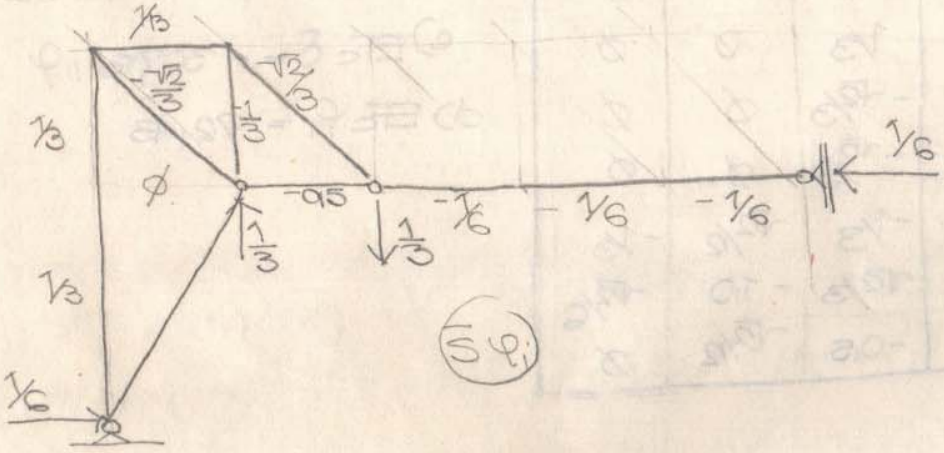



3,0
3√2
3
30
60
√45
[m]

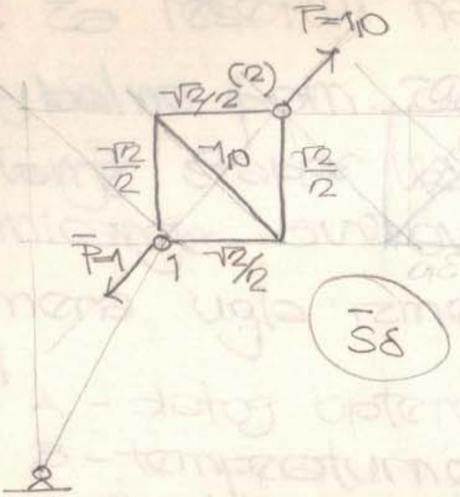
a)


F̄=1,0
(2)
1,0
-√2
√2
-1,0
-2,0
-√5
$\bar{S}_{2v}$

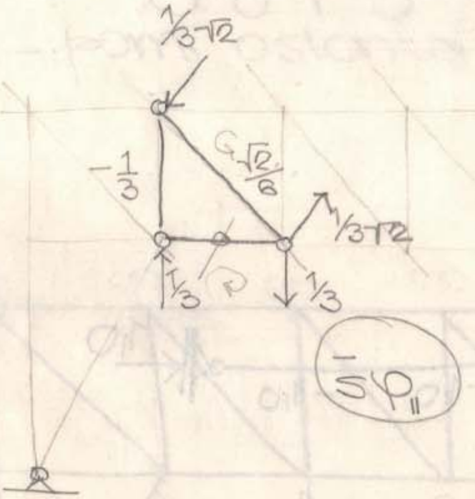
b)


1/3
-√2/3
√2/3
-1/3
-0,5
1/6
$\bar{S}_{\varphi_i}$

c)



d)



A]

STAP	l	S	$\bar{S}v$	$\bar{S}\varphi_1$	$\bar{S}\delta$	$\bar{S}\varphi_{II}$
Va	6	10	1	1/3	∅	∅
V0	3	10	1	1/3	∅	∅
O1	3	30	1	1/3	∅	∅
D1	$3\sqrt{2}$	$-10\sqrt{2}$	$-\sqrt{2}$	$-\sqrt{2}/3$	∅	∅
U1	3	$-44,72$	$-\sqrt{5}$	$-\sqrt{2}/6$	∅	∅
V1	3	-30	-1	$-1/3$	$\sqrt{2}/2$	$-1/3$
D2	$3\sqrt{2}$	$-30\sqrt{2}$	$\sqrt{2}$	$\sqrt{2}/3$	$-1,0$	$\sqrt{2}/6$
U2	3	-30	-2	$-0,5$	$-\sqrt{2}/2$	∅
EFcδ						

usled spolj. opterećenja,

a) $EF_c\delta = 1480,20$

b) $EF_c\varphi_1 = 359,94$

c) $EF_c\delta = -307,3$

d) $EF_c\varphi_{II} = 72,43$

B] $\delta_t = \sum_s \bar{S} \cdot \alpha_t \cdot t^\circ \cdot l$

STAP	l	$\alpha_t \cdot t^\circ$	$\bar{S}_V$	S_{φ_I}	$\bar{S}_S$	$S_{\varphi_{II}}$
01	310	$125 \cdot 10^{-5}$	1/0	1/3	$\emptyset$	$\emptyset$
02	310	↓	$\emptyset$	$\emptyset$	$\frac{\sqrt{2}}{2}$	↓
03	310		$\emptyset$	$\emptyset$	$\emptyset$	
04	310		$\emptyset$	$\emptyset$	$\emptyset$	
05	310		$\emptyset$	$\emptyset$	$\emptyset$	

a) $v_2 = 75 \cdot 10^{-5} m = 0{,}75 mm$

b) $\varphi_I = 25 \cdot 10^{-5} m - 0{,}25 rad$

c) $\delta = 53 \cdot 10^{-5} - 0{,}53 mm$

d) $\varphi_{II} = \emptyset$

C]

$$\delta_o = -\sum \bar{C}_i \, a_i$$

a) $v_2 = -(-1/0 \cdot 0{,}03) = 0{,}03 m$

b) $\varphi_I = \emptyset$

c) $\delta = \emptyset$

d) $\varphi_{II} = \emptyset$