

Optimal allocation of attention in user-generated content platforms

Iván Rendo Barreiro

Advisor: Alexandre de Cornière



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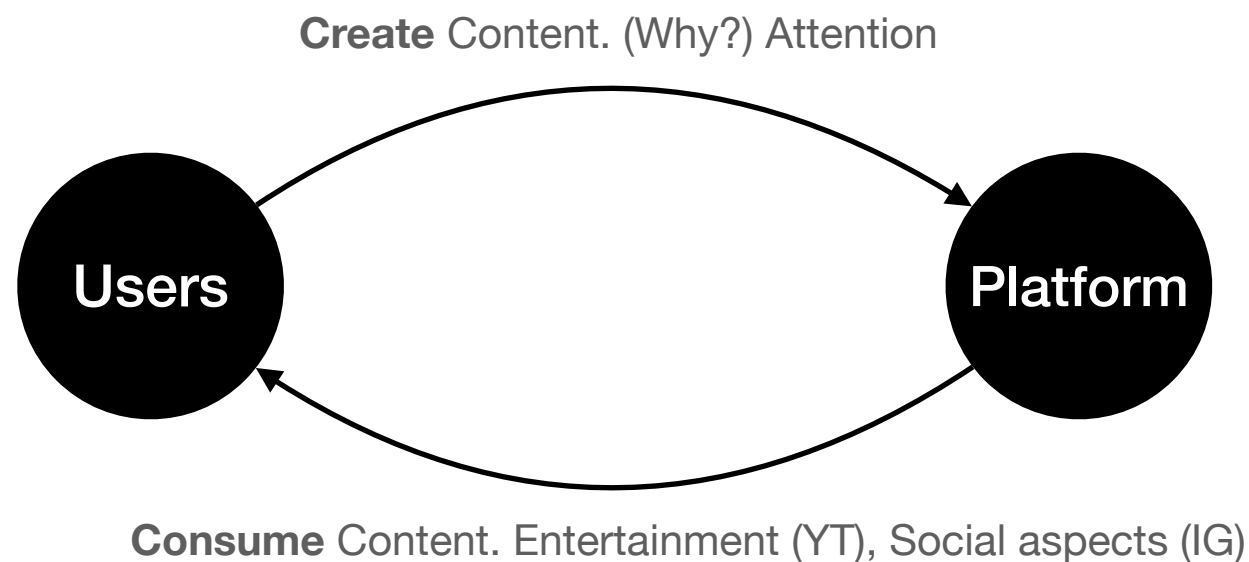
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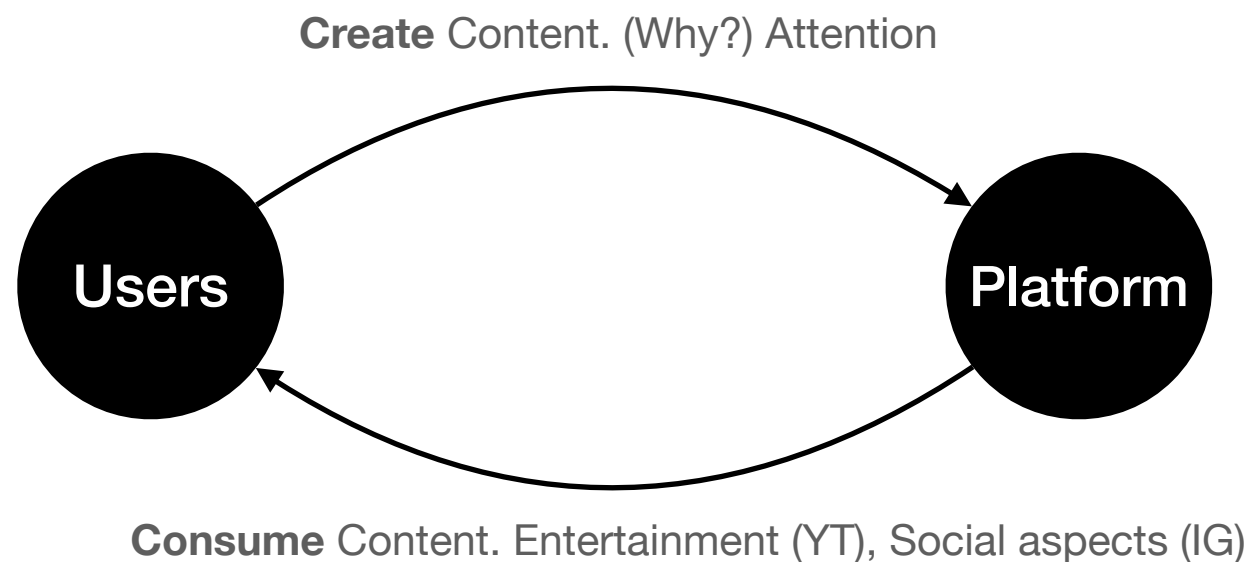
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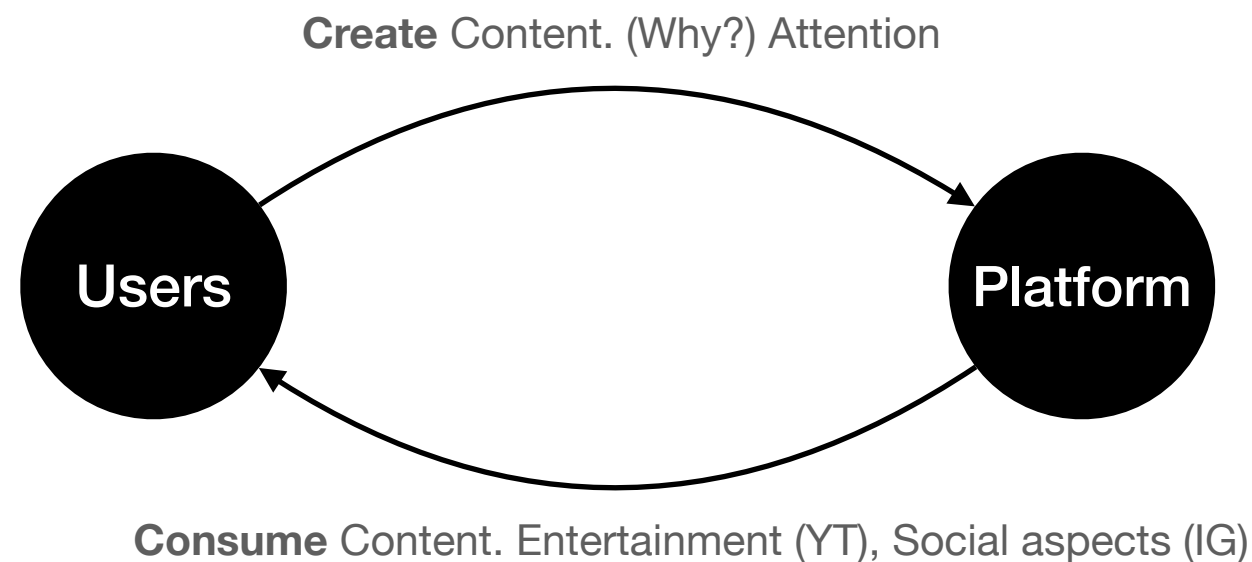


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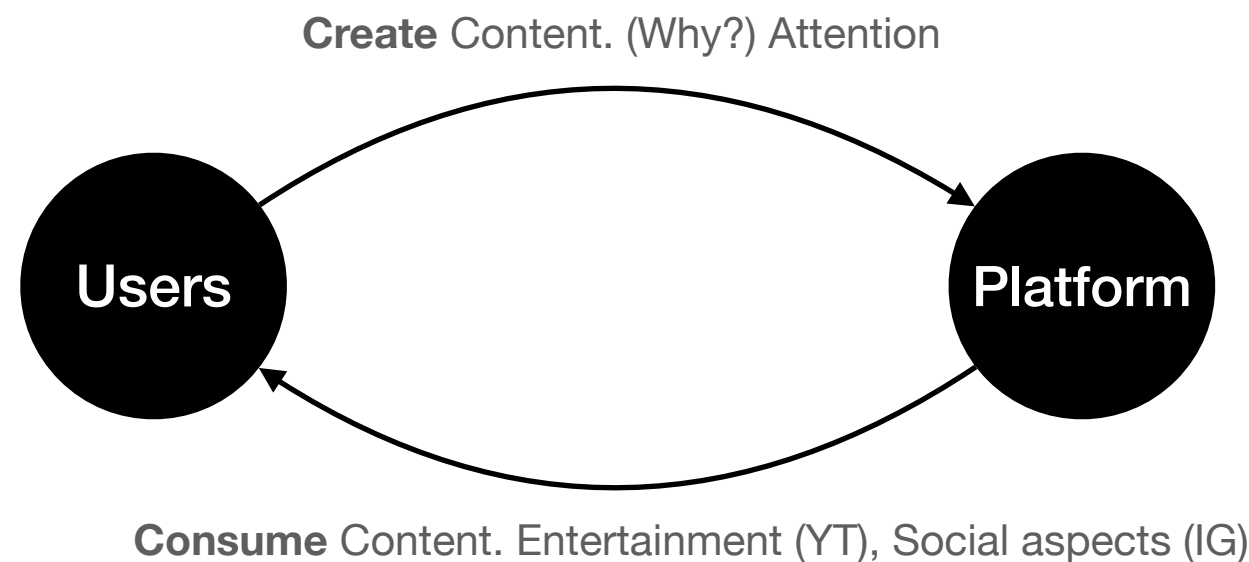


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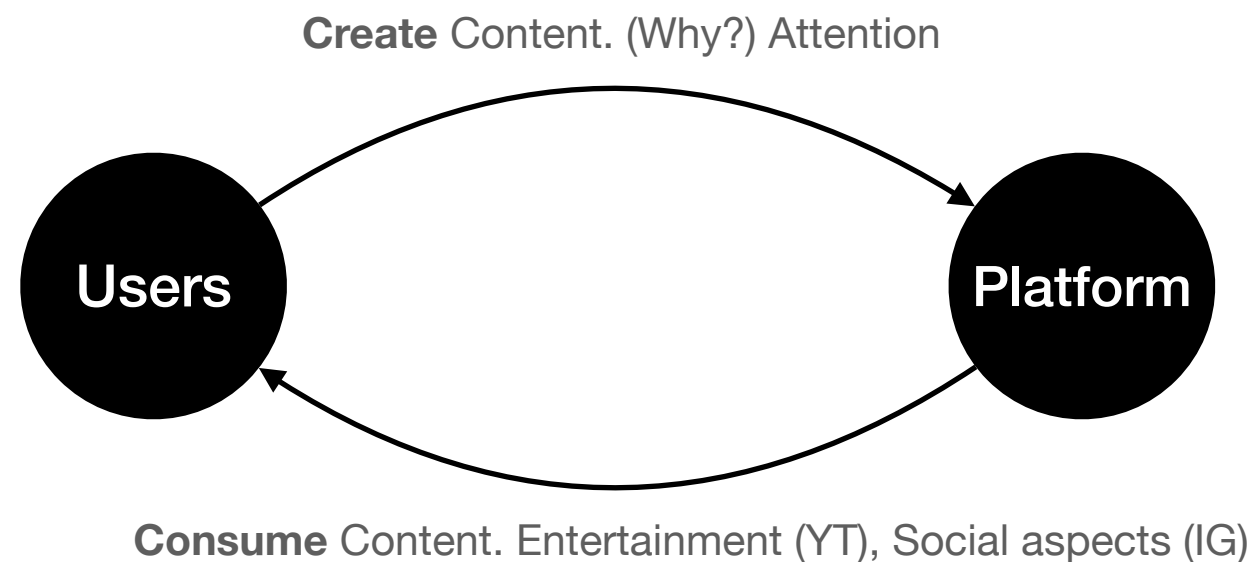


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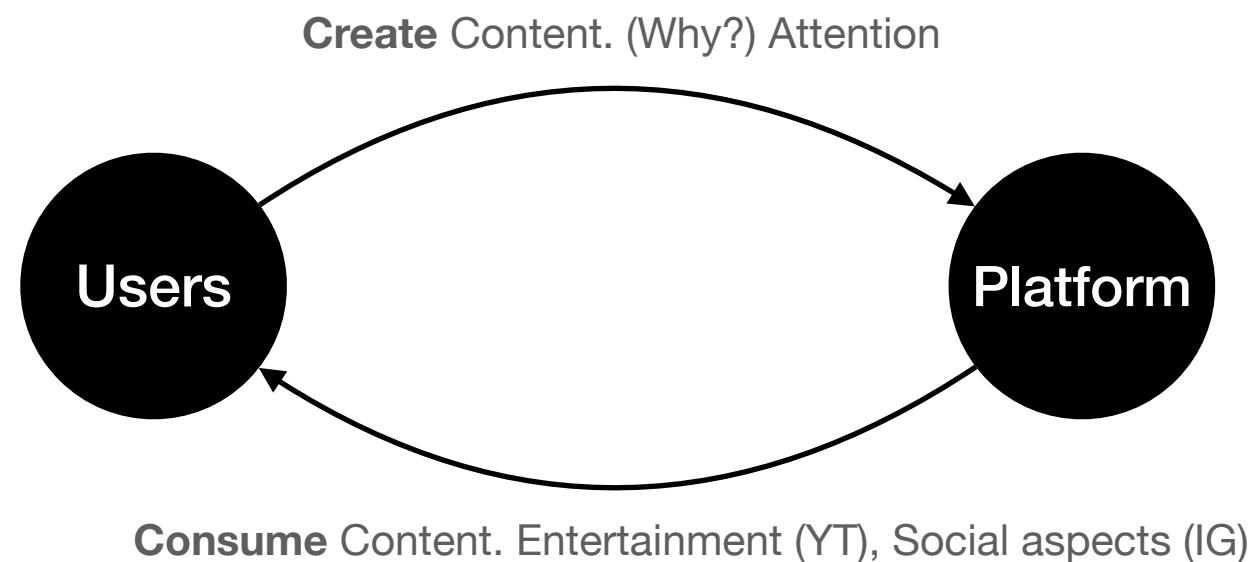


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 - E.g. Instagram (stories introduction), BeReal... <— “Low quality” content, attention more distributed

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Question to answer in this thesis: For a monopolist platform, which is the **best way to distribute attention** across users such that they are incentivised to create content in a way that maximises its utility (profit/sum of users utilities)?

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Social platforms (IG, Snapchat): users prefer to consume content from a lot of creators
VS Entertainment platforms (Youtube, Twitch)... where quality comes first

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2. **Utility** of any user in the platform **depends on the transfers** (attention) **paid to the rest** of users.

Outline

1. General Model (theoretical framework)
2. Binary Model (more results)
3. Ad-funded Platforms (application)

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 - Total attention is bounded: $\sum_{i=1}^N A_i \leq 1$.

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Creation utility Consumption utility

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- In the consumption utility, I use $A_j q_j$ and not just q_j because the relevant variable is the **perceived quality**. Otherwise, users derive utility from quality they are not paying attention to.

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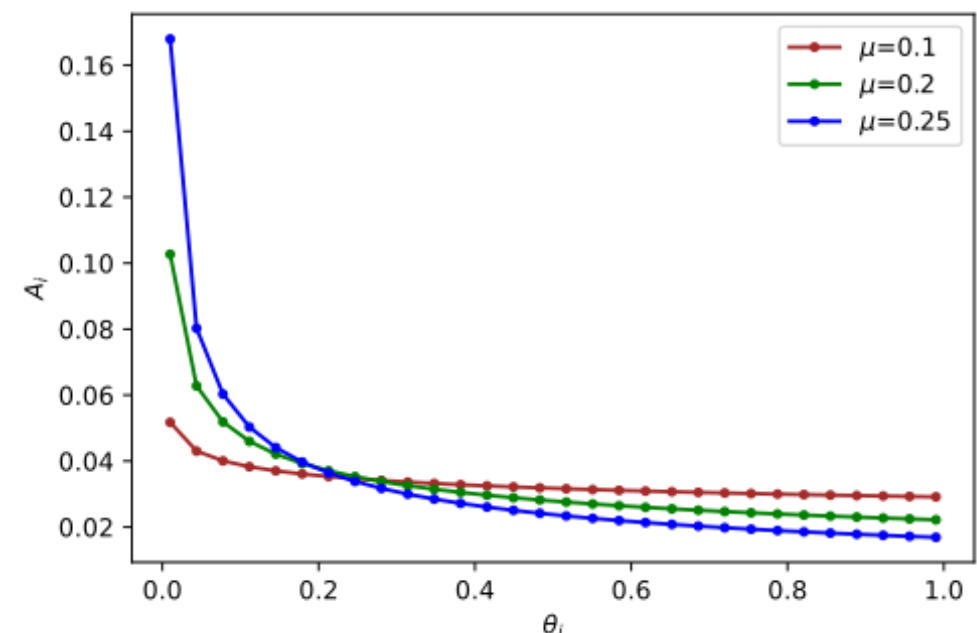
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- **Optimal attention shares and qualities:**

$$A_i^* = \frac{\theta_i^{\frac{\mu}{2\mu-1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu-1}}} \quad q_i^* = \frac{A_i^*}{\theta_i} = \frac{\theta_i^{\frac{1-\mu}{2\mu-1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu-1}}}$$

Example. $N = 30$ and equidistant costs.



Moreover...

- **Proposition 2:**
- In the First Best setting, the optimal attention allocation with respect to qualities follows a **Generalized Tullock Contest**:

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(more elegant and tractable seems to be the case of the continuum of agents explored minimally in Appendix B, but its study is left out of this thesis)

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Proposition 3:

Under standard assumptions, quality of the low-cost type is distorted

$$\exists \mu \in \left(0, \frac{1}{2}\right) : q_L(\mu)^{FB} \neq q_L(\mu)^{SB}$$

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$$\begin{aligned} \max_{A_L, A_H, q_L, q_H} \quad & N_L \left(A_L - q_L \theta_L + (N-1)(A_L q_L)^\mu \right) + N_H \left(A_H - q_H \theta_H + (N-1)(A_H q_H)^\mu \right) \quad \equiv \max_{\mathbf{A}, \mathbf{q}} \sum_{i=1}^N U_i \\ \text{s.t.} \quad & \begin{cases} A_L - q_L \theta_L \geq A_H - q_H \theta_L & (\text{IC}_L) \\ A_H - q_H \theta_H \geq 0 & (\text{IR}_H) \\ N_L A_L + N_H A_H \leq 1 & (\text{Feasibility 1}) \\ 0 \leq A_i \leq 1 & (\text{Feasibility 2}), i \in \{L, H\} \end{cases} \end{aligned}$$

Analytical solutions difficult to get! There is a numerical example next slide.

Proposition 3:

Under standard assumptions, quality of the low-cost type is distorted

$$\exists \mu \in \left(0, \frac{1}{2}\right) : q_L(\mu)^{FB} \neq q_L(\mu)^{SB}$$

Conjecture 1:

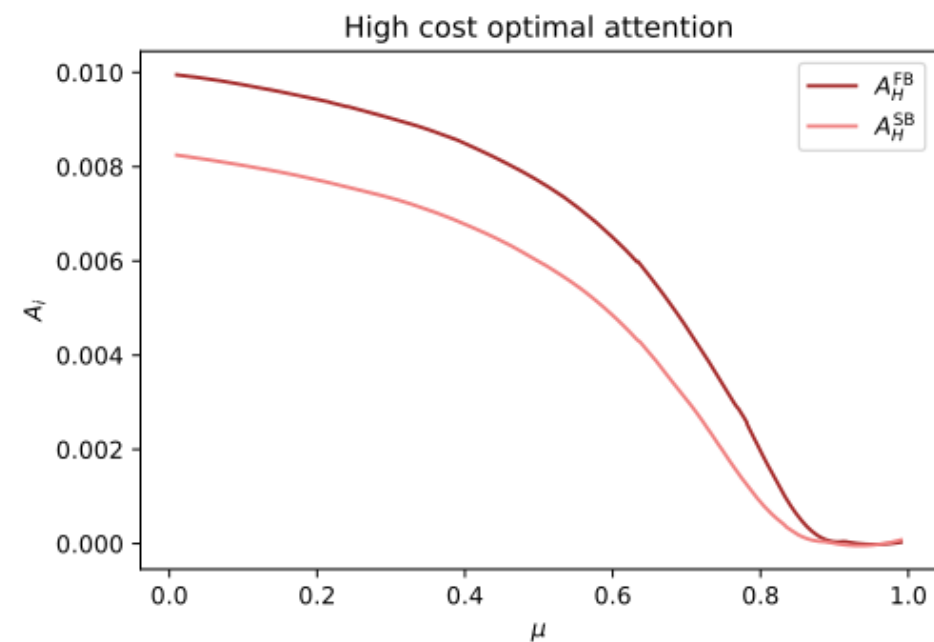
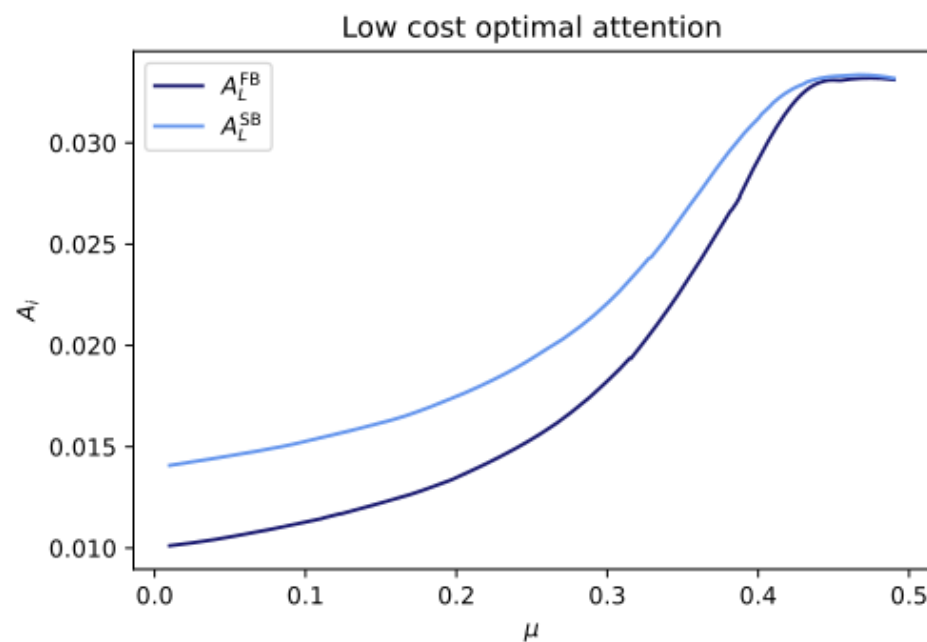
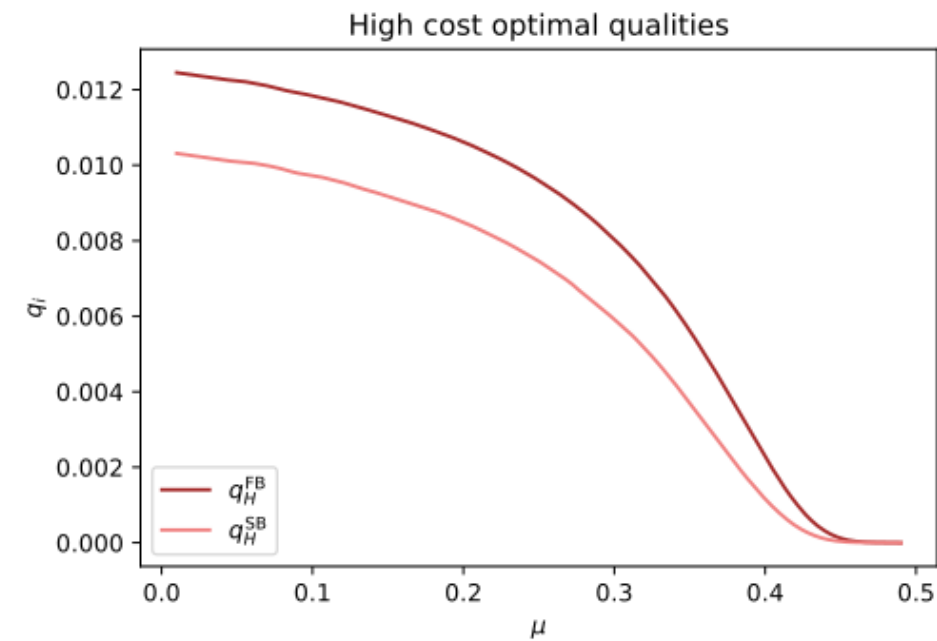
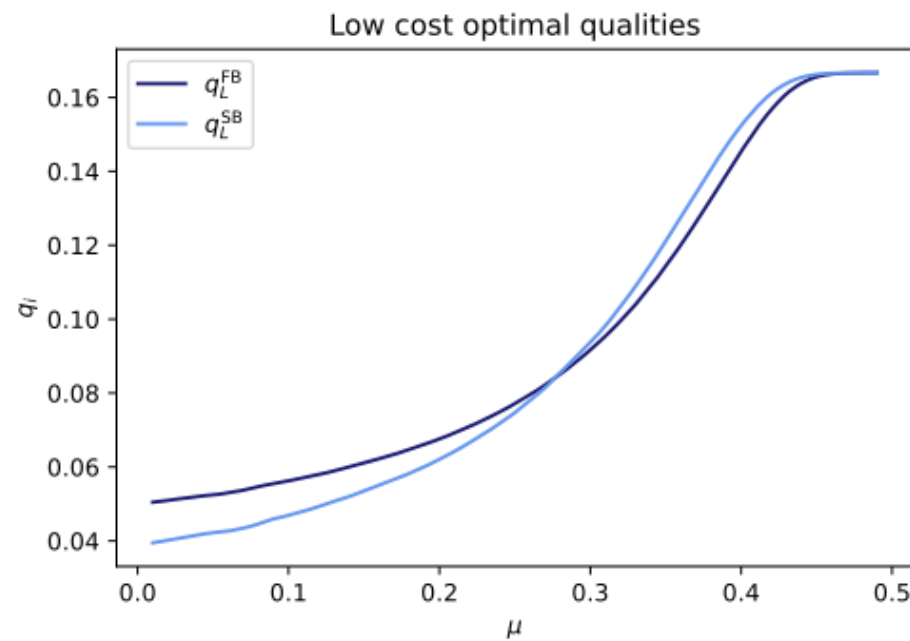
Moreover, the direction of the distortion depends on the preference for variety μ

$$\begin{cases} q_L(\mu)^{SB} < q_L(\mu)^{FB} & \text{iff } \mu < \mu^* \\ q_L(\mu)^{SB} = q_L(\mu)^{FB} & \text{iff } \mu = \mu^* \\ q_L(\mu)^{SB} > q_L(\mu)^{FB} & \text{iff } \mu > \mu^* \end{cases}$$

Example: Numerical Solutions

2 options to meet IC: $\begin{cases} \downarrow q_L \\ \uparrow A_L \downarrow A_H \end{cases}$

Optimal one depends on preference for variety μ !



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Only in First Best

Only in Second Best

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Does not depend on the info context !

Does not depend in any parameter but μ !

Conclusion

Takeaways:

- In complete information, distribution of attention shaped by preferences on diversity
- In the second best, qualities are distorted upwards or downwards depending on μ

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Different directions in **future research**:

- Make the model continuous
- Heterogeneous μ_i across agents and platforms
- Behavioural aspects (e.g. addiction)