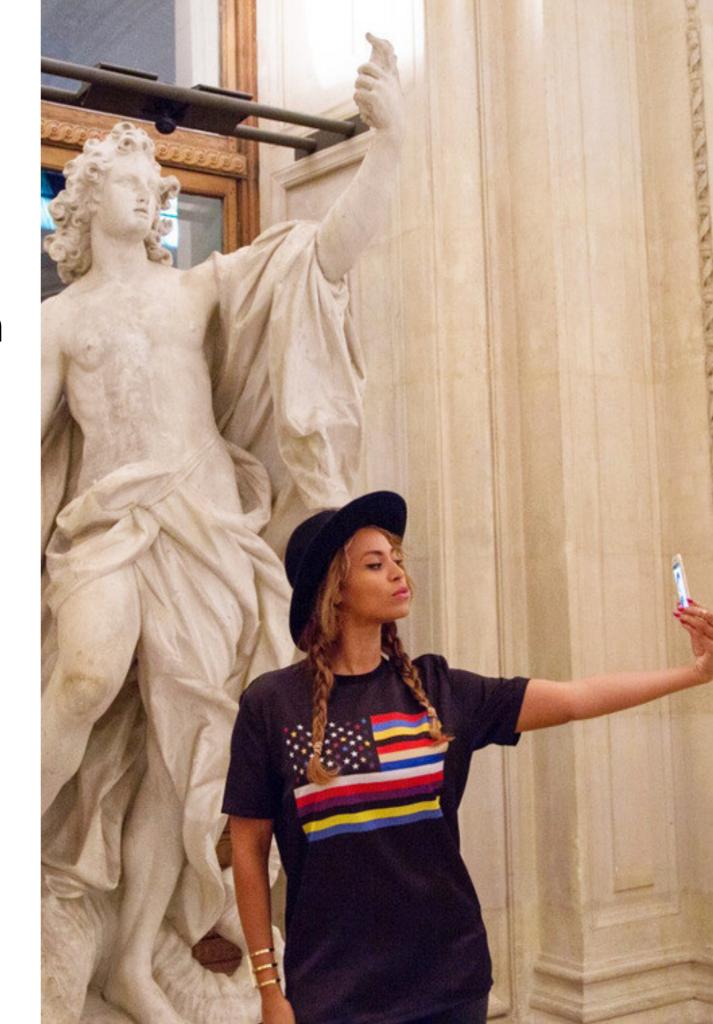
Optimal allocation of attention in user-generated content platforms

Iván Rendo Barreiro Advisor: Alexandre de Cornière

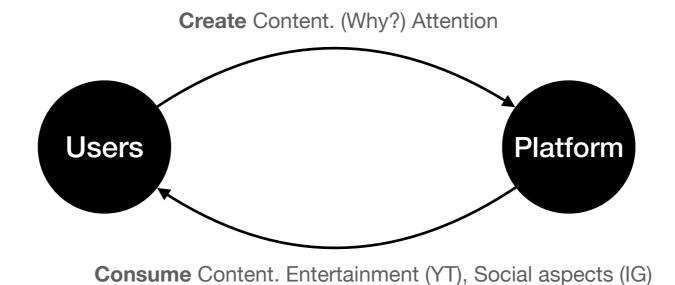


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• Except for Google, the 6 most viewed websites are UGC

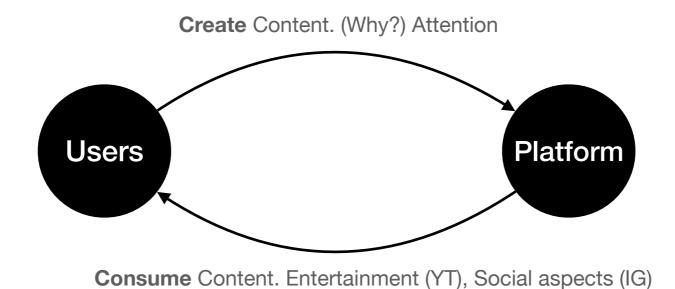
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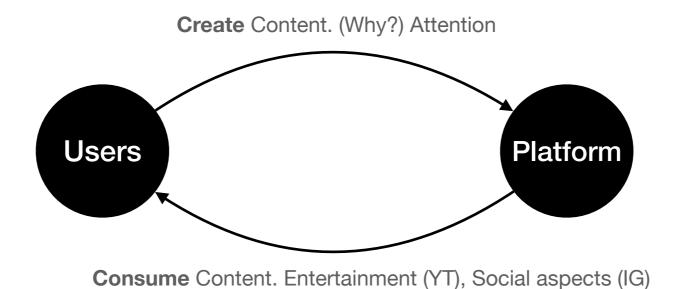
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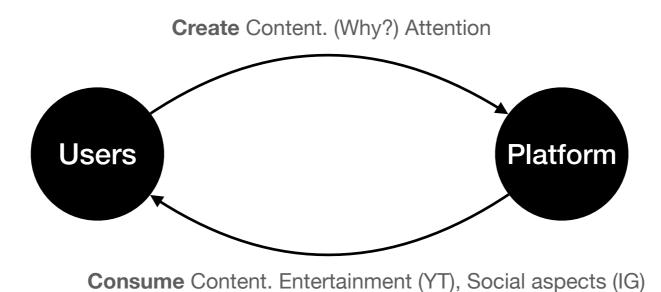
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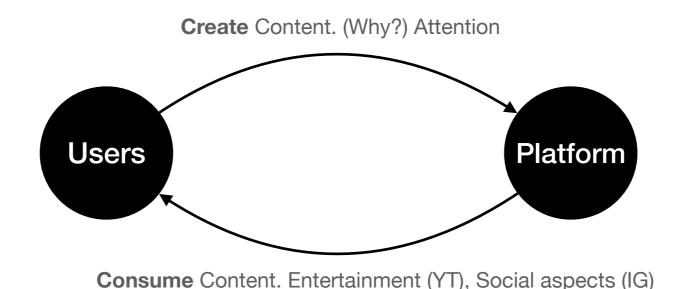
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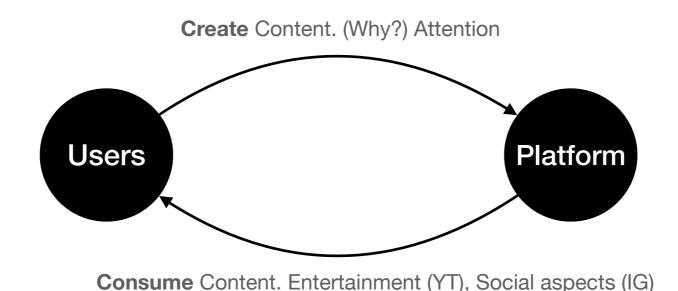
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Social platforms (IG, Snapchat): users prefer to consume content from a lot of creators VS Entertainment platforms (Youtube, Twitch)... where quality comes first

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- 2. **Utility** of any user in the platform **depends on the transfers** (attention) **paid to the rest** of users.

Outline

- 1. General Model (theoretical framework)
- 2. Binary Model (more results)
- 3. Ad-funded Platforms (application)

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- In the consumption utility, I use A_jq_j and not just q_j because the relevant variable is the **perceived quality**. Otherwise, users derive utility from quality they are not paying attention to.

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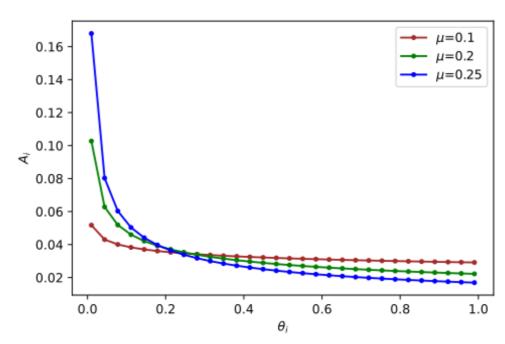
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Optimal attention shares and qualities:

$$A_i^* = \frac{\theta_i^{\frac{\mu}{2\mu - 1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu - 1}}} \qquad q_i^* = \frac{A_i^*}{\theta_i} = \frac{\theta_i^{\frac{1 - \mu}{2\mu - 1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu - 1}}}$$

Example. N = 30 and equidistant costs.



Moreover...

- Proposition 2:
- In the First Best setting, the optimal attention allocation with respect to qualities follows a Generalized Tullock Contest:

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(more elegant and tractable seems to be the case of the continuum of agents explored minimally in Appendix B, but its study is left out of this thesis)

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Under standard assumptions, quality of the low-cost type is distorted

$$\exists \, \mu \in \left(0, \frac{1}{2}\right) \ : \ q_L(\mu)^{FB} \neq q_L(\mu)^{SB}$$

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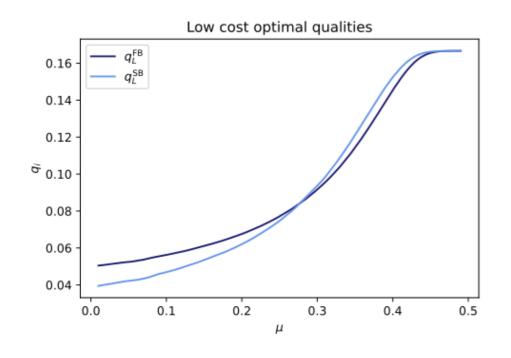
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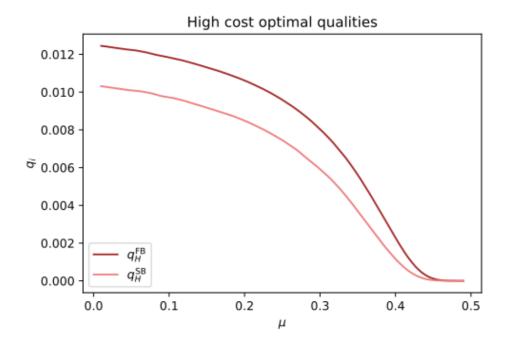
Conjecture 1:

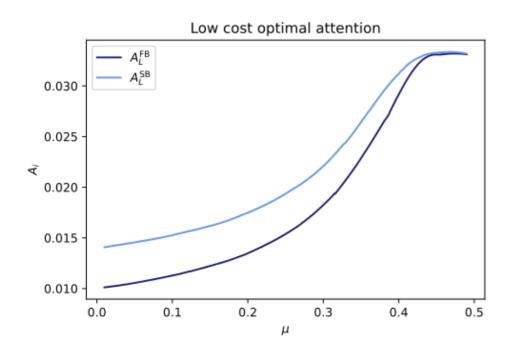
Moreover, the direction of the distortion depends on the preference for variety μ

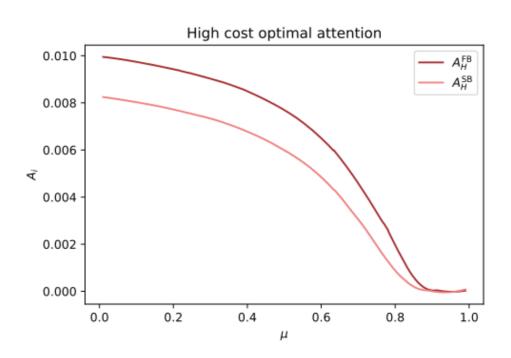
$$\begin{cases} q_L(\mu)^{SB} < q_L(\mu)^{FB} & \text{iff} \quad \mu < \mu^* \\ q_L(\mu)^{SB} = q_L(\mu)^{FB} & \text{iff} \quad \mu = \mu^* \\ q_L(\mu)^{SB} > q_L(\mu)^{FB} & \text{iff} \quad \mu > \mu^* \end{cases}$$

Example: Numerical Solutions









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Does not depend on the info context! Does not depend in any parameter but μ !

Conclusion

Takeaways:

- In complete information, distribution of attention shaped by preferences on diversity
- \bullet In the second best, qualities are distorted upwards or downwards depending on μ

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Different directions in **future research**:

- Make the model continuous
- Heterogeneous μ_i across agents and platforms
- Behavioural aspects (e.g. addiction)