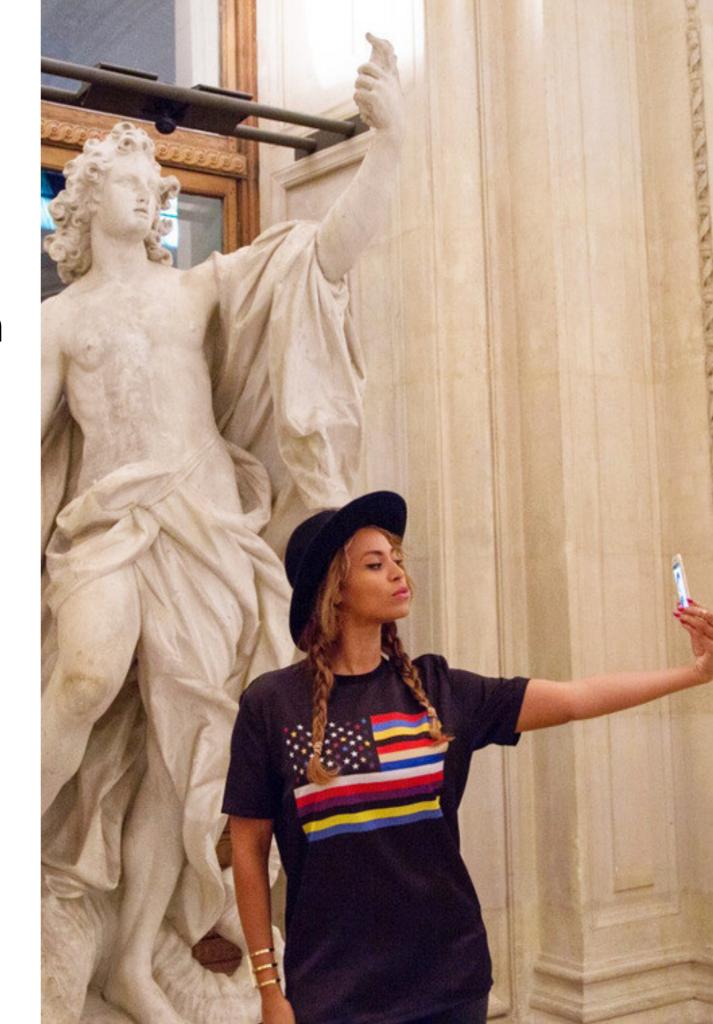
Optimal allocation of attention in user-generated content platforms

Iván Rendo Barreiro Advisor: Alexandre de Cornière

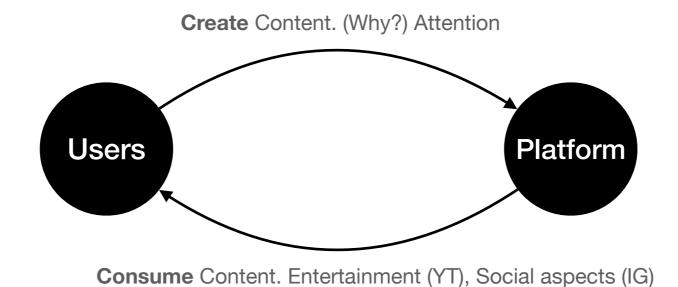


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• Except for Google, the 6 most viewed websites are UGC

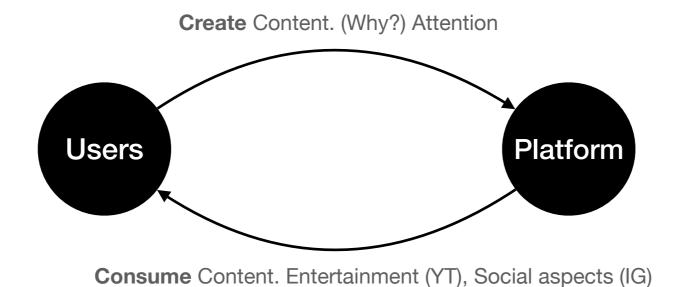
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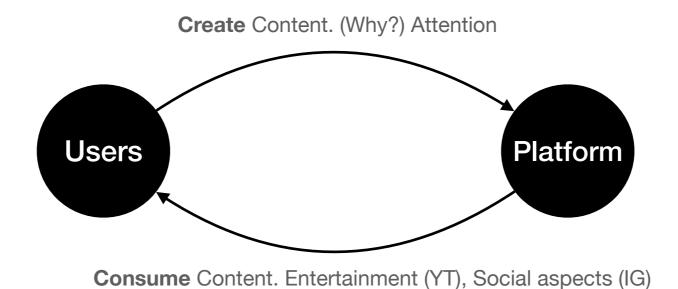
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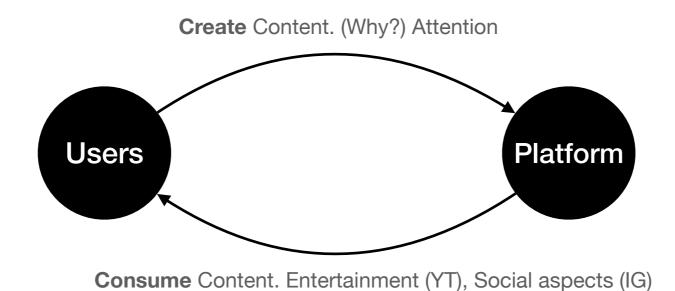
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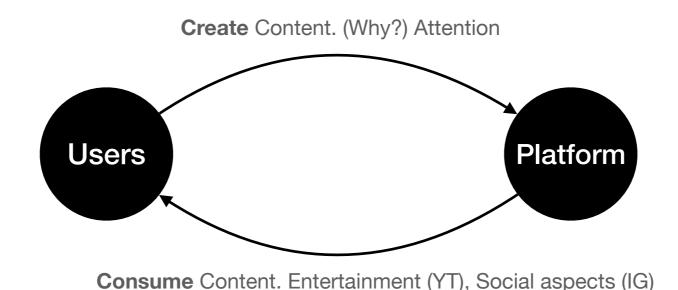
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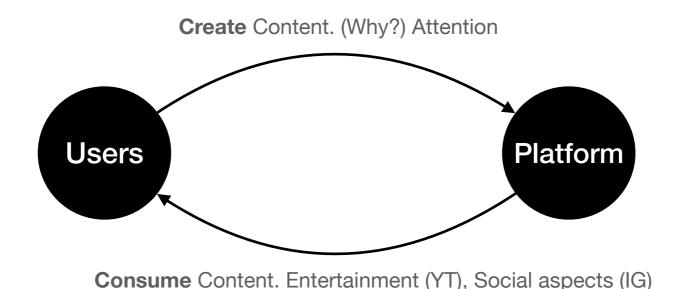
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 - E.g. Instagram (stories introduction), BeReal... < "Low quality" content, attention more distributed

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Social platforms (IG, Snapchat): users prefer to consume content from a lot of creators VS Entertainment platforms (Youtube, Twitch)... where quality comes first

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- 2. **Utility** of any user in the platform **depends on the transfers** (attention) **paid to the rest** of users.

Outline

- 1. General Model (theoretical framework)
- 2. Binary Model (more results)
- 3. Ad-funded Platforms (application)

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- In the consumption utility, I use A_jq_j and not just q_j because the relevant variable is the **perceived / consumed quality**. Otherwise, users derive utility from quality they are not paying attention to.

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Problem of the platform:

$$\max_{\mathbf{A},\mathbf{q}} \sum_{i=1}^{N} \left(A_{i} - \theta_{i} q_{i} + \sum_{j \neq i} \left(A_{j} q_{j} \right)^{\mu} \right) \equiv \max_{\mathbf{A},\mathbf{q}} \sum_{i=1}^{N} U_{i}$$
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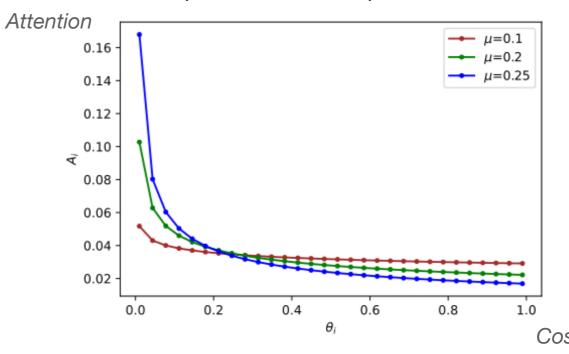
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Optimal attention shares and qualities:

$$A_i^* = \frac{\theta_i^{\frac{\mu}{2\mu - 1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu - 1}}} \qquad q_i^* = \frac{A_i^*}{\theta_i} = \frac{\theta_i^{\frac{1 - \mu}{2\mu - 1}}}{\sum_{j=1}^N \theta_j^{\frac{\mu}{2\mu - 1}}}$$

Example. N = 30 and equidistant costs.



Moreover...

- Proposition 2:
- In the First Best setting, the optimal attention allocation with respect to qualities follows a
 Generalized Tullock Contest:

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For simplicity, the **second best** setting and its relation with the first best is studied in the framework of N users divided in two types of users, L and H, that have costs $\theta_L < \theta_H$

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Under standard assumptions, quality of the low-cost type is distorted

$$\exists \mu \in \left(0, \frac{1}{2}\right) : q_L(\mu)^{FB} \neq q_L(\mu)^{SB}$$

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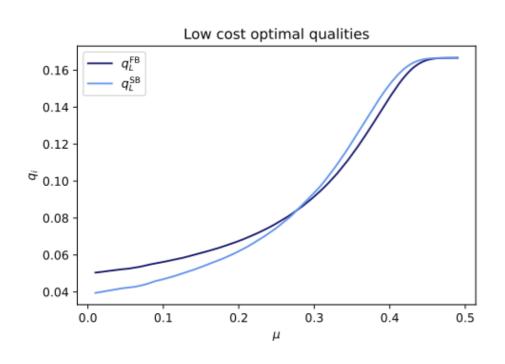
Moreover, the direction of the distortion depends on the preference for variety μ

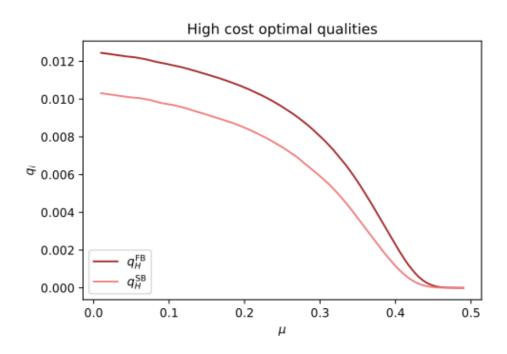
$$\begin{cases} q_L(\mu)^{SB} < q_L(\mu)^{FB} & \text{iff} \quad \mu < \mu^* \\ q_L(\mu)^{SB} = q_L(\mu)^{FB} & \text{iff} \quad \mu = \mu^* \\ q_L(\mu)^{SB} > q_L(\mu)^{FB} & \text{iff} \quad \mu > \mu^* \end{cases}$$

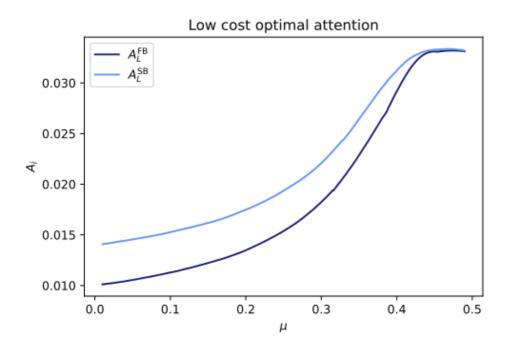
Example: Numerical Solutions

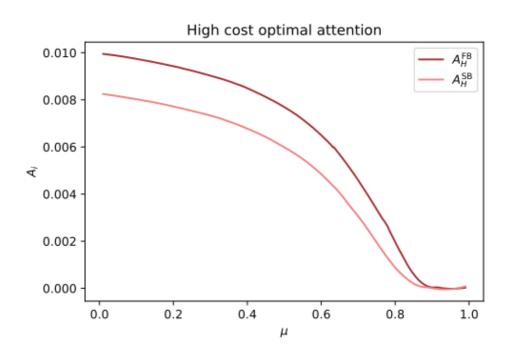
2 options to meet IC: $\left\{\begin{array}{c} \downarrow q_L \\ \uparrow A_L \downarrow A_H \end{array}\right.$

Optimal one depends on preference for variety μ !









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Does not depend on the info context! Does not depend in any parameter but μ !

Conclusion

Takeaways:

- In complete information, distribution of attention shaped by preferences on diversity
- \bullet In the second best, qualities are distorted upwards or downwards depending on μ

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Different directions in **future research**:

- Make the model continuous
- Heterogeneous μ_i across agents and platforms
- Behavioural aspects (e.g. addiction)