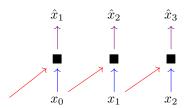
autoregressive network

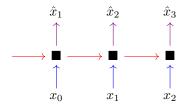
$$x_{0...i} \rightarrow x_{i+1}$$



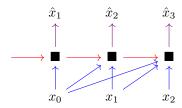
 ${\rm convolution}$ 



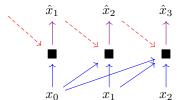
recurrent



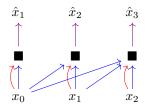
recurrent attention



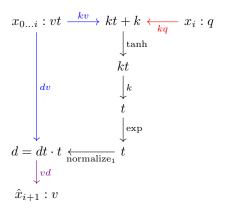
recurrent attention redirected



 ${\it transformer}$ 



## additive attention



## multiplicative attention

$$x_{0...i} : vt \xrightarrow{kv} kt \cdot {}^{T}k \xleftarrow{kq} x_{i} : q$$

$$\downarrow^{dv} \qquad \downarrow^{\exp}$$

$$d = dt \cdot t \xleftarrow{\text{normalize}_{1}} t$$

$$\downarrow^{vd}$$

$$\hat{x}_{i+1} : v$$

dv is unnecessary. since  $vd \cdot (dv \cdot vt) \cdot t = (vd \cdot dv) \cdot (vt \cdot t)$ , the model could simply learn vd as  $vd \cdot dv$ .

kv is unnecessary. since the model could simply learn kq as  $vk\cdot kq.$ 

$$\begin{split} v, k, q : \mathbb{N}_{>0} \\ V : \mathbb{R}^v \\ Q : \mathbb{R}^q \\ K^V : \mathbb{R}^v \to \mathbb{R}^k \\ K^Q : \mathbb{R}^q \to \mathbb{R}^k \\ V^K &= \operatorname{transpose} K^V \\ Q^K &= \operatorname{transpose} K^Q \\ (K^V \cdot V) \cdot (K^Q \cdot Q) &= (Q^K K^V \cdot V) \cdot Q \\ &= V \cdot (V^K K^Q \cdot Q) \end{split}$$