i for each task (dynamic, static, shuffle), j for each participant.

Hyperpriors of the slope

$$\mu_{\beta} \sim \text{StudentT}(3,0,10)$$

$$\sigma_{\beta} \sim \text{HalfNormal}(10)$$

Hyper-prior of the breakpoint

$$\tau \sim \text{Uniform}(0, 100)$$

Hyperprior of the recognition ability at τ

$$\theta \sim \text{Uniform}(0,1)$$

$$\kappa \sim \text{Uniform}(0, Nt)$$

(reparameterized as the mode of Beta Distribution)

$$a = \theta * (\kappa - 2) + 1$$

 $b = (1 - \theta) * (\kappa - 2) + 1$

For each stimuli type $i \in \text{static}$, dynamic, shuffled:

Prior of the recognition ability at τ

$$\theta_i \sim \text{Beta}(a,b)$$

Priors of the breakpoint

$$\tau_i \sim \text{Normal}(\tau, 10)$$

Priors of the slopes (a indicates before age τ)

$$\beta_i^{a,b} \sim \text{Normal}(\mu_\beta, \sigma_\beta)$$

The intercepts before and after age τ

$$b_i^{a,b} = logit(\theta_i) - \tau_i * \beta_i^{a,b}$$

Linear function and invlogit transform

$$\beta_{i}, Intercept_{i} = \begin{cases} \beta_{i}^{a}, b_{i}^{a} & \text{if } age < \tau_{i} \\ \beta_{i}^{b}, b_{i}^{b} & \text{if } age \ge \tau_{i} \end{cases}$$

$$\theta_{i,j} = \beta_{i} \otimes age_{j} + Intercept_{i}$$

$$\hat{y}_{i,j} = \text{invlogit}(\theta_{i,j})$$

Observed accurate categorizations

$$k_{i,j} \sim \text{Binomial}(\hat{y}_{i,j}, n_{i,j})$$