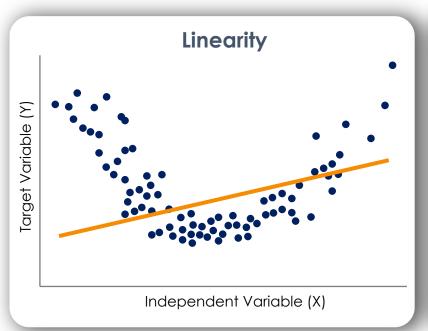
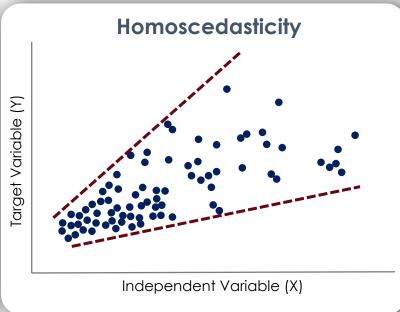
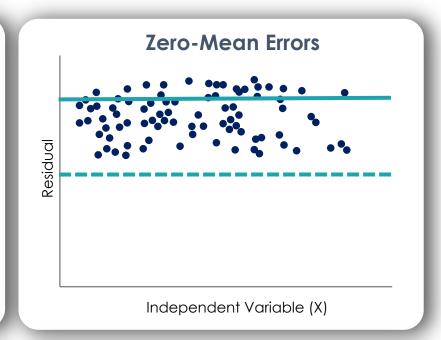
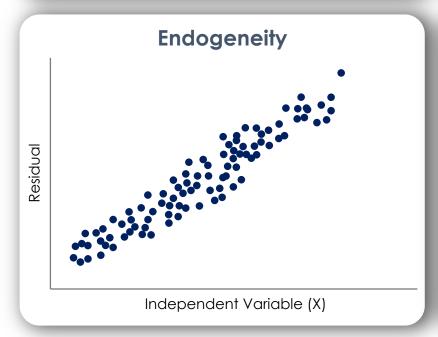


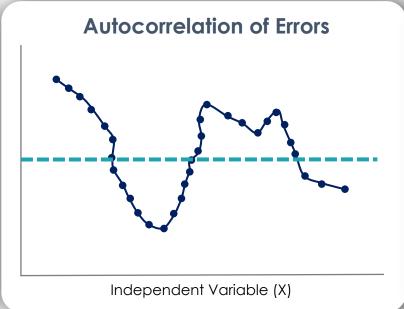
OLS Assumptions

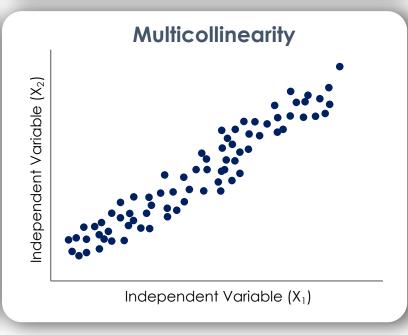












Properties of **estimators**

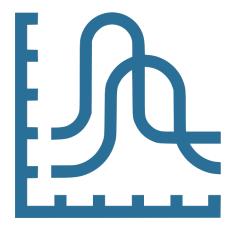
Unbiasedness

Consistency

Efficiency

Sufficiency







If expected vale is identical to population parameter

Estimator approaches parameter as sample size increases

If two estimator are unbiased, we choose the one with smaller variance (it is efficient) It is sufficient if information in it about the parameter is enough

Importance of functional form

Okay but...what is the importance of functional form?

Think about the complex world which is not always linear...how can we show a relationship that is not linear in a linear regression?



Importance of functional form

"linearity in parameters but not necessarily in variables"

$$Y_1 = b_0 + b_0 X_{1i} + b_2 X_{2i}^2 + u_i$$

For example:

$$Wage_1 = \underbrace{b_0}_{\text{Linear}} + \underbrace{b_1}_{\text{exp}_i} + \underbrace{b_2}_{\text{exp}_i} + \underbrace{b_3}_{\text{exp}_i}^2 + u_i$$

Importance of functional form

Let's check several functional forms used in econometrics and other related fields

Linear

$$Y = \beta_1 + \beta_2 X$$

Log-Linear (log-log)

$$ln Y = \beta_1 + \beta_2 ln X$$

Log-lin

$$\ln Y = \beta_1 + \beta_2 X$$

Lin-log

$$Y = \beta_1 + \beta_2 \ln X$$

Reciprocal

$$Y = \beta_1 + \beta_2 \left(\frac{1}{x}\right)$$

Log-Reciprocal

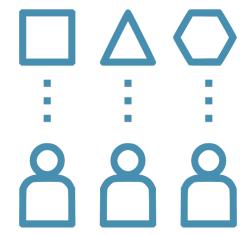
$$\ln Y = \beta_1 - \beta_2 \left(\frac{1}{x}\right)$$

Models

You have to ask yourself about



Why this model?



Characteristics



Appropiate cases

Log-Linear model

Economists look for the rate of growth in some economic variables such as population, GDP, monetary supply, employment...

Notice that just one side of the equation is logarithmic

Log side
$$\ln Y_1 = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i}^2 + u_i$$
 or

$$Y_1 = \beta_0 + \beta_1 \ln X_{1i} + \beta_2 \ln X + u_i$$
Log side

The difference is on the assigned variable

Log side
$$\ln Y_1 = \beta_0 + \beta_1 \, X_{1i} + \beta_2 X_{2i}^2 + u_i \qquad \qquad \text{log-lin}$$
 or

$$Y_1 = \beta_0 + \beta_1 \ln X_{1i} + \beta_2 \ln X + u_i$$
 lin - log Log side

$$\ln Y_1 = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i}^2 + u_i$$

Estimated percentage change in your dependent variable for a unit change in your independent variable

$$Y_1 = \beta_0 + \beta_1 \ln X_{1i} + \beta_2 \ln X + u_i$$
Log side

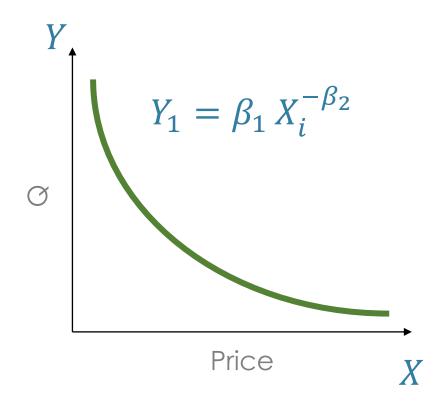
Estimated unit change in your dependent variable for a percentage change in your independent variable

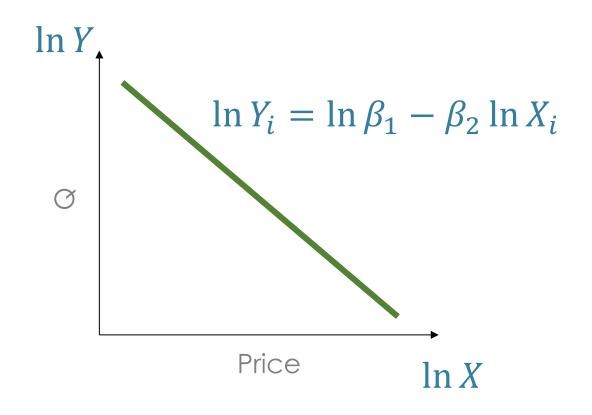
On the other hand, if we want to use elasticities we adopt a log-log model

$$Y_1 = \beta_1 X_i^{\beta_2} + e^{ui}$$

or

$$\ln Y_i = \alpha + \beta_2 \ln X_i + u_i$$





What we may focus on is the slope β_2 which measures the elasticity of Y respect to X

or

the percentage change in Y for a small percentage change in X

Log-Log model

NOTE: there is a difference between percentage change and percentage points

For example, the rate of unemployment is stated as percentage

Imagine that Mexico unemployment rate for 2019 is 4%, but in 2020 it grows to 8%

It is said that the percentage point change in unemployment rate is 2

but

The percentage change is $\frac{8-6}{6}$ or $\approx 33\%$



Log-Log model

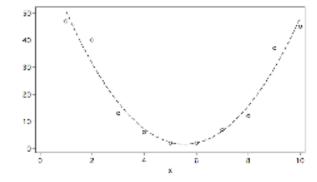
Suppose we have the following equation

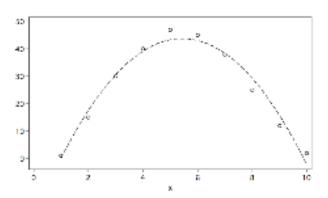
$$y = \alpha + \beta_1 X_1 + \beta_2 X_2^2$$

Stata will output these coefficients

Model A	 I	Coef.
Model A	-+-	
X		1839751
x2		1.016747
constant		.2076584

Model D		Coef.
	+-	
X	1	.1839751
x2		-1.016747
constant	Ī	99.79234





Practice (Quadratic)

The data set in MUS08 contains data panel information about wages and salaries in the USA from 1976-1982.

Then we plot the relationship between salary and experience.

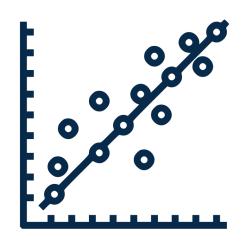
Finally, generate linear regression with 1wage as dependent and exp, exp2, wks and ed as independent.

STATA COMMANDS

- graph twoway (scatter lwage exp) (qfit lwage exp)
 (lowess lwage exp)
- 2. regress lwage exp exp2 wks ed

Practice (Quadratic)

We can read the output as:







$$R^2 = 0.28$$

Salaries increase in 0.6% for each additional work week

Salaries increase in 0.6% for each additional year of education

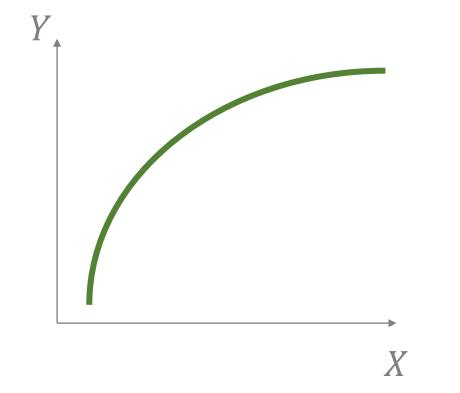
How to find the slope of the curve?

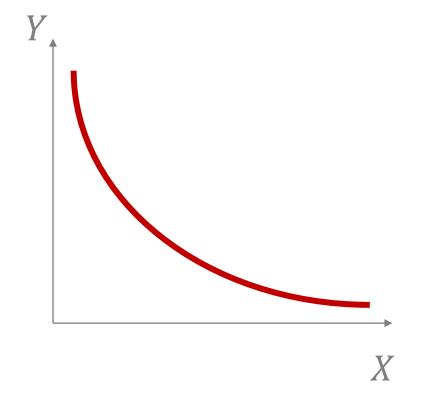
Hint: look into x_2^2

$$y = \beta_0 + \beta_1 X_1 + \beta_2 X_2^2$$

$$y = \beta_0 + \beta_1 X_1 + \beta_2 X_2^2$$

$$y = \beta_0 + \beta_1 X_1 - \beta_2 X_2^2$$





By solving for it

$$y = \beta_0 + \beta_1 X_1 + \beta_2 X_2^2$$

Then calculate the derivative with respect to X

$$y' = \beta_1 + 2\beta_2 X_2^2$$

Finally, equal to zero and solve for finding tipping points

1. State the output in econometrics terms

$$\hat{y} = 4.097 + 0.44675 \exp 0.00072 \exp^2 + 0.0058 wks + 0.7604 ed + \varepsilon$$

2. If we take first derivative respect to exp we have

$$y' = 0.4467 - (2 \times (0.00072) exp)$$

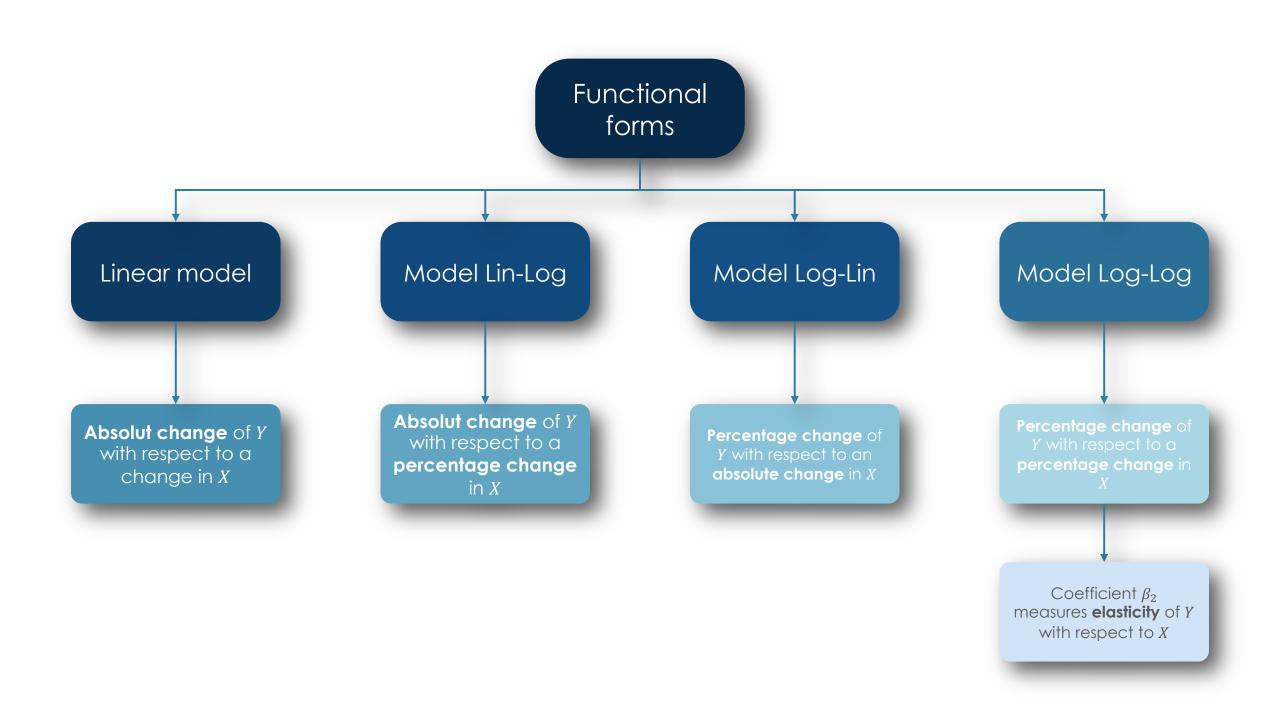
3. If we solve for exp we have:

$$exp = \frac{0.4467}{2 \times 0.00072} = 31$$

We can read the output as:



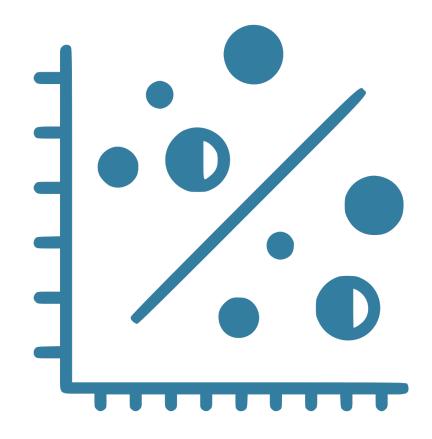
Salaries increase as experience grows up to 31 years $\frac{0.0447}{(2\times0.00072)}$ and from there it decreases



Ramsey Regression Equation Specification Error Test (RESET) is a general specification test for linear regression models

It tries to prove if non-linear combinations of adjusted values have any explanatory force over dependent variable

If any of this non-linear combinations have explanatory influence over *Y*, then model is specified incorrectly



We use auto.dat dataset. We will try to explain car prices depending on mileage, weight, engine capacity, and whether car was produced in USA or not.

Run a linear regression.

Standardize data (mean 0 and variance 1).

Then we generate powers over adjusted values (y^2, y^3, y^4) .

Finally we run the regression using powers.

STATA COMMANDS

- 1. reg price mpg weight foreign
- 2. predict y
- 3. sum y
- 4. replace y = (y-r(mean))/r(sd)
- 5. gen $y^2 = y^2$
- 6. gen $y3 = y^3$
- 7. gen $y4 = y^4$
- 8. reg price mpg weight foreign y2 y3 y4

Practice (RESET)

We will prove coefficient significance in order to inspect powers using F test (apply test over linear constraint)

Due to output, we cannot reject H_0 , our model is well specified.

Then, apply Ramsey test over well specified form.

What is the conclusion?

STATA COMMANDS

- 9. test y2 y3 y4
- 10. reg price mpg weight foreign
- 11. ovtest

References

- Salvatore, D., & Sarmiento, J. C. (1983). Econometría (No. HB141 S39). McGraw-Hill.
- Kumari K., J. Pract Cardiovasc, Wooldridge, J. (2020). Introductory econometrics: a modern approach. Boston, MA: Cengage. Gujarati, D. & Porter, D. (2009). Basic econometrics. Boston: McGraw-Hill Irwin.
- Gujarati, D. N. (2009). Basic econometrics. Tata McGraw-Hill Education.