# Chapter 6: Complexities of epidemic modeling

In the prior Chapter, we derived and simulated the most basic epidemic model. We assumed that people can be in only one of three states (susceptible, infected, or recovered), and that people mix homogeneously throughout the population (the Law of Mass Action). In this Chapter, we examine how the Kermack-McKendrick model can be extended to simulate a wide variety of diseases and circumstances, including the complex ways that people come into contact with each other.

# Extending the standard Kermack-McKendrick model

Once we leave the context of the Kermack-McKendrick model, the calculation of  $R_{\theta}$  unfortunately gets complicated, often too complicated to produce any simple formulas that are memorable enough to be recalled for day-to-day public health practice (although we note that the  $R_{\theta}$  can still be calculated using mathematics that are beyond the level of this textbook, as detailed in some of the References to this Chapter). So, we often have to resort to simulation to identify what effect a disease will have in a population, and to measure the potential impact of a public health intervention on the disease.

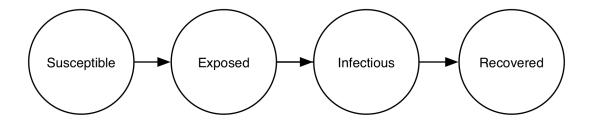
We can extend our basic Kermack-McKendrick simulation to incorporate a wide variety of diseases and interventions. Suppose, for example, that we want to model two potential interventions to reduce the burden of tuberculosis (TB). People who are infected with TB are not always infectious. Rather, people often go into a "dormant" or

"latent" state of disease (which is not dangerous, and not infectious), sometimes for several decades, before "re-activating" to the form of lung disease that we associate with TB (which is both infectious and potentially fatal, if untreated).

Suppose that you are a public health program manager and want to compare two different proposals for reducing the burden of TB: (1) investment in a program to find and treat people with latent TB, preventing them from reactivating to active TB sometime in the future; and (2) investment in a program to expand treatment for people with active TB, preventing them from infecting susceptible people.

There is no way to compare these programs using the standard Kermack-McKendrick model, but we can extend the model to address the unique pathogenesis of TB. We can approach the problem with the same strategy we have used for all of our models: first draw the model diagram, then write down equations describing the diagram.

Our model diagram is shown in Figure 6.1. In the diagram, we have extended the classical Kermack-McKendrick model to account for the unique nature of TB. Here, we have extended the Kermack-McKendrick model to an "SEIR model", which expands the SIR structure by adding a group of "exposed" people (state E) between the susceptible and infectious group. The exposed group is latently infected, but not yet infectious. They can move on to the infectious state at some rate  $\cdot$ . Also, since TB is a potentially deadly disease, we have added a rate of death—from the active, infectious state, which reflects the additional death rate beyond the "usual" or "background" death rate  $\cdot$ .



We can write down a series of equations based on our model diagram:

[Equation 6.1] 
$$\frac{dS(t)}{dt} = \ \mu N(t) - \beta I(t) S(t) - \mu S(t)$$

[Equation 6.2] 
$$\frac{dE(t)}{dt} = \ \beta I(t)S(t) - \gamma E(t) - \mu E(t)$$

[Equation 6.3] 
$$\frac{{\scriptstyle dI(t)}}{{\scriptstyle dt}} = \ \gamma E(t) - vI(t) - \kappa I(t) - \mu I(t) \label{eq:equation}$$

[Equation 6.4] 
$$\frac{dR(t)}{dt} = vI(t) - \mu R(t)$$

There are several differences between the SEIR model and the Kermack-McKendrick SIR model. First, we see that we have added one equation for the exposed (latent) TB state. People enter that state from the susceptible class, and flow to the active TB state at the rate. We have additionally added a rate of death from TB of from the active, infectious state. Hence, we should not expect to have a constant population size in our model.

The textbook website has the R code corresponding to this model. The code utilizes the following set of parameters: N = 100,000 people, = 0.001, = 1/75 years<sup>-1</sup>, = 0.05 years<sup>-1</sup>, v = 2 years<sup>-1</sup>, and = 0.1 years<sup>-1</sup> (note that we are using convenient round numbers here and elsewhere in the book for teaching purposes; these parameters should not be misconstrued to reflect actual TB epidemics). We also set the initial conditions such that S = 99,999 people, E = 0 people, I = 1 person, and R = 0 people.

As in the previous Chapter, we begin our R model code by first specifying our

# parameters:

```
N = 100000
beta = 0.001
mu = 1/75
gamma = 0.05
v = 2
kappa = 0.1
```

Second, we declare our time horizon of interest, let's say 20 years, and a small

time step:

```
\begin{array}{l} time = 20 \\ dt = 0.01 \end{array}
```

Third, we insert our initial conditions and initiate some vectors for each state:

```
S = 99999
E = 0
I = 1
R = 0
Svec = S
Evec = E
Ivec = I
Rvec = R
```

Fourth, we insert our equations in two for loops (the first spanning across all times, and the second for each small time step within each time period). The current state in each loop is then added to the vectors for each state:

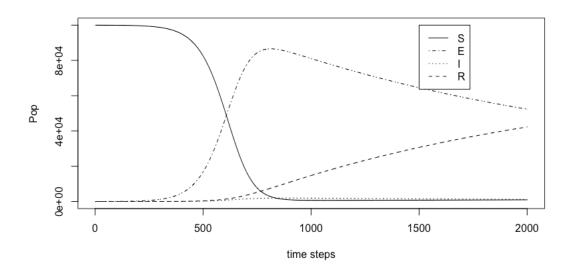
```
 \begin{array}{l} & \text{for (i in 1:time)} \{ \\ & \text{for (i in 1:(1/dt))} \{ \\ & S = S + mu^*N^*dt - beta^*S^*I^*dt - mu^*S^*dt \\ & E = E + beta^*S^*I^*dt - gamma^*E^*dt - mu^*E^*dt \\ & I = I + gamma^*E^*dt - v^*I^*dt - kappa^*I^*dt - mu^*I^*dt \\ & R = R + v^*I^*dt - mu^*R^*dt \\ & Svec = c(Svec, S) \\ & Evec = c(Evec, E) \\ & Ivec = c(Evec, E) \\ & Ivec = c(Rvec, R) \\ & N = S + E + I + R \\ & \} \\ \} \\ \end{aligned}
```

Note that we have updated the total population size N with each time step, since we are no longer assuming a constant population size, because TB is deadly and will reduce the size of the population if untreated.

Finally, we can plot our results, adding the exposed group to our plot in purple, as shown in Figure 6.2:

```
\begin{array}{l} plot(Svec, lty=1, type="l", xlab="time steps", ylab="Pop", ylim=c(0,100000)) \\ lines(Evec, lty=4) \\ lines(Ivec, lty=3) \\ lines(Rvec, lty=2) \\ legend(1500, 100000, c("S", "E", "I", "R"), lty=c(1,4,3,2)) \end{array}
```

As with our Kermack-McKendrick model in the previous Chapter, we first plot one vector, specifying its line type, labels, and the limits of the y-axis (from 0 to 100,000 people in this case). Then we plot other vectors as lines, and add a legend, specifying the legend's position, text, and line types; the commands produce Figure 6.2.



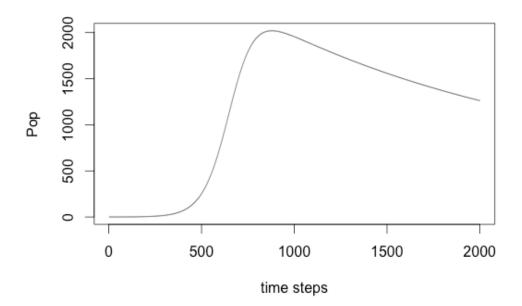
We see in Figure 6.2 that the curves for the disease are very different from the original Kermack-McKendrick SIR model. The disease spreads over a longer period of

time. Many people become latently infected, though only a few are actively infectious. Because Figure 6.2 is zoomed out, we can't see the infected line very clearly. Hence, we can just plot the infectious group by themselves:

plot(Ivec,lty=3,xlab="time steps",ylab="Pop")

This produces Figure 6.3, where we see an interesting shape to the infectious pool, which peaks at a prevalence of about 2,000 people, with a very gradual rise and an even slower fall:

 $> \max(Ivec)$  [1] 2019.316



Now that we have built our TB model, we can compare the two interventions we hope to contrast: (1) investment in a program to find and treat people with latent TB, preventing them from transitioning to active TB sometime in the future; or (2) investment in a program to expand treatment for people with active TB, preventing

them from infecting susceptible people. Let's suppose that investment in treating people with latent TB would add a new rate that would remove people from the exposed state and put them in the recovered state at a rate = 0.1 year<sup>-1</sup>. Suppose, by contrast, that more investment in expanding treatment would increase the recovery rate to a value of 3 year<sup>-1</sup>. Which program would make more impact on the total number of people who die from tuberculosis over the next 20 years?

For the treatment of latent TB, we can modify the equations slightly to add on the rate  $= 0.1 \text{ year}^{-1}$  shifting people from the latent to the recovered state. We first add the code:

tau = 0.1

We can include the code defining tau with the other parameters at the beginning of the code. We can then modify the equations to reflect the new rate of flow from the exposed to the recovered state:

```
\begin{split} S &= S + mu^*N^*dt - beta^*S^*I^*dt - mu^*S^*dt \\ E &= E + beta^*S^*I^*dt - gamma^*E^*dt - mu^*E^*dt - tau^*E^*dt \\ I &= I + gamma^*E^*dt - v^*I^*dt - kappa^*I^*dt - mu^*I^*dt \\ R &= R + v^*I^*dt - mu^*R^*dt + tau^*E^*dt \end{split}
```

We next need to determine what the overall number of people who die from TB would be over the time period, which is 20 years. We can add one more vector before the "for loop" to hold this quantity:

Deaths = 0

Then we can update its value within the "for loop":

Deaths = c(Deaths, kappa\*I\*dt)

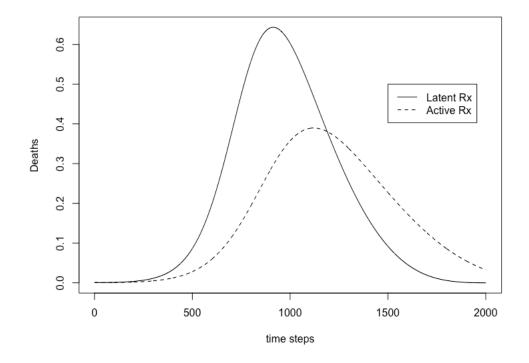
When we run the model, we see that the total deaths after introducing the latent TB treatment program is about 400:

> sum(Deaths) [1] 395.0552

Next, we can compare the number of deaths to the situation if we increased the recovery rate to a value of 3 year<sup>-1</sup>. We first set the value of to 0, to show the absence of the latent treatment case, then set the value of v to 3. Running the model in this scenario, we see that the total number of deaths has been reduced, to just under 320:

> sum(Deaths) [1] 313.3521

The comparison between the two treatment alternatives can be visualized in Figure 6.4.



Our example reveals that we can extend the Kermack-McKendrick model in several ways to accommodate a variety of diseases and interventions. In addition to adding new states, we can add new flows between states. We can quickly extend the model in R and define the metrics we want to compare. In the next section, we'll also look at how to relax a key assumption we've used so far: The Law of Mass Action, which assumed that people are homogeneously mixing together and thereby all share the same risk.

# <2>Heterogeneous mixing

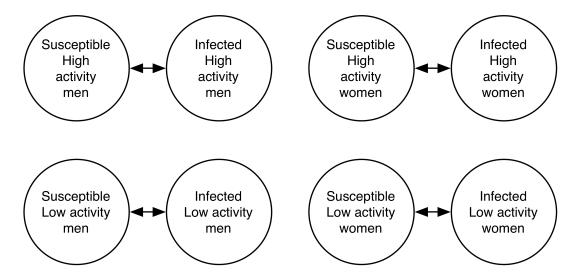
Up to this point, we've been assuming homogeneous mixing of a population—
meaning that people contact one another at an even rate throughout the population,
such that every person experiences the same average risk of disease. That's often a
pretty good approximation to understand the general trends of infectious disease
transmission in large populations, but in some cases—for example, in the case of many
sexually-transmitted diseases (STDs)—we need to modify that assumption. In the case
of STDs, some people who have minimal amounts of sexual contact will be at very low
risk for disease, while others who change sexual partners frequently will be at much
higher risk. Many other diseases that present a serious public health burden also involve
such heterogeneous mixing, such as diseases that travel via injection drug use, or
diseases that are segregated to only the poorest or most crowded areas of cities. Public
health workers take a great deal of care to find the target population for their
interventions, which often means identifying those people who are at highest risk for

disease and providing them with both preventative and therapeutic interventions that are not directed to the general population.

It has been observed that the American population tends to cluster around sexual activity "classes", in which a majority of people have a low level of sexual activity, and a smaller pool of people have very high rates of activity. A question has been whether it is more worthwhile to focus many resources for sexually transmitted disease prevention or treatment on a few people at the high end of the activity distribution, or whether a more even spread of resources across a broader population would result in less overall disease burden at the population-level.

To address the dilemma of whether targeting treatment or broadening treatment might have more impact, let's build a model to simulate a simple heterosexually-transmitted STD. Suppose we want a model of a disease like gonorrhea, in which infected/infectious people can be treated and return to the susceptible state without immunity, meaning that instead of an SIR model, we just have an SI model.

As with any other model, we can start the modeling process by drawing a diagram describing our model, followed by a set of equations translating our diagram into symbols.



In Figure 6.5, we have drawn an SI model, but created four subsets of persons for each of the four subsets of a heterosexual STD epidemic: high-activity men, high-activity women, low-activity men, and low-activity women. We end up with eight states to draw, because we have two states of disease, for each of two sexes, for each of two classes of sexual activity.

Since we are only simulating heterosexual transmission of the STD, we will have the rate of infection among men depend on the prevalence of infected women, and the rate of infection among women depend on the prevalence of infected men.

But a key challenge is how we can model the transmission rate. We need some strategy to overcome the Law of Mass Action. Rather than simply providing an estimate of the transmission risk coefficient—for all people, we need to account for the differences in risk levels between the high-activity and low-activity groups of people.

One strategy to account for the complex mixing of people would be to break up the general transmission risk coefficient—into three underlying component parts: (1) a part that has to do with the rate of risky contact (e.g., unprotected sexual encounters per year); (2) a second part that has to do with the biology of the organism being analyzed (e.g., the probability of transmission of the organism from one person to another, per each unprotected sexual encounter between a susceptible and an infected person); and (3) a third part, which captures the probability of mixing with a person of the same or different activity level (i.e., is transmission from a high-activity or lowactivity person, or vice versa, or between high and high or low and low). Let's say that the rate of unprotected contact is variable c, the probability of transmission of the organism from an infected to a susceptible person per unprotected contact is p, and the probability of mixing with a person of the same or different class is w. Hence,  $= c \times p$ x w. An advantage of breaking up one variable into two components, in this case, is that the interventions that we'll model may alter the rate of risky contact (e.g., educational interventions), and/or the probability of transmission (e.g., condom use), hence the extra complexity is justified since we know what the impact of STD-related interventions are on these parameters, but we don't know their effect on a generic transmission rate

Furthermore, it's not simply the case that highly-active people interact with people who have high activity, and vice versa. Otherwise we would have two different populations of people altogether; to the contrary, there are a proportion of people who mix between the two groups. This can be represented by a matrix, often called the "contact matrix", "mixing matrix", or "who acquires infection from whom" (WAIFW) matrix. Table 6.1 provides an example of a WAIFW matrix, which we note is not symmetrical because from the perspective of a high-activity person, the chances of

encountering another highly-active person is much greater than the probability of encountering a low-activity person.

Table 6.1:

Example of a who acquires infection from whom (WAIFW) matrix

Contact matrix (w)	Probability each sexual encounter is with:	
Subject:	low activity person	high activity person
low activity person	0.6	0.4
high activity person	0.1	0.9

To refer to this matrix, we can use conventional notation: w[row, column], such that w[1,1] means the probability a low activity person has unprotected sex with a low activity person, 0.6. Similarly, w[1,2] means the probability a low activity person has sex with a high activity person, 0.4. If the matrix were different between men and women, we could use two matrices (one for each gender), but we can assume the same matrix for men and women for simplicity in this example.

Next, we can write down equations for our model. Looking at our model diagram, we will have eight equations for each of the eight categories of people, where we can use the subscript m to refer to men, f to refer to women, h to refer to high-activity, and j to refer to low-activity. For simplicity, we will also assume that birth and death are such

small rates from the perspective of a short-term STD epidemic that we will omit those rates from these equations and just focus on infection and recovery (rate v):

[Equation 6.5] 
$$\frac{dS_{m,h}}{dt} = -pc_h(w[2,1]I_{f,j} + w[2,2]I_{f,h})S_{m,h} + vI_{m,h}$$
[Equation 6.6] 
$$\frac{dI_{m,h}}{dt} = +pc_h(w[2,1]I_{f,j} + w[2,2]I_{f,h})S_{m,h} - vI_{m,h}$$

[Equation 6.6] 
$$\frac{dI_{m,h}}{dt} = +pc_h(w[2,1]I_{f,j} + w[2,2]I_{f,h})S_{m,h} - vI_{m,h}$$

[Equation 6.7] 
$$\frac{dS_{f,h}}{dt} = -pc_h(w[2,1]I_{m,j} + w[2,2]I_{m,h})S_{f,h} + vI_{f,h}$$

[Equation 6.8] 
$$\frac{dI_{f,h}}{dt} = + pc_h \big( w[2,1] I_{m,j} + w[2,2] I_{m,h} \big) S_{f,h} - v I_{f,h}$$

[Equation 6.9] 
$$\frac{dS_{m,j}}{dt} = -pc_j(w[1,1]I_{f,j} + w[1,2]I_{f,h})S_{m,j} + vI_{m,j}$$

[Equation 6.10] 
$$\frac{dI_{m,j}}{dt} = + pc_j (w[1,1]I_{f,j} + w[1,2]I_{f,h})S_{m,j} - vI_{m,j}$$

[Equation 6.11] 
$$\frac{dS_{f,j}}{dt} = -pc_j(w[1,1]I_{m,j} + w[1,2]I_{m,h})S_{f,j} + vI_{f,j}$$

[Equation 6.12] 
$$\frac{dI_{f,j}}{dt} = +pc_j (w[1,1]I_{m,j} + w[1,2]I_{m,h})S_{f,j} - vI_{f,j}$$

In each equation, we see that the infection rate is a product of the biological probability of transmission upon an unprotected encounter, the rate of such encounters (conditional on the activity class of the person), the probability that the infected person being contacted is of one class or another (high- or low-activity), and the prevalence of infection among such persons. The textbook website has accompanying R code to implement this model. As with prior models, we begin the model with the input parameters, which in this case include a contact vector with two components (a value of 5 per year for high-risk people and 1 per year for low-risk people), and a WAIFW matrix:

```
p = 0.00015
c = c(1,5)
w = matrix(c(.6,.4,.1,.9),ncol=2,byrow=TRUE)
v=2
```

We next set the time horizon for the model and the time steps:

```
\begin{array}{l} time = 10 \\ dt = 0.01 \end{array}
```

As with other models, we specify initial conditions and starting vectors for our states; in this case, we have arbitrarily split the population into 50% males and 50% females, with 10% of each sex in the high-activity class, and use a for loop to make it easier for us to keep track of the susceptible and infected people. In particular, we create a matrix for susceptible and for infected people, with rows corresponding to sexes and columns corresponding to activity classes (low or high activity class(:

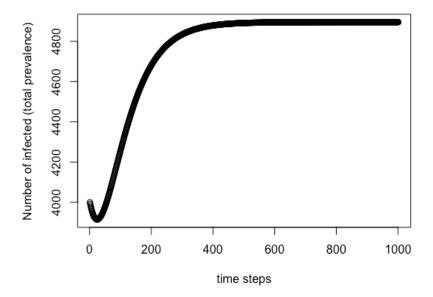
```
S = matrix(ncol=2,nrow=2) \\ I = matrix(ncol=2,nrow=2) \\ for (sex in 1:2) \\ for (group in 1:2) \\ S[sex,group]=4000 \\ I[sex,group]=1000 \\ \} \\ \}
```

Inside our for loop, we insert the equations just as they appear in Equations 6.5 through 6.12, but using R's ability to lookup the c vector and w matrix to find the right beta for each group of people and to fill in the values over a loop across both sexes and both activity classes, saving us from having to type out eight equations. Here we define a vector 'Numinf' to keep track of the total number of people infected in each time step:

```
\label{eq:beta_ematrix} \begin{split} & \text{beta} = \text{matrix}(\text{ncol} = 2, \text{nrow} = 2) \\ & \text{Numinf} = \text{sum}(I) \\ & \text{for (i in 1:(time/dt))} \{ \\ & \text{for (sex in 1:2)} \{ \\ & \text{for (group in 1:2)} \{ \\ & \text{beta[sex,group]} = \text{p*c[group]*(w[group,1]*I[3-sex,1]+w[group,2]*I[3-sex,2])} \\ & \text{S[sex,group]} = \text{S[sex,group]} - \text{beta[sex,group]*S[sex,group]*dt} + \text{v*I[sex,group]*dt} \\ & \text{I[sex,group]} = \text{I[sex,group]} + \text{beta[sex,group]*S[sex,group]*dt} - \text{v*I[sex,group]*dt} \\ & \text{} \} \\ & \text{} \} \\ & \text{Numinf} = \text{c(Numinf,sum}(I)) \\ \} \end{split}
```

Finally, after our "for loop", we can plot the total number of people infected over each time step:

plot(Numinf)



As shown in Figure 6.6, the number of infected people decreases then increases over time.

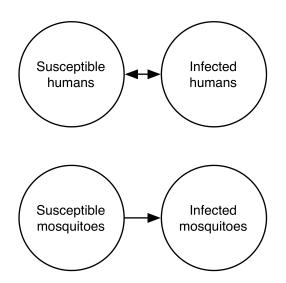
Overall, the example of the STD epidemic shows us how an SIR model can be extended when we wish to depart from the Law of Mass Action and instead consider a heterogeneous mixing matrix. As illustrated in this example, even a simple deviation to two classes of risk produces a large number of equations and complexities for modeling. An even more complex strategy for modeling heterogeneous transmission is the approach of simulating dynamic social networks and how they influence disease transmission. Although the mathematics of network simulation are beyond the scope of this book, the 'EpiModel' package in R provides a user-friendly approach to simulate

epidemics over networks, and can be installed and utilized just like any other package to produce simulations of epidemics incorporating dynamic social networks.

# <2>Vector-borne disease

Particularly in the context of climate change and rising temperatures that spread mosquitoes and other insects, infectious disease epidemiologists are increasingly concerned about the potential threat of increasing vector-borne (e.g., mosquito-driven) epidemics. When more than one species is involved in the spread of disease, it may not be obvious how we can adapt the Kermack-McKendrick model to address epidemics of vector-borne disease. Here, we illustrate how SIR-type models can be extended to address diseases where more than just the human species is involved.

Suppose, for example, that we wish to simulate the prevalence of malaria. We can simulate malaria as an SI model in which both humans and mosquitoes can be infected, as shown in Figure 6.7. Note that while humans can recover from infection, mosquitoes typically do not.



We can designate humans with subscript h and mosquitoes as subscript m. Humans catch malaria from mosquitoes, and mosquitoes catch malaria from humans. Translating these dynamics into equations, we have Equations 6.13 through 6.16:

[Equation 6.13] 
$$\frac{dS_h}{dt} = \mu_h N_h + v I_h - \beta I_m S_h - \mu_h S_h$$

[Equation 6.14] 
$$\frac{dI_h}{dt} = \beta I_m S_h - v I_h - \kappa_h I_h - \mu_h I_h$$

[Equation 6.15] 
$$\frac{dS_m}{dt} = \mu_m N_m - \beta I_h S_m - \mu_m S_m$$

[Equation 6.16] 
$$\frac{dI_m}{dt} = \beta I_h S_m - \kappa_m I_m - \mu_m I_m$$

We can see that the first two equations describe an SI model among humans with recovery rate v and death rate from malaria . The rate of infection depends on the number of infected mosquitoes. Similarly, mosquitoes face an infection rate dependent on the number of infected humans. The R code corresponding to this model can be downloaded from the textbook website. First, we used the following parameters vectors, where the first element of each vector is the parameter corresponding to humans, and the second is the parameter corresponding to mosquitoes, with time units in years:

$$mu = c(.015,12)$$
  
beta = 0.00003

```
kappa = c(1/5, 10)
v = 2
```

Second, we specify our time horizon and time step:

```
\begin{array}{l} time = 1 \\ dt = 0.0001 \end{array}
```

Here, we've intentionally chosen to simulate just one year in very small time steps to illustrate the complex dynamics between humans and mosquitoes.

Next, we specify our initial conditions and populate empty vectors:

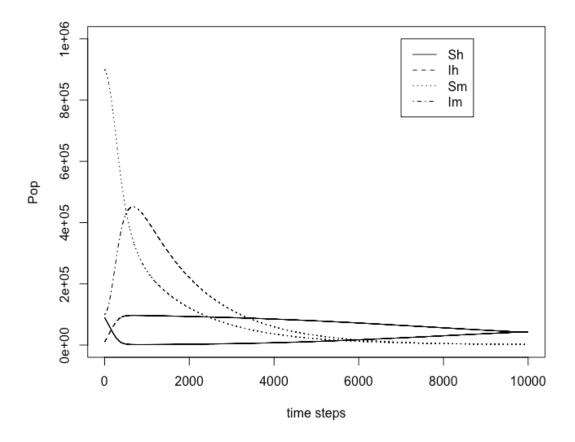
```
Sh = 90000
Ih = 10000
Sm = 900000
Im = 100000
Shvec = Sh
Ihvec = Ih
Smvec = Sm
Imvec = Im
```

Finally, we insert our equations into a for loop:

```
 \begin{array}{l} \mbox{for (i in 1:time)} \{ \\ \mbox{for (i in 1:(1/dt))} \{ \\ \mbox{Nh} = \mbox{Sh} + \mbox{Im} \\ \mbox{Nm} = \mbox{Sm} + \mbox{Im} \\ \mbox{Sh} = \mbox{Sh} + \mbox{mu[1]}^* \mbox{Nh}^* \mbox{dt} + \mbox{v}^* \mbox{Ih}^* \mbox{dt} - \mbox{beta}^* \mbox{Im}^* \mbox{Sh}^* \mbox{dt} - \mbox{mu[1]}^* \mbox{Sh}^* \mbox{dt} \\ \mbox{Sm} = \mbox{Sm} + \mbox{mu[2]}^* \mbox{Nm}^* \mbox{dt} - \mbox{beta}^* \mbox{Ih}^* \mbox{Sm}^* \mbox{dt} - \mbox{mu[2]}^* \mbox{Sm}^* \mbox{dt} \\ \mbox{Im} = \mbox{Im} + \mbox{beta}^* \mbox{Ih}^* \mbox{Sm}^* \mbox{dt} - \mbox{kappa[2]}^* \mbox{Im}^* \mbox{dt} - \mbox{mu[2]}^* \mbox{Im}^* \mbox{dt} \\ \mbox{Shvec} = \mbox{c}(\mbox{Shvec}, \mbox{Sh}) \\ \mbox{Ihvec} = \mbox{c}(\mbox{Ihvec}, \mbox{Ih}) \\ \mbox{Smvec} = \mbox{c}(\mbox{Smvec}, \mbox{Sm}) \\ \mbox{Imvec} = \mbox{c}(\mbox{Imvec}, \mbox{Im}) \\ \mbox{Smvec} = \mbox{c}(\mbox{Imvec}, \mbox{Imvec}, \mbox{Imvec
```

When we insert commands to plot our output, we obtain Figure 6.8:

```
\label{localization} $\operatorname{plot}(\operatorname{Shvec,lty=1,type="l",xlab="time steps",ylab="Pop",ylim=c(0,1000000))$ lines(Ihvec,lty=2) lines(\operatorname{Smvec,lty=3}) lines(\operatorname{Imvec,lty=4}) legend(7000,1000000,c("Sh","Ih","Sm","Im"),lty=c(1,2,3,4)) \\
```



We see that because humans and mosquitoes live on such different time scales, the prevalence of malaria tends to change wildly as the two species infect each other. One can further introduce seasonality by adjusting the birth rate of mosquitoes to be a sine wave over time, enabling us to re-introduce more susceptible mosquitoes over time, in turn producing new waves of infection and a harmonic back-and-forth of infection seasons.

Overall, we can see from this Chapter that the Kermack-McKendrick model is not limited in its capacity, but actually quite versatile in how it can be extended to a wide range of infectious diseases and interventions. Our models can serve as a complex and meaningful tool for public health planners to understand the dynamics of infectious diseases, allowing us to combine our knowledge of disease with our knowledge of populations to gain a sense of how we might better prevent and treat epidemic diseases.