

## **Multivariable Calculus**

## **BSCS Semester III**

**Department of Computer Science Bahria University, Lahore Campus** 

## **Assignment:**

Deadline: Week 6, 1 April 2023

Evaluation of CLO	Question Number	Marks	Obtained Marks
CLO1: CLO statement Comprehend the basic concepts and techniques of differential and integral calculus of functions of several	1,2,3	10+5+10=25	
variables. <b>CLO3: CLO statement</b> Analyze the given problems and apply integrals to compute physical quantities like area/volume.	4	10	
Tota	al Marks	35	

**Question 1.** The weekly consumption of chicken, C = f(I, P), (in Kgs) of an average household as a function of the price of chicken in ( $\S\kg$ ) and I, annual household income (in  $\S$  1000s) as shown in the following table

P	3.00	3.50	4.00	4.50
20	2.65	2.59	2.51	2.43
40	4.14	4.05	3.94	3.88
60	5.11	5.00	4.97	4.84
80	5.35	5.29	5.19	5.07
100	5.79	5.77	5.60	5.53

- a) Evaluate  $f_I(80,4.00)$  and  $f_P(40,4.50)$ , also interpret it.
- b) Write down the table for f(20, P).
- c) Write down the table for f(1, 3.5).

**Question 2.** Let h(x,t) = 5 + cos(0.5x - t) describe a wave. The value of h(x,t) gives the depth of the water in cm at a distance x meters from a fixed point and at time t seconds. Evaluate  $h_x(2,5)$  and  $h_t(2,5)$  and interpret each in terms of the wave.

**Question#3** For the function  $u = \frac{1}{\sqrt{x^2 + y^2 + z^2}}$  verify  $u_{xx} + u_{yy} + u_{zz} = 0$ .

## Question#4

- **a)** Evaluate  $\int_0^{\ln 2} \int_0^{\ln 3} e^{x+y} \ dx \ dy$ .
- b) Find the volume of the solid lying under the surface  $f(x,y) = 3x^3 + 3x^2y$  and over the region  $R: 1 \le x \le 3, 0 \le y \le 2$ .