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Assignment: 1

Ques) Analysis:

Lets analyze loop step by step

- 1) initialization: The loop initialize  $i$  with  $n$
- 2) condition: The loop continue as long as  $i > 1$
- 3) update: In each iteration,  $i$  is updated to  $\text{fun}(i)$
- 4) Body: The contain some  $O(1)$  expression

Worst case Analysis:

The worst case time is depend on the number of iteration the loop will perform

Lets assume that  $\text{fun}(i)$  reduces  $i$  by constant factor say ' $c$ '

In geometric form

$$n, \frac{n}{c}, \frac{n}{c^2}, \dots$$

let  $K$  be the number of iteration

$$\frac{n}{c^K} < 1$$

Solving for  $k$ ,

$$k > \log_c(n)$$

Therefore, the worst case time complexity is :  $O(\log n)$

when  $\text{fun}(i)$  reduces  $i$  by a constant factor in each iteration  
 "Logarithm"

Ans 2) The first loop has a time complexity of  $O\left(\frac{n}{c}\right)$

The second loop has a time complexity :  $O\left(\frac{n}{c}\right)$

Worst case:

first The worst-case time complexity is  $O(n/c)$  (assuming  $c > 0$ )

second The worst-case time complexity is  $\bar{O}\left(\frac{n}{c}\right)$  (assuming  $c > 0$ )  
 "Linear"

Ques 3.) Basic operation:

→ comparison and swap inside the loop

.) loop Analysis :-

→ The outer loop runs 'n' times

→ n is the size of input array

→ Inner loop perform on the current iteration of outer loop.

.) Time complexity:

→ The inner loop perform  $\frac{n \cdot (n-1)}{2}$  in

the worst case

.) Expressing complexity :-

→ The overall time complexity is  $O(n^2)$

because the dominant term is  $n^2$

"Quadratic complexity"