

### **Bahria University**

# Lahore Campus Department of Computer Sciences

## THEORY OF AUTOMATA

#### **Assignment #01**

**DUE DATE: 14, OCTOBER 2023** 

Instructor Name: Mr. Tahir Iqbal

**Program:** BSCS 4A

#### Q.1 Consider the following recursive definition of PALINDROME:

- a. Rule 1. a and b are in PLANILDROME
   Rule 2. If x is in PALINDROME then so are axa and bxb.
   Unfortunately the words defined by the rules have odd lengths. Fix the problem such that all appropriate words are included.
- b. Prove that if x is in PALINDROME then so is  $x^n$  for any n.
- c. Prove that if  $z^n$  is in PALINDROME (for positive integer n) then so is z.
- d. Prove that PALINDROME has as many word of length 2n as it does of length 2n-1. How many words is that?
- Q.2 Construct a regular expression defining each of the following languages over {a, b};
  - a. All strings such that the number of a's is a multiple of 3.
  - b. All strings such that the number of a's is odd.
- Q.3 Construct a regular expression over  $\{a, b\}$  of all words that do not have both the substrings bba and abb.
- Q.4 Construct a regular expression over  $\{a, b\}$  containing all string that have an even number of a's an odd number of b's
- Q.5 Show that the following pair of regular expressions define the same language over alphabet  $\{a, b\}$ : a(ba+a)\*b and aa\*b(aa\*b)\*
- Q.6 Show that the following pair of regular expressions define the same language over alphabet  $\{a, b\}$ :  $a(aa)*(\Lambda+a)b+b$  and a\*b