

Assignment No. 1

Theory of Automata

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Q No 1)

(b) prove that if x is in palindrome then so is x^n for any n

step 1: x^n is also in palindrome for $n=1$

step 2: if x is in palindrome, then so is xx

step 3: All above are the recursive language

(c) prove that if 2^n is in palindrome then so is 2

step 1: if 2^n ($n=1$) is in palindrome then 2 is in palindrome

step 2: if 2^k is in palindrome, then 2 is 2

step 3: All above are recursive language

(a) prove that a palindrome has as many words of length $2n$ as it does of length $2n-1$. How many words is that?

step 1. $2n$ and $2n-1$ words of length is in palindrome

step 2. The number of words of length $2n$ is 2^n , and the number of words of length $2n-1$ is also 2^n . Therefore a palindrome has as many of length $2n$ as it does of length $2n-1$, and there are 2^n words of each length.

step 3. All above are recursive language.

Q No 2)

(a) All string such that the number of a's is a multiple of 3.

Ans $b^* (aaa)^* + (aaa)^* b^* + b^* (aaa)^* b^*$

(b) All string such that the number of a's is odd.

Ans ~~$(a+b)^*$~~

Q No 4) over $\{a, b\}$ of all words that do not have the substring bba and abb .

Ans $[a^+bb^+ + bb^+a^+]$

Q No 5) over $\{a, b\}$ containing all string that have an even number of a 's and an odd number of b 's

Ans $^+[(aa + bb + (ab + ba)(aa + bb))^+ (ab + ba)]$

Q No 6) define the same language over alphabet $\{a, b\}$,

1) $a(ba + a)^+b$

$L = \{ aab, abab, ab, ababab, aabab, aababab, \dots \}$

2) $aab/aab)^+$

$L = \{ aab, abab, aabab, aababab \}$

Qno 6) Define the language over alphabet $\{a, b\}$ $a(aa)^n(bbb)^m$ and ab

1) $L = \{ aabb, aab, aaaaaabb, abbb \dots \}$

2) $L = \{ ab, aab, aabb \dots \}$