

به نام خدا



Performance Evaluation of Computer Systems

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Performance Modeling and Design of Computer Systems

7- MODIFICATION ANALYSIS: “WHAT-IF” FOR CLOSED SYSTEMS

Asymptotic Bounds for Closed Systems

- **m** : number of devices in our system
- $D = \sum_{i=1}^m E[D_i]$
- $D_{\max} = \max_i \{E[D_i]\}$
- Bounds are **asymptotes** → For large **N** or small **N**, the curve comes very close to touching these lines

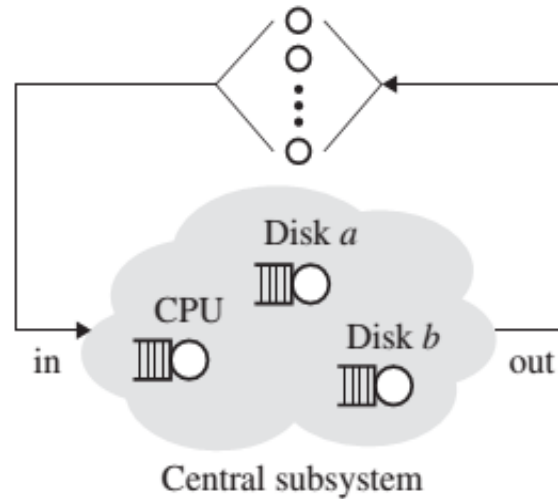
Theorem 7.1 *For any closed interactive system with N terminals,*

$$X \leq \min \left(\frac{N}{D + \mathbf{E}[Z]}, \frac{1}{D_{\max}} \right).$$
$$\mathbf{E}[R] \geq \max (D, N \cdot D_{\max} - \mathbf{E}[Z]).$$

Importantly, the first term in each clause ($\frac{N}{D + \mathbf{E}[Z]}$ or D) is an asymptote for small N , and the second term ($\frac{1}{D_{\max}}$ or $N \cdot D_{\max} - \mathbf{E}[Z]$) is an asymptote for large N .

Example

- $\mathbf{E}[Z] = 18$
- $\mathbf{E}[D_{\text{CPU}}] = 5 \text{ sec}$
- $\mathbf{E}[D_{\text{disk a}}] = 4 \text{ sec}$
- $\mathbf{E}[D_{\text{disk b}}] = 3 \text{ sec}$

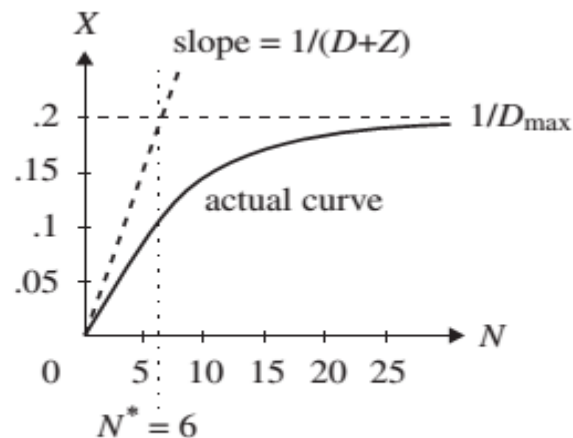


- $\mathbf{X} ?$
- $\mathbf{E}[R] ?$

Example

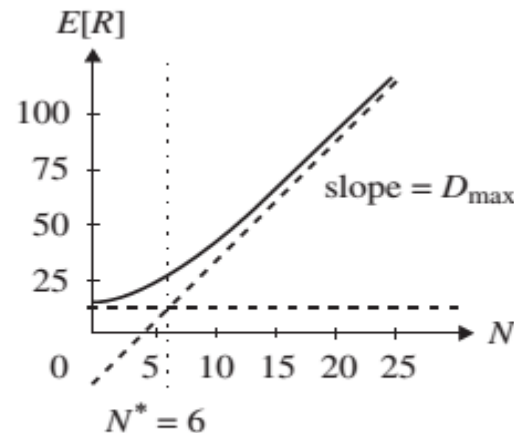
- $D = 5 + 4 + 3 = 12$ seconds
- $D_{\max} = 5$ (the CPU is the bottleneck device)

$$X \leq \min\{N/30, 1/5\}$$



(a) X versus N

$$\mathbf{E}[R] \geq \max\{12, 5N - 18\}$$



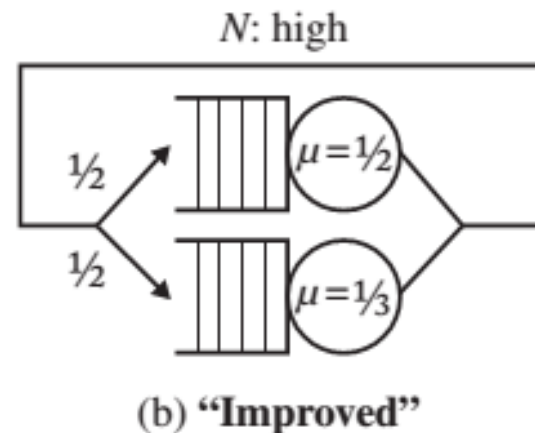
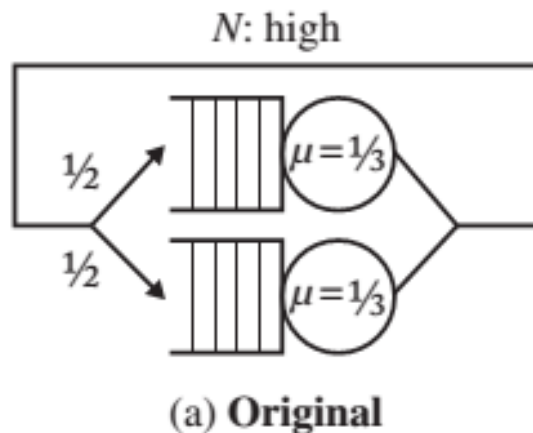
(b) $\mathbf{E}[R]$ versus N

N^* ?

- Point beyond which there must be some queuing in the system ($E[R] > D$)
- N : fixed and $N > N^*$
 - Get more throughput \rightarrow Decrease D_{max}
 - Get lower response time \rightarrow Decrease D_{max}
 - Decrease $D_{next_to_max}$?
 - Performance for $N \gg N^*$ does not change
 - Performance for $N \ll N^*$ will improve a little

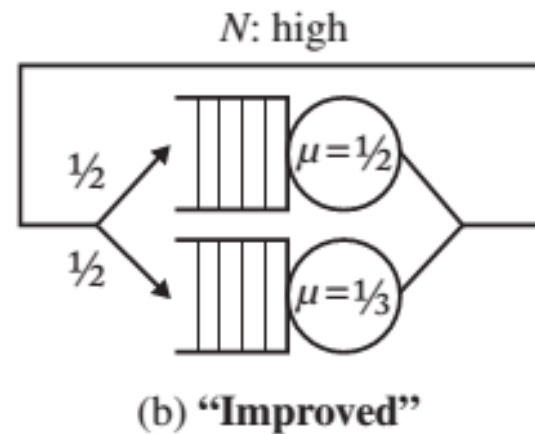
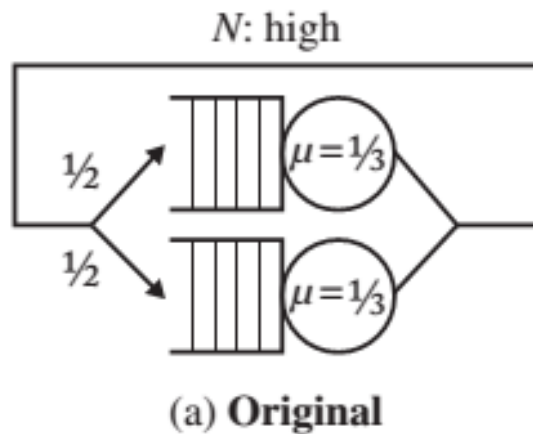
Modification Analysis

- How much does the throughput improve?
- How much does the mean response time improve?



Modification Analysis

- **Neither throughput nor mean response time changes!**



Summary

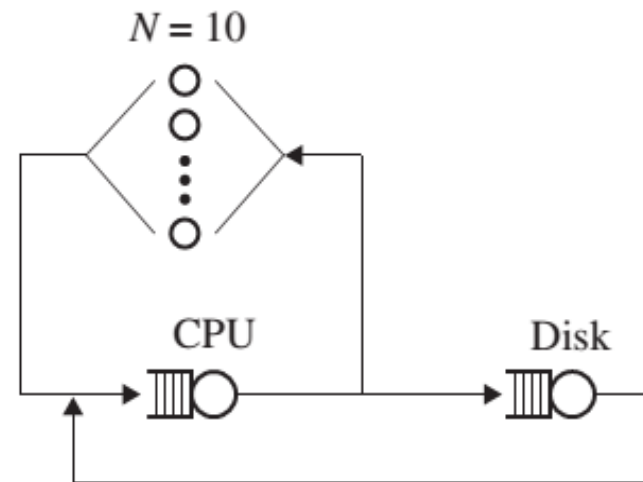
- D_{max} : **Bottleneck device**
- Key limiting factor to improve system performance
- Improving other devices will have little effect

Example

- $D_{cpu} = 4.6$ and $D_{disk} = 4.0$
- $D_{cpu} = 4.9$ and $D_{disk} = 1.9$

$$N_A^* = \frac{D + \mathbf{E}[Z]}{D_{\max}} = \frac{13.6}{4.6} < 3$$

$$N_B^* = \frac{11.8}{4.9} < 3$$



- For both systems : $N \gg N^*$
- A wins \rightarrow lower D_{\max}

Modification Analysis

- Easy and computation-feasible
- Independent of any assumption such as
 - Distribution of the service time
 - Distribution of the inter-arrival time
 - Scheduling order
- If N is sufficiently far from N^*
 - These bounds are sufficient to analyze

Why don't they make sense for open networks?

- Because they are not asymptotic bounds in the open case!
- Still : $X \leq \frac{1}{D_{max}}$
 - We know $X = \lambda$
 - So, it is not a tight upper bound
 - The same is true for $E[R]$
- It applies only if
 - Outside arrival rate is high enough that X is close to $\frac{1}{D_{max}}$

Modification Analysis

- **Open Network**
 - The mean response time, $E[T]$, will certainly improve by speeding up just one of the two devices

