



Machine Design Project

Mechanism Analysis (54)

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1 Mechanism

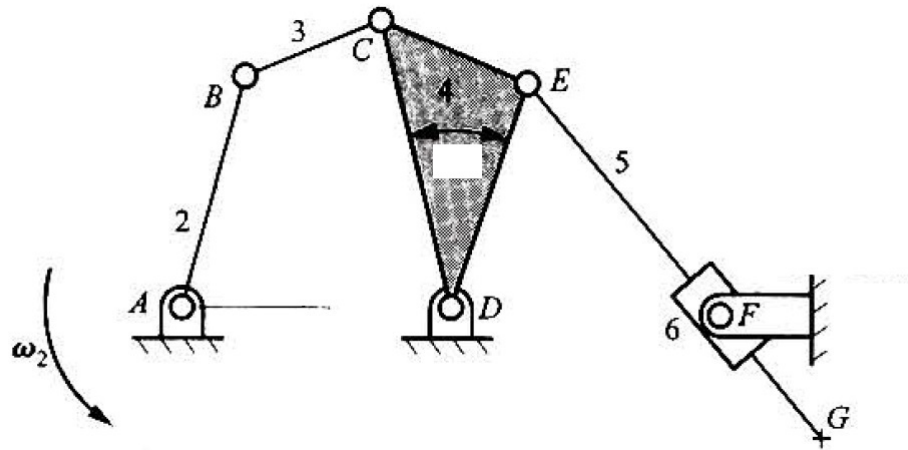


Figure 1: Slider crank mechanism connected with a 3 bar mechanism

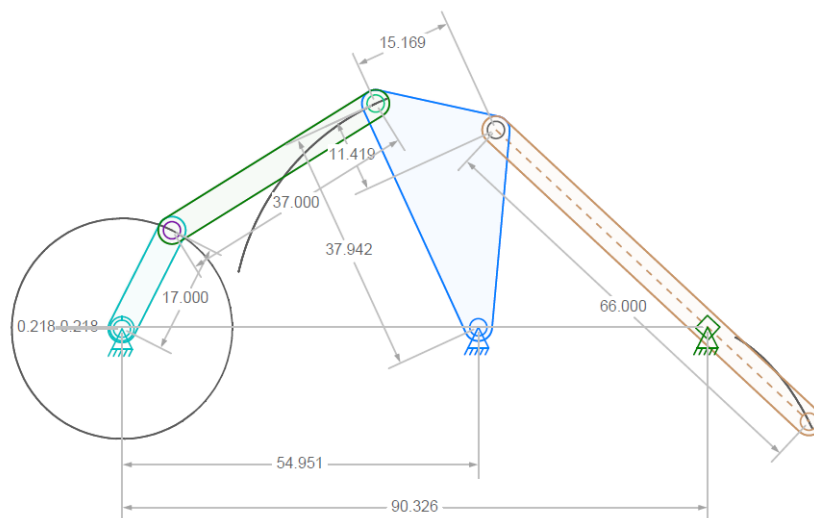


Figure 2: The mechanism's motion analysis using LINKAGE

- **Dimensions assumption:** $r_1 = 54.951\text{cm}$, $r_2 = 17\text{cm}$, $r_3 = 34.8\text{ cm}$, $r_4 = 37.942\text{ cm}$, $r_5 = 43.71\text{ cm}$, $r_6 = 34.8\text{ cm}$. $\omega_2 = 50\text{ rpm} = 5.23\text{ rad/s}$

2 Polar Analysis

The analysis is divided into two parts first part for the first mechanism and the second is related to the other one.

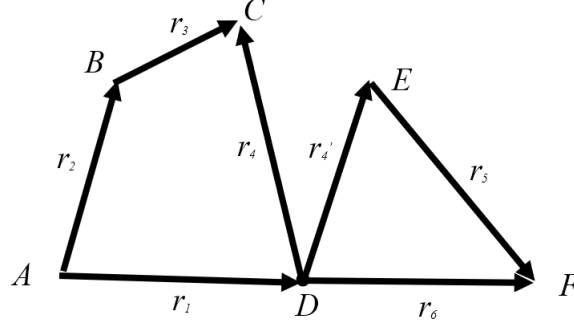


Figure 3: Mechanism analysis

2.1 Position Analysis

- $r_2 + r_3 = r_1 + r_4$

$$x : r_2 \cos \theta_2 + r_3 \cos \theta_3 = r_1 + r_4 \cos \theta_4 \quad (1)$$

$$y : r_2 \sin \theta_2 + r_3 \sin \theta_3 = r_4 \sin \theta_4 \quad (2)$$

input : θ_2 output : θ_3, θ_4

- $r_4' + r_5 = r_6$

$$x : r_4' \cos \theta_4' + r_5 \cos \theta_5 = r_6 \quad (3)$$

$$y : r_4' \sin \theta_4' + r_5 \sin \theta_5 = 0 \quad (4)$$

input : θ_4' output : θ_5, r_5

2.2 Velocity Analysis

- $r_2 + r_3 = r_1 + r_4$

$$\dot{x} : -r_2 \sin \theta_2 \omega_2 - r_3 \sin \theta_3 \omega_3 = -r_4 \sin \theta_4 \omega_4 \quad (5)$$

$$\dot{y} : r_2 \cos \theta_2 \omega_2 + r_3 \cos \theta_3 \omega_3 = r_4 \cos \theta_4 \omega_4 \quad (6)$$

input : ω_2 output : ω_3, ω_4

- $r_4' + r_5 = r_6$

$$\dot{x} : -r_4' \sin \theta_4' \omega_4 - r_5 \sin \theta_5 \omega_5 + r_5 \cos \theta_5 \dot{r}_5 = 0 \quad (7)$$

$$\dot{y} : r_4' \cos \theta_4' \omega_4 + r_5 \cos \theta_5 \omega_5 + r_5 \sin \theta_5 \dot{r}_5 = 0 \quad (8)$$

input : ω_4 output : ω_5, r_5

2.3 Acceleration Analysis

- $r_2 + r_3 = r_1 + r_4$

$$\ddot{x} : -r_2 \cos \theta_2 \omega_2^2 + r_3 \cos \theta_3 \omega_3 = r_1 + r_4 \cos \theta_4 \omega_4 \quad (9)$$

$$\ddot{y} : r_2 \sin \theta_2 \omega_2^2 + r_3 \sin \theta_3 \omega_3 = r_1 + r_4 \sin \theta_4 \omega_4 \quad (10)$$

input : $\alpha_2 \omega_2 \omega_3$ output : α_4, α_4

- $r_4' + r_5 = r_6$

$$\ddot{x} : -r_4' \cos \theta_4' \omega_4^2 - r_4' \sin \theta_4' \alpha_4 - r_5 \sin \theta_5 \omega_5^2 - r_5 \sin \theta_5 \alpha_5 - r_5 \sin \theta_5 \omega_5 \dot{r}_5 - r_5 \sin \theta_5 \omega_5 \dot{r}_5 + r_5 \cos \theta_5 \ddot{r}_5 = 0 \quad (11)$$

$$\ddot{y} : r_4' \sin \theta_4' \omega_4^2 + r_4' \cos \theta_4' \alpha_4 - r_5 \sin \theta_5 \omega_5^2 + r_5 \cos \theta_5 \alpha_5 + r_5 \cos \theta_5 \omega_5 \dot{r}_5 + r_5 \cos \theta_5 \omega_5 \dot{r}_5 + r_5 \sin \theta_5 \ddot{r}_5 = 0 \quad (12)$$

input : $\omega_4 \alpha_4 \omega_5$ output : α_5, \ddot{r}_5

3 Analytical Solution

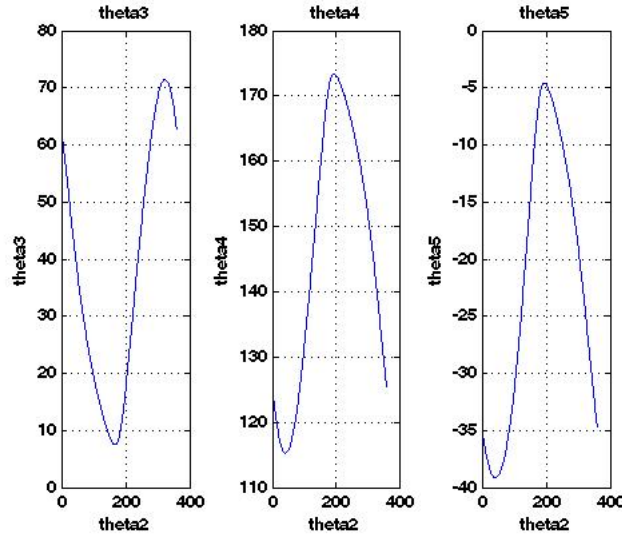


Figure 4: Position Graphs

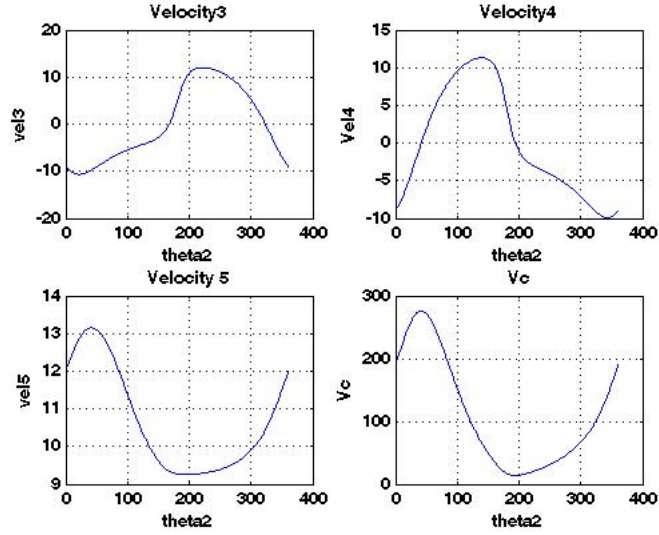


Figure 5: Velocity Graphs

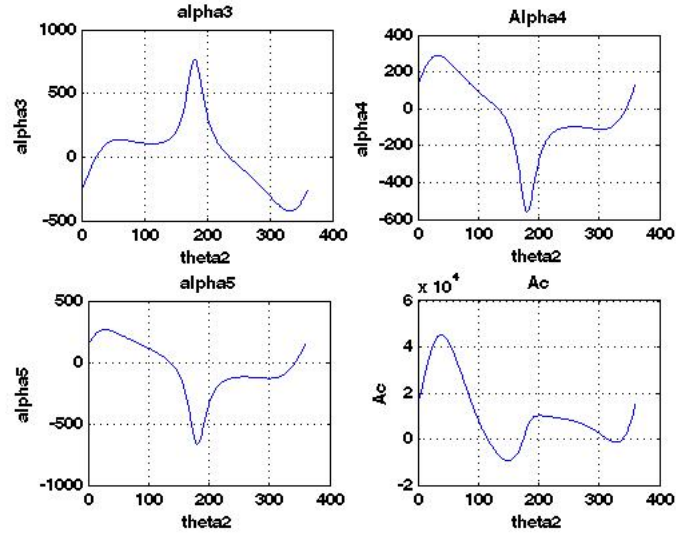


Figure 6: Acceleration Graphs

4 MATLAB codes

4.1 Position 1

```

1 function w=Position1(output , input)
2 r1 = 54.951;
3 r2 = 17;
4 r3 = 34.8;
5 r4 = 37.942;
6 w=[(r2*(cosd(input)))-r1+(r3*cosd(output(1)))-(r4*cosd(output(2)))]

```

```

;
7 (r2*sind(input))+(r3*sind(output(1)))-(r4*sind(output(2)))] ;
8 end

```

4.2 Position 2

```

1 function w=Position2(output, input)
2
3 r4_2 =30.5 ;
4 r5 = 43.71 ;
5 theta5=output(1);
6 r6 = output(2) ;
7 w=[(r4_2*(cosd(input)))+(r5*cosd(theta5))-r6 ;
8 (r4_2*sind(input))+(r5*sind(theta5))];
9 end

```

4.3 Velocity 1

```

1 function w=velocity1(output, input)
2 omega2=20;
3 r2 = 17;
4 r3 = 34.8;
5 r4 = 37.942;
6 theta2=input(1);
7 theta3=input(2);
8 theta4=input(3);
9 omega3=output(1);
10 omega4=output(2);
11 w=[omega2*r2*sind(theta2)+omega3*r3*sind(theta3)-omega4*r4*sind(
    theta4);
12 omega2*r2*cosd(theta2)+omega3*r3*cosd(theta3)-omega4*r4*cosd(
    theta4)];
13 end

```

4.4 Velocity 2

```

1 function w=velocity2(output, input)
2 r4_2 =30.5 ;
3 r5 = 43.71 ;
4 r6 = 34.8 ;
5 theta4_2=input(1);
6 theta5=input(2);
7 omega4=input(3);
8 omega5=output(1);
9 Vc=output(2);
10 w=[omega4*r4_2*sind(theta4_2)+omega5*r5*sind(theta5)-Vc*cosd(
    theta5);

```

```

11 omega4*r4_2*cosd(theta4_2)+omega5*r5*cosd(theta5)+Vc*sind(theta5)
    ];
12 end

```

4.5 Acceleration1

```

1 function w=Acceleration1(output , input)
2 r4_2 =168 ;
3 r5 = 141 ;
4 theta4_2=input(1);
5 theta5=input(2);
6 omega4 =input(4);
7 omega5 = input(5);
8 Vc=input(6);
9 alpha4 = input(7);
10 alpha5 = output(1);
11 Ac = output(2);
12 w=[((-alpha4)*r4_2*sind(theta4_2))-((omega4^2)*cosd(theta4_2)*
    r4_2)+(Ac*cosd(theta5))-((omega5)*sind(theta5)*Vc)-((omega5)*
    sind(theta5)*Vc)-((omega5^2)*cosd(theta5)*r5)-((alpha5)*sind(
    theta5)*r5));
13 (((r4_2)*cosd(theta4_2)*alpha4)-(r4_2*sind(theta4_2)*(omega4^2)))+(
    Ac*sind(theta5))+(Vc*cosd(theta5)*omega5)+(Vc*cosd(theta5)*
    omega5)-(r5*sind(theta5)*(omega5^2))+(r5*cosd(theta5)*alpha5))
    ];
14 end

```

4.6 Acceleration 2

```

1 function w=Acceleration1(output , input)
2 r4_2 =168 ;
3 r5 = 141 ;
4 theta4_2=input(1);
5 theta5=input(2);
6 omega4 =input(4);
7 omega5 = input(5);
8 Vc=input(6);
9 alpha4 = input(7);
10 alpha5 = output(1);
11 Ac = output(2);
12 w=[((-alpha4)*r4_2*sind(theta4_2))-((omega4^2)*cosd(theta4_2)*
    r4_2)+(Ac*cosd(theta5))-((omega5)*sind(theta5)*Vc)-((omega5)*
    sind(theta5)*Vc)-((omega5^2)*cosd(theta5)*r5)-((alpha5)*sind(
    theta5)*r5));
13 (((r4_2)*cosd(theta4_2)*alpha4)-(r4_2*sind(theta4_2)*(omega4^2)))+(
    Ac*sind(theta5))+(Vc*cosd(theta5)*omega5)+(Vc*cosd(theta5)*

```



```
    omega5)-(r5*sind(theta5)*(omega5^2))+(r5*cosd(theta5)*alpha5))  
];  
14 end
```

5 Graphical Verification

References

1. C. E. Wilson J. P. Sadler “Kinematics and Dynamics of Machinery” third Edition (2005) Pearson Education, Prentice Hall, ISBN 0-13-186-642-9
2. Robert L. Norton “ Design of Machinery”, fourth Edition (2008) McGraw Hill Publishing Co., New York, NY, ISBN 978-0-07-312158-1
3. David H. Myszka “Machines and Mechanisms – Applied Kinematic Analysis” third edition (2005) Pearson Education, Prentice Hall, ISBN 0-13-183-776-1