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Maths	Class			

# Year 11 Mathematics Preliminary Course Final Exam September 2017

Time allowed: 120 minutes

#### General Instructions:

- Marks for each question are indicated on the question.
- Approved calculators may be used
- All necessary working should be shown
- Full marks may not be awarded for careless work or illegible writing
- · Begin each question on a new page
- Write using black or blue pen
- All answers are to be in the writing booklet provided
- A reference sheet is provided at the rear of this Question Booklet, and may be removed at any time.

Section 1 Multiple Choice

Questions 1-8

8 Marks

Section II Questions 9-16

80 Marks

Total = 88 marks

# SECTION 1 (10 marks)

Choose the letter corresponding to the correct answer and fill in the Answer sheet provided at the front of your answer booklet.

# DO NOT REMOVE THIS SHEET

20 HOL KENIOVE LHIS SHEEL											
Which of the following is NOT always a true statement?											
A. The diagonals of a rhombus bisect at right angles     B. The opposite angles of a rhombus are equal											
C. The diagonals of a parallelogram bisect at right angles											
D. The opposite angles of a parallelogram are equal											
The quadratic equation $2x^2 - 4x + 5 = 0$ has:											
A. No real roots											
B. 1 real root											
C. 2 equal roots											
D. 2 distinct Real roots											
Which statement below is true for the diagram shown?											
5 60° x											
A. $\cos 60^{\circ} = \frac{5^2 + 4^2 - x^2}{2 \times 5 \times 4}$ B. $\frac{4}{\sin 60^{\circ}} = \frac{x}{\sin 100^{\circ}}$											
C. $x^2 = 25 + 16 - 2 \times 5 \times 4 \cos 60^\circ$ D. $\frac{5}{\sin 80^\circ} = \frac{x}{\sin 40^\circ}$											
Find $\lim_{x \to \infty} \frac{3x^2 - 2x + 3}{2x^2 - 5}$											

D. 1

5	If $=\frac{2\sqrt{3}+3}{\sqrt{3}-2} = x + y\sqrt{3}$ , then
and the state of t	A. $x = 12$ and $y = 7$ B. $x = -12$ and $y = 7$ C. $x = 12$ and $y = -7$ D. $x = -12$ and $y = -7$
	y = y
6	If $y = \frac{1}{(5x-1)^2}$ then $\frac{dy}{dx} =$
	A. $\frac{-10}{(5x-1)^3}$ B $\frac{-10}{(5x-1)}$ C. $\frac{-2}{(5x-1)^3}$ D. $\frac{-2}{(5x-1)}$
7	If $\cos\theta = \frac{k}{5}$ for an acute angle $\theta$ , then $\tan\theta =$
	A. $\frac{\sqrt{25-k^2}}{k}$ B. $\frac{\sqrt{25-k^2}}{5}$ C. $\frac{5}{\sqrt{25-k^2}}$ D. $\frac{k}{\sqrt{25-k^2}}$
8	If $5^{2x-1} = \frac{1}{125}$ then $x =$
	A. 13 B12 C2 D1

:

#### **SECTION 2**

Marks

Complete all answers in your answer booklet provided

# **QUESTION 9: (10 Marks)**

(a)		Expand and simplify: $(x+3)(x^2-3x+9)$	1
(b)		Solve the equation: $ 3x - 4  = 5$	2
<b>Q</b> (c)		What is the size of one of the exterior angles of a regular pentagon?	1
(d)	(i)	What are the Domain and Range of the function $f(x) = \sqrt{16 - x^2}$ ?	2
	(ii)	Sketch $y = f(x)$	2
(e)		Find the equation of the tangent to the curve $y = \frac{1}{4}x^3 - 4$ at the point P (2, $-3$ )	2

# QUESTION 10: (10 Marks) Start a new page

#### Marks

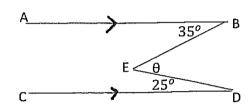
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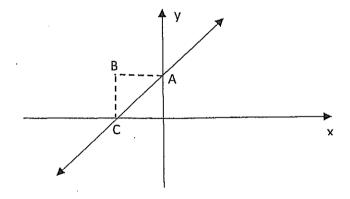
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- (a) Find the derivatives of:
  - (i)  $y = x^3 + 3x 1$
  - (ii)  $y = (3x 5)^4$
  - (iii)  $y = \frac{2}{x}$
  - (iv)  $2\sqrt{x}$
- (b) Find the size of  $\,\theta$  in the following., given AB  $\,\parallel$  CD, (no reasons necessary



(c) In the diagram below, the line AC is given as 3x - 2y + 6 = 0



B has the same x-coordinate as C and the same y-coordinate as A

- (i) Find the point B.
- (ii) Find the equation of the line through B perpendicular to line AC

### QUESTION 11: (10 marks) Start a new page

(a) For the function defined by:

Marks

- $f(x) = \begin{cases} 2x, & x \ge 1\\ 2-2x, & x < 1 \end{cases}$  (i) Sketch y = f(x)
- (i) Sketch y = f(x)
- (ii) Find the value of f(-1) + f(1) + f(3)
- (b) Solve simultaneously  $\begin{cases} 4x y = 19 \\ x + 2y + 2 = 0 \end{cases}$
- (c) In the diagram below, AB bisects  $\angle DBC$ ,  $\angle ACB = 60^{\circ}$  and  $\angle CDB = 40^{\circ}$

Copy the diagram into your answer booklet
Setting out a formal proof, prove that ΔCBA || ΔCDB

# QUESTION 12: (10 marks) Start a new page

(a) Find the equation of the normal to the curve  $y = 2x^3 - 4x^2$  at the point (1, -2) 3

(b)  $\alpha$  and  $\beta$  are the roots of the quadratic equation  $2x^2 - 3x + 5 = 0$  (DO NOT ATTEMPT TO FIND THESE ROOTS)

Find the value of:

(i) 
$$\alpha + \beta$$

(ii) 
$$\alpha\beta$$

(iii) 
$$\frac{1}{\alpha} + \frac{1}{\beta}$$

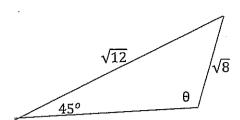
(iv) 
$$\alpha^2 + \beta^2$$

$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$$

### QUESTION 13: (10 Marks) Start a new page

this point.

(a)



Marks

3

In the diagram above, find the value of  $\theta$ , if  $90^{\circ} < \theta < 180^{\circ}$ 

(b) (i) On the same diagram shade the region corresponding to the simultaneous solution of:

3

$$(x-3)^2 + y^2 \le 4 \quad \text{and} \quad x+y \ge 3$$

(ii) The point P lies somewhere in the shaded region described in part (i).

At what point in the region above is P furthest from the origin? Give the co-ordinates of

1

(c) If the roots of the quadratic equation  $kx^2 + (k-1)x + (2k+1) = 0$  are such that one root is the reciprocal of the other, find the value of k.

3

# QUESTION 14: (10 Marks) Start a new page

#### Marks

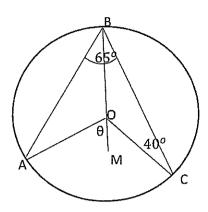
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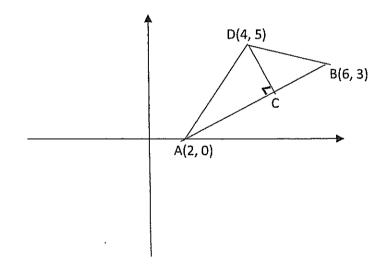
(a) For the figure below, O is the centre of the circle,  $\angle BCO = 40^{o}$  $\angle ABC = 65^{\circ}$ BO is produced to M.



- (i) Find the size of  $\angle ABM$
- (ii) Find the size of  $\angle AOM$ 2

You must provide reasons for each line of your proofs.

The point A is (2,0) while B is (6, 3) and D (4, 5) as shown. (b)



(i) Find the length of AB

(ii)

- Find the equation of the line AB in general form
- (iii) Find the shortest distance of the point D from AB (ie CD)
- (iv) Find the area of ∆ABD 1

## QUESTION 15: (10 Marks) Start a new page

(a) If 
$$f(x) = 3x^2$$
, find  $\frac{f(x+h)-f(x)}{h}$ 

Marks

(b) Prove that 
$$\frac{tan^2x}{secx+1} = secx - 1$$

2

(c) Solve 
$$4\sin^2\theta - 3 = 0$$
 for  $0^o \le \theta \le 360^o$ 

3

(d) If 
$$f(x) = x^{\frac{3}{2}}$$
 find the value of  $f'(4)$ 

2

## QUESTION 16: (10 Marks) Start a new page

(a) Find  $\frac{dy}{dx}$  if:

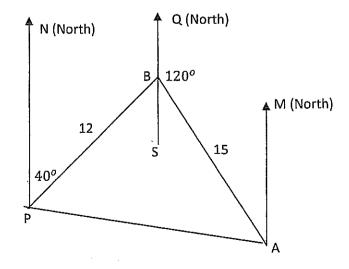
(i) 
$$y = \sqrt{x^3 + 3}$$

2

(ii) 
$$y = \frac{x}{x+1}$$

2

(b) The diagram below shows the course of a ship, which sails from a port P on a bearing of  $040^0$  for 12 km before changing course to a bearing of  $120^0$  and travelling a further 15 km to a destination A.



(i) Explain why 
$$\angle PBA = 100^{\circ}$$

1

(ii) Find the distance of A from P to the nearest km.

2

(iii) Find the bearing of P from A to the nearest degree.

3

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(c) (i) A is $(0,3)$ This $(-2,0)$ .: B is $(-2,3)$ .
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2	(c) T = (x - 8x	at (1,2) m=-2	MA 2 /2	17/1 *	ير [`	5 - n = 60	(b) (i) 4+ B = 3/ (ii) 4B = 5/4		(11) X+P= 26 (W) X+P=(X+B)-2013	5 31/32 = 34-5	3/5	6 176	1 なしの	ı	ALT	2	(a) By sine rule, sine	V. 7/ = 3/1/2			- 1	51	(ii) P is (So)	7 3 7 5 1	7 7 7 7.	Peoner = 1 = 2k+/	V		

14: L	(i) $AB = V(6-2) + 3$ (ii) $AB = V(6-2) + 3$ AB = V(6-2) + 3 AB = V(6-2) AB = V(6-2)	(b) $f(x+k) - f(x) = 3(x+k) - 3^{n}$ (c) $f(x+k) - f(x) = 3(x+k) - 3^{n}$ (b) $f(x) = 3f(x) = 3f(x)$
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71.	= 1% (1)	$\frac{1}{1}\frac{dy}{(k+1)\cdot 1-x\cdot 1}$	2 3001	(1) 1100 = 40 (alana engla grad 150 A = 60° (	.   `	21 km		Bearing in (360 - 9424)	= 266			
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