

Name: FILE COPY

Teacher: \_\_\_\_\_

**SYDNEY TECHNICAL HIGH SCHOOL**

**YEAR 8**

**MATHEMATICS**

**COMMON TEST**

**JUNE 2011**

<b>A</b>	<b>Non-Calculator</b>	<b>/ 12</b>
<b>B</b>	<b>Pythagoras</b>	<b>/ 16</b>
<b>C</b>	<b>Percentages</b>	<b>/ 12</b>
<b>D</b>	<b>Algebra</b>	<b>/ 18</b>
<b>E</b>	<b>Geometry</b>	<b>/ 19</b>
	<b>Total:</b>	<b>/ 77</b>

**Time Allowed: 70 minutes**

**Place all answers in the spaces provided.**

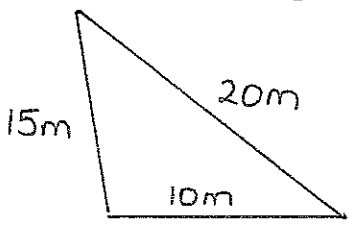
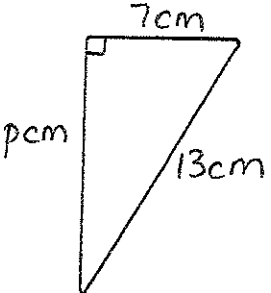
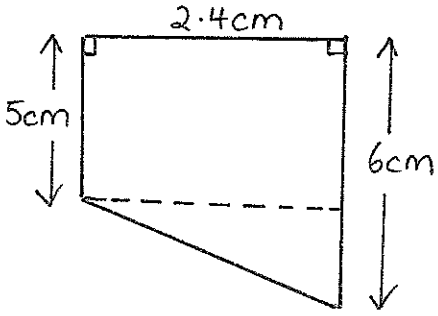
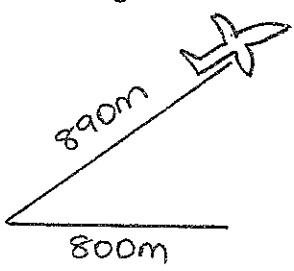
**Show all necessary working.**

# B. Pythagoras Theorem

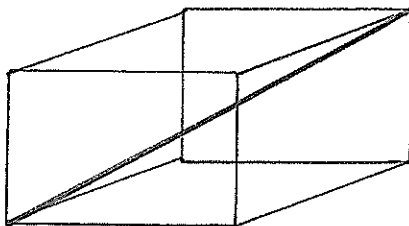
Name: \_\_\_\_\_

Show all working.

Marks

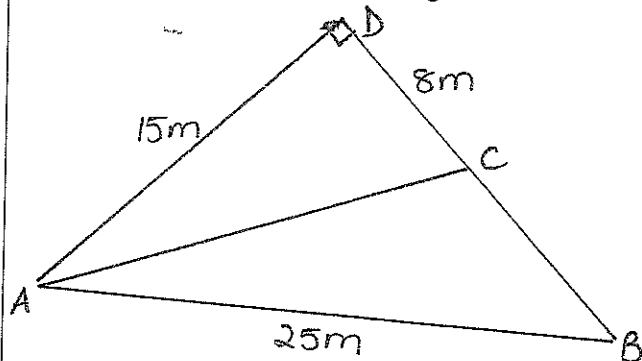
<p>1. Circle the correct answer</p> <p>The value of <math>\sqrt{1.7^2 - 1.5^2}</math> is closest to:</p> <p>A. 0.64      B. 0.8      C. 0.20      D. 0.45</p>	1
<p>2. State whether this triangle is right angled or not.</p> 	1
<p>3. Find p. Leave your answer in exact form.</p> 	2
<p>4. Find the perimeter of this shape, correct to the nearest cm.</p> <p>Show all working.</p> 	3
<p>5. After taking off, a plane flies 890m but covers a ground distance of 800m. How high is the plane off the ground?</p> <p>Show all working.</p> 	2

6. A rectangle prism box measures 6 cm wide, 20 cm long and 5 cm high. Find the length of the longest pencil that can fit into the box in exact form.



3

7. For the diagram, find the length of BC



2

8. A ramp is 9 metres long and rises to a height of 250cm. What is the horizontal distance in metres, between the bottom and the top of the ramp correct to 2 decimal places?

2

### C. Percentages

Show all working

Marks

1. Express $66\frac{2}{3}\%$ as a fraction in its simplest form.	1
2. Find 78% of 200	1
3. What percentage of $360^\circ$ is $117^\circ$ ?	1
4. All items in a shop are on sale at 15% discount off the marked price. Find the sale price of a shirt marked \$48.	1
5. An amount of \$760 is decreased by 30% and the resulting amount is then increased by 20%. What is the final amount?	2
6. Albert received a pay rise at work of \$21.60 per week. If this pay rise represented an 8% increase, how much is his weekly wage now.	2
7. The sale price of a cricket bat including 10% GST is \$253. Find the cost of the bat before GST.	2
8. Zac works at an electronics shop. He is paid a weekly wage of \$110.50. At the end of a certain week his income is a total of \$548 and he has sold \$12500 worth of goods. What percentage commission is he paid on the sale of the goods?	2

# D. Algebraic Expressions

Marks

1. Simplify		
(a) $4a + 3b - 3a + 5b$ _____		1
(b) $3x^2 \div -27y$ _____		1
2. Expand and simplify		
(a) $8(2e-5) + 24 - 28e$	(b) $3d-(4-2d) - 15$	2
		2
3. Simplify: $(5q^3)^4$		1
4. $15a^8 \div 5a^2 =$		1
A. $3a^4$ B. $3a^6$ C. $10a^4$ D. $10a^6$		
5. Factorise		
(a) $36d-54d^2$	(b) $-4m-12$	2
6. Simplify $\frac{-3m^3 \times (3m^2)^2}{(3m^2)^3}$		2
7. If $f(x) = 2x^2 - 3$ , find:		
(a) $f(0)$		1
(b) $f(2)$		1
(c) $f(-1)$		1
(d) $f(2) + f(-1)$		1

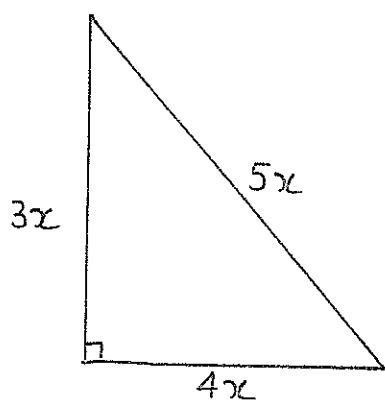
8. Find a simplified expression for the :

(i) area

1

(ii) perimeter of this figure

1



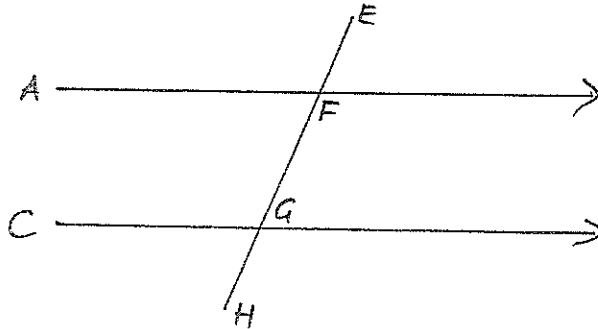
# E. Geometry

Marks

1. In the diagram below, complete the following sentences

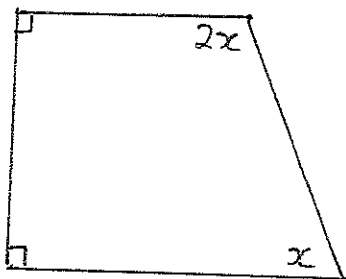
4

- (a) Angles EFB and EGD are called \_\_\_\_\_ angles  
 (b) Angles BFG and CGE are called \_\_\_\_\_ angles  
 (c) Angles AFG and CGF are called \_\_\_\_\_ angles  
 (d) Angles EFA and \_\_\_\_\_ are corresponding angles



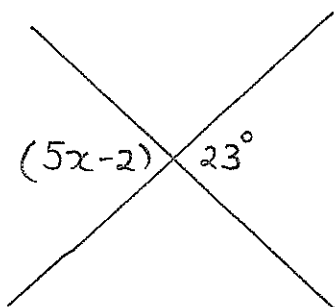
2. Find  $x$ , giving reasons

2



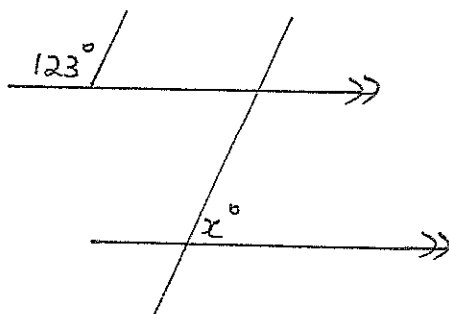
3. Find the value of  $x$ , giving reasons for your answer

2

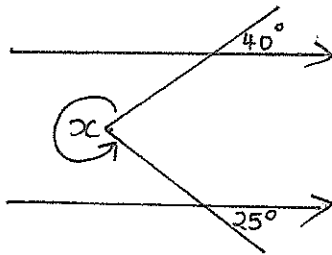


4. Find  $x$  (no reasons required)

1

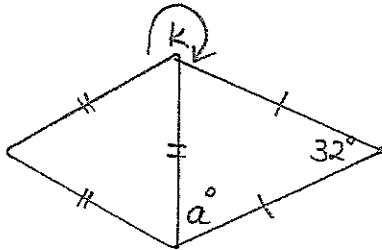


5. Find  $x$  (reason not required)



1

6 Find the angle measure of  $a$  and  $k$



$a =$  \_\_\_\_\_

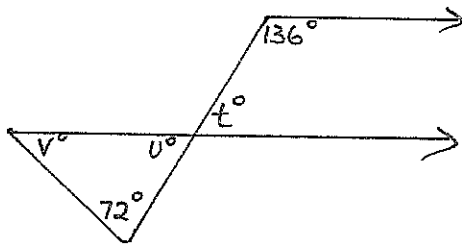
reason \_\_\_\_\_

$k =$  \_\_\_\_\_

(reason not required)

3

7.



$t =$  \_\_\_\_\_

reason \_\_\_\_\_

$u =$  \_\_\_\_\_

reason \_\_\_\_\_

$v =$  \_\_\_\_\_

reason \_\_\_\_\_

6



A. Non-Calculator (Time allowed 15min) (1 mark each) Name: \_\_\_\_\_

1. Express 81.298 correct to 2 decimal places.	1.
2. Find $2\frac{1}{2} \times 3\frac{2}{5}$	2.
3. Convert $12\frac{1}{2}\%$ to a decimal	3.
4. Find $\sqrt{6\frac{1}{4}}$	4.
5. Find two numbers such that their product is 216 and their sum is 30.	5.
6. Find the number that is halfway between 27.15 and 27.98	6.
7. Change $\frac{5}{8}$ to a decimal	7.
8. Find $9 \times 3 - 16 \div 4 + 15$	8.
9. If $a = -6$ , $b = 3$ and $c = -2$ , find (a) $ab \div c$  (b) $a - b - c$  (c) $\sqrt{a \times b \times c}$	9. (a) _____  (b) _____  (c) _____
10. The average of six numbers is 19. A seventh number is added and the new average is 20. What is the seventh number?	10.



Name: ANSWERS

Teacher: \_\_\_\_\_

# SYDNEY TECHNICAL HIGH SCHOOL

## YEAR 8

## MATHEMATICS

## COMMON TEST

MAY 2011

A	Non-Calculator	/ 12
B	Pythagoras	/ 16
C	Percentages	/ 12
D	Algebra	/ 18
E	Geometry	/ 19
	Total:	/ 77

Time Allowed: 70 minutes

Place all answers in the spaces provided.

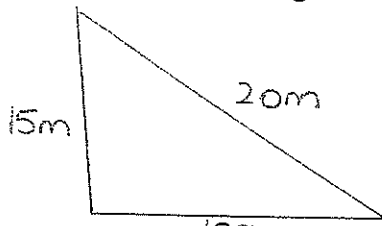
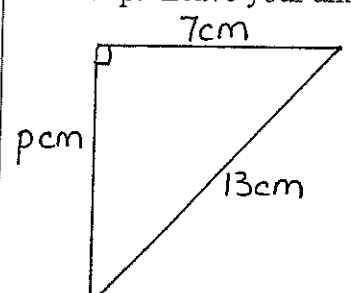
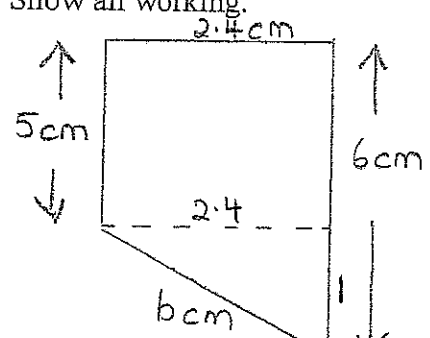
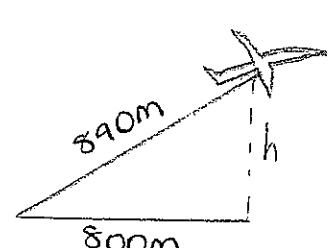
Show all necessary working.

# B. Pythagoras Theorem

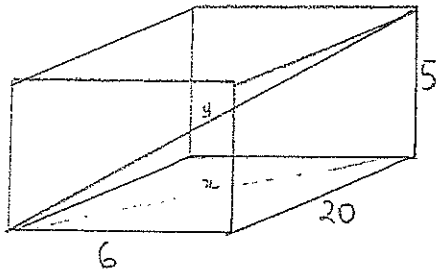
Name: \_\_\_\_\_

Show all working.

Marks

<p>1. Circle the correct answer</p> <p>The value of <math>\sqrt{1.7^2 - 1.5^2}</math> is closest to:</p> <p>A. 0.64      B. 0.8      C. 0.20      D. 0.45</p>	<p>1</p> <p>B</p>
<p>2. State whether this triangle is right angled or not.</p>  <p><math>15^2 + 10^2 \neq 20^2</math></p>	<p>1</p> <p>NO</p>
<p>3. Find p. Leave your answer in exact form.</p>  <p><math>p^2 = 13^2 - 7^2</math>  <math>p^2 = 120</math>  <math>p = \sqrt{120}</math></p>	<p>2</p>
<p>4. Find the perimeter of this shape, correct to the nearest cm.</p> <p>Show all working.</p>  <p><math>b^2 = 2.4^2 + 1^2</math>  <math>b = \sqrt{6.76} = 2.6</math>  <math>p = 2.4 + 6 + 2.6 + 5</math>  <math>p = 16 \text{ cm}</math></p>	<p>3</p>
<p>5. After taking off, a plane flies 890m but covers a ground distance of 800m. How high is the plane off the ground to the nearest metre?</p> <p>Show all working.</p>  <p><math>h^2 = 890^2 - 800^2</math>  <math>h = \sqrt{152100}</math>  <math>h = 390 \text{ m}</math></p>	<p>2</p>

6. A rectangle prism box measures 6 cm wide, 20 cm long and 5 cm high. Find the length of the longest pencil that can fit into the box.



$$x^2 = 6^2 + 20^2$$

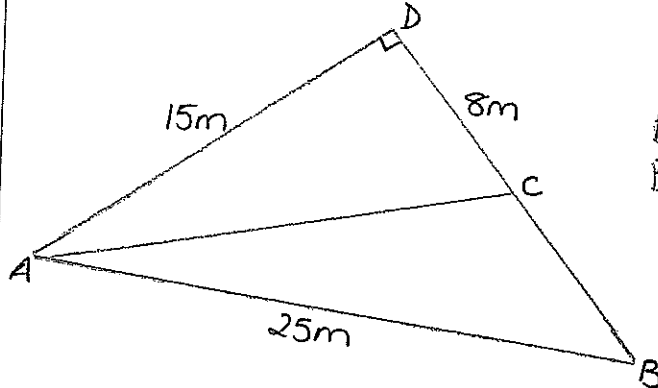
$$x = \sqrt{436}$$

$$y^2 = 5^2 + \sqrt{436}^2$$

$$y = \sqrt{461} = 21.47 \text{ cm.}$$

3

7. For the diagram, find the length of BC



$$BD^2 = 25^2 - 15^2$$

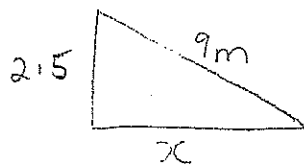
$$BD^2 = 400$$

$$BD = 20$$

$$\therefore BC = 12 \text{ m}$$

2

8. A ramp is 9 metres long and rises to a height of 250cm. What is the horizontal distance in metres, between the bottom and the top of the ramp?



$$x^2 = 9^2 - 2.5^2$$

$$x^2 = 74.75$$

$$x = \sqrt{74.75} = 8.65 \text{ m}$$

2

### C. Percentages

Show all working

Marks

1. Express $66\frac{2}{3}\%$ as a fraction in its simplest form.	$\frac{2}{3}$	1
2. Find 78% of 200	$0.78 \times 200 = 156.$	1
3. What percentage of $360^\circ$ is $117^\circ$ ?	$\frac{117}{360} \times 100 = 32.5\%$	1
4. All items in a shop are on sale at 15% discount off the marked price. Find the sale of a shirt marked \$48.	$\frac{85}{100} \times 48 = \$40.80.$	1
5. An amount of \$760 is decreased by 30% and the resulting amount is then increased by 20%. What is the final amount?	$= 0.7 \times 760$ $= \$532$ $= 1.2 \times 532$ $= \$638.40.$	2
6. Albert received a pay rise at work of \$21.60 per week. If this pay rise represented an 8% increase, how much is his weekly wage now.	$\frac{8}{100} \times x = 21.60.$ $x = 270$ $\text{Weekly Wage} = 270 + 21.60$ $= \$291.60$	2
7. The sale price of a cricket bat including 10% GST is \$253. Find the cost of the bat excluding GST.	$\frac{110}{100} \times x = 253$ $x = \$230$	2
8. Zac works at an electronics shop. He is paid a weekly wage of \$110.50. At the end of a certain week his income is a total of \$548 and he has sold \$12500 worth of goods. What percentage commission is he paid?	$548 - 110.50$ $= \$437.50$ $\frac{x}{100} \times 12500 = 437.50.$ $\frac{x}{100} = 0.035$ $x = 3.5\%$	2

# D. Algebraic Expressions

Marks

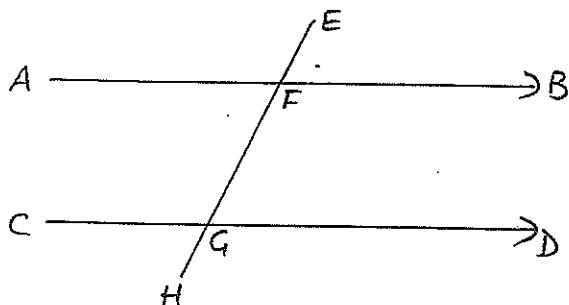
<p>1. Simplify</p> <p>(a) <math>4a + 3b - 3a + 5b</math> <u><math>a + 8b</math></u></p> <p>(b) <math>3x^2 \div -27y</math> <u><math>\frac{3x^2}{27y} = -\frac{x^2}{9y}</math></u></p>	<p>1</p> <p>1</p>
<p>2. Expand and simplify</p> <p>(a) <math>8(2e-5) + 24 - 28e</math>  <math>= 16e - 40 + 24 - 28e</math>  <math>= -12e - 16</math></p> <p>(b) <math>3d - (4 - 2d) - 15</math>  <math>= 3d - 4 + 2d - 15</math>  <math>= 5d - 19</math></p>	<p>2</p> <p>2</p>
<p>3. Simplify: <math>(5q^3)^4</math> <u><math>625q^{12}</math></u></p>	<p>1</p>
<p>4. <math>15a^8 \div 5a^2 =</math></p> <p>A. <math>3a^4</math>    <u>B. <math>3a^6</math></u>    C. <math>10a^4</math>    D. <math>10a^6</math></p>	<p>1</p>
<p>5. Factorise (a) <math>36d - 54d^2</math> <u><math>18d(2 - 3d)</math></u></p> <p>(b) <math>-4m - 12</math> <u><math>-4(m + 3)</math></u></p>	<p>1</p> <p>1</p>
<p>6. Simplify <math>\frac{-3m^3 \times (3m^2)^2}{(3m^2)^3}</math> <u><math>\frac{-3m^3 \times 9m^4}{27m^6} = \frac{-27m^7}{27m^6} = -m</math></u></p>	<p>2</p>
<p>7. If <math>f(x) = 2x^2 - 3</math>, find</p> <p>(a) <math>f(0) = 0 - 3 = -3</math></p> <p>(b) <math>f(2) = 2 \times 4 - 3 = 5</math></p> <p>(c) <math>f(-1) = 2 \times (-1)^2 - 3 = -1</math></p> <p>(d) <math>f(2) + f(-1) = 5 + (-1) = 4</math></p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p>
<p>8. Find an expression for the</p> <div data-bbox="183 1601 566 1960"> </div> <p>(i) area <math>A = \frac{1}{2} \times 4x \times 3x</math>  <math>A = 6x^2</math></p> <p>(ii) perimeter of this figure  <math>P = 3x + 5x + 4x</math>  <math>P = 12x</math></p>	<p>1</p> <p>1</p>

# E. Geometry

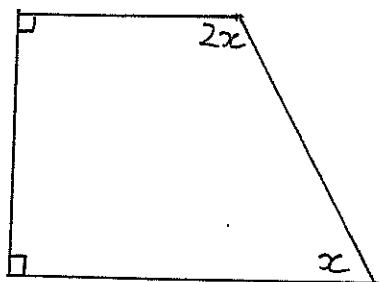
Marks

1. In the diagram below, complete the following sentences

- (a) Angles EFB and EGD are corresponding angles  
 (b) Angles BFG and CGE are alternate angles  
 (c) Angles AFG and CGF are co-interior angles  
 (d) Angles EFA and  $\angle FGC$  are corresponding angles



2. Find  $x$ , giving reasons



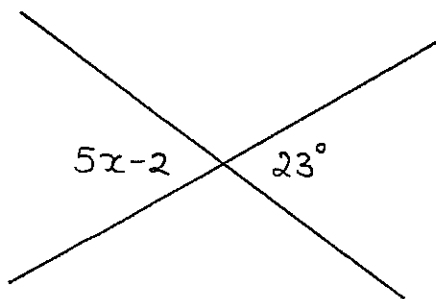
$$180 + 3x = 360$$

$$3x = 180$$

$$x = 60.$$

angle sum of quadrilateral.

3. Find the value of  $x$ , giving reasons for your answer



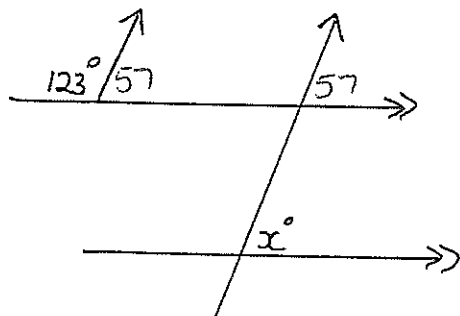
$$5x - 2 = 23$$

$$5x = 25$$

$$x = 5$$

Vertically opposite angles are equal

4. Find  $x$  (no reasons required)

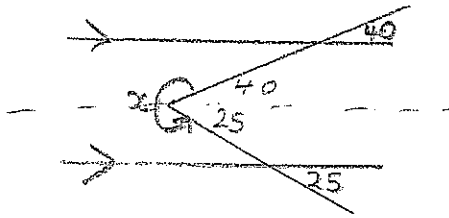


$$x = 57$$



5. Find  $x$  (reason not required)

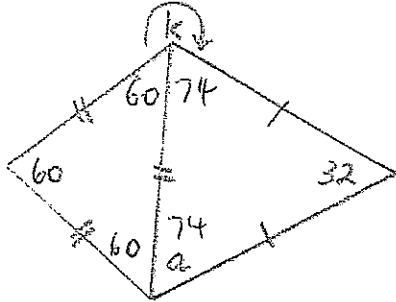
1



$$x = 295$$

6 Find the angle measure of  $a$  and  $k$

3



$$a = 74$$

reason base angles of isosceles triangle

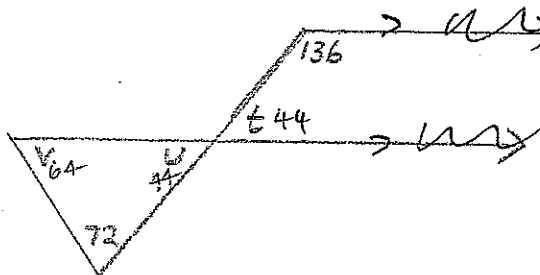
$$k = 226$$

(reason not required)

7.

$$t = 44$$

6



reason = co-interior  $\angle$ 's suppl in  $\parallel$  lines

$$u = 44$$

reason = vertically opp  $\angle$ 's =

$$v = 64$$

reason = angle sum of triangle

A. Non-Calculator (Time allowed 15min) (1 mark each) Name: \_\_\_\_\_

1. Express 81.298 correct to 2 decimal places.	1. 81.30
2. Find $2\frac{1}{2} \times 3\frac{2}{5}$	2. $\frac{17}{2} = 8\frac{1}{2}$
3. Convert $12\frac{1}{2}\%$ to a decimal	3. 0.125
4. Find $\sqrt{6\frac{1}{4}}$	4. $\frac{5}{2}$
5. Find two numbers such that their product is 216 and their sum is 30.	5. 18 & 12
6. Find the number that is halfway between 27.15 and 27.98	6. 27.565.
7. Change $\frac{5}{8}$ to a decimal	7. 0.625
8. Find $9 \times 3 - 16 \div 4 + 15$	8. 38
9. If $a = -6$ , $b = 3$ and $c = -2$ , find (a) $ab \div c$ $-18 \div -2$  (b) $a - b - c$ $-6 - 3 - -2$  (c) $\sqrt{a \times b \times c}$ $\sqrt{36}$	9. (a) 9  (b) -7  (c) 6
10. The average of six numbers is 19. A seventh number is added and the new average is 20. What is the seventh number?  $\frac{x}{6} = 19$ $\frac{114+y}{7} = 20$ $x = 114$ $114+y = 140$ $y = 26$	10. 26