Name:	Maths Class:

# SYDNEY TECHNICAL HIGH SCHOOL (Est. 1911)



# Year 11

# Mathematics Extension 1 May 2013

Time allowed: 70 min

#### Instructions:

- Write your name and class at the top of this page.
- These questions must be handed in on the top of your answers
- Attempt all questions.
- Begin each question on a new page.

Use only blue or black pen for your answers

Total Marks - 60

# Question 1 (10 marks) Use a SEPARATE page

(a) Simplify the following expression  $\frac{x^3 - y^3}{x^2 - y^2}$ .

2

(b) (i) By factorising, simplify  $2^{n+1} + 2^n$ .

1

(ii) Hence, or otherwise, write  $\frac{2^{1001} + 2^{1000}}{3}$  as a power of 2.

2

(c) Simplify:  $\frac{10^x + 15^x}{2^5 \times 3^x + 2^{x+5}}.$ 

- 3
- (d) Find the exact value of  $\sin 120^{\circ} \tan 210^{\circ}$ . Express your answer with a rational denominator.
- 2

# Question 2 (10 marks) Use a SEPARATE page.

- (a) The sum of the interior angles of a regular polygon is  $3960^{\circ}$ .
  - (i) How many sides does the polygon have?

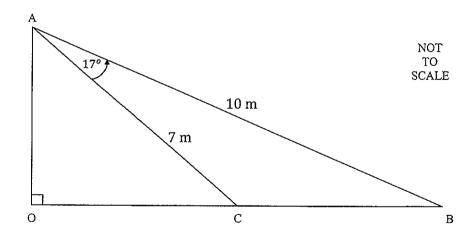
1

(ii) Find the size of each interior angle.

(iii) Hence or otherwise find the size of the exterior angle.

1

(b)



(i) Find the area of  $\triangle$ ABC to 2 significant figures.

2

(ii) Find the length of BC to 2 significant figures.

2

(iii) Find the length of BO to 2 significant figures.

3

### Question 3 (10 marks) Use a SEPARATE page.

(a) Find the exact solutions of  $x + 8 = \frac{6}{x}$ 

3

(b) (i) Draw the graph of y = |x - 1| and y = x + 3 on the same axes.

2

(ii) Hence or otherwise solve |x-1| > x+3.

2

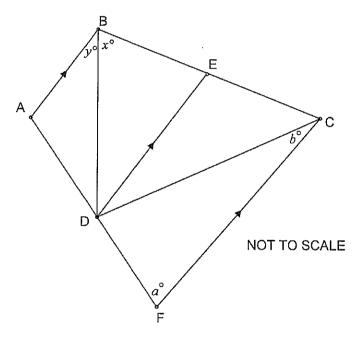
(c) Solve for x:

3

$$\frac{4x-1}{x+2} \ge 3$$

# Question 4 (10 marks) Use a SEPARATE page.

(a) In quadrilateral ABCD, AB = AD, CB = CD and FC is parallel to AB and DE.



(i) Show that a = 2y, giving reason(s).

3

(ii) Show that b = x - y, giving reason(s).

2

3

(b) (i) Use the method of grouping in pairs to factorise fully

2

 $3x^3 + 3x^2 - x - 1.$ 

- (ii) Hence or otherwise solve
  - $3\tan^3\theta + 3\tan^2\theta \tan\theta 1 = 0$  for  $0 \le \theta \le 180^\circ$ .

Question 5 (10 marks) Use a SEPARATE page.

- (a) For the function  $f(x) = \frac{9}{9 x^2}$ 
  - (i) Giving reasons, is the function odd, even or neither?

1

2

3

1

(ii) Find the equation(s) of the asymptotes.

- (iii) Using a ruler, sketch the graph of y = f(x), showing all key features.
- (iv) Hence, or otherwise, state the domain and range of the function.
- (b) If  $3\cos\theta + 2 = 0$  and  $\tan\theta > 0$ , what is the exact value of  $\sin\theta$ ?

Question 6 (10 marks) Use a SEPARATE page.

- (a) Jade is on a ship and observes two lighthouses on the shore. The lighthouse at Addison Head has a bearing of 224° from the ship. The lighthouse at Blake Beach has a bearing of 195° from the ship and 165° from Addison Head. The lighthouses are 3.4 km apart.
  - (i) Draw a diagram showing all necessary information.

2

2

3

- (ii) What is the distance of Jade's ship from the Addison Head lighthouse (1 decimal place)?
- 3

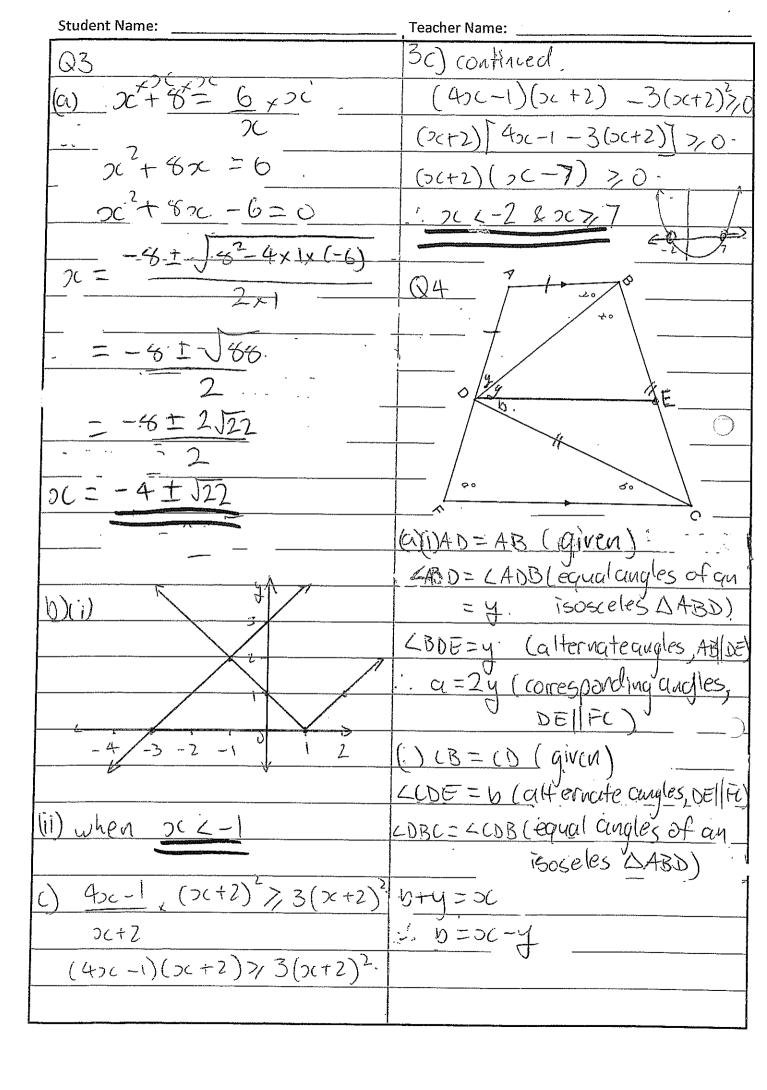
(b) Prove

$$\frac{(1 + \tan^2 \theta) \cot \theta}{\csc^2 \theta} = \tan \theta$$

(c) If  $2^a + 3^b = 17$  and  $2^{a+2} - 3^{b+1} = 5$ , find the values of a and b.

End of test

Student Name:	Teacher Name:
Q1	Q2
(a) (21-4) (212+24+42).	a) (i) $(3960 \div 180) + 2 = 24$
(7c-y) (x+y).	(ii) $3960 + 24 = 165^{\circ}$
2 2 + 2 4 + 4 2	(iii) 180 - 165 = 15°
(xxy)	
N	(D) DA = 1 x 10x7 x Sin17
(b)(i) $2 \times 2^{n} + 2^{n}$	2 (0.233
$= 2^{n}(2+1)$	= 10 m(2.5.f.)
$=3\times2^{n}$	(ii) 2 2
(ii) 2, 2 1000 + 2 1000	BC= 102+72-2×10+7×10517
	= 15.117
3.	:.BC=3.9m.
= 3,21000 - 21000	(ii) sinB = SinT7 7 3.9
$2^{2} \times 5^{2} + 3^{2} \times 5^{2}$	SinB = 0.5247697
$\frac{2^{5} \times 3^{12} + 2^{5} \cdot 2^{5}}{2^{5} \times 3^{12} + 2^{5} \cdot 2^{5}}$	3= 3-1,6527.
$-5^{\circ (2^{\circ (7^{\circ} + 3^{\circ})})}$	i. OB = (0531.6527
25 (3° +2° ).	10
5 <sup>)C</sup>	03= 10 (05.31.6527
2 5	= 8.5 m
d) Sin (160-60) - tun (160+36	
= 51/160 - tan30	
$\frac{1}{\sqrt{3}} - \frac{1}{\sqrt{3}}$	
2 \( \sqrt{3} \) . \( \sqrt{3} \) .	
$\frac{\sqrt{3}-\sqrt{5}}{2}$	
$\frac{2}{6} = \frac{513 - 213}{6} = \frac{5}{6}$	



CANDIDATE NO:	-t
Q4 continued	(b) (050 = -2 (050 40
(5)(i) 3 2c2 (2c+1) - (2c+1)	-2 3 temoro
$(3c+1)(3x^2-1)$	J5 2
(2c+1) (J32c-1) (J32c+1)	7
	$\int 3^2 - (-2)^2 = \int 5$
ii) (tan 0+1) (J3tano -1) (J3tano+1)=	D.1. SMD = - J5
: tand=-1 tand=-1 \[ \frac{1}{3} \] \[ \frac{1}{3} \]	3
V3 V3	Q6 N
0=135° 0=30° 0=150°	(i)
	290 195
05	A 3.4 15
$\frac{(i) f(-ic) = \frac{6}{9 - 12} = \frac{6}{9 - 12} = f(3c)}{9 - 12}$	B
9-(->2) 9-71 even.	$ii) \frac{3c}{51n30} = \frac{3.4}{51n29}$
(i) 9-22 +0	1. oc = 3.5 km
· 2c # ±3 4 ± 0.	(b) Sec <sup>2</sup> 0 x (oso 1 -1
lii)	- Costo Sino - S
	= tano=RHS
	(c) Let > C-29 & y=36.
; \	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
<u>(</u>	$2^{\alpha+2} - 3^{br1} = 5 \Rightarrow 2^{2} \times 2^{3} \times 3^{5} = 5$
3	142c-3y=50
	3.x0 30c+3y=10
	3+0 7 = 56 : 2 = 8
	8+4=17 2"=8
	$y=9$ $\therefore \alpha=3$
iv) R: 42 1 and 460 Dialloc, except	: 3 <sup>6</sup> =4
2 4 + 2	$l_n = 2$

oc#±3 :-.