Name:	Teacher:

SYDNEY TECHNICAL HIGH SCHOOL

(Est. 1911)



Year 12

Mathematics

Assessment Task 2

March 2013

Time allowed: 70 minutes

Instructions:

- Write your name and class at the top of this page.
- These questions must be handed in on the top of your answers
- Attempt all questions.
- All necessary working must be shown.
- Begin each question on a new page.
- Answer Section I on the Multiple Choice answer sheet provided.
- Answer Section II on the blank paper provided.

Section 1	Q6	Q7	Q8	Q9	Q10	TOTAL
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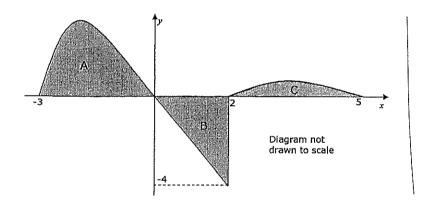
Section I

Use the multiple choice answer sheet. Select the alternative A, B, C or D that best answers the question. Fill the response oval completely.

- 1. Given that $(x) = \frac{1}{(3x+1)^3}$, which is the correct expression for f'(x)?

 A. $\frac{-3}{(3x+1)^2}$ B. $\frac{-9}{(3x+1)^2}$ C. $\frac{-3}{(3x+1)^4}$ D. $\frac{-9}{(3x+1)^4}$

- 2. If f'(x) < 0 and f''(x) > 0 for all x over a given domain, which of the following describes the graph of y = f(x)?
 - A. Increasing and concave up
 - B. Increasing and concave down
 - C. Decreasing and concave up
 - D. Decreasing and concave down
- 3. The graph of y = f(x) is shown in the diagram below. The shaded areas are bounded by the curve and the x-axis. The area of region A is 8 square units and the area of region C is 1 square unit.



The value of $\int_{-3}^{5} f(x) dx$ is:

- A. 5
- B. 13
- C. 1

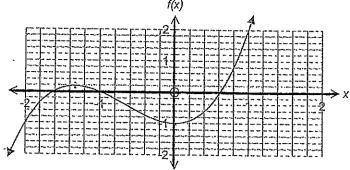
D 17

$$\sum_{n=5}^{30} (2n-1) =$$

A.59

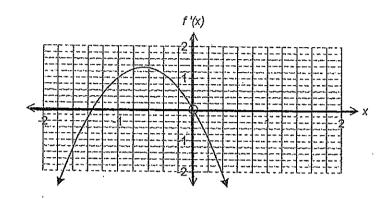
- B. 50
- C. 884
- D. 85



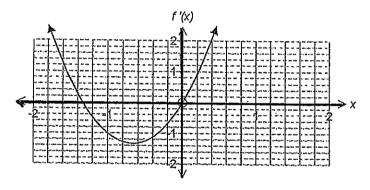


Given the f(x) curve above, which of the following represents the curve for f'(x)?

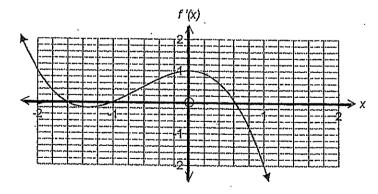
(A)



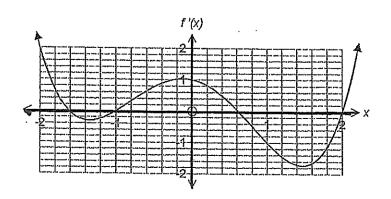
(B)



(C)



(D)



Section II

Total marks 55
Attempt questions 6 – 10
Allow about 65 minutes for this section
Show all necessary working out
Start each question on a new page

QUESTION 6 (11 marks)

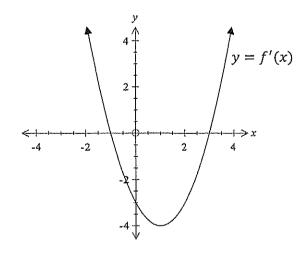
MARKS

2

a) Differentiate

i)
$$y = (x+3)(x^2-1)$$
 2
ii) $y = x\sqrt{2x-5}$ 2
iii) $y = \frac{2x+3}{x^2+1}$

- b) The first term of a Geometric Series is 16 and the common ratio is $\frac{1}{n}$.
 - i) For what values of n will this series have a limiting sum? 2
 - ii) Calculate the limiting sum of the series where n = 4
- c) Below is a graph of y = f'(x). Given that f(-1) = 3 and f(3) = -1, sketch a graph of y = f(x).



domain?

- a) Find the equation of the tangent to the curve $y = 2x^2 2$ at the point where the tangent is parallel to the line y = 4x + 1
- b) Find
 - i) $\int \sqrt{x^3} \, dx$ 1
ii) $\int \frac{2x-1}{x^3} \, dx$
- c) Joan deposits \$350 into a special savings account on the first day of each month for two years. The interest rate is 9 %p.a. compounded monthly. Find the total amount in her savings account at the end of the two year period.
- d) The gradient function for a curve which passes through the point (1, 2) is $4x^3 3x^2 + 6$. Find the equation of the curve.

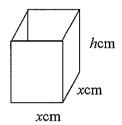
a) Evaluate $\int_3^5 (3x-2)^5 dx$

2

1

- b) A sum of \$15 000 is borrowed at 12% pa interest, calculated on the balance owing at the end of each month. The money is to be repaid at monthly intervals over 5 years.
 - i) If M stands for the monthly repayment, show that the amount owing at the end of the second month is given by $A_2 = 15\ 000\ (1.01)^2 M\ (1.01 + 1)$
 - ii) Write a general expression for the amount owing after n months.
 - iii) Find the monthly repayment.
- c) Find the area bounded by the curve $y = x^3 + 1$ and the x-axis between x = -1 and x = 3.

- a) Find a value for n which when added to each 2, 5 & 9 will give a set of three numbers in geometric progression.
- b) Find the area between the curve $y = \sqrt{2x 1}$, the y-axis and the lines y = 1 & y = 3
- c) A box with a square base and an open top is made of thin material. The box is to have a capacity of $32cm^3$



- i) Find an expression for the height of the box, hcm, in terms of x. 1
- ii) Show that the surface area, A, of the box is given by

$$A = x^2 + \frac{128}{x}$$
 2

iii) Find the dimensions of the box that give the minimum surface 3 area.

STANDARD INTEGRALS

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, \quad n \neq -1; \quad x \neq 0, \text{ if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \quad x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \quad a \neq 0$$

$$\int \cos ax dx = \frac{1}{a} \sin ax, \quad a \neq 0$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax, \quad a \neq 0$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax, \quad a \neq 0$$

$$\int \sec ax \tan ax dx = \frac{1}{a} \sec ax, \quad a \neq 0$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \quad a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}, \quad a > 0, \quad -a < x < a$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln \left(x + \sqrt{x^2 - a^2} \right), \quad x > a > 0$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln \left(x + \sqrt{x^2 + a^2} \right)$$

NOTE: $\ln x = \log_e x$, x > 0

Name	Teacher	
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Mathematics

March 2013

SECTION I

Completely fill the response oval representing the most correct answer.

1.	$A \bigcirc$	ВО	$c \bigcirc$	$D \bigcirc$

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- 3. A O BO CO DO
- 4. A O BO CO DO
- 5. A O BO CO DO

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	Min by at (3,-53)		<u> </u>	
ψ iv) Absolute maximum = 11	at x=3, on >0 : lancar y		٠ ١١٤ .	
	:. Stat ots at (3, -53) + (-1, 11)		* 1-4	
- 600 +	y=-53 y=11		") S = 127	
55)[#3] o[= -]		n>1, n<-1	***************************************
/ On-	0= (1+x)(&-x)		i) For limiting sum r < 1	
	6(x2-2x-3)=0	(1+-X)	b) 0=16 7=3	
8	6712-18=0	= -2x2-6x+2		
12 3 4 5 5	5thet of the =0	(x++1)2	3-10 + (S-xg)=	
	972 = 12x-12	$= 2x^2+2-4x^2-6x$	on 1. (2x-5)2+ = (2x-5)-2 x 2 x x	
	81	$\frac{\partial u}{\partial x} = \frac{(x^2+1)^2}{(x^2+1)^2}$		
	i) oly = 6x2 - 1221 - 18	x2+1		
iii)	b) 4=2x3-6x2-18x+1	(ii) y = 2x+3	1 - 31 + 6× -1	
			a) i) 4 = 25 + 3x2 - 21 - 3	
			QUESTION 6	
			SECTION 2	
	Sa = 2 (a+ l)			
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	»-1 =1)		# C	
	-777 (1-1)		3. A	the transfer of transmers.
	-27 = 50 + (n-1) x-7		2. C	
	Tn= a+ (n-1) od		1. 0	
	a) a=50 d=-7 Tc==27		SECTION I	
	(P) (S) (P) (P)			

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		+1-x9+x-h=B.
-1 3 = 24 mitc2		at x=1 + y=2 c=-4
+ + V	and the state of t	h = x4-x3+6x+C
	and the second s	_Q /M
$\frac{1}{2}$ $\frac{1}$	And the second s	d) $dy = 4x^3 - 3x^2 + 6$
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	and the same of th	シャー・ナキュ・ディー・
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1-10-1		$\int_{-\infty}^{\infty} \frac{1}{x^2} \int_{-\infty}^{\infty} \frac{1}{x^2} \int_{-\infty}^$
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0= (10.1 + + 10.1 + 1) W - 04 10.1 × 000 SI	**************************************	total = 350 x 1.0075 (1.007524-1)
but Abo = 0	V	(at \$350 = 350 × 1-0075
iii) $A_{bo} = 15000 \times 1.01^{bo} - M(1 + 1.01 + + 1.01^{sq})$		\\ \frac{1}{2} \\ \tag{\text{:}}
200		
" A = 15 000 x 1.01" - M (+ 1.01 + + 1.01")		b) Frat 4350 = 350 × (-0075 ²⁴
- 10 000 x 3:01 - F1 (1:01 + 1)		
18 000 x 1 01	***************************************	η = 4x -4
3 15 000 v 1:01 = 1:01 M = M		$y_{-0} = 4(3t-1)$
11	-	$y - y_1 = m(x - x_1)$
	^	y = 0
nis 000 0= 10/		
		: the = 4 (parable lines
ĺ	,	MZ=4
= 18 (3×5-2)6- 18 (3×3-2)6		y = 4×1+1
- 1		₩± dx
$\frac{\omega_{1}}{3} = \left[\frac{1}{k_{12}}(3\chi-2)^{b}\right]^{5}$		on = 4×c
$a = \frac{1}{2} \left(\frac{1}{2} \left(\frac{1}{2} \right) \right)^{2} \frac{1}{2}$	d manage from	a) 4 = 2x - 4
		8 Nollsand

i A A. I.	
X=4	
O=(41+x4+2x)(x2-x)	
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35.5-128 = 0	
$\frac{\partial x}{\partial t^2} = 0$	
2)1 - 128x 2 =0	
	i
: Dimensions are	
ola Minimum at se	
2× 211- 1€	
1. 1831 + 2K= 35 + 2K=	-
ii) A > 3(2+ 4xh	
$h = \frac{32}{20^2}$	
32 = x²h	
c) i) $V = x \times x \times x \times h$	
= 5\frac{1}{3} units 2	
= 2 (((()) + 3 - (() + 1))	
- ² [³ り ³ + り],	
Area = (31 (42+1) dy	
$\sum_{x=2}^{2} (y^{2}+1)$	
, 1	
3	
b) $\eta = \sqrt{2x-1}$	
٦	
25+10n+n2=18+11n+n2	
$(5+n)^2 + (9+n)(2+n)$	
2+n 5+n	
S+n * 9+n	
a) 2+0 5+0 9+0	
QUESTION 10	

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