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SYDNEY TECHNICAL HIGH SCHOOL



YEAR 12 HSC COURSE

Extension 2 Mathematics

TRIAL HIGHER SCHOOL CERTIFICATE

August 2009

TIME ALLOWED: 120 minutes

READING TIME: 5 minutes

Instructions:

- Write your name and class at the top of this page, and on all your answer sheets.
- Hand in your answers attached to the rear of this question sheet.
- All necessary working must be shown. Marks may not be awarded for careless or badly arranged work.
- All questions are of equal value.
- Marks indicated within each question are a guide only and may be varied at the time of marking
- START ALL QUESTIONS ON A NEW PAGE
- Approved calculators may be used.
- A table of Standard Integrals is attached. You may detach this page now.

(FOR MARKERS USE ONLY)

1	2	3	4	5	6	7	8	TOTAL
/15	/15	/15	/15	/15	/15	/15	/15	/120

QUESTION 1:

Marks

(a) Find

2

(i) $\int \cos^3 x \ dx$

2

(ii)
$$\int \frac{dx}{x^2 - 4x + 8}$$

2

(iii)
$$\int_{1}^{5} \frac{dx}{(2x-1)\sqrt{2x-1}}$$

4

(b) Prove that $secx = \frac{secxtanx + sec^2x}{secx + tanx}$

and hence show that $\int_0^{\frac{\pi}{4}} \sec x \, dx = \ln(\sqrt{2} + 1)$

5

(c) (i) Find values of A, B and C so that

$$\frac{5}{(x^2+4)(x+1)} = \frac{Ax+B}{x^2+4} + \frac{C}{x+1}$$

(ii) Hence find
$$\int \frac{5 dx}{(x^2+4)(x+1)}$$

QUESTION 2: (Start a new page)

Marks

6 (a) If z = 1 - i, find

(i) \bar{z} (ii) |z| (iii) arg z (iv) arg iz (v) z^6 (in simplest form)

2 (b) (i) Sketch the region where the inequalities

$$|z-2| \le |z-2i|$$
 and $|z-1-2i| \le 1$

hold simultaneously.

3 (ii) P is a point on the boundary of the region in part (i) above, and is represented by the complex number z, where $arg z = \frac{\pi}{4}$.

Find the 2 possibilities for z (in the form a+ib).

4 (c) A plane curve is defined by the equation

$$x^2 + 2xy + y^5 = 4$$

The curve has a horizontal tangent at the point P(X, Y).

By using implicit differentiation, or otherwise, show that X is the unique solution to

$$X^5 + X^2 + 4 = 0$$

QUESTION 3: (Start a new page)

Marks

- 2 (a) (i) Without using calculus, sketch the curve $y = (x+1)^2(1-x)$
- 2 (ii) On a separate diagram from above, but using the same scale on the axes, *and also without calculus*, sketch the curve

$$y^2 = (x+1)^2(1-x)$$

In your answer, pay close attention to the shape of the curve as y approaches zero.

- 6 (b) Sketch each of the following curves on separate axes for $0 \le x \le 2\pi$
 - (i) $y = \sin^2 x$

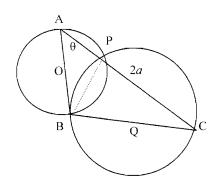
(ii) y = |sinx|

(iii) $y = \sqrt{\sin^2 x}$

(iv) $y = \frac{1}{\sin x}$

 $(v) y = \frac{|sinx|}{sinx}$

- (vi) $y = e^{\sin x}$
- (c) The hypotenuse AC of a <u>right-angled triangle ABC</u> has a length of 2a units and makes an angle of θ with one of the shorter sides, as shown below.



Circles are drawn using the two shorter sides as diameters, intersecting at points B and P. For this diagram, P is <u>NOT</u> on the side AC.

O and Q are the centres of the circles.

- (i) Redraw the diagram in your answer book. (No marks)
- 2 (ii) Prove that the point P lies on AC (you may initially assume that it doesn't)
- 3 (iii) Show that the length of PB is $asin2\theta$

QUESTION 4: (Start a new page)

Marks

- 2 (a) Show that $\int_0^{\frac{\pi}{4}} tan\theta d\theta = \frac{1}{2} \ln 2$
- 2 (b) (i) Prove that, for any complex numbers z_1 and z_2

$$\arg(z_1 z_2) = \arg z_1 + \arg z_2$$

3 (ii) Hence, using the method of Mathematical Induction, prove that

$$arg(z_1z_2...z_n) = arg z_1 + arg z_2 + ... + arg z_n$$

(c) A cubic polynomial is given by $P(x) = x^3 + ax + b$

where a and b are constants.

It is given that the polynomial equation P(x) = 0 has three roots, α , β , and γ

- 1 (i) Find the value of $\alpha + \beta + \gamma$
- 2 (ii) Show that $\alpha^2 + \beta^2 + \gamma^2 = -2a$
- 3 (iii) If the polynomial has a double root, show that this double root is $\frac{-3b}{2a}$
- 2 (iv) If the polynomial has 3 distinct roots, show that $4a^3 + 27b^2 < 0$

QUESTION 5: (Start a new page)

Marks

2

2

5 (a) Given the hyperbola $16x^2 - 9y^2 = 144$, find

- (i) the length of the major axis
- (ii) the eccentricity
- (iii) the co-ordinates of the foci
- (iv) the equations of the directrices
- (v) the equations of the asymptotes

(b) The parametric co-ordinates of a point
$$P$$
 on the curve $y^2 = x^3$ are $x = t^2$ and $y = t^3$

(i) Show that the equation of the tangent to this curve at P is

$$t^3 - 3tx + 2y = 0$$

1 (ii) Explain why there can be no more than 3 distinct tangents to $y^2 = x^3$ drawn from any remote point (x_1, y_1) , which is not on the curve.

(iii) Show that if the tangents to the curve at the points on it having parameters t_1 , t_2 and t_3 all pass through the remote point(x_1 , y_1), then

$$t_1^2 + t_2^2 + t_3^2 = 6x_1$$

5 (c) The area under the curve $y = x^2$, above the x-axis and between the lines x = 1 and x = 2, is rotated through 2π radians about the line x = 2.

Using the method of cylindrical shells, show that the volume of the solid so formed is $\frac{11\pi}{6}$ cubic units.

QUESTION 6: (Start a new page)

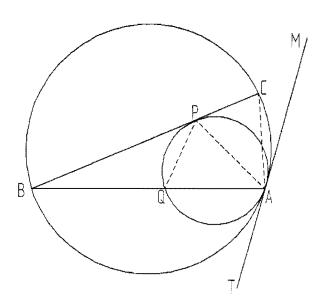
Marks

5

(a) Two circles touch internally at a point A and have a common tangent TAM as shown below.

A tangent to the inner circle through a point P (which is not the centre of either circle) meets the outer circle at B and C.

AB cuts the inner circle at Q.

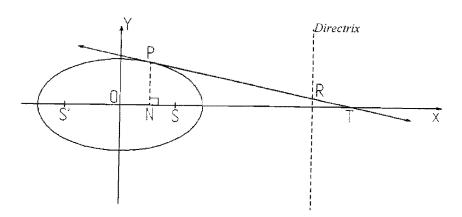


- (i) Redraw the diagram neatly onto your answer page (no marks).
- (ii) Giving all appropriate reasons, prove that AP bisects the angle BAC.

QUESTION 6 continues over the page....)

QUESTION 6 continued.....)

(b) $P(a\cos\theta, b\sin\theta)$ is any point on the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$



The tangent at P cuts the major axis of the ellipse at T and the Directrix at R, while N is the foot of the perpendicular from P to the x-axis.

O is the centre of the ellipse, while S and S' are the foci.

- Show that the equation of the tangent at P is $\frac{x\cos\theta}{a} + \frac{y\sin\theta}{b} = 1$ (Show all working)
- 2 (ii) Show that ON.OT = a^2
- 5 (iii) Showing all steps carefully, prove that PR subtends a right angle at S.

QUESTION 7: (Start a new page)

Marks

Using the substitution $x = a \tan \theta$, or otherwise, find $\int \frac{dx}{(a^2 + x^2)^{\frac{3}{2}}}$

(b) You are given the complex polynomial $P(z) = z^5 - 1$

The roots of P(z) = 0 are $1, \omega_1, \omega_2, \omega_3, \omega_4$ which are in cyclic order around the unit circle.

3 (i) Prove the following:

(a)
$$\omega_1 = \overline{\omega_4}$$
 and $\omega_2 = \overline{\omega_3}$

$$(\beta) \quad \omega_1 + \omega_2 + \omega_3 + \omega_4 = -1$$

(
$$\gamma$$
) $\cos \frac{2\pi}{5} + \cos \frac{4\pi}{5} = -\frac{1}{2}$

2 (ii) Using the sum of the products of the roots taken in pairs, or otherwise, show that

$$4\cos\frac{2\pi}{5}\cos\frac{4\pi}{5} + 1 = 0$$

1 (iii) Deduce that $\cos \frac{2\pi}{5}$ and $\cos \frac{4\pi}{5}$ are solutions to $4x^2 + 2x - 1 = 0$

4 (c) (i) If $I_n = \int_0^{\frac{\pi}{4}} sec^n \theta d\theta$,

show that $(n-1)I_n - (n-2)I_{n-2} = (\sqrt{2})^{n-2}$, for $n \ge 2$

2 (ii) Using part (i) above, evaluate $\int_0^{\frac{\pi}{4}} sec^4 \theta d\theta$

QUESTION 8: (Start a new page)

Marks

3

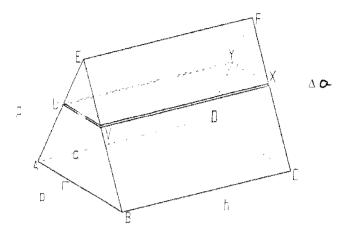
(a) In the right triangular prism shown,

$$AB=DC=b$$
 units

M is the midpoint of AB

$$EM = p$$
 units

$$BC=AD=EF=h$$
 units

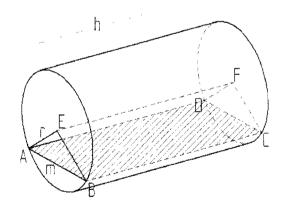


A "slice" UVXY of thickness Δa is taken a units above the base ABCD and parallel to it.

(i) Show that the volume of the rectangular slice is given by

$$\Delta V = \left(\frac{p-a}{p}\right)bh\Delta a$$

- 2 (ii) Hence, show that the volume of the triangular prism is given by $V = \frac{1}{2}pbh$
- 4 (iii) The triangular prism above is fitted into a right circular cylinder, of base radius r units and height h units, as shown below, where the points \underline{E} and \underline{F} are the centres of the circular bases.



Taking the angle AEB as $\frac{2\pi}{n}$, verify that the volume of the cylinder is $\pi r^2 h$ (In your proof you may use the result $\lim_{x \to c} \tan x = x$)

QUESTION 8 continues over.....)

QUESTION 8 continued.....)

6 (b) A particle P moves in the x, y-plane and its co-ordinates (x, y) satisfy the equations

$$\frac{d^2x}{dt^2} = -n^2x$$
 and $\frac{d^2y}{dt^2} = -n^2y$, where *n* is a constant

Initially (t=0), it is given that
$$x = 4$$
, $y = 0$, $\frac{dx}{dt} = 0$ and $\frac{dy}{dt} = 3n$

Show that, as t varies, x and y describe the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$

END OF EXAMINATION PAPER

STANDARD INTEGRALS

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, \quad n \neq -1; \quad x \neq 0, \text{ if } n < 0$$

$$\int \frac{1}{x} dx = \ln x, \quad x > 0$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}, \quad a \neq 0$$

$$\int \cos ax dx = \frac{1}{a} \sin ax, \quad a \neq 0$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax, \quad a \neq 0$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax, \quad a \neq 0$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}, \quad a \neq 0$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}, \quad a > 0, \quad -a < x < a$$

$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left(x + \sqrt{x^2 + a^2} \right), \quad x > a > 0$$

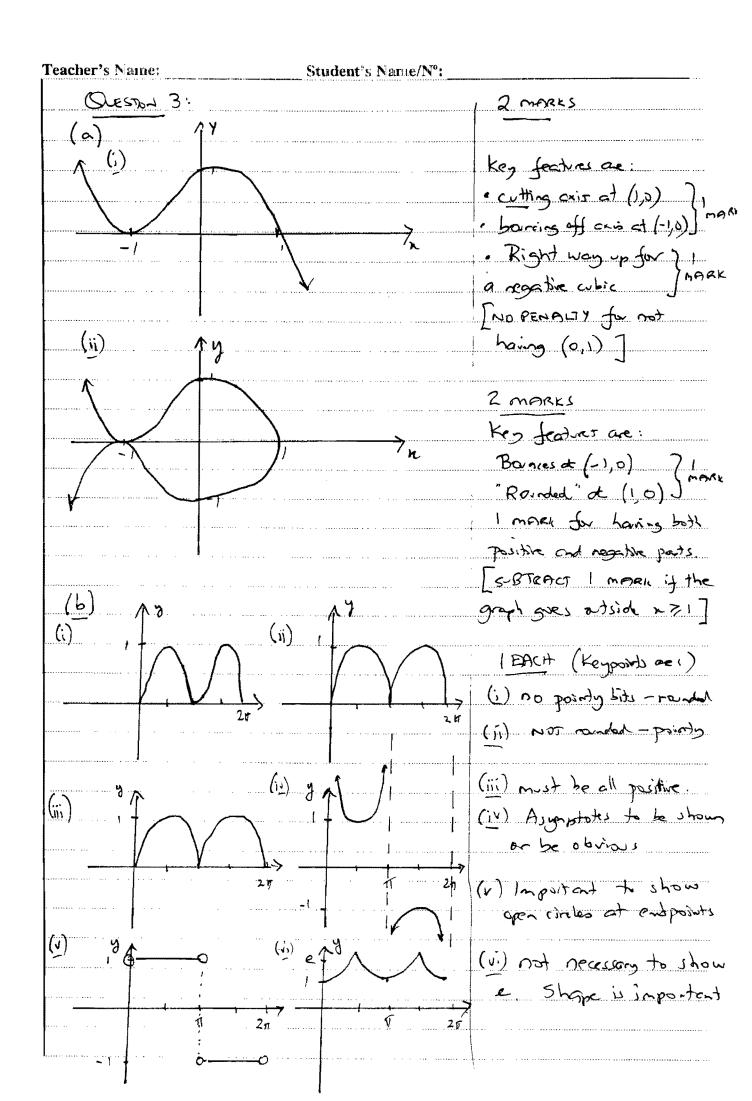
$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left(x + \sqrt{x^2 + a^2} \right)$$

NOTE: $\ln x = \log_e x$, x > 0

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01 A)		
		2 marks for
(Ant B) x+1	$) + ((x^2 + 4)^2 5$	A,B, C.
$\Rightarrow A = -1$	~A+B=0=7B=1	no nother how!
1 (x2+4/x+1)	$= \int \frac{1-\kappa}{\lambda^2++} d\lambda + \int \frac{d\kappa}{\lambda+1}$	\
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<u></u>	= tan 3 - 21, (1+4)+1	(x+1)+ k)
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QUESTION	3 :	LMARKS
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3		(i) to (v)
(1ii) a	9 3 = (77/4 (in) agiz = 7/4.	
		2 marks for just (v)
(u) 3	= \(\begin{aligned} 2 \alpha \	() ONLY for 800 1/2)
3	6= 8 cis (-3%)	
	= 8cis(1/2)	
	= 81	
(6) (1)	1 75= x.	2 morks
	2	acasinide circle and
		below y=x
	1 2 2	
<i>L</i>		
(ii) P	lier on y= x as arg z = T/4	3 marks
	Solving somethoneously	I for reasoning this
	$y=n$ and $(x^2-1)^2+(y-2)=1$	1)
gies.	$2x^2 - 6x + 5 = 1$	
		I for this stop
. `	$-2\chi_{k-1})=0$	non
1	x=2 or $x=1$	3 for P no mater how.
, P	J=2 Z+2i og J+i.	
		122
(c) 2,	1+2y+2n +5y+2 = 0	4 MARKS
1	dy (2x+5y+) = -2(x+y)	
	$\frac{\partial y}{\partial x} = \frac{2(x+y)}{2x+5x+4}$	- I mak
	· · · · · · · · · · · · · · · · · · ·	
Since the	er is a horizontal terrent at (XY) a	= 0 < 1 for this
L	-2(X+Y)=0	
	: y =-x	- 1 for this

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Tagen	quotion becomes $X^{2} + 2X(-x) + (-x)^{5} = 4$ $X^{5} + X^{2} + 4 = 0 \qquad \qquad$
	5 ×2+1/-0
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3 con)	
(c) A	
P	
S	
(ii) By joining AP and PC,	(;) 2 MARKS
In smaller circle, AB is a dionate	They have to consince
: LAPB= 90° (angle in a semi-circle)	you.
Similarly in the larger circle 1618 = 90"	Do not accept things like
: LAPC = 180°	"obvious"
Plies on AC.	
(iii) In ABC, BCAC = sino	3 MARKS
Bc = 2asho	1 MARK
In a BPC, IPCB = (90-0) (onde sun of a BPC)
$PB/BC = \sin(90-0)$	
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= a si, 20	I MARK
A R	
In a ABC, AB/AC = cos O	
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INDAPB, PB/AB = 5h0	
PB = ABsin O	
= 2 a au 0 1 1 10	IMORK
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QUESTION Y:	······ 17)			
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(b) (i) het	3,= T, as 0, and	3= 1, 450,		
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	T. (000,0002 - 5	1700, 17402 1700, + 0020	siho,))	2 marks
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	T,T, cis (0,+0;	_)		
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(ii) For n=2 +1	e formula is to	e (above)	3 mg	ork)
Assume the for				
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ag (3,323h	36n)= ag(13, 36)34,,]	<- 1 ,	\AR
	09(3, 3k) +a			
	for (part (1)		
	from assumption	139", 239"+	,<- 1	MARK
the state of the s	who is true for n= kg	** 1 ** *******************************	**********	
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QUESTONS	•	
(a)	2/9- 5/16=1	
(i) le	ingth of ones = 6) (S MARK)
(<u>ii</u>)	$16 = 9(e^2 - 1)$	
1	$e^2 = 1 + \frac{16}{9}$ $e = \frac{5}{3}$	1 each
(iii)	foci at $(\pm 5,0)$ Directries at $x = \pm \frac{9}{5}$	
1	Asymptotes are y = ± 432	
(6)(1)	$\begin{cases} 1 & (t^2, t^3) \\ 2u & du = 3u^2 \end{cases}$	2 moric)
	$\frac{2y}{dy} = 3x^{2}$ $\frac{dy}{dx} = 3x^{2}$	
	$m_{T} = \frac{3t}{2}$	1 for slope
Equation	of tangent is: $t^3 = 3t/2(n-t^2)$	
t ³	3 - 3tx + 2y = 0	I for egation
	conametes of any Polat P(not on	
) which has a torgent to the (x, y,) solve t3-3tn+3=0	I for seeing this connection
L	es at most 3 solutions for t	The Connection
ie. Here a	re no more than 3 transants	
(iii) If there	e are 3 points, then their paremetes	2 MARK)
t, t.	to are solution to t=3ta+ly=	o I for connecting the
Som at	there = titti = 0	
Since	Pairs = t,t,tt,t,+t,+t,=-	3x, « (t.t.) t,t.)
	= 0 + 6x,	

=6x,

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06 0017 ()		
(b)(i) D (2+	9/2)=0	
$2u/2 + \frac{2u}{b}$	dy = 0	
dy da	$-\frac{\lambda b^2}{\lambda a^2}$	
A+P mT		3 MARKS
=	~ <u> </u>	(con be groted)
At P, tengent is	_5000/	(6, 56 4,0,000)
ansino - absi	$nO = \frac{-b coo}{a \sin o} (n - a coo)$ $n^2O = -b coo + abcos^2$	
ay sino +baci	(o'(o) + o'(o)) do = oa	I make to here
ncoso +		I for division by ob
		2 marks
(ii) N is the	point (acoo,0)	1 for N
	tagent cuti $y = 0$ $\left(\frac{a}{\cos 0}, 0\right)$	1 Jar T
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0.N. OT	= awo. /wo	
(iii) R is where	the tengent meets x = %	5 MARKS
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y = s	0 (1- coo d)	1 for R
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	$b = a \cos \theta - \alpha e$	I MAKE to
slope RS=	1112 = 75100 (1	bih
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QUESTION -	7:	3 marks
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d	n/ = a sec ² 0	
	In = asec'o do	I for this or
. (_0	In Casecodo	equivalent.
(a²	$\frac{\ln}{(a^2 + a^2 + cn^2)^{3/2}} = \int \frac{asee^2 \circ do}{(a^2 + a^2 + cn^2)^{3/2}}$	
	$= \int \frac{\alpha^3 (1 + + c^2) \alpha}{\alpha^3 (1 + + c^2) \alpha}$	
	$= \int \frac{d\theta}{a^2 s c e \theta}$	
		, , , , , , , , , , , , , , , , , , , ,
	$= a^2 \sin \theta + k$	I to get here.
Vx ta n		
/10	Since 2 = atono	
20	$\sin 0 = \sqrt{n^2 + \alpha^2}$	I for sin O
	$\int \frac{dn}{(a^2 + n^2)^{3/2}} = \frac{n}{a^2 \sqrt{n^2 + c^2}} + k$	[no revolute for no k]
	the note of Z=1 be	
the	solutions to $cis50 = 1$	
50	9 = 0, 2π, 4π, 6π, 8π	
	= 0, 27/5, 47/5, 67/5, 87/5	
z=1,	cis 27/5, as 47/5 as 67/5, cis 87/5	. , ,
(i)	217/ 211/2	3 MARKS
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W4 =	CAD 81/2 + 5734 81/8	I MAKK.
=	- cop 27/5 - isin 317/5	
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	- 5	say"similady".
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67 cons	.)		
(B) 51	m of noo)s of 2	,5_1,-0	1 NORW
.: 1+1 .: w	W, +W, +W3+W, +W, +W3+W,	= 0	
(8) W	,) W, +W3+W	4 = - \	
•	$90^{27/5} + 200^{1}$? I MARK
<i>i.</i> c	ص ع ^{بر} ة + حص ⁴⁷	ς = - ½	
-	of nots in pa		
			+ W_W3+W3W4+W8W4=0
	$(+ \overline{U}_{2}) + \omega_{1} ^{2} -$		$(\omega, \overline{\omega}, + \overline{\omega}, \overline{\omega}, = 0)$ $(\omega_{\star} + \overline{\omega}_{\star}) = 0$
. 2000	4π , $(w, +\bar{w},)$	+1=0	I for using w =1 I for using congregates.
	cos 27/5 cos 47/5	+1=0) 66.3.34,63.
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QUAT A	2ATTC 13 C+1/2 N - 1/4 =		
4	元 r 2 n - 1 =	0	

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07 con)		
(c) (i) In = Seci = Sec	٥ مل و عود أن مل	4 MARKS
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	0 = (n-2) sec 0 (-1) coo 0 (-	sino) I for the
	(n-2) sec 0 tono	differentiation of
i Stono Jose	er o do	Sec O
= .	(n-2) (tr) o sec do	I for obasis
and the second s		
In = tono sec	0 - (n-2) [secodo + (n-2)	secodo
= toposec	$(2 - (n-2)I + (n-2)I_{-2}$	
$(n-i)I_n = (n-i)I_n $	$t_{0} = 0$ t_{0	I for evaluating the limits
	odo means n=4.	
3I ₄ - 2	$\Gamma_{n-2} = \left(\sqrt{2}\right)^2$	1 for this
3T4 =	$I_{n-2} = (\sqrt{2})^2$ $2 + 2 \int_0^{\pi/4} \sec^2 \theta d\theta$	
	$2+2[too]_0$	1 for this
$ \overline{V}_{1} = \int_{V_{1}} sec^{\gamma} $	4. todo = 4/3	NO PARTICULAR MARK

O - '1-'1	3 WHEKS
By Smilority	21

$$\frac{Dy}{b} = \frac{P}{P}$$

$$\frac{2}{b} = \frac{1}{A}$$

$$\frac{2}{b}$$

$$(slice)=\Delta V = \frac{b(p-a)}{p}.l.\Delta a$$
 | mark

$$= \int (Rb - \frac{bah}{P}) da \qquad \leftarrow 1 \text{ for this}$$

$$= hba \int_{0}^{P} - \frac{bah}{2P} \int_{0}^{P} da \qquad = hba \int_{0}^{P} - \frac{bh}{2} \int_{0}^{P} da \qquad = hba \int_{0}^{P} - \frac{bh}$$

$$= \frac{hbp - \frac{bn}{2}}{4bhp}.$$

50 volume of cylinder is

lim n V where V is from (ii) above

Now In DEMB, ton = \(\frac{1}{\rangle} \)

As n \rightarrow \alpha, \(\frac{1}{\rangle} \rightarrow \)

As n \rightarrow \alpha, \(\frac{1}{\rightarrow} \rightarrow \)

As n \rightarrow \(\frac{1}{\rightarrow} \rightarrow \)

As n \(\frac{1}{\rightarrow} \rightarrow \rightarrow \)

As n \(\frac{1}{\rightarrow} \rightarrow \rightarrow \rightarrow \rightarrow \rightarrow

Teacher's Name: Student's Name/N°:		
08(0) cons)		<u></u>
Since VOLG	made = lim ov	
	= $\lim_{n \to \infty} o\left(\frac{1}{2}pbh\right)$	
	$= n \left(\frac{\pi p^2 L}{2} \right)$	I for implification
	= TPL	
	= TI CZL [Since]	1 for p =>1
	(Y - > 1	J
(c) 12.	······································	6 MARKS
$\frac{\partial h}{\partial t^2} = -h^2$	n and $\int_{-\infty}^{2} (1-x)^2 y$	
		, !
=> x=awo fit+	$x)$ $y = b \cos(nt + B)$	
: , x= -an sin (nt +	-d) y=-nbsin(nt+ps)	I for both of these
$A^{\dagger} t = 0$, $dn = 0$	A++=0, y=30	
Tt = 0	3n = -bnsin/3	
, , ∠=0	$\therefore \sin \beta = -\frac{3}{5}b$	Ifw d
ie i = - on sin (nt		9
ALSO at t=0 n=1	/ / / / / / / / / / / / / / / / / / /	-
4 = a	$0 = b \cos \beta$	1 for a
	$\beta = \sqrt{2}$	1 for la
x= 400 nt	Since Sin 3 = -3/6	
	b = -3	1 for p
	· y = 3600 (nt+7)	
	= 3 sin(nt))
n'/6 + 3 =	16 cont 9 sin'nt	& I for fairling
16 + 19 -	16 + 9	
=	<u> </u>	<u></u>
<u></u>		