Name:	MathsTeacher:	File
	TVARRANCE CERCITICS.	

SYDNEY TECHNICAL HIGH SCHOOL



Year 11

Mathematics

Assessment 2

JULY, 2015

Time allowed: 90 minutes

General Instructions:

- Marks for each question are indicated on the question.
- Approved calculators may be used
- All necessary working should be shown
- Full marks may not be awarded for careless work or illegible writing
- Begin each question on a new page
- Write using black or blue pen
- All answers are to be in the writing booklet provided

- Section 1 Multiple Choice
 - Questions 1-5
 - 5 Marks
- Section II Questions 6-13
 - 63 Marks

(A)
$$x = \frac{-5 \pm \sqrt{17}}{4}$$

ı

b)

(B)
$$x = \frac{5 \pm \sqrt{17}}{4}$$

(C)
$$x = \frac{-5 \pm \sqrt{33}}{4}$$

(D)
$$x = \frac{5 \pm \sqrt{33}}{4}$$

2. Which inequality defines the domain of the function $f(x) = \frac{1}{\sqrt{x+3}}$?

(A)
$$x > -3$$

(B)
$$x \ge -3$$

(C)
$$x < -3$$

(D)
$$x \le -3$$

3. Find the values of m for which $24 + 2m - m^2 \le 0$

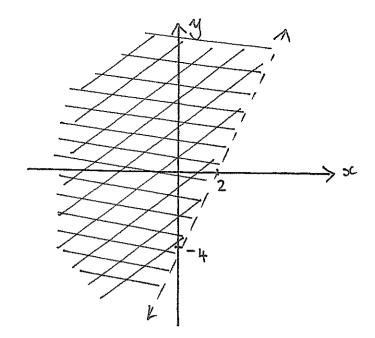
(A)
$$m \le -4$$
 or $m \ge 6$

(B)
$$m \le -6 \text{ or } m \ge 4$$

(C)
$$-4 \le m \le 6$$

(D)
$$-6 \le m \le 4$$

4



The shaded region is best described by the inequality.

(A)
$$2x - y - 4 \ge 0$$

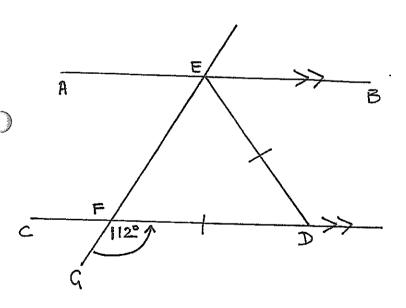
(B)
$$2x - y - 4 \le 0$$

(C)
$$2x - y - 4 > 0$$

(D)
$$2x - y - 4 < 0$$

5.

(A) 112°



(C) 68°

(D) 44°

(B) 24°

If AB \parallel CD, ED = FD and \angle DFG = 112° then \angle BED =

Section II

Question 6 – (8 marks)

Mark

2

)

a) Evaluate $\sqrt[3]{\frac{651}{4\pi}}$ to four significant figures

b) Solve $2 - 3x \le 8$ and sketch your solution on a number line

2

c) Solve $x^2 - 6x = 0$

2

d) Solve 4 < 4x - 3 < 9

2

Question 7 – (8 marks) – Start a new page

Express $\frac{a^{-1}+b^{-1}}{a+b}$ in simplest fraction form without using negative indices.

2

b) Solve |5x-2| = |3x+4|

2

c) Solve $\frac{5}{8}(x+4) = 4x - \frac{1}{2}$

a)

2

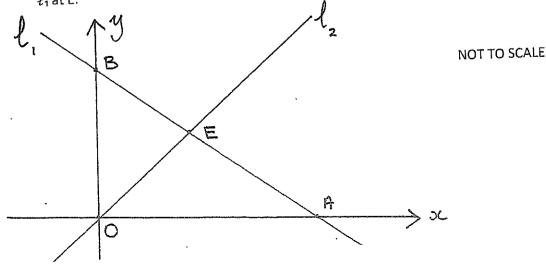
d) Express $\frac{3\sqrt{2}}{3\sqrt{2}+2\sqrt{3}}$ in the form $a+b\sqrt{6}$

2

Question 8 – (8 marks) – Start a new page

a) The diagram shows a line ℓ_1 with equation 3x + 4y - 12 = 0, which intersects the y axis at B.

A second line ℓ_2 with equation 4x-3y=0, passes through the origin O and intersects ℓ_1 at E.



(i) Show that coordinates of B are (0, 3).

1

(ii) Show that ℓ_1 is perpendicular to . ℓ_2

2

- (iii) Show that the perpendicular distance from O to ℓ_1 is $\frac{12}{5}$ units
- 1
- (iv) Using Pythagoras' theorem, or otherwise, find the length of the interval BE. 1
- (v) Hence, or otherwise, find the area of $\triangle BOE$.

1

b) Simplify $\frac{x^3-1}{x^2-1} \div \frac{3x^2+3x+3}{x^2-4x-5}$

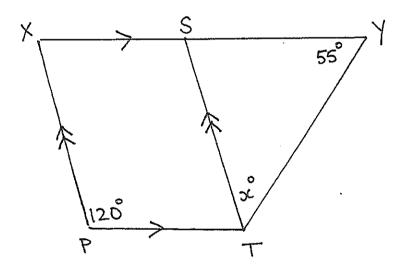
2

Question 9 – (7 marks) – Start a new page

Mark

a)

)_)



2

XY || PT and XP || ST

Redraw the diagram in your answer booklet.

Find x giving reasons for your answer.

b) A function is defined as follows

$$f(x) = \begin{cases} 0 & \text{if } x \le -3 \\ -1 & \text{if } -3 < x < 0 \\ x & \text{if } x \ge 0 \end{cases}$$

Find

i)
$$f(-3)+f(-2)+f(2)$$

1

ii) $f(a^2)$

1

- c) i) Sketch y=|x-1| and y=x+1 on the same axes. Use a ruler and label each function carefully. Show any points of intersection with the x and y axes. Your sketch should be approximately half a page.
 - ii) Hence solve |x-1| > x+1

2

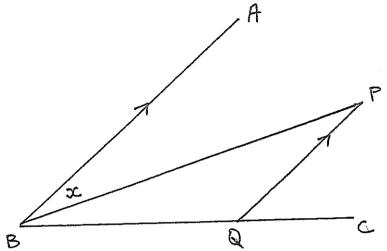
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1

1

1

Question 10 – (8 marks) – Start a new page



Let ABP=x
BP bisects ABC and AB||PQ
Redraw this diagram in your answer booklet. Use a ruler.
Your diagram should be approximately half a page in size.
Prove that BQ=PQ

- b) Find the exact value of
 - i) $\sin 225^{\circ}$

a)

- ii) $tan(-30^{\circ})$
- c) If θ is obtuse and $\tan \theta = \frac{1}{5}$ find the exact value of $\cos \theta$
- d) $\operatorname{Prove} \frac{1}{\sin\theta.\cos\theta} \tan\theta = \cot\theta$

Question 11 – (8 marks) – Start a new page

- a) Solve the following in the domain $0^{\circ} \le x \le 360^{\circ}$. (write your answers correct to the nearest minute)
 - i) $\tan 2\theta = -1$

2

ii) $3 \sin^2 \theta + 2 \sin \theta = 0$

2

iii) $3\sin\theta = 2\cos\theta$

2

b) Find $\lim_{x\to 3} \frac{x-3}{x^2-6}$

2

Question 12 - (8 marks) - Start a new page

ר (ר) Differentiate the following

i)
$$y = 4x^3 - x + 5$$

1

ii)
$$y = (3x^2 - 4)^4$$

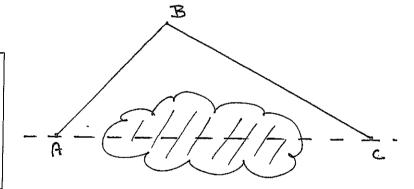
2

iii)
$$y = \frac{x+1}{x-1}$$

2

b)

A surveyor walking due east turns at A to avoid marshy country and walks 270 metres to B on a bearing of 048° and then turns and walks on a bearing of 112° to C. C is due east of A.



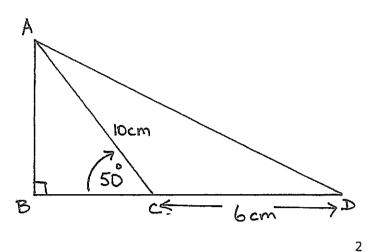
i) Redraw the diagram showing the size of angles BÂC, ABC and BCA.

1

ii) Hence find the length of AC to the nearest metre.

2

a) In the figure CD = 6cm, AC = 10cm, angle ACB = 50° and angle ABC = 90° . Find:



i) AD to the nearest cm

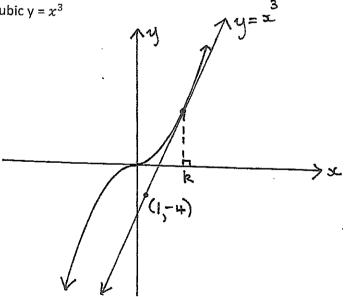
ii) Area of ΔACD to the nearest cm².

1

b) i) Show that k = 2 is a solution to the equation $2k^3 - 3k^2 - 4 = 0$

1

ii) The diagram shows a tangent at the point where x = k (where k > 0) to the cubic $y = x^3$



 \propto . Find the gradient of the tangent at x=k

1

 β . Find the equation of the tangent at x = k

2

 γ . If the tangent is found to pass through (1,-4) find the value of k.

1

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c)
$$x^2 - 6x = 0$$

 $x(x - 6) = 0$

d)

$$\frac{-12-0}{4 < 4x - 3 < 9}$$

$$\frac{(b+a)}{ab} \times \frac{1}{(a+b)}$$

ab

$$5x-2=3x+4 \quad 5x-2=-(3x+4)$$

$$2x = 6$$
 $5x - 2 = -3x$
 $3x = 3$ $8x = -2$
and $3x = -\frac{1}{4}$

c)
$$\frac{5}{8}(x+4) = 4x - \frac{1}{2}$$

 $5(x+4) = 32x - 4$

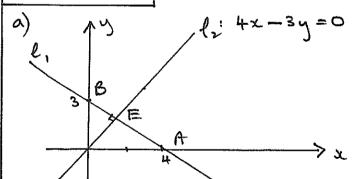
$$\alpha = \frac{24}{27}$$

$$\frac{8}{9} = K \cdot \dot{}$$

$$\frac{3\sqrt{3}}{3\sqrt{2}+2\sqrt{3}} \times \frac{3\sqrt{2}-2\sqrt{3}}{3\sqrt{2}-2\sqrt{3}}$$

$$\frac{3\sqrt{2}}{3\sqrt{2}+2\sqrt{3}} = 3-\sqrt{6}$$

Question 8

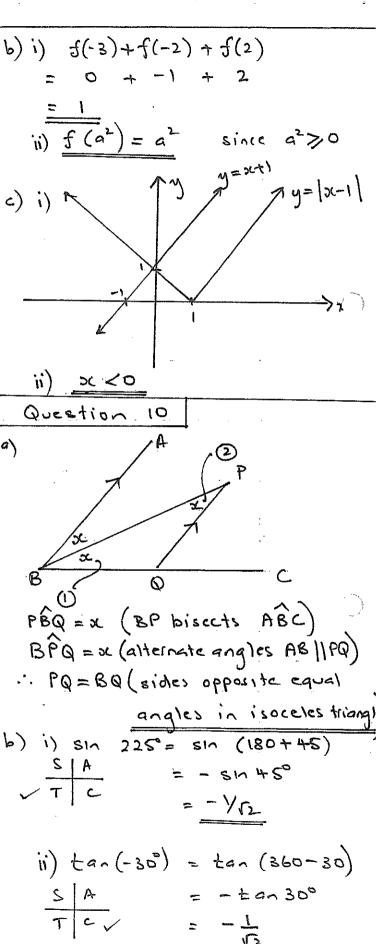


i) sub.
$$H = 0$$
 into 1: $3x + 4y - 12 = 0$
 $4y = 12$
 $y = 3$

$$\frac{1}{1}$$
 $m_{\xi_{1}} = -\frac{3}{14}$ $m_{\xi_{2}} = \frac{4}{3}$

since
$$\frac{-3}{4} \cdot \frac{4}{3} = -1$$

11)
$$P = \frac{3.0 + 4.0 - 12}{\sqrt{9 + 16}}$$
 $l_1: 3x + 4y - 12 = 0$
 $P = \frac{12}{5}$
 $\therefore P = \frac{12}{5}$
 $\therefore P = \frac{12}{5}$
 $\therefore P = \frac{12}{5}$
 $\Rightarrow P = \frac{12}{5}$
 \Rightarrow



c)
$$tan \theta = -\frac{1}{5}$$
 $tan \theta = -\frac{1}{5}$
 t

b)
$$\lim_{x \to 3} \frac{1(x-3)}{(x+3)(x+3)}$$

= $\frac{1}{6}$

Question 12

a)i) $\frac{1}{6}(4x^3-x+5) = \frac{12x^2-1}{2x^2-1}$

ii) $\frac{1}{6}(3x^2-4)^4 = 4 \cdot 6x(3x^2-4)^3$

= $\frac{24x(3x^2-4)^3}{2x^2-1}$

iii) Let $u = x + 1$ $v = x - 1$
 $v' = 1$
 $v' =$

AC = 648 m (nearest m)

Question 13 A i). AD= 102+62 - 2.10.6 cos 130° = 100 + 36 - 120 cos 130° AD = 15 cm (nearest cm) ii) area DACD = 1.6.10. sin 130° = 23cm (nearest cm2) b) i) sub te = 2 into $2k^3 - 3k^2 - 4 = 0$ LHS = 16 - 12 - 4 = RHS : | k = 2 is a solution (i)

 $\beta. pt (-k, k^3)$ $tangent: y-k^3 = 3k^2(x-k)$ $y-k^3 = 3x-k^2-3k^3$ $y = 3x-k^2-2-k^3$

8. sub (1,-4) into tangent $-4 = 3k^2 - 2k^3$ $2k^3 - 3k^2 - 4 = 0$ Soon part i) k = 2