## SYDNEY TECHNICAL HIGH SCHOOL



Year 11 2 Unit May 2006

Common Test

Time allowed: 70 mins	Name:	
	Teacher:	
	reaction.	

#### **Instructions**:

- Begin each question on a new page
- Marks shown are approximate and may be varied
- Show necessary working
- Full marks may not be awarded if working is poorly set out or difficult to read

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	TOTAL
/8	/7	/7	/7	/8	/7	/8	/6	/58

#### Question 1

- a) Evaluate  $\frac{1.3 \times 10^{-3}}{8.6 4.2}$ . Give your answer in scientific notation using 2 significant figures. 2
- b) Express 0.42 as a simplified fraction.
- c) Simplify  $\sqrt{27} \sqrt{12}$
- d) Evaluate  $x^2 3x + 1$  when  $x = 3\sqrt{5}$ . Leave your answer in simplest form 2

#### Question 2

- a) Simplify: (i) 3x 4x(3 x) 1
  - (ii)  $(4a^3b)^2 \times \frac{a^2}{6b^3}$  2
- b) Express the answer to  $\sqrt{x} \div \frac{1}{x}$  in simplified index form
- c) Express  $8^a \times 4^{a+1}$  as a power of 2

# Question 3

- a) Factorise (i)  $x^2 5x 6$ 
  - (ii)  $x^3 8$
  - (iii)  $x^3 + x^2 + x + 1$
- b) Simplify (i)  $\frac{x^2 x}{x^2 1}$ 
  - (ii)  $\frac{4}{x+2} \frac{1}{x}$

#### Question 4

- a) Evaluate  $|-3| |-4|^2$
- b) Solve (i)  $\frac{2x-4}{3} = x+2$ 
  - (ii)  $2x^2 + 9x 5 = 0$
  - $(iii) \left| 1 2x \right| = 6$

#### **Question 5**

- a) Solve simultaneously 3x y = 0 and 4x 2y = 3
- b) Solve  $\frac{4}{x+2} + x = 3$
- c) Given  $f(x) = 3x^2 2x$ , find and simplify:
  - (i) f(-3)
  - (ii) f(x+h) + f(x) 2

#### Question 6

a) Sketch each function. Use a ruler for all straight lines and show any x, y intercepts:

(i) 
$$y = \frac{1}{x+1}$$

(ii) 
$$y = -\sqrt{4 - x^2}$$

(iii) 
$$y = |3x - 6|$$

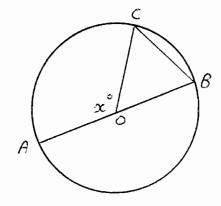
- b) (i) Sketch  $y = x^2 + 2x 3$ . Show all intercepts 2
  - (ii) Solve  $x^2 + 2x 3 \le 0$ . You may use the sketch above to help
  - (iii) What is the range of the function in (i)

### Question 7

- a) State the domain and range of the function  $y = \sqrt{x-4}$
- b) Find the centre of the circle  $x^2 4x + 4 + y^2 + 6y = 0$
- c) (i) Sketch  $y = 2^x$  and y = |x 1| on the same axes
  - (ii) Hence or otherwise, solve  $|x-1| > 2^x$
  - (iii) On your graph in (i), neatly shade the intersected region of  $x \ge 0$  and  $y \ge 2^x$

# Question 8

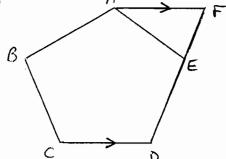
a)



O is the centre of the circle. If  $\angle AOC = x^o$ , prove

that 
$$\angle B = \frac{x^o}{2}$$

b)



ABCDE is a regular pentagon. AF//CD and DE is produced to F.

Set out a geometrical proof to find the size of  $\angle$  FAE. 3

# SOLUTIONS

$$99x = 42$$
 Ofor convert

 $x = 42$ 

method

$$0 = \frac{14}{33} \leftarrow 0$$

a) 
$$3\sqrt{3} - 2\sqrt{3} = \sqrt{3} = \sqrt{0}$$

$$(3J5)^2 - 3(3J5) + 1$$

$$(2/a)$$
 (i)  $3x - 12x + 4x^2$   
=  $4x^2 - 9x$  0

$$\frac{(11) (6a^{6}b^{2} \times a^{2})}{(11) (6a^{6}b^{2} \times a^{2})} = \frac{8a^{8}}{34} = 0$$

$$\frac{k}{x} = x^{-1} = x^{\frac{3}{2}} \quad \bigcirc$$

$$(2^{3})^{n} \times (2^{2})^{n+1} \leftarrow \emptyset$$

$$= 2^{3n} \times 2^{2n+2}$$

$$(3)_{(1)}(x-6)(x+1) \qquad 0$$

$$(1)_{(x-2)(x^2+2x+4)} \qquad 0$$

$$(iii) x^{2}(x+1)+1(x+1)$$
  
=  $(x+1)(x^{2}+1)$ 

$$\frac{(x+1)(x+1)}{(x+1)(x+1)} = \frac{x}{x+1}$$

$$\frac{(i(i))}{\varkappa(\varkappa+2)} \frac{4\varkappa}{-\varkappa(\varkappa+2)} - \frac{1(\varkappa+2)}{\varkappa(\varkappa+2)} \odot$$

$$= \frac{4\varkappa-\varkappa-2}{\varkappa(\varkappa+2)}$$

$$= \frac{3\varkappa-2}{\varkappa(\varkappa+2)} \odot$$

(iii) 
$$1-2x = 6$$
 or  $-(1-2x) = 6$  (0)  $-2x = 5$  or  $-1+2x = 6$ 

$$(5)$$
a)  $3x-y=0$  —  $0$   
 $4x-2y=3$  —  $0$ 

$$0x-2:-6x+2y=0$$
 | mark for  $(2)+(3):-2x=2$ 

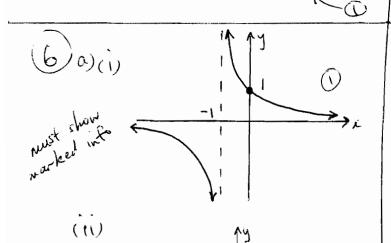
$$(2+3): -2x = 3$$

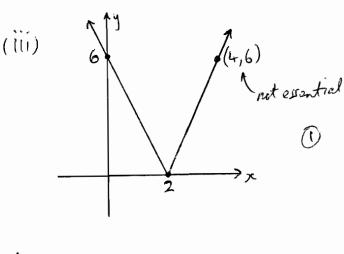
b) 
$$4 + x(x+2) = 3(x+2)$$
  
 $4 + x^2 + 2x = 3x + 6$   
 $x^2 - x - 2 = 0$   $(x-2)(x+1) = 0$   
 $x = 2 \text{ or } -1$   $0$ 

c)(i) 
$$f(-3) = 27+6$$
  
= 33  $\leftarrow 0$ 

$$(11) 3(x+h)^{2}-2(x+h)+3x^{2}-2x$$

$$= 3x^{2}+6xh+3h^{2}-2x-2h+3x^{2}-2x$$





b) (i) 
$$y = (x-1)(x+3)$$
 $-3$ 
 $-3$ 
 $-3$ 
 $-3$ 
 $-3$ 

(B) a) 
$$x = 4 \ge 0$$

(B) a)  $x = 4 \ge 0$ 

(B) a)  $x = 4 \ge 0$ 

(C) (i)

(B) a)  $x = 4 \ge 0$ 

(B) a)  $x = 4 \ge 0$ 

(C) (ii)

(B) a)  $x = 4 \ge 0$ 

(B) a)  $x = 4 \ge 0$ 

(C) (iii)

(D) (10)  $x = 6 \ge 0$ 

(D) (11)  $x = 6 \ge 0$ 

(12)  $x = 6 \ge 0$ 

(13)  $x = 6 \ge 0$ 

(14)  $x = 6 \ge 0$ 

(15)  $x = 6 \ge 0$ 

(16)  $x = 6 \ge 0$ 

(17)  $x = 6 \ge 0$ 

(17)  $x = 6 \ge 0$ 

(17)  $x = 6 \ge 0$ 

(18)  $x = 6 \ge 0$ 

(19)  $x = 6 \ge$