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SYDNEY TECHNICAL HIGH SCHOOL



Year 11 Mathematics Extension 1

Preliminary Course
Assessment 1

May, 2015

Time allowed: 70 minutes

General Instructions:

- Marks for each question are indicated on the question.
- · Approved calculators may be used
- All necessary working should be shown
- Full marks may not be awarded for careless work or illegible writing
- Begin each question on a new page
- Write using black or blue pen
- All answers are to be in the writing booklet provided

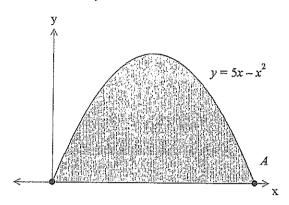
Section 1 Multiple Choice Questions 1-5 5 Marks

Section II Questions 6-11 51 Marks



Section 1 - Multiple Choice - Answer on the sheet provided.

1 The diagram shows the graph of the function $y = 5x - x^2$.



Which pair of inequalities specify the shaded region?

(A)
$$y \le 5x - x^2$$
 and $y \le 0$.

(B)
$$y \le 5x - x^2$$
 and $y \ge 0$.

(C)
$$y \ge 5x - x^2$$
 and $y \le 0$.

(D)
$$y \ge 5x - x^2$$
 and $y \ge 0$.

2 What is the solution to the equation |2x-5| = x+2?

(A)
$$x = 1$$

(B)
$$x = 7$$

(C)
$$x = 1$$
 or $x = 7$

(D)
$$x = 1 \text{ or } x = -7$$

3 If $3\cos\theta + 2 = 0$ and $\tan\theta > 0$, what is the exact value of $\sin(\theta + 180^\circ)$?

(A)
$$-\frac{\sqrt{5}}{3}$$

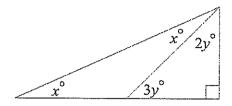
(B)
$$-\frac{\sqrt{5}}{2}$$

(C)
$$\frac{\sqrt{5}}{2}$$

(D)
$$\frac{\sqrt{5}}{3}$$

- 4 A woman is standing on level ground 70 metres from the base of a vertical cliff. If the angle of elevation to the top of the cliff is 40°, what is the height of the cliff, correct to the nearest metre?
- (A) 58 metres
- (B) 59 metres
- (C) 60 metres
- (D) 61 metres

5



What is the value of x?

- (A) 18°
- (C) 36°

- (B) 27°
- (D) 45°

End of section 1

SECTION II

(Start each new question on a new page)

QUESTION 6: (8 Marks)

(a) Fully factorise, $x^4 - xy^3$ 2

(b) Write down the exact value of $sin^2 225^o + cosec150^o$ 2

(c) Solve for x: $27^x \times (\frac{1}{3})^{x-1} = 81$ 2

(d) State the Domain and Range of $y = \frac{2x+1}{x-2}$

QUESTION 7: (8 Marks) Start a new page

Marks

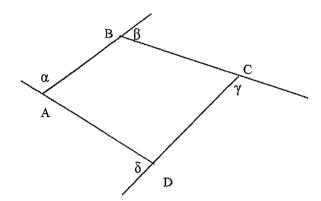
(a) If $\tan\theta = p$ and $\sec\theta < 0$, find an expression for $\sin\theta$

2

2

(b) ABCD is a quadrilateral with external angles α , β , γ and δ .

Explain why $\sin (\alpha + \beta + \gamma + \delta) = 0$

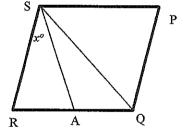


(c) PQRS is a rhombus. SA bisects ∠RSQ

$$\angle RSA = x^o$$

Prove: (i) $\angle RSP = 4x^o$

(ii)
$$\angle SAR = 3x^o$$



2

2

QUESTION 8: (8 Marks) Start a new page

Marks

(a) Solve for θ , if $\sin 2\theta = \cos \theta$ and $0^{\circ} < \theta < 90^{\circ}$

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(b) If $f(x) = \frac{1}{x}$ write $\frac{f(x+h)-f(x)}{h}$ as a simplified fraction.

3

(c) If f(x) = 2x - 3, find a simplified expression for f(f(-x))

2

(d) Sketch the function $y = \frac{1}{\sqrt{4-x}}$ showing all necessary information.

2

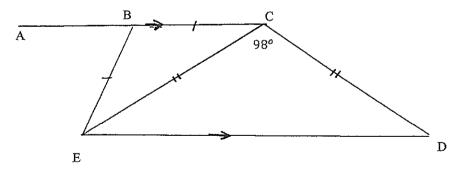
QUESTION 9: (8 Marks) Start a new page

Marks

(a) Solve $sec\theta = -2$ for $-180^{\circ} \le \theta \le 180^{\circ}$

2

(b) Consider the quadrilateral BCDE where BC is parallel to ED and CB is produced to A, \angle ECD = 98°, BC = BE and EC = CD



3

Copy the diagram showing all given information and find the size of angle ABE, giving reasons.

(c) Solve the inequality $\frac{x-2}{x+3} > -2$

3

QUESTION 10: (10 Marks) Start a new page

Marks

(a) (i) Sketch the region $y \le 6 - |2x|$ on a number plane

3

(ii) Solve 6 - |2x| = |x|

2

(iii) Find the area of the region held simultaneously by

2

- $y \le 6 |2x|$ and $y \ge |x|$
- (b) Solve for θ , $2\sin^2\theta = \sin\theta\cos\theta$, $0^o \le \theta \le 360^o$, correct to the nearest minute.

3

QUESTION 11: (9 Marks) Start a new page

Marks

(a) Show that
$$sec\theta + tan\theta = \frac{cos\theta}{1-sin\theta}$$

(b) (i) Sketch the function $f(x) = \frac{1}{x^2+1}$

2

3

(ii) On a separate number plane, sketch the function y = -f(x) - 1

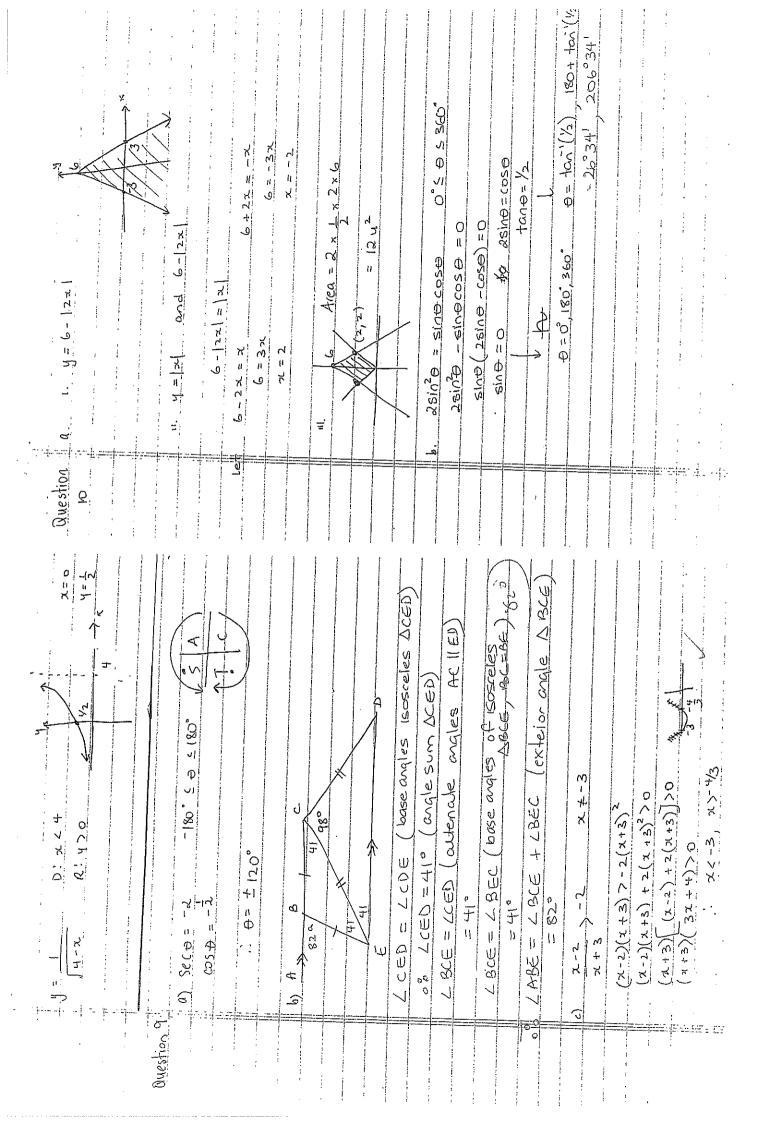
2

(c) Solve |x+2| + |x-2| = 6 - 4x

2

End of Assessment task

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ouestino.	3 x x 3 x / 2 / 2 x / 2	2 PSA = LPSQ+ LQSA (adjacent ancles)
9		
	$ b\rangle (\sin 225^{\circ})^{2} + \frac{1}{2} = (-1/5)^{2} + (1/1)^{\circ}$	į
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70017011	x-2 R. 46R, 4+2	b) $x+h - \frac{1}{x} / x (x+h)x$
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	c) 1. LRSA=x given	4
To the relation of the second	LASO = LRSA (given SA bilects / RSA)	= 2[-2x-3]-3
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1. 1. Show that secont tang = 10050	$\frac{z}{\cos 5} + \sin 6$ $\cos 5$ $\cos 6$ $\cos 6$ $\cos 6$ $\cos 6$ $\cos 6$ $\cos 6$	$ \mathbf{a}\cdot\mathbf{f}(x) = \frac{1}{x^2 + 1}$	
11. 11.			