

Name: Maths Class:

SYDNEY TECHNICAL HIGH SCHOOL



Year 10 Mathematics Yearly

Examination

2015

Time allowed: 2 hours

General Instructions:

- Marks for each question are indicated on the question.
- Approved calculators may be used
- All necessary working should be shown
- Full marks may not be awarded for careless work or illegible writing
- ***Begin each question on a new page***
- Write using black or blue pen
- All answers are to be in the writing booklet provided

Section 1 Multiple Choice
Questions 1-25
20 Marks

- Attempt Questions 1 - 25
- Allow about 40 minutes for this section
- Answer on the Multiple choice answer sheet provided

Section II Questions 26-30
50 Marks

- Attempt questions 21 to 25
- Allow about 80 minutes for this section

Section I

25 marks

Attempt Questions 1–25

Allow about 40 minutes for this section

Use the multiple-choice answer sheet for Questions 1–25.

1. Expand and simplify $2x^2 + 3xy - 2x(x - 4y)$.

- (A) $11xy$
- (B) $4x^2 - 5xy$
- (C) $-4x^2 - 11xy$
- (D) $-11xy$

2. If $U = a^3 + bc^2$, find U when $a = 2$, $b = -1$ and $c = 2$.

- (A) $U = 9$
- (B) $U = 2$
- (C) $U = 12$
- (D) $U = 4$

3. The solution to $2x + 9 = 5x - 12$ is:

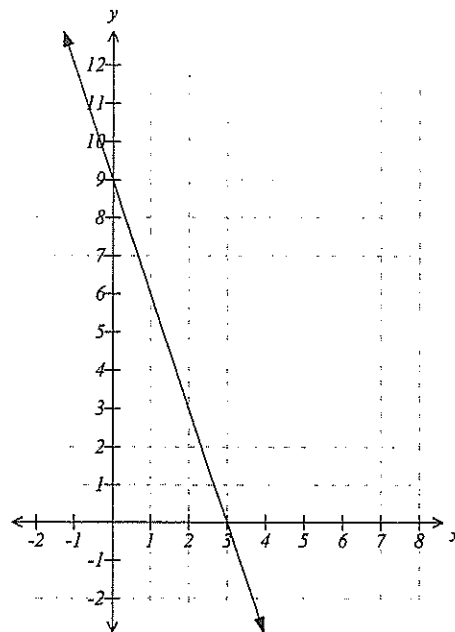
- (A) $x = -1$
- (B) $x = 7$
- (C) $x = 3$
- (D) $x = \frac{3}{7}$

4. Roger works for a fast food outlet where he is paid \$14.00 per hour for up to 8 hours per day and time and a half after that. What would he earn for a day where he works for 12 hours?

- (A) \$168.00
- (B) \$196.00
- (C) \$252.00
- (D) \$224.00

5. The line shown at right has gradient:

- (A) 9
- (B) 3
- (C) -3
- (D) $-\frac{1}{3}$



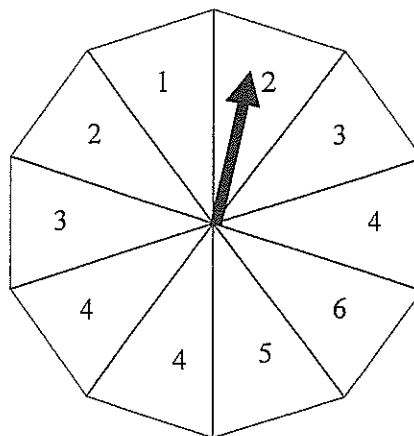
6. Kerrie has a taxable income of \$45 200. The Medicare levy is calculated as 1.5% of taxable income. What is her Medicare levy?

- (A) \$2 260.00
- (B) \$6 780.00
- (C) \$301.33
- (D) \$678.00

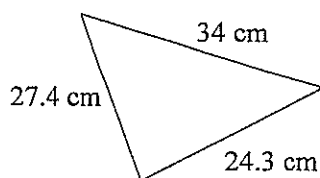
7. Lasseter invests his lottery win of \$20 000 in a term deposit which pays 9% p.a. compounded monthly. What will the investment be worth after the term of 2 years?
- (A) \$20 301
(B) \$23 600
(C) \$23 928
(D) \$23 762
8. Marika buys a camera for \$308.00 including GST. She can claim the GST back, as she is travelling overseas. How much is the GST? (Assume GST is 10%)
- (A) \$28.00
(B) \$30.80
(C) \$280.00
(D) \$20.00
9. When a single card is drawn from a normal pack of 52 cards, what is the probability that it is not an Ace?
- (A) $\frac{1}{13}$
(B) $\frac{12}{13}$
(C) $\frac{1}{4}$
(D) $\frac{3}{4}$

10. The spinner below is used to determine the number of squares moved in a game. What is the probability that, on a single spin, the outcome is a number greater than 4?

- (A) $\frac{1}{5}$
(B) $\frac{1}{2}$
(C) $\frac{4}{5}$
(D) $\frac{1}{10}$



11. The smallest angle in the triangle below is θ



What is the value of θ to the nearest degree?

- (A) 30°
(B) 45°
(C) 53°
(D) 82°
12. A glass has its capacity measured as 250 mL to the nearest 10 mL. What is the percentage error in this measurement?
- (A) $\pm 10\%$
(B) $\pm 0.2\%$
(C) $\pm 4\%$
(D) $\pm 2\%$

13. The ratio of sand : cement in a mortar mix is 9 : 2. How many buckets of sand would be needed to go with 12 buckets of cement?

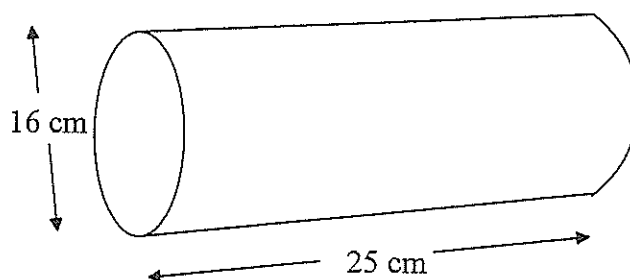
- (A) $1\frac{1}{2}$ buckets.
- (B) $14\frac{2}{3}$ buckets.
- (C) $2\frac{2}{3}$ buckets.
- (D) 54 buckets.

14. A car travels from Bourke to Dubbo at an average speed of 96 km/h. Write this as an average speed in m/s.

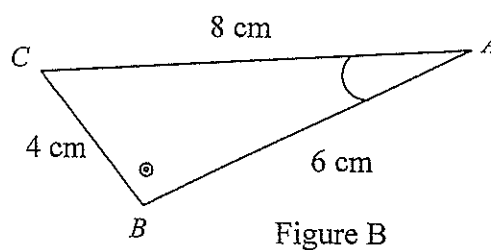
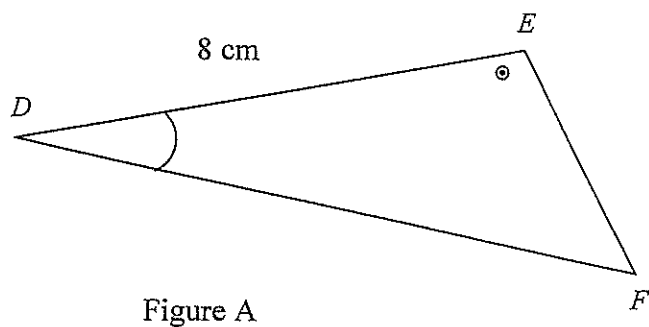
- (A) 16 m/s.
- (B) $345\frac{3}{5}$ m/s.
- (C) $26\frac{2}{3}$ m/s.
- (D) $66\frac{2}{3}$ m/s.

15. Find the volume of the cylinder shown below.

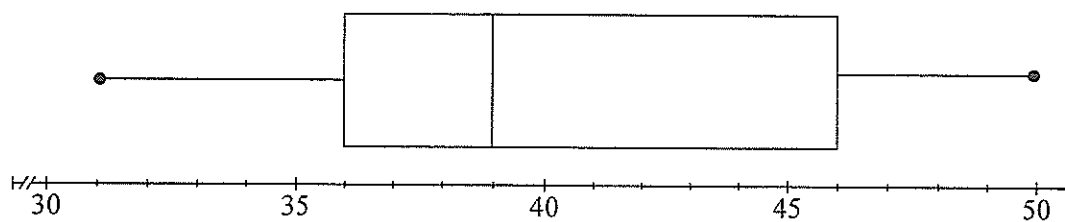
- (A) 20 106 cm³
- (B) 5 027 cm³
- (C) 1 257 cm³
- (D) 1 659 cm³



16. Figure A and Figure B, shown below, are similar. What is the scale factor which would transform Figure A to Figure B?



- (A) $\frac{3}{4}$ (B) $\frac{4}{3}$
 (C) 2 (D) $\frac{1}{2}$
17. The box and whisker plot shows the results of a test out of 50 (fifty). What information **cannot** be found from the plot?



- (A) The median mark.
 (B) The interquartile range of the marks.
 (C) The range of the marks.
 (D) The mean mark.

18. The stem and leaf plot gives the ages of a group of people at a function. What is the median age?

- (A) 37.5
(B) 37
(C) 38
(D) 41

2	3 4 6 6 7
3	0 2 4 5 7 8 9
4	1 2 4 6 8
5	2 5 6
6	0

19. A formula for finding the sum (S) of the angles in a regular polygon is:

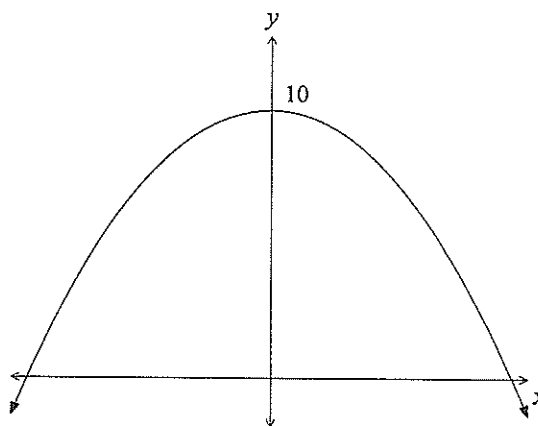
$$S = (2n - 4) \times 90^\circ,$$

where n is the number of sides in the figure. Which of the following formulae could give the same result?

- (A) $S = (n - 2) \times 45^\circ$
(B) $S = 4(n - 2) \times 90^\circ$
(C) $S = (n - 2) \times 180^\circ$
(D) $S = 4(n - 8) \times 180^\circ$

20. Which equation could describe the graph shown?

- (A) $y = x^2 + 10$
(B) $y = 2x + 10$
(C) $y = 10 - x^2$
(D) $y = 10 - 2x$



21. What is the centre and radius of the circle with the equation $x^2 + y^2 + 6x - 8y - 11 = 0$?

- (A) Centre $(-3, -4)$ and radius 36
- (B) Centre $(-3, 4)$ and radius 36
- (C) Centre $(-3, -4)$ and radius 6
- (D) Centre $(-3, 4)$ and radius 6

22. What is the midpoint of $(-3, 5)$ and $(2, -3)$?

- (A) $(-\frac{1}{2}, 1)$
- (B) $(\frac{1}{2}, -1)$
- (C) $(0, 1)$
- (D) $(2\frac{1}{2}, 4)$

23. The line $6x - ky = 2$ passes through the point $(3, 2)$. What is the value of k ?

- | | |
|--------------------|---------------------|
| (A) $\frac{10}{3}$ | (B) $-\frac{10}{3}$ |
| (C) -8 | (D) 8 |

24. What is the solution to the quadratic equation $x^2 - 5x + 3 = 0$?

- (A) $x = \frac{-5 \pm \sqrt{13}}{2}$
- (B) $x = \frac{-5 \pm \sqrt{38}}{2}$
- (C) $x = \frac{5 \pm \sqrt{13}}{2}$
- (D) $x = \frac{5 \pm \sqrt{38}}{2}$

25. The sum of the interior angles of a regular polygon is 2520° . What is the size of each interior angle?

(A) $140^\circ 30'$

(B) $157^\circ 30'$

(C) 210°

(D) 315°

Section II

50 Marks

Attempt all questions 25 to 30

Allow about 80 minutes for this section

Answer all questions, starting each question on a new sheet of paper in your answer booklet, with the question number at the top of the page. Your responses should include relevant mathematical reasoning and/or calculations.

Question 26

(10 marks)

Start a new sheet of paper.

- a) Round 183 479 208 to 3 significant figures 1
- b) Solve the equation $\frac{2x}{3} + 5 = x + 2$. 1
- c) Write the formula $g = \frac{sm}{2} + a$ with m as the subject. 1
- d) Factorise $4a - 2b - 6ab + 3b^2$ 1
- e) Write the following as powers of 2:
- (i) $\sqrt[5]{2}$ (ii) $\sqrt[3]{32}$ (iii) $\frac{1}{\sqrt[5]{64}}$ 3
- f) The probability of tossing a head on a biased coin is 0.7.
What is the probability of tossing a tail on this coin? 1
- g) Given $x = \sqrt{5} + 2$, find b if $x + \frac{1}{x} = 2\sqrt{b}$ 2

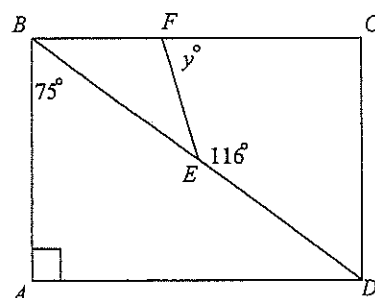
Question 27

(10 marks)

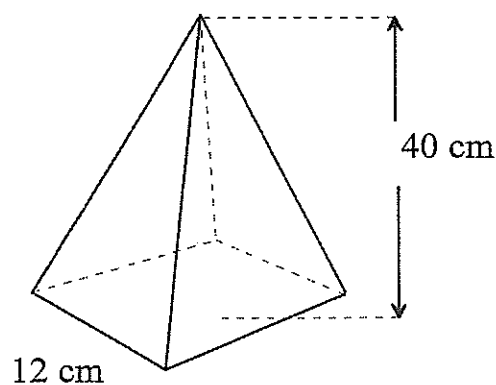
Start a new sheet of paper.

- a) $ABCD$ is a rectangle. The value of y is:

1



- b) A square pyramid is shown below.



- (i) Find the volume of the pyramid. 1
- (ii) The height of the pyramid is increased by 20%, while the base is left unchanged. Calculate the new volume. 1
- (iii) What is the percentage increase in the volume of the pyramid when this change is made? 2

- c) Using the table below or otherwise, answer the following questions.

The table below shows the rate of return on \$1,000 when invested at the compound interest rate shown.

Term (Years)	Compound Interest Rate(p.a.)						
	5.0%	5.5%	6.0%	6.5%	7.0%	7.5%	8.0%
1	\$1,050.00	\$1,055.00	\$1,060.00	\$1,065.00	\$1,070.00	\$1,075.00	\$1,080.00
2	\$1,102.50	\$1,113.03	\$1,123.60	\$1,134.23	\$1,144.90	\$1,155.63	\$1,166.40
3	\$1,157.63	\$1,174.24	\$1,191.02	\$1,207.95	\$1,225.04	\$1,242.30	\$1,259.71
4	\$1,215.51	\$1,238.82	\$1,262.48	\$1,286.47	\$1,310.80	\$1,335.47	\$1,360.49
5	\$1,276.28	\$1,306.96	\$1,338.23	\$1,370.09	\$1,402.55	\$1,435.63	\$1,469.33
6	\$1,340.10	\$1,378.84	\$1,418.52	\$1,459.14	\$1,500.73	\$1,543.30	\$1,586.87
7	\$1,407.10	\$1,454.68	\$1,503.63	\$1,553.99	\$1,605.78	\$1,659.05	\$1,713.82
8	\$1,477.46	\$1,534.69	\$1,593.85	\$1,655.00	\$1,718.19	\$1,783.48	\$1,850.93
9	\$1,551.33	\$1,619.09	\$1,689.48	\$1,762.57	\$1,838.46	\$1,917.24	\$1,999.00

- (i) What would be the value of an investment of \$2 500, invested at 5.5% p.a. compound interest after 4 years? 1
- (ii) For what term would \$10 000 need to be invested at 6% p.a. compound interest, to grow to at least \$15 000? 1
- (iii) Calculate the principal (to the nearest \$ 1 000) which would need to be invested at 8% p.a. compound interest for 8 years, to grow to \$61 000. 1
- d) The angle of depression of a ship at sea from a cliff due west of the ship is 23° . The ship sails 100m due east and the angle of depression is 12° . Find the height of the cliff 2

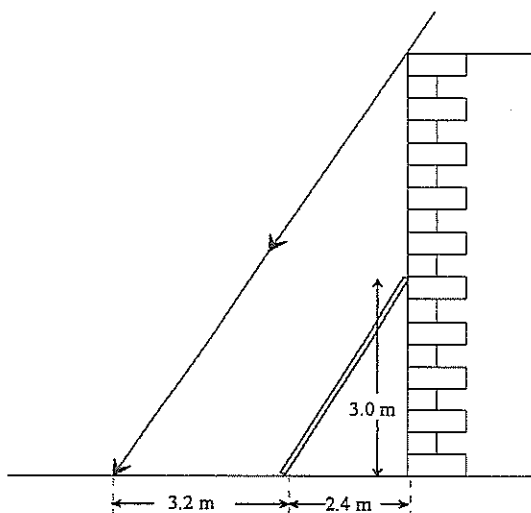
Question 28

(10 marks)

Start a new sheet of paper

- a) Liam leans a pole against a wall at the same angle as the sun's rays at a given time, and takes the measurements shown below.
Calculate the height of the wall to the nearest metre.

2



- b) Given $y = x^2 + 7x - 5$, find the values(s) of x such that $y = 25$

2

- c) Match each quadratic function with its corresponding graph:

4

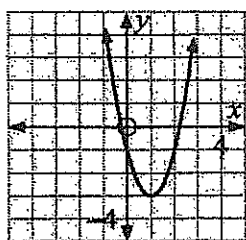
a $y = -(x - 1)^2 + 2$

b $y = 2(x - 1)^2 - 3$

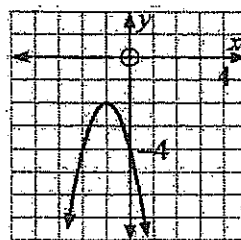
c $y = -2(x + 1)^2 - 2$

d $y = (x + 1)^2 + 3$

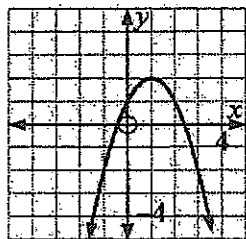
A



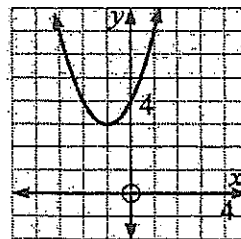
B



C



D



- d) If θ is an acute angle and $\cos \theta = \frac{7}{11}$, without using a calculator, find the exact values of $\sin \theta$ and $\cot \theta$

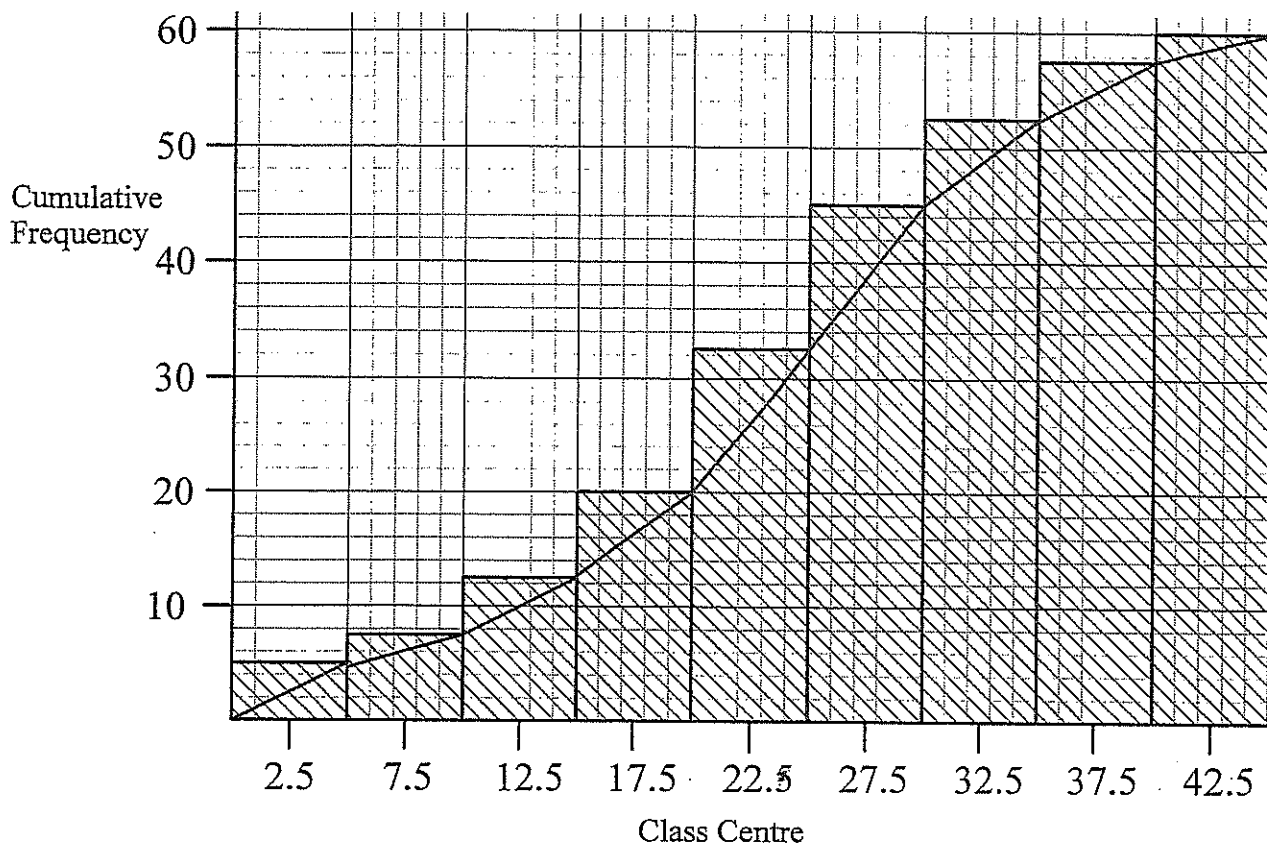
2

Question 29

(10 marks)

Start a new sheet of paper

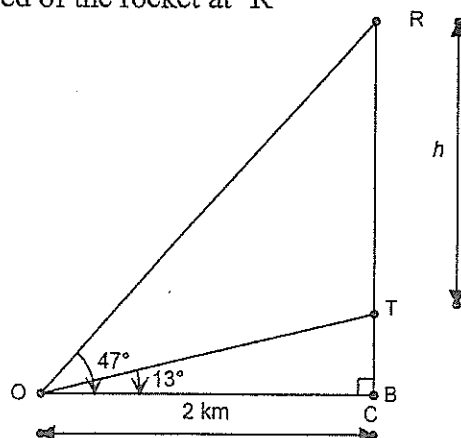
- a) A cumulative frequency histogram and polygon are shown below.



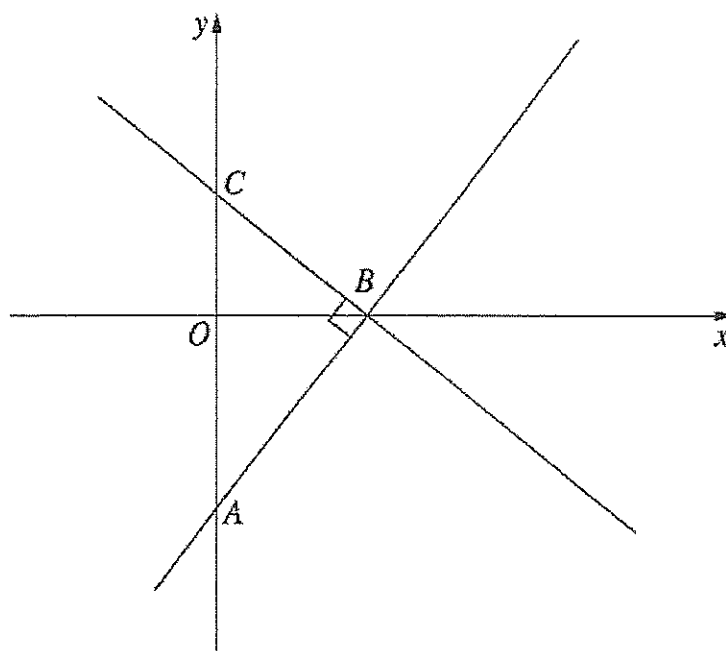
- (i) Estimate the median of the data. 1
- (ii) Estimate the interquartile range of the data. 2

- b) A rocket is launched from the top of a tower (point T), and is observed a distance of 2km away, at point O, as shown in the diagram. The angle of elevation to the top of the launch tower is 13° . Twenty seconds (20s) after launch the angle of elevation of the rocket is 47° .

- (i) What height has the rocket gained in 20 seconds?
- (ii) Find the speed of the rocket at 'R' 3



- c) In the diagram, the points A and C lie on the y -axis and the point B lies on the x axis. The line AB has equation $y = (\sqrt{3})x - 3$. The line BC is perpendicular to AB



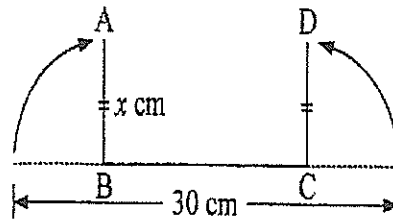
- (i) Find the equation of the line BC , in the form $y = mx + b$ 2
- (ii) Find the area of the triangle ABC . 2

Question 30

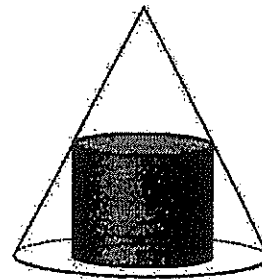
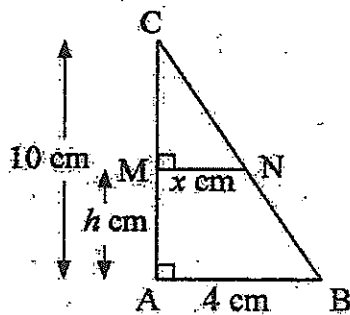
(10 marks)

Start a new sheet of paper

- a) Find the value of a , to the nearest minute, of a triangle that has two sides of length 35cm and 42cm and an included angle of a° , given that the triangle's area is 120 cm^2 2
- b) A rectangular gutter is formed by bending a 30cm wide sheet of metal as shown in the illustration below:



- (i) If $AB = x \text{ cm}$, show that the area of the cross section of the gutter ABCD is given by $A = x(30 - 2x) \text{ cm}^2$ 1
- (ii) Where must the bends be made in order to maximise the water carried by the gutter? 1
- c) Given that A (3,n), B (2,-1) and C (-1,5) are collinear, find n 2
- d) A cylinder fits exactly inside a right circular cone of radius 4 cm and height 10 cm such that the cylinder is just touching the cone as shown in the diagram.



- (i) Prove that Δ 's ABC and MNC are similar 2
- (ii) Show that $h = 10 - 2.5x$ 1
- (iii) Find the height and volume of the cylinder given that its radius is 2cm 1



SYDNEY TECHNICAL HIGH SCHOOL

MULTIPLE CHOICE ANSWER SHEET

Name :

ANSWERS

Teacher:

Course: YEAR 10 YEARLY 2015

Completely fill the response oval representing the most correct answer.

Do not remove this sheet from the answer booklet.

- | | |
|--|--|
| 1. A <input checked="" type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input type="radio"/> | 14. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> |
| 2. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> | 15. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> |
| 3. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> | 16. A <input checked="" type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input type="radio"/> |
| 4. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> | 17. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> |
| 5. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> | 18. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> |
| 6. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> | 19. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> |
| 7. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> | 20. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> |
| 8. A <input checked="" type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input type="radio"/> | 21. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> |
| 9. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> | 22. A <input checked="" type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input type="radio"/> |
| 10. A <input checked="" type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input type="radio"/> | 23. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> |
| 11. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> | 24. A <input type="radio"/> B <input type="radio"/> C <input checked="" type="radio"/> D <input type="radio"/> |
| 12. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> | 25. A <input type="radio"/> B <input checked="" type="radio"/> C <input type="radio"/> D <input type="radio"/> |
| 13. A <input type="radio"/> B <input type="radio"/> C <input type="radio"/> D <input checked="" type="radio"/> | |

PART B SOLUTIONS

Question 26:

1 (a) 183 000 000

1 (b) $x = 9$

1 (c) $m = \frac{29-29}{3}$

1 (d) $(2a-b)(2-3b)$

1 (e) (i) $2^{1/5}$

1 (ii) $2^{5/3}$

1 (iii) $2^{-6/5}$

1 (f) 0.3.

(g) $\sqrt{5+2} + \frac{1}{\sqrt{5+2}} = 2\sqrt{5}$

$\sqrt{5+2} + \sqrt{5-2} = 2\sqrt{5}$

2

$\therefore b = 5$

Question 27:

(a) 79°

(b) (i) 1920 cm^3

(ii) 2304 cm^3

(iii) $\frac{2}{3} = \frac{384}{1520} \times \frac{100}{1}$

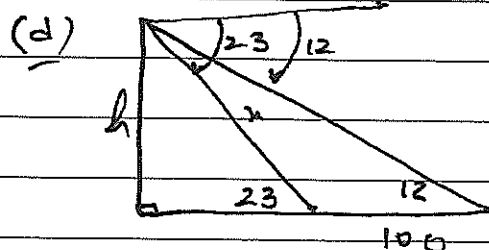
$= 20\%$

(k) (i) $\frac{2500}{1000} \times 1238.82$

$= 3097.05$

(ii) $10000 \rightarrow 15000$
in 7 years.

(iii) \$33 000



$\frac{x}{\sin 12^\circ} = \frac{100}{\sin 11^\circ}$

$x = 108.96$

$\frac{h}{108.96} = \sin 23^\circ$

$\therefore h = 42.58 \text{ m}$

QUESTION 28:

(a) $\frac{h}{3} = \frac{5.6}{2.4}$

$\therefore h = 7$

(b) $x^2 + 7x - 5 = 25$

$x^2 + 7x - 30 = 0$

$(x-3)(x+10) = 0$

$x = 3$ or $x = -10$

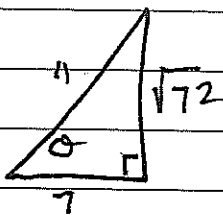
(c) a C

b A

c B

d D

(d)



$\sin \theta = \frac{\sqrt{72}}{11}$

$= \frac{6\sqrt{2}}{11}$

$\cos \theta = \frac{7}{\sqrt{72}}$

$= \frac{7}{6\sqrt{2}}$

QUESTION 29:

(a) (i) 24 (ii) $30-17 = 13$

(b) (i) $TB_{\frac{1}{2}} = \tan 13$

$TB = 0.46174$

$RB = 2 \tan 47$

$= 2.14474$

$\therefore h = 1.68300 \text{ km.}$

(ii) $S = \frac{D}{T}$

$= \frac{1.683}{20}$

$\approx 84.15 \text{ m/s}$

(c) $m_{AB} = \sqrt{3}$

$m_{BC} = -\frac{1}{\sqrt{3}}$

B is $(\sqrt{3}, 1)$

A is $(0, -3)$

BC is

$y - 0 = -\frac{1}{\sqrt{3}}(x - \sqrt{3})$

$y = -\frac{1}{\sqrt{3}}x + 1$

C is $(0, 1)$

(ii) Area = $\frac{1}{2} \times AC \times OB$

$= \frac{1}{2} \times 4 \times \sqrt{3}$

$= 2\sqrt{3} \text{ u}^2$

QUESTION 30:

$$(a) 120 = \frac{1}{2} \cdot 35 \cdot 42 \sin \theta$$

$$\sin \theta = \frac{240}{35 \times 42}$$

$$\theta = 9^\circ 24'$$

$$(b)(i) A = \text{length} \times \text{height} \\ = x \times (30 - 2x)$$

$$(ii) \text{Vertex at } x = 7\frac{1}{2}$$

$$(c) \frac{-1 - n}{2 - 3} = \frac{6}{-3}$$

$$n + 1 = -2$$

$$n = -3$$

$$(d)(i) \text{ In } \triangle ABC \text{ and } \triangle MNC$$

$$\angle CAB = \angle CMN = 90^\circ \text{ (given)}$$

LC is common

$\therefore \triangle ABC \parallel \triangle MNC$ (equiangular)

$$(ii) \frac{10}{10 - h} = \frac{4}{x}$$

$$40 - 4h = 10x$$

$$h = 10 - 2.5x$$

$$(iii) \text{ If } x = 2, \underline{h = 5}$$

$$\therefore V = \pi (2)^2 5$$

$$= 20\pi$$

$$\approx 62.8 \text{ cm}^3$$