SYDNEY TECHNICAL HIGH SCHOOL



MATHEMATICS

YEAR 11 PRELIMINARY EXAMINATION

SEPTEMBER 2007

Time Allowed: 120 minutes

Direction to Candidates:

- > Approximately marks are shown alongside each question
- > All necessary working should be shown .Marks may not be awarded for careless or badly arranged work
- > Begin answering each question on a new page

Name:	Teacher:

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	TOTAL
/10	/11	/11	/11	/11	/11	/10	/11	/86

QUESTION 1 (10 marks)

a) Simplify
$$5\sqrt{2} - \sqrt{32}$$

b) Solve for
$$x$$
, 2

$$|x+1|=3$$

c) State the domain of
$$y = \sqrt{x-1}$$

d) Solve for
$$x$$
:

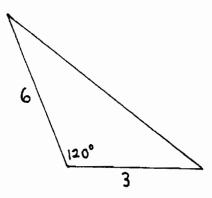
$$\frac{2x}{3} - 1 = \frac{x+1}{4}$$

e) (i) Sketch the graph of
$$y = |x + 1|$$

f) Find
$$\lim_{x \to 2} \frac{x^2 - 4}{x - 2}$$

QUESTION 2 (11 marks)

- a) If $sin\theta = \frac{3}{7}$ and $0^{\circ} \le \theta \le 90^{\circ}$, find $cos\theta$ in surd form 2
- b) Find the area of the triangle below leaving your answer in surd form. 2



c) Sketch the region given by:
$$(x-2)^2 + (y+3)^2 > 9$$

d) Simplify
$$\frac{4a+2b}{8a+4b}$$

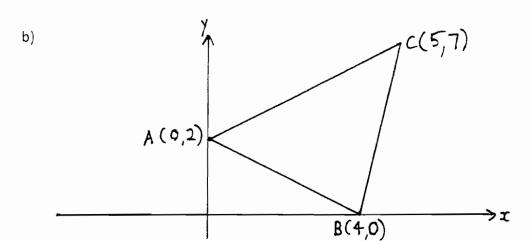
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c) Sketch the region given by:
$$(x-2)^2 + (y+3)^2 > 9$$
d) Simplify $\frac{4a+2b}{8a+4b}$
e) $f(x) = \begin{cases} x^3 + 1 & \text{if } x > 2 \\ 2x & \text{if } -1 \le x \le 2 \\ 5 & \text{if } x < -1 \end{cases}$
Find $f(-2) - f(3) + f(2)$

Find
$$f(-2) - f(3) + + f(2)$$

QUESTION 3 (11 marks)

a) Find the perpendicular distance from the point (3,2) to the line 3x - 4y + 7 = 0



i) Find the gradient of AB

2

- ii) Find the coordinates of D, the midpoint of AB
- iii) Find the equation of the line passing through D and perpendicular to AB
- iv) Show that C lies on this line
- v) Find the lengths of AB and CD in surd form.
- vi) Find the area of the quadrilateral ACBO

QUESTION 4 (11 marks)

a) Solve
$$|2x - 1| < 3$$

b) Write as a single fraction
$$\frac{1}{x-3} + \frac{1}{x+3}$$

c) Solve
$$2 \sin \theta = -1$$
 for $0^{\circ} \le \theta \le 360^{\circ}$

d) Simplify
$$\cos\theta + \cos\theta \tan^2\theta$$

e) Prove that
$$sec^2\theta = \frac{1}{(1-sin\theta)(1+sin\theta)}$$

QUESTION 5 (11 marks)

a) Differentiate

i)
$$-3x^4$$

ii)
$$\frac{2x-1}{x+4}$$

iii)
$$(3x^2 - 5)^6$$

iv)
$$(2x+3)(x^2+x+1)$$

b) Find the
$$x$$
 co-ordinate of the point on the curve $y = x^2 + 2$ where the tangent has the gradient of -2

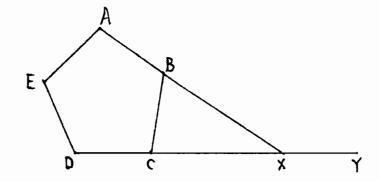
c) Find the equation of the tangent to
$$y = 2x^2 - 2x + 1$$
 at he point $x = 1$

QUESTION 6 (11 marks)

a) Factorise $8 - 27x^3$

2

b)



In the diagram, ABCDE is a regular pentagon and AB and DC are produced to meet at X. The point Y lies on DCX produced.

(i) Find
$$\angle ABC$$

(ii) Find $\angle BXY$ giving reasons

3

c) (i) Find the discriminant of
$$x^2 + (k-1)x + 1$$
 in simplest form 2

(ii) Find the range of values of k for which the quadratic expression above is positive definite.

QUESTION 7 (10 marks)

- a) (i) Express the equation of the parabola $8y = x^2 8x 24$ in the form $(x h)^2 = 4a(y k)$

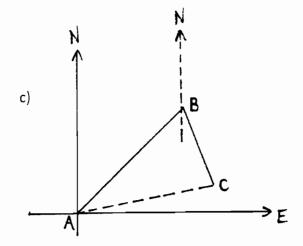
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- (ii) Write down the coordinates of the vertex and equation of the directrix for this parabola
- 2
- b) If a and β are the roots of the quadratic equation $x^2 + 3x 5 = 0$, find
 - (i) $\alpha + \beta$
 - (ii) $\alpha\beta$
 - (iii) $\alpha^2 + \beta^2$
 - (iv) $\alpha^3 \beta + \alpha \beta^3$

QUESTION 8 (11 marks)

a) If
$$f(x) = \frac{x-1}{x+2}$$
, show that $f(1-x) = \frac{x}{x-3}$

b) Solve $9^x + 3.3^x - 18 = 0$ by first reducing this equation to a quadratic 3



Copy this diagram onto your answer sheet and mark the following information on it.

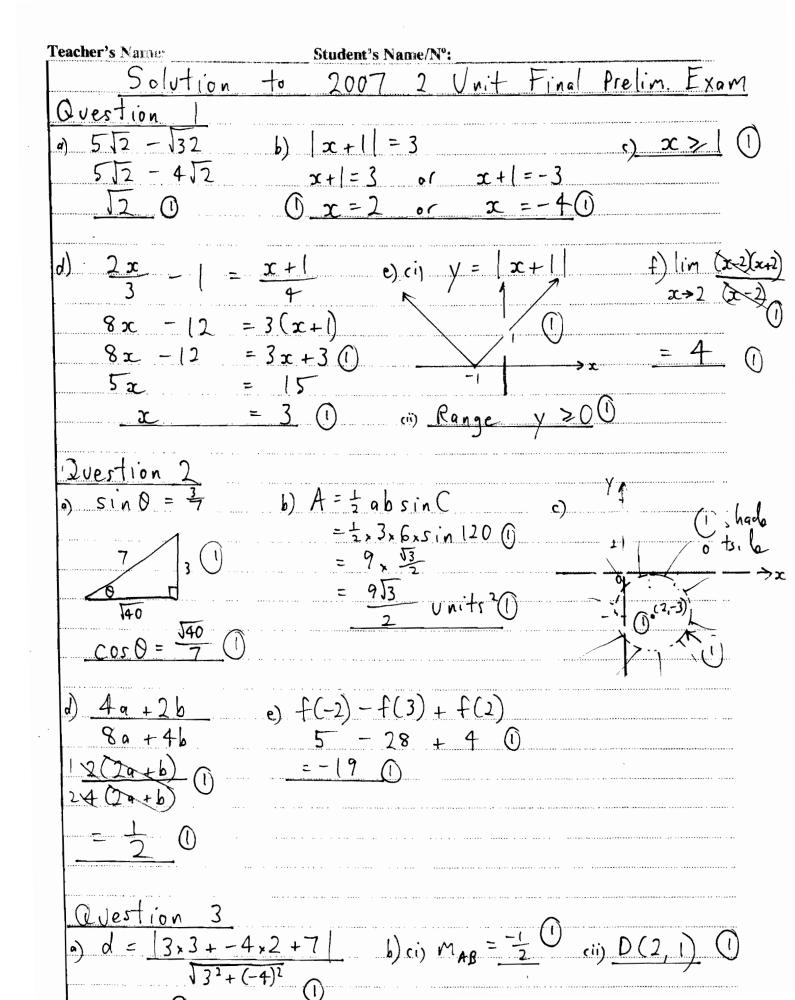
(i) An ultralight plane is flown from an airport A on a bearing of $030^{\circ}T$ for 150km to a position B. From position B the ultralight is then flown 200km on a new course bearing $135^{\circ}T$ to position C. Use the above diagram to find how far (to the nearest km) C is from A.

3

3

(ii) Use the Sine Rule to help find the bearing of C from A.

(nearest degree)



Teacher's Name: Student's Name/No: (ii) 7 = 2,5-3= $\sqrt{(4-0)^2+(0-2)^2}$ (vi) Area 19 units2 (1) Question (x-3)(x+3)2x < 4 and 2x > -2x < 1 $\alpha - 1$ $\alpha > -1$ c) 2sin0 = d) cos0 + cos0 tan20 $sin\theta = \frac{1}{2}$ (1) $cos\theta(1+tan^2\theta)$ (1) Working angle is 30 coso, sec20 () cos 2 Q

