# Project 1 Compute the Projectile Motion

Distribute on August 28, 2023 Due before September 24, 2023 (Sunday) at 12:00 midnight

**Learning Outcomes** ((CLO) vs (SO) Mapping)

- Recognize the software and hardware components of a computer system (1)vs(6)
- Recognize and apply the software development phases (2)vs(6)
- Utilize Java syntax in fundamental programming algorithms (3)vs(1)
- Recognize and apply the various input and output devices in programming (4)vs(2)

## **Objectives**

In completing this project, you will gain experience with the following Java features:

- definition of a Java class
- variable declaration and assignment
- JOptionPane dialog boxes for input and output
- the Math class
- the String class
- the String.format() method and the printf() method
- selection logic
- arithmetic expressions and data manipulations

#### **Problem Statement**

We encounter projectile motion whenever we attempt to catch a fly ball, hit a long drive, or shoot a free throw. Projectile motion is the motion of an object thrown or projected into the air, subject only to the acceleration of gravity. The object is called a projectile, and its path is called its trajectory, which is of the form  $y = ax + bx^2$ , in which a and b are constants. The laws of physics, which describe projectile motion, are well known. They were first studied by Napoleon's generals.

To simplify the problem, we will assume that we can

- consider the surface of the Earth to be a plane
- ignore the effect of the drag from air friction

Under the simplifying conditions above, the following formulas hold for a projectile with an initial velocity of  $\mathbf{v}$  feet/sec and a launch angle of  $\mathbf{r}$  (note that these expressions are not written according to the syntax of the Java language).

- 1. Time span of the flight:  $T = 2 \mathbf{v} \sin \mathbf{r} / g$
- 2. Maximum height:  $y_{max} = (\mathbf{v} \sin \mathbf{r}) t \frac{1}{2} g t^2$ , where t = T/2
- 3. Range (distance traveled by the projectile):  $x_{max} = (\mathbf{v} \cos \mathbf{r}) T$

Here g is the gravitational acceleration g = 32 ft/sec<sup>2</sup>, and **r** is measured in radians.

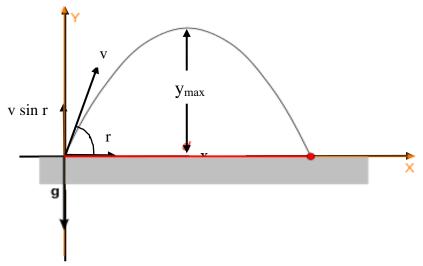


Figure: Projectile motion – a trajectory and distance of a projectile.

This project simulates the process of repeated attempts to hit a target with a projectile. The goal is to shoot the projectile within a 1-foot distance from the target since such a short miss is accepted as a hit. You will construct a Java program that

- can determine the trajectory data of a projectile for a given initial velocity and a launch angle, in particular for an initial choice of a 45-degree angle;
- can check whether the initial attempt is a launch angle of 45 degrees. If the first attempt is not at the launch angle of 45 degrees, the window as shown in Figure 5a displays the information, and then the program exits. Then restarted with a launch angle of 45;
- can check if the shot of the initial attempt falls short of the target with less than -1 foot (such as target missed by -1.1, -25.0, -154.55, etc.); if so, the process terminated and then restarted with an increased initial velocity. Note that for any initial velocity, the longest range is attained if the launch angle is 45 degrees;
- can determine the error of a shot (error = projectile range distance to target);
- can check if the error is less than 1 foot in absolute value; if so, the user is notified about the result and the process terminates. That is, the error is between (-1, 1);
- can offer the user four chances to modify the launch angle and try to hit the target;
- can keep track of the smallest error produced by the subsequent attempts; the best result is reported to the user.

# **Analysis and requirements**

The analysis describes the logical structure of the problem in a way that helps us to plan (design) a solution.

#### Input

Initial input values are

- (i) initial velocity (feet/sec),
- (ii) distance to the desired target (feet), and
- (iii) launch angle (degree), and

(iv) the gravitational acceleration (a defined constant).

Additional input values are the launch angles for the repeated attempts if applicable. The angle must always be in the range of 0.0 - 45.0 degrees.

Distance, velocity, and launch angle are solicited from the user on JOptionPane input windows. See Figures 1, 2, and 3.

For using dialog boxes of JOptionPane class, you need to have the following statement import javax.swing.JOptionPane;

before the main() method, and include a statement System.exit(0);

before the end of the body of the main() method, shown as follows:

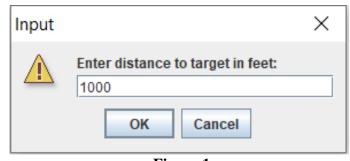


Figure 1

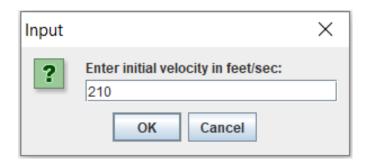
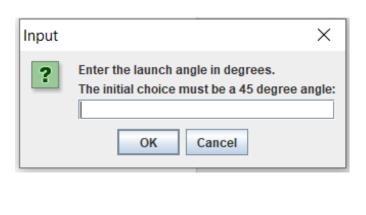
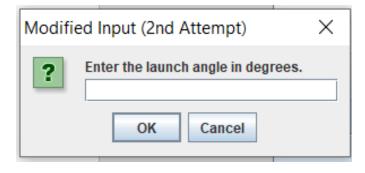
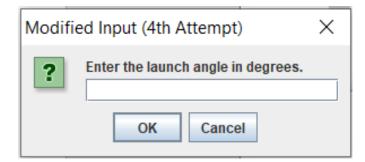


Figure 2





• • •



Modified Input (5th Attempt)		×
?	Enter the launch angle in degrees.  OK Cancel	

Figure 3

#### **Output**

Output messages are displayed both on JOptionPane windows and on the console. Every time a launch has been executed by the program, a report providing the details of the trajectory must be displayed as shown in Figure 4.

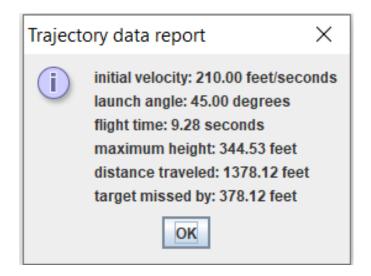


Figure 4

#### Each report must contain

- (1) the initial velocity in feet/sec,
- (2) the current launch angle in degrees,
- (3) the flight time in seconds,
- (4) the maximum height attained in feet,
- (5) the distance traveled by the projectile (range) in feet, and
- (6) the error with which the projectile missed the target in feet.

Note that the error is a positive value when the projectile overshoots, and negative for short shots. All real numbers displayed must be rounded to the nearest hundredth. Hints: an exemplary code is as follows:

```
String range = String.format("launch angle: %.2f degrees.\n" + "distance traveled: %.2f feet.\n", launchAngle, distanceTraveled);
```

String title = "Trajectory data report";

JOptionPane.showMessageDialog(null, range, title,

JOptionPane.INFORMATION\_MESSAGE);

The first trajectory data report is based upon a launch angle of 45 degrees (which provides the longest possible range) to see if the target is within reach for the given velocity. The program enforces the initial (first) attempt with a launch angle of 45 degrees. If the initial (first) attempt *falls short* of the target, another window as shown in Figure 5 displays the information, and then the program exits. If the initial (first) attempt is not at the launch angle of 45 degrees, after displaying the trajectory data report, the window as shown in Figure 5a displays the information, and then the program exits.

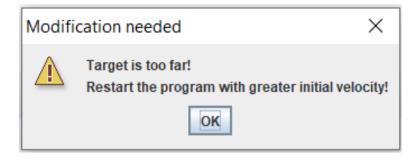


Figure 5

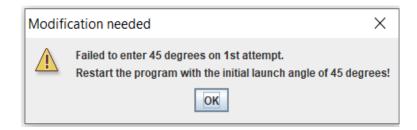


Figure 5a

At the launch angle of 45 degrees in the initial (first) attempt, if the first shot is long enough (i.e., an overshoot occurs), the window of Figure 3 shall be used to input all subsequent launch angle modifications as chosen by the user. The title of the window is also displaying the number of attempts, such as Modified Input (2<sup>nd</sup> Attempt) in the title of the window, etc. The corresponding reports in Figure 4 show the re-calculated trajectories. Naturally, the user will try to modify the angle to make the projectile land nearer and nearer to the target. After each unsuccessful attempt a warning is printed on the console, see a sample in Figure 6.

Shot went beyond the target. Decrease the launch angle from 45.0! Figure 6

Figure 7 shows a sample output on the console after all five angle modifications failed to hit the target. One of the following statements is displayed on the console.

Second Attempt: Shot went beyond the target. Decrease the launch angle from 40.0! Second Attempt: Shot fell short of the target. Increase the launch angle from 20.0! Third Attempt: Shot fell short of the target. Decrease the launch angle from 30.0! Fourth Attempt: Shot went beyond the target. Decrease the launch angle from 24.0! Fourth Attempt: Shot fell short of the target. Increase the launch angle from 23.0! Fifth Attempt: Shot went beyond the target. Decrease the launch angle from 23.5! Fifth Attempt: Shot fell short of the target. Increase the launch angle from 23.26! Your best shot missed the target with 7.90 feet.

Your best shot missed the target with 0.01 feet.

Figure 7

Note that it is necessary to keep track of the least absolute error that occurred in the series of attempts since it has to be reported as one of the last two lines in Figure 7 shows.

Figure 8 shows a successful launch. Such a report is followed by the message in Figure 9.

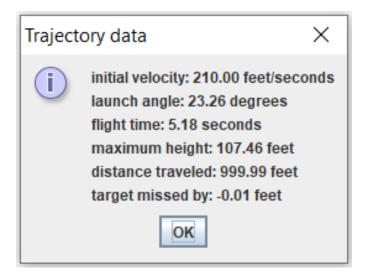


Figure 8



Your best shot missed the target with 0.01 feet. or Your best shot missed the target with -0.91 feet. or Your best shot missed the target with 0.00 feet.

Figure 9

If the fifth attempt fails to hit the target, after displaying one of the messages in Figure 7 on the console, the program also displays the console the following message

End of the fifth attempt. Restart the program and try again.

Figure 10

#### **Relevant Formulas**

The basic formulas 1, 2, and 3 in the **Problem Statement** will be used for all trajectory computations. The input value for a launch angle shall be solicited and given in degrees. The previous formulas shall be implemented by making use of the trig methods Math.sin(angle) and Math.cos(angle) from the Math class. These methods require the parameter angle in radians. Therefore, an angle given in degrees must be converted to radians. The conversion formula runs as follows:

```
(angle in radians) = (angle in degrees) \pi/180
```

Note that it can be used in either direction, from degrees to radians or vice versa. The value of  $\pi$  (PI) is available as a named constant **Math.PI** from the Math class of the Java library. The Java API (Application Programmer Interface) provides a class named Math which contains numerous methods, such as Math.sqrt, Math.cbrt, Math.PI, Math.sin, Math.cos. Math.abs, Math.pow methods.

## Design

For this project, you shall design a single class that contains all the necessary data and operations. A suggested class name is **Projectile**. You must decide upon the necessary import(s).

The **Projectile** class contains the main method, which in turn contains all the variable declarations. The main method should carry out the following tasks in the order given:

- declares and assigns a named constant for the gravitational acceleration; the value is 32;
- declares the following local variables (mentioned in the following table) in the main method
- solicits and stores the input values as explained in the Analysis and Requirements section; to accomplish this task, create a call statement, and define a called method to input the value of a launch angle in degrees and returns the value of the launch angle in degrees to the call statement. An example is as follows:

}//end of class Projectile

- computes all the trajectory data and saves those in variables;
- builds up and stores the output message in a single string variable (the content of Figures 4, 8); including the following two bullet tasks, create a call statement and a called method() to accomplish these tasks. An example is as follows:

- displays the output windows;
- numbers in the output are formatted to the nearest hundredth; for this purpose, the String.format() and printf() methods are used;
- uses if and/or if-else logic to decide if additional launches are necessary and repeats the operations at most four times if needed; and
- terminates the program when it is due.

The above two tasks are related to Figures 6, 7, 9, and 10. This can be done by creating a call statement

```
errorAnalysis(attempt, error, minError, launchAngle);
```

which calls the following called method:

See also the detailed class description below. You may declare any additional local variables in the main method.

Projectile			
METHOD			
main	The method opens input windows (see Figures 1, 2, and 3) to obtain the initial data. The input values are assigned to the corresponding data fields. The method computes the flight time, maximum height, and range. The results display on a message window (see Figure 4). Display Figures 5 – 9 as needed. After the last attempt, the program exits.		
Local variables in main()			
GRAVITATION	Named constant with <b>final</b> , initialize with a value is 32; this value cannot change during the execution of the program		
distanceToTarget	double; to store the distance in feet to the desired target (input)		
initialVelocity	double; to store the projectile's initial velocity in feet/second (input)		
launchAngle	double; to store the current input for launch angle in degrees (input)		
radian	double; to store the value of the angle in radians (calculated)		
flightTime	double; to store the flight time of the projectile as defined by formula 1 in the description (calculated)		
highestPoint	double; to store the maximum height of the projectile as defined by formula 2 in the description (calculated)		
distanceTraveled	double; to store the distance traveled by the projectile as defined by formula 3 in the description (calculated)		
error	double; to store the difference between distance traveled and distance to the target (calculated)		
minError	double; to store the least absolute error; update every time a new error value was generated (calculated)		
trajectory	String; to store the current output message built upon the trajectory data		
attempt	String; to record the number of attempts of input for launch angle; such as, for the initial attempt, assign attempt = ""; for the second attempt, assign attempt = "Second Attempt"; etc.		

# **Testing**

Test your program with input values shown in the description. See if your results match the output data.

# **Requirements and Hints**

- 1. Having your program tested, run the program with a new set of input data of your own choice. **The distance to the target must be at least 800 feet**. Copy your trajectory report as a comment block after the class code.
- 2. You must have a comment block preceding the header of each of your classes that has the following content:

```
/*
 * <your name>
 * CS 16000-01 - 02/03, Fall Semester 2023
 * (specify your lab section only)
 * Project 1: Compute the Projectile Motion
 *
 * Description. <Summarize the purpose of the class here.>
 *
 */
```

3. You are NOT allowed to use iteration structures (loops) to code repeated attempts. The relevant part of the code that calculates and displays the trajectory results must be copied four times into the program. Here is the pseudo-code version of the code you must copy five times in your program:

```
errorAnalysis(attempt, error, minError, launchAngle);
       if error positive
               send an overshoot message to the console
       else
               send an undershot message to the console
launchAngle = reenterLaunchAngle(attempt);
       solicit new input for the launch angle
calculate radian
re-calculate all trajectory data
calculate error
update minError
trajectoryDataReport(initialVelocity, launchAngle, flightTime,
                             highestPoint, distanceTraveled, error);
       compose output message
       display output message
errorAnalysis(attempt, error, minError, launchAngle);
       if the absolute error is less than 1
               display hit on the window
               terminate the program
```

- 4. Use the Math.abs() method to calculate the absolute value of the error, when you decide the accuracy of the shot.
- 5. Set up a variable minError as suggested in the class description. Every time the program generates a new error, update the mirror such that it stores the least absolute error that occurred thus far. Use the Math.abs() and Math.min() methods for this purpose.
- 6. Use the Math.sin() and Math.cos() methods for the sin and cosine functions.
- 7. The first input for the launch angle must be 45 degrees, you choose the four additional modifications
- 8. Do not round the numeric values while needed in calculations. Apply formatting only when the output message is composed

Note that in 3, stated that "... The relevant part of the code that calculates and displays the trajectory and error analysis results must be repeated four times in the program. ..." an easy approach to writing a code, which calls a method four times, such as errorAnalysis(...), trajectoryDataReport(...), and errorAnalysis(...) for this purpose instead of copying a repetitive code segment. (Hint!)

## **Evaluation**

## **Documentation and style: 10 points.**

Your program must conform to the Computer Science Department's Java Documentation and Style Requirements. Emphasis will be placed on having the required banner and internal comments, indentation, and overall stylish appearance. Comments must be written with correct grammar and spelling. Do not neglect the documentation and style.

Correctness: 90 points.

These points will be allocated as follows:

1.	Error-free compilation of the Java source file	10 points
2.	Correct declaration of the variables	.20 points
3.	Correct implementation of the projectile formulas	15 points
4.	Correct use of selection logic	15 points
5.	Correct application of dialog windows	10 points
6.	Correct display of correct formatted output messages	20 points

Total: 100 points