

# Bahria University

Software Engineering Department



Course: SEL-221 Artificial Intelligence Lab

Term: Fall 2020, Class: BSE 5(B)

Assignment No:

0	2
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Submitted By:

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Submission Date							
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(Date: DD/MM/YY)

Submitted To:

Engr. M. Rehan Baig

(Subject Teacher)

Signature: \_\_\_\_\_ Max Marks: \_\_\_\_\_ Marks Obtained: \_\_\_\_\_

[Qaiser Abbas]  
[BSE (5B)]

[Enrolment No. 02-131182-030]

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**Bahria University**  
Discovering Knowledge

## **BAHRIA UNIVERSITY (KARACHI CAMPUS)**

**ASSGINMENT # 2 - FALL 2020**

**Artificial Intelligence Lab**

Class: **BSE 5(B)**

Lab Instructor: **Engr. Muhammad Rehan Baig**

**Submission Deadline: 31<sup>th</sup> December, 2020**

Max Marks: **5**

**Question:** Apply *Breadth First Search, Depth First Search, Uniform Cost Search, A\* Search, Simulated Annealing* and *MIN MAX Algorithms* to Solve Sales Man Traveling problem. Identify **Time Complexity** for each algorithm and find best suited algorithm for solving this problem with stated algorithms along with complete code.

**Note:**

- Please Provide Proper documentation of your Assignment.
- If you submit your assignment after the given deadline then **2 Marks** will be deducted for the late submissions.
- Copied assignment will be marked **zero**.
- ***Please don't share your assignment*** with any of your colleagues Because **Same Assignments** will be marked as copied and **ZERO** will be assigned to both. Author and Copier

## Breadth First Search and Depth First Search:

```
__author__ = "Qaiser Abbas"
__copyright__ = "Copyright 2020, Artificial Intelligence Assignment-02"
__email__ = "qaiserabbas889@yahoo.com"

edges = []
print("Enter the distance of All cities from City A:")
edges_cityA = []
edges_cityB = []
edges_cityC = []
edges_cityD = []
edges_cityE = []
cost = int(input())
edges_cityA.append(0)
edges_cityA.append(cost)
cost = int(input())
edges_cityA.append(cost)
cost = int(input())
edges_cityA.append(cost)
cost = int(input())
edges_cityA.append(cost)
print("Enter the distances of All cities from city B")
cost = int(input())
edges_cityB.append(cost)
edges_cityB.append(0)
cost = int(input())
edges_cityB.append(cost)
cost = int(input())
edges_cityB.append(cost)
cost = int(input())
edges_cityB.append(cost)
print("Enter the distance of All cities from city C")
cost = int(input())
edges_cityC.append(cost)
cost = int(input())
edges_cityC.append(cost)
edges_cityC.append(0)
cost = int(input())
edges_cityC.append(cost)
cost = int(input())
edges_cityC.append(cost)
print("Enter the distance of All cities from city D")
cost = int(input())
edges_cityD.append(cost)
cost = int(input())
edges_cityD.append(cost)
cost = int(input())
edges_cityD.append(cost)
edges_cityD.append(0)
cost = int(input())
edges_cityD.append(cost)

print("Enter the distance of All cities from city E")
cost = int(input())
edges_cityE.append(cost)
cost = int(input())
```

```
edges_cityE.append(cost)
cost = int(input())
edges_cityE.append(cost)
cost = int(input())
edges_cityE.append(cost)
edges_cityE.append(0)

edges.append(edges_cityA)
edges.append(edges_cityB)
edges.append(edges_cityC)
edges.append(edges_cityD)
edges.append(edges_cityE)

def TSP_bfs(edges):
    q = []
    path = []
    visited = [False] * 6
    p = [0]
    q.append((0, 0, visited, p))
    while len(q) != 0:
        cnt = 0
        curr = q.pop(0)
        curr[2][curr[0]] = True
        for i in range(5):
            if curr[2][i] == False:
                cnt += 1
        if cnt == 0:
            P = curr[3]
            P.append(0)
            path.append((curr[1] + edges[curr[0]][0], P))
        for i in range(5):
            if curr[2][i] == False:
                tmp = [False] * 6
                for j in range(5):
                    tmp[j] = curr[2][j]
                P = []
                for j in range(len(curr[3])):
                    P.append(curr[3][j])
                P.append(i)
                q.append((i, curr[1] + edges[curr[0]][i], tmp, P))

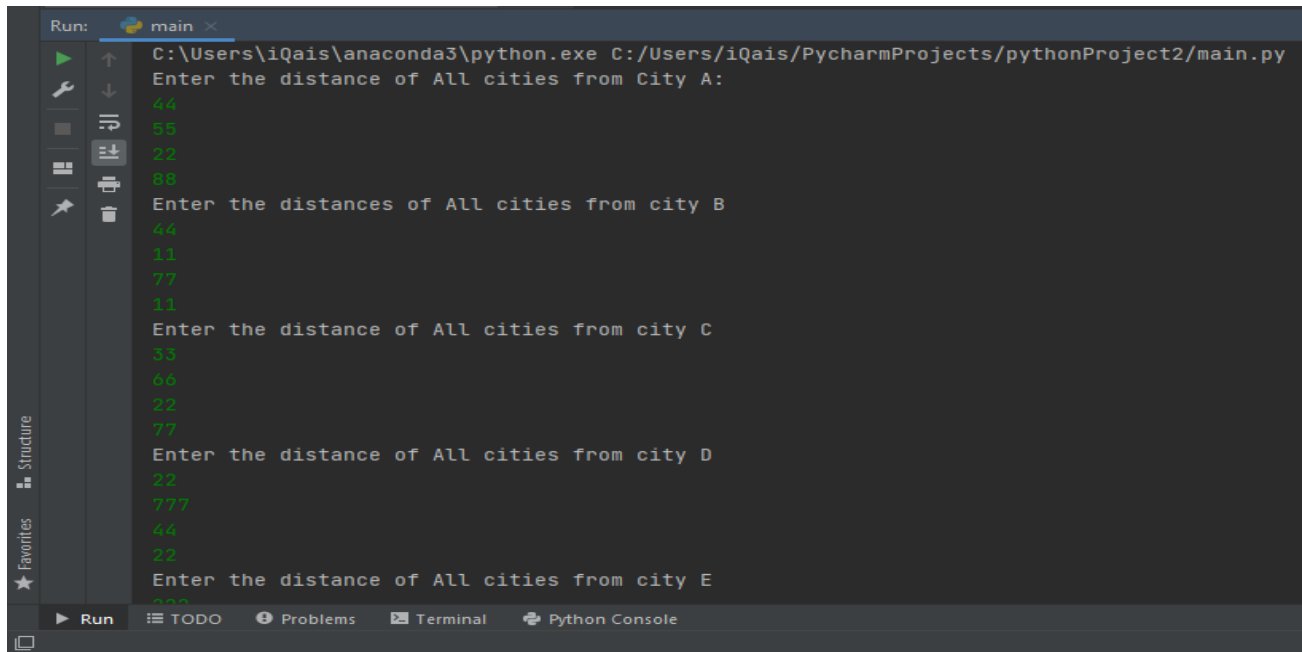
    mini = 1000
    P = []
    for i in range(len(path)):
        if mini > path[i][0]:
            mini = path[i][0]
            P = path[i][1]
    return mini, P
print('*****BFS Solution*****')
print(TSP_bfs(edges))
```

```
def TSP_dfs(node, edges, visited, cost, path):
    cnt = 0
    path.append(node)
    visited[node] = True
    for i in range(5):
        if visited[i] == False:
            cnt += 1
    if cnt == 0:
        path.append(0)
        return (cost + edges[node][0]), path
    mini = 10000
    A = []
    for i in range(5):
        if visited[i] == False:
            tmp = [False]*6
            for j in range(5):
                tmp[j] = visited[j]
            P = []
            for j in range(len(path)):
                P.append(path[j])
            t, l = TSP_dfs(i, edges, tmp, cost + edges[node][i], P)
            if mini > t:
                mini = t
                A = l
    return mini, A

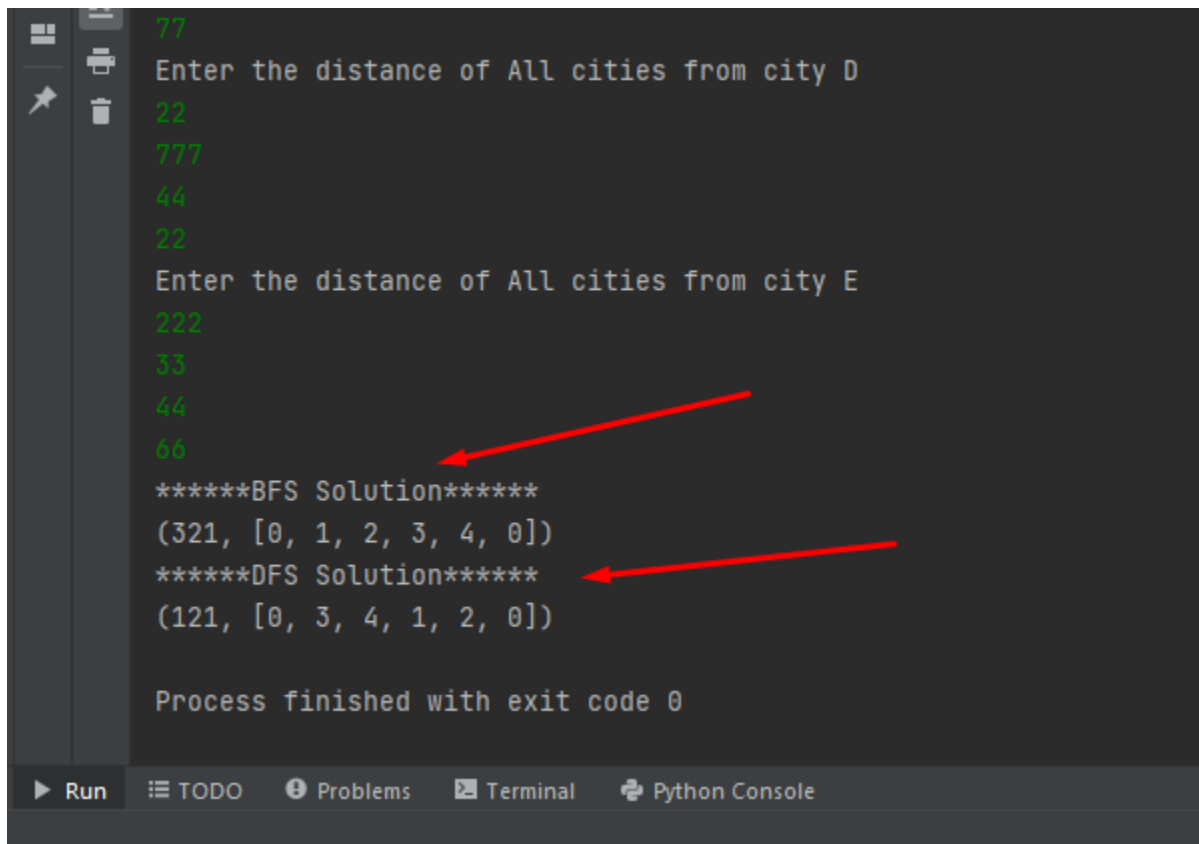
visited = [False]*6
path = []
print('*****DFS Solution*****')
print(TSP_dfs(0, edges, visited, 0, path))
```

**Time complexity of BFS:  $O(b^d)$**

**Time complexity of DFS:  $O(b^m)$**

**OUTPUT:**

```
Run: main x
C:\Users\iQais\anaconda3\python.exe C:/Users/iQais/PycharmProjects/pythonProject2/main.py
Enter the distance of All cities from City A:
44
55
22
88
Enter the distances of All cities from city B
44
11
77
11
Enter the distance of All cities from city C
33
66
22
77
Enter the distance of All cities from city D
22
777
44
22
Enter the distance of All cities from city E
222
```



```
77
Enter the distance of All cities from city D
22
777
44
22
Enter the distance of All cities from city E
222
33
44
66
*****BFS Solution*****
(321, [0, 1, 2, 3, 4, 0])
*****DFS Solution*****
(121, [0, 3, 4, 1, 2, 0])

Process finished with exit code 0
```

## Uniform Cost Search:

## CODE:

```
# Owned
__author__ = "Qaiser Abbas"
__copyright__ = "Copyright 2020, Artificial Intelligence lab-06"
__email__ = "qaiserabbas889@yahoo.com"
#=====
# {code}
import queue as Q
def search(graph, start, end):
    while iterations = 0
    for iteration = 0
    if start not in graph:
        raise TypeError(str(start) + ' not found in graph !')
    if end not in graph:
        raise TypeError(str(end) + ' not found in graph !')
    queue = Q.PriorityQueue()
    queue.put((0, [start]))
    while not queue.empty():
        while iterations = while iterations+1
        node = queue.get()
        current = node[1][len(node[1]) - 1]

        cost = node[0]
        for neighbor in graph[current]:
            for iteration = for iteration+1
            temp = node[1][:]
            temp.append(neighbor)
            queue.put((cost + graph[current][neighbor], temp))
def main():
    graph = {
        'A': {'B': 75, 'C': 118, 'D': 140, 'E': 131},
        'B': {'C': 120, 'D': 175, 'E': 110, 'A': 39},
        'C': {'D': 110, 'E': 241, 'A': 29, 'B': 180},
        'D': {'E': 130, 'A': 111, 'B': 99, 'C': 60},
        'E': {'A': 190, 'B': 151, 'C': 199, 'D': 180},
    }
main()
```



**Time complexity of UCS:** Let  $C^*$  is Cost of the optimal solution, and  $\epsilon$  is each step to get closer to the goal node. Then the number of steps is  $= C^*/\epsilon + 1$ . Here we have taken  $\epsilon = 1$ , as we start from state 0 and end to  $C^*/\epsilon$ .  $= O(b^{1 + \lceil C^*/\epsilon \rceil})$

## OUTPUT:

```

PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL
Windows PowerShell
Copyright (C) Microsoft Corporation. All rights reserved.

Try the new cross-platform PowerShell https://aka.ms/pscore6

PS C:\Users\iQais> & C:/Users/iQais/AppData/Local/Programs/Python/Python38-32/python.exe C:/Users/iQais/AppData/Local/Programs/Python/Python38-32/Scripts/python.exe C:/Users/iQais/AppData/Local/Programs/Python/Python38-32/Scripts/python.exe ling_salesman_problem.py
Path Found: A C B E D A Total Cost 263
PS C:\Users\iQais>

```

## A\* Search:

```

# Owned
__author__ = "Qaiser Abbas"
__copyright__ = "Copyright 2020, Artificial Intelligence Assignment-02"
__email__ = "qaiserabbas889@yahoo.com"
#=====

import random

class TSP(object):

    def getDistance(self, P1, P2):
        """
        Generates distance between 2 points
        """
        self.P1 = P1
        self.P2 = P2
        distance = ((self.P1[0] - self.P2[0]) ** 2 + (self.P1[1] -
self.P2[1]) ** 2) ** (1 / 2)
        return distance

    def generateCoordinates(self):
        """
        This function generates random coordinates for cities

```

```

Returns
-----
list
    Returns x and y coordinates in the list.

    """
    x = random.randint(0, 101)
    y = random.randint(0, 101)
    return [x, y]

def calculateDist(self, s, n):
    """
        Calculates the total distance in a state, eg [0,1,2,3]
    """
    self.calD = s
    self.nu = n
    dist = 0
    total = 0
    for i in range(self.nu):
        xi = self.calD[i]
        yj = self.calD[i + 1]
        dist = self.getDistance(self.coord[xi], self.coord[yj])
        total += dist
    return total

def hue(self, chosenList, cityList):
    """
        Generates the total heuristic plus path cost and sends it out
    """
    toCheck = cityList[:]
    SPL = chosenList[:]
    dl = 999999999
    fCost = []
    l = []

    for i in chosenList:
        toCheck.remove(i)

    for e in toCheck:
        l.clear()
        l.append(e)
        rest = cityList[:]
        totalDist = 0

        while len(rest) > 0:
            dl = 99999
            for i in l:
                if i in rest:
                    rest.remove(i)

            for n in l:
                for m in rest:
                    d = self.getDistance(self.coord[n], self.coord[m])
                    if d < dl:
                        dl = d
                        c = m
```

```

        if c not in l:
            l.append(c)

        totalDist += d

        g = self.getDistance(self.coord[e], self.coord[SPL[-1]])
        k = self.getDistance(self.coord['0'], self.coord[e])
        f = g + totalDist + k

        fCost.append((f, e))

    fCost.sort()

    return fCost[0][1])

def solver(self):
    """
        Main function that solves the TSP and output

    Returns
    -----
    None.

    """

    cities = int(input("How many cities do you want to generate: "))

    self.coord = {}
    cityList = []
    chosenList = ['0']
    self.cities = cities

    for i in range(self.cities):
        a = str(i)
        l = self.generateCoordinates()
        self.coord[a] = l
        cityList.append(a)

    # currentState = cityList[:]

    for i in range(len(cityList) - 1):
        x = self.hue(chosenList, cityList)
        chosenList.append(x)

    final = chosenList + ['0']
    il = cityList + ['0']

    fd = self.calculateDist(final, len(final) - 1)
    id = self.calculateDist(il, len(il) - 1)

    print("\nCoordinates:")
    for each in self.coord.items():
        print('City {} has coordinate {}'.format(each[0], each[1]))

    print("\nInitial state to travel: ", il, "\n")
    print("Initial distance was %.2f km. \n" % id)

```

```

print("Final state (optimized) to travel: ", final, "\n")
print("Optimized distance is %.2f km. \n" % fd)

def main():
    tsp = TSP()
    tsp.solver()

if __name__ == "__main__":
    main()

```

**Time complexity of A\*:** A\* is cost-optimal, the worse case time complexity is  $O(E)$ , where  $E$  is the number of edges in the graph

OUTPUT:

```

Run: main ×
C:\Users\iQais\anaconda3\python.exe C:/Users/iQais/AppData/Local/Temp/tsp.py/main.py
How many cities do you want to generate: 4

Coordinates:
City 0 has coordinate [82, 79]
City 1 has coordinate [36, 88]
City 2 has coordinate [68, 54]
City 3 has coordinate [59, 63]

Initial state to travel: ['0', '1', '2', '3', '0']

Initial distance was 134.31 km.
Final state (optimized) to travel: ['0', '2', '3', '1', '0']
Optimized distance is 122.22 km.

Process finished with exit code 0

```

Simulated Annealing on Tkinter:

```

# Owned
__author__ = "Qaiser Abbas"
__copyright__ = "Copyright 2020, Artificial Intelligence Assignment-02"
__email__ = "qaiserabbas889@yahoo.com"
#=====

import math
import random
import matplotlib.pyplot as plt

```

```
from util import City, read_cities, write_cities_and_return_them,
generate_cities, visualize_tsp, path_cost

class SimAnneal(object):
    def __init__(self, cities, temperature=-1, alpha=-1,
stopping_temperature=-1, stopping_iter=-1):
        self.cities = cities
        self.num_cities = len(cities)
        self.temperature = math.sqrt(self.num_cities) if temperature == -1
else temperature
        self.T_save = self.temperature
        self.alpha = 0.999 if alpha == -1 else alpha
        self.stopping_temperature = 1e-8 if stopping_temperature == -1 else
stopping_temperature
        self.stopping_iter = 100000 if stopping_iter == -1 else stopping_iter
        self.iteration = 1
        self.route = None
        self.best_fitness = float("Inf")
        self.progress = []
        self.cur_cost = None

    def greedy_solution(self):
        start_node = random.randint(0, self.num_cities) # start from a
random node
        unvisited = self.cities[:]
        del unvisited[start_node]
        route = [cities[start_node]]
        while len(unvisited):
            index, nearest_city = min(enumerate(unvisited), key=lambda item:
item[1].distance(route[-1]))
            route.append(nearest_city)
            del unvisited[index]
            current_cost = path_cost(route)
            self.progress.append(current_cost)
            return route, current_cost

    def accept_probability(self, candidate_fitness):
        return math.exp(-abs(candidate_fitness - self.cur_cost) /
self.temperature)

    def accept(self, guess):
        guess_cost = path_cost(guess)
        if guess_cost < self.cur_cost:
            self.cur_cost, self.route = guess_cost, guess
            if guess_cost < self.best_fitness:
                self.best_fitness, self.route = guess_cost, guess
        else:
            if random.random() < self.accept_probability(guess_cost):
                self.cur_cost, self.route = guess_cost, guess

    def run(self):
        self.route, self.cur_cost = self.greedy_solution()
        while self.temperature >= self.stopping_temperature and
self.iteration < self.stopping_iter:
            guess = list(self.route)
            left_index = random.randint(2, self.num_cities - 1)
```

```
        right_index = random.randint(0, self.num_cities - left_index)
        guess[right_index: (right_index + left_index)] =
reversed(guess[right_index: (right_index + left_index)])
        self.accept(guess)
        self.temperature *= self.alpha
        self.iteration += 1
        self.progress.append(self.cur_cost)

    print("Best fitness obtained: ", self.best_fitness)

def visualize_routes(self):
    visualize_tsp('simulated annealing TSP', self.route)

def plot_learning(self):
    fig = plt.figure(1)
    plt.plot([i for i in range(len(self.progress))], self.progress)
    plt.ylabel("Distance")
    plt.xlabel("Iterations")
    plt.show(block=False)

if __name__ == "__main__":
    cities = read_cities(64)
    sa = SimAnneal(cities, stopping_iter=15000)
    sa.run()
    sa.plot_learning()
    sa.visualize_routes()
```

Data file: with 8 cities

591 917

315 81

895 990

508 595

367 539

73 728

344 842

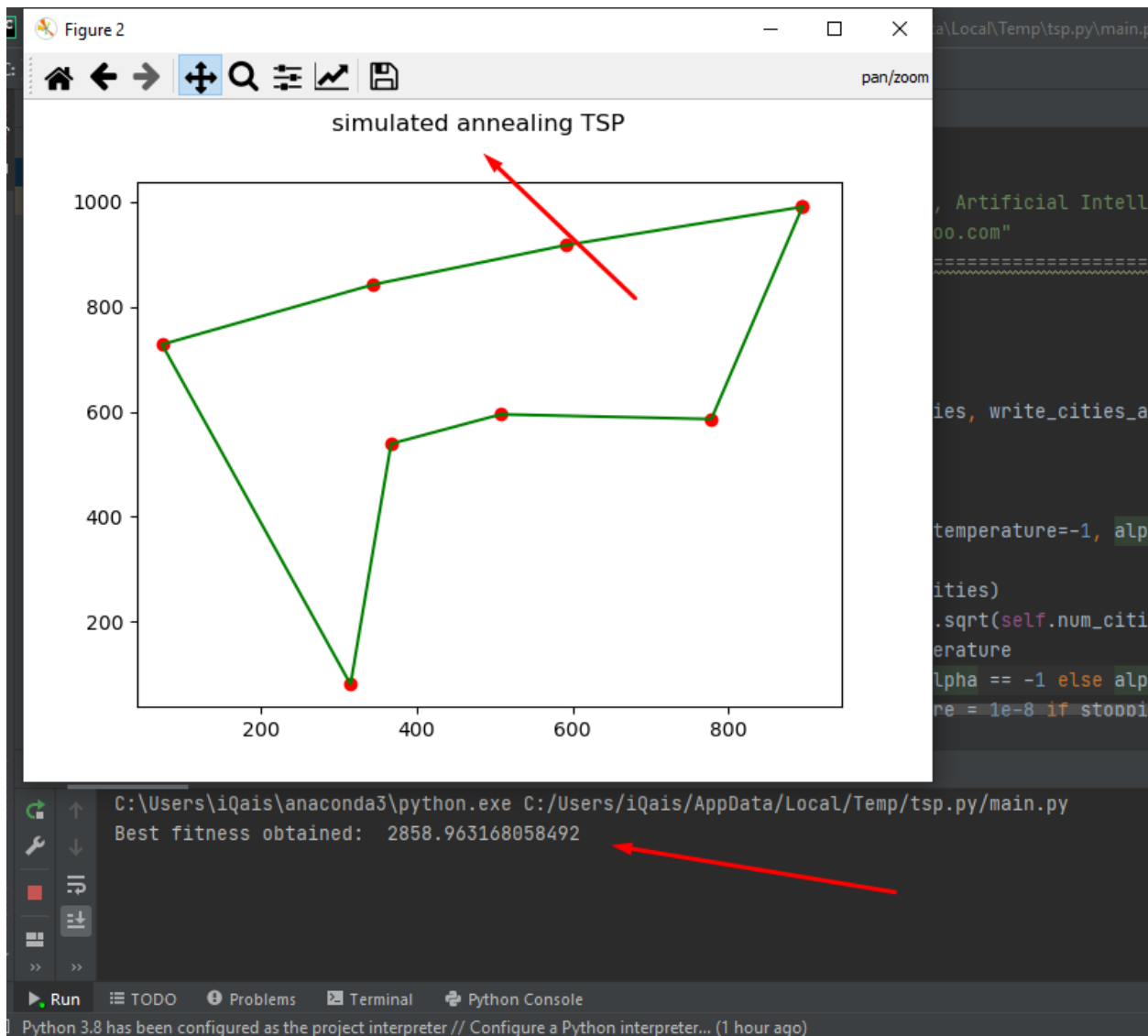
778 586

**Time complexity of Simulated Annealing:** if the maximum degree is bounded, the upper bound is  $O(v^5)$ , where  $v$  is the number of vertices.

The best thing about simulated annealing is that it requires very less

memory. It will not give optimal solution, but the solution provided by this will be good in reasonable time.

OUTPUT:



MIN MAX Algorithm:

```
__author__ = "Qaiser Abbas"
```

```

__copyright__ = "Copyright 2020, Artificial Intelligence Assignment-02"
__email__ = "qaiserabbas889@yahoo.com"
from gurobipy import *
import itertools
from math import sqrt

def min_max_length_under_complete_graph(city_num, deliver_num, weight_metrix,
TL):
    model = Model("TSP")
    model.setParam(GRB.Param.TimeLimit, TL)
    # Create variables
    x = {}
    for i in range(city_num):
        for j in range(city_num):
            for k in range(deliver_num):
                x[i, j, k] = model.addVar(vtype=GRB.BINARY, name='e_' + str(i
) + '_' + str(j) + '_' + str(k))
    Q = model.addVar(name='Q')

    model.setObjective(Q, GRB.MINIMIZE)

    for k in range(deliver_num):
        model.addConstr(quicksum(x[0, j, k] for j in range(1, city_num)) == 1
)
        model.addConstr(quicksum(x[i, 0, k] for i in range(1, city_num)) == 1
)

    for i in range(1, city_num):
        model.addConstr(quicksum(x[i, j, k]
                                for j in range(city_num)
                                for k in range(deliver_num)) == 1
)

    for j in range(1, city_num):
        model.addConstr(quicksum(x[i, j, k]
                                for i in range(city_num)
                                for k in range(deliver_num)) == 1
)

    for r in range(1, city_num):
        for k in range(deliver_num):
            model.addConstr((quicksum(x[i, r, k] for i in range(city_num))
                            - quicksum(x[r, j, k] for j in range(city_num)))
                            == 0
)

    model.addConstrs((x[i, i, k] == 0
                      for k in range(deliver_num))

```



```

        for i in range(1, city_num)), name='C'
    )
    for k in range(deliver_num):
        model.addConstr(quicksum(weight_metrix[i][j] * x[i, j, k]
                                for i in range(city_num)
                                for j in range(city_num)) <= Q)

    # Callback - use lazy constraints to eliminate sub-tours
    def subtourelim(model, where):
        if where == GRB.callback.MIPSOL:
            # make a list of edges selected in the solution
            for k in range(deliver_num):
                selected = []
                visited = set()
                for i in range(city_num):
                    sol = model.cbGetSolution([x[i, j, k] for j in range(city
_num)]]
                    new_selected = [(i, j) for j in range(city_num) if sol[j]
> 0.5]
                    selected += new_selected

                if new_selected:
                    visited.add(i)

            tour = subtour(selected, visited)

            if len(tour) < len(visited):
                # add a subtour elimination constraint
                expr = quicksum(x[i, j, k] for i, j in itertools.permutat
ions(tour, 2))
                model.cbLazy(expr <= len(tour) - 1)

    # Optimize model
    model.update()
    model.params.LazyConstraints = 1
    # model.optimize()
    model.optimize(subtourelim)

```

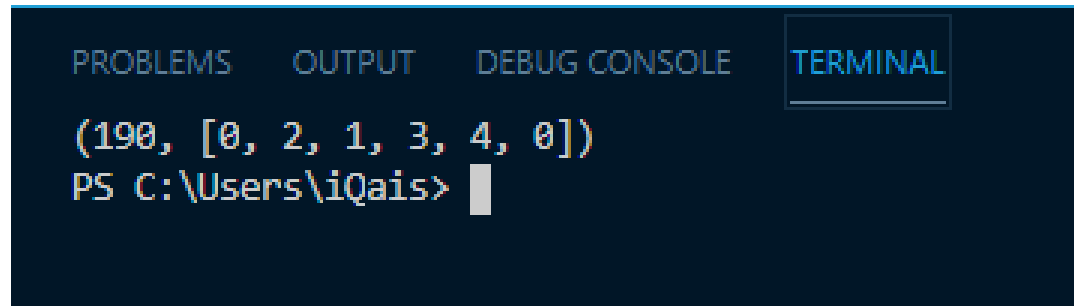
```
node_mat = [[0 for i in range(city_num)] for i in range(city_num)] for i
in range(deliver_num):
    for k in range(deliver_num):
        for i in range(city_num):
            for j in range(city_num):
                node_mat[k][i][j] = x[i, j, k].x

allpath = []
for k in range(deliver_num):
    path = []
    cnt = 0
    while True:
        path.append(cnt)
        for j in range(city_num):
            if node_mat[k][cnt][j] > 0.5:
                cnt = j
                break
        if cnt in path:
            path.append(cnt)
            break
    allpath.append(path)
return allpath

def subtour(edges, visited):
    unvisited = list(visited)
    cycle = range(len(visited) + 1)
    selected = {}
    for x, y in edges:
        selected[x] = []
    for x, y in edges:
        selected[x].append(y)
    # print (selected)
    while unvisited:
        thiscycle = []
        neighbors = unvisited
        while neighbors:
            current = neighbors[0]
            thiscycle.append(current)
            unvisited.remove(current)
            neighbors = [j for j in selected[current] if j in unvisited]
        if len(cycle) > len(thiscycle):
            cycle = thiscycle
    return cycle
```

**Time complexity of Min Max Algorithm:** Time complexity of Min-Max algorithm is  $O(b^m)$ , where  $b$  is branching factor of the city-tree, and  $m$  is the maximum depth of the tree.

OUTPUT:



```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL
(190, [0, 2, 1, 3, 4, 0])
PS C:\Users\iQais>
```