maths

$$\mathrm{Var}[\mathbf{b}|x] = \sigma(\mathbf{X}'\mathbf{X})^{-1}$$

$$\mathrm{Var}[\boldsymbol{\beta}|\boldsymbol{X}] = \sigma^2 (\mathbf{X}'\mathbf{X})^{-1} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}' \left(\ ^2\mathbf{I} \right) \mathbf{X} = (\mathbf{X}'\mathbf{X})^{-1}\sigma^2 \mathbf{X}' \mathbf{X} = \sigma^2 \sum_{i=1}^n \mathbf{x}_i' \mathbf{x_i} (\mathbf{X}'\mathbf{X})^{-1}$$

$$\mathrm{Var}[\boldsymbol{\beta}|\boldsymbol{X}] = \sigma^2 (\mathbf{X}'\mathbf{X})^{-1} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}' \left(\ ^2\mathbf{I} \right) \mathbf{X} = (\mathbf{X}'\mathbf{X})^{-1}\sigma^2 \mathbf{X}' \mathbf{X} = \sigma^2 \sum_{i=1}^n \mathbf{x}_i' \mathbf{x_i} (\mathbf{X}'\mathbf{X})^{-1}$$

$$E(\hat{\sigma}2) = \frac{n-1}{n}\sigma$$