



BAHRIA UNIVERSITY, (Karachi Campus)

Department of Software Engineering

Quiz 4 - Fall 2022

COURSE TITLE: Calculus and Analytical Geometry
Class: BSE-I (B)
Course Instructor: MR. DANIYAL UR REHMAN
Date: 10-1-2023

COURSE CODE: GSC-110
Shift: Morning
Time Allowed: 20 min
Max. Marks: 2.5 Marks

[CLO2: 2.5 Marks]

Question No. 1

- Illustrate the value of c which is guaranteed by Rolle's Theorem for the function $f(x) = (x-3)(x+1)^3$, $[-1,3]$
- Illustrate the value of c which is guaranteed by Mean value Theorem for the function $f(x) = x^3 + 2x$, $[-1,1]$
- If $y = f(x) = \log(x + \sqrt{x^2 + 1})$, show that $(1 + x^2) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 0$
- predict the first four term of maclaurin series for the function $f(x) = e^{-x}$

$$\begin{aligned} a) \quad f(x) &= (x-3)(x^3+3x^2+x+1) = x^4 + 3x^3 + x^2 + x \\ &\quad - 3x^3 - 9x^2 - 3x - 3 = x^4 - 8x^2 - 2x - 3 \\ f'(x) &= 4x^3 - 16x - 2 \\ f'(c) &= 4c^3 - 16c - 2 \end{aligned}$$

$$c = 2.05, -0.12, -1.9$$

$$\boxed{c = 2.05, -0.12}$$

$$\begin{aligned} b) \quad f(b) &= f(1) = 3 \\ f(a) &= -1 + 2 = 1 \end{aligned}$$

$$= \frac{3-1}{1+1}$$

$$= \frac{2}{2}$$

$$3x^2 + 2 = 1$$

$$3x^2 = -1$$