CSE427s Homework 7

Adrien Xie, Guangda Ouyang

TOTAL POINTS

73 / 100

QUESTION 1

Computing Word Co-Occurrence 50 pts

- 1.1 Implementing Co-Occurence 20 / 20
 - √ + 6 pts Correct \$\$\small\textsf{WordCo.java}\$\$
 - √ + 2 pts Student comments in
 - \$\$\small\textsf{WordCo.java}\$\$
 - √ + 10 pts Correct
 - \$\$\small\textsf{WordCoMapper.java}\$\$
 - √ + 2 pts Student comments in

\$\$\small\textsf{WordCoMapper.java}\$\$

- + 7 pts Partially correct WordCoMapper.java
- 1.5 pts Pages not selected
- + 0 pts No WUSTL key or missing files
- + 0 pts No credit
- + 0 pts Graded by ET
- 1.2 Checking the Output 5 / 5
 - √ + 1 pts Correct number of word pairs:
 - \$\$\small298,917\$\$
 - √ + 1 pts Correct number of pairs
 - \$\$\small\text{the,lovers}\$\$: \$\$\small3\$\$
 - √ + 1 pts Correct number of pairs
 - \$\$\small\text{loved,you}\$\$: \$\$\small15\$\$
 - √ + 1 pts Correct number of pairs
 - \$\$\small\text{you,loved}\$\$: \$\$\small6\$\$
 - √ + 1 pts Correct number of pairs
 - \$\$\small\text{verona,julia}\$\$: \$\$\small2\$\$
 - 0.5 pts No pages selected
 - + 0 pts No credit
- 1.3 Communication Costs 5 / 5
 - √ + 5 pts Correct communication cost: \$\$\small
 - 1.012.561\$\$
 - 0.5 pts Pages not selected
 - + 0 pts No credit
- 1.4 The Drawbacks 10 / 10

- + 5 pts Partially Correct
- 1 pts Pages not selected
- + 0 pts No credit
- \checkmark + 10 pts Correct drawback: it fails to model the complete pattern of linguistic semantics, ie. the context window might be too small compared to trigram or n-gram.
- 1.5 Stripes 10 / 10
 - √ + 5 pts Correct communication cost: \$\$k\$\$
 - + 3 pts Partially correct communication cost
 - √ + 5 pts Correct explanation of effect on memory usage
 - + 3 pts Partially correct explanation of effect on memory usage
 - + 0 pts No Credit
 - 1 pts Page not selected

QUESTION 2

Collaborative Filtering: Similarity

Measures 20 pts

- 2.1 Pearson Correlation 5 / 10
 - + 10 pts totally correct with proof and provide math equation
 - √ + 5 pts not efficient proof with math equation
 - + 2 pts partially correct
 - + 0 pts no credit
 - + 0 pts Grade by YQ
- 2.2 Quality vs. Feasibility 5 / 5
 - √ + 2.5 pts benefit Correct
 - √ + 2.5 pts Disadvantage Correct
 - + 0 pts No credict
 - + 0 pts grade by YQ
- 2.3 Jaccard Similarity 5 / 5
 - √ + 0 pts Graded by GD
 - √ + 5 pts Correct

- + 4 pts Mostly correct
- + 2.5 pts Partially correct

QUESTION 3

Collaborative Filtering in MapReduce 30 pts

3.1 Benefits 5 / 5

- √ + 2.5 pts Correct benefit (1/2). Benefits of the dual approach include: being more efficient to compute if there are significantly more users than items, reducing the bias of user comparison since classifications for items tend to be more well-defined leading to more accurate predictions, finding similar items is easier than finding similar people
 - + 1.5 pts Partially correct benefit (1/2)
 - + 0 pts Incorrect benefit (1/2)
- √ + 2.5 pts Correct benefit (2/2)
 - + 1.5 pts Partially correct benefit (2/2)
 - + 0 pts Incorrect benefit (2/2)
 - 0.5 pts Pages not selected
 - + 0 pts No credit
- √ + 0 pts Graded by CS

3.2 Implementing your Program 3 / 25

- + 5 pts Correct first mapper output:
- \$\$\small\textsf{(user-id, (movie-id, rating))}\$\$
 - + 3 pts Partially correct first mapper output
 - + 5 pts Correct first reducer input:
- $\$ \small\textsf(user-id, [(movie-id, rating), (movie-id, rating), \ldots])\\$\$
 - + 3 pts Partially correct first reducer input
 - + 5 pts Correct first reducer output:
- \$\$\small\textsf{(movie-id, movie-id), (} \mathbf{r_1, r_2,
- r_1 r_2, r_1^2, r_2^2\\textsf())\$\$
 - + 3 pts Partially correct first reducer output
 - + 5 pts Correct second reducer input:
- \$\$\small\textsf{((movie-id, movie-id), [(\mathbf{r_1,
- r_2, r_1 r_2, r_1^2, r_2^2}\textsf(), \ldots])}\$\$
 - + 3 pts Partially correct second reducer input
 - + 5 pts Correct second reducer output:
- \$\$\small\textsf{((movie-id, movie-id), cosine_similarity)}\$\$

√ + 3 pts Partially correct second reducer output

- 2.5 pts Pages not selected
- + 0 pts No credit

√ + 0 pts graded by CS

You do not show any of the inputs or outputs for the MR jobs.

- (b) By using "wc -l part-r-00000" and "grep pattern part-r-00000" commands, we have:
 - 298917 pairs.
 - the,lovers 3
 - loved,you 15
 - you,loved 6
 - verona, julia 2

(c)

communication cost = map input records + reduce input records

= 173126 + 839435 = 1012561

w		FILE: Number of bytes read	0	13452222	13452222	
rs		FILE: Number of bytes written	14025780	13595552	27621332	
ration		FILE: Number of large read operations	0	0	0	
sks		FILE: Number of read operations	0	0	0	
tasks	File System Counters	FILE: Number of write operations	0	0	0	
		HDFS: Number of bytes read	5284754	0	5284754	
		HDFS: Number of bytes written	0	4124037	4124037	
		HDFS: Number of large read operations	0	0	0	
		HDFS: Number of read operations	12	3	15	
		HDFS: Number of write operations	0	2	2	
		Name	_ Map	≎ Reduce	≎ Total	
		Data-local map tasks	0	0	5	
		Killed map tasks	0	0	1	
		Launched map tasks	0	0	5	
		Launched reduce tasks	0	0	1	
		Total megabyte-milliseconds taken by all map tasks	0	0	230532096	
	Job Counters	Total megabyte-milliseconds taken by all reduce tasks	0	0	36761600	
		Total time spent by all map tasks (ms)	0	0	225129	
		Total time spent by all maps in occupied slots (ms)	0	0	225129	
		Total time spent by all reduce tasks (ms)	0	0	35900	
		Total time spent by all reduces in occupied slots (ms)	0	0	35900	
		Total vcore-milliseconds taken by all map tasks	0	0	225129	
		Total vcore-milliseconds taken by all reduce tasks	0	0	35900	
		Name	→ Map	♦ Reduce	≎ Total	
		Combine input records	0	0	0	
	Map-Reduce Framework	Combine output records	0	0	0	
		CPU time spent (ms)	8960	3270	12230	
		Failed Shuffles	0	0	0	
		GC time elapsed (ms)	2594	411	3005	
		Input split bytes	523	0	523	
		Map input records	173126	0	173126	
		Map output bytes	11773346	0	11773346	
		Map output materialized bytes	13452240	0	13452240	
		Map output records	839435	0	839435	
		Merged Map outputs	0	4	4	
		Physical memory (bytes) snapshot	830238720	150646784	980885504	
		Reduce input groups	0	298917	298917	
		Reduce input records	0	839435	839435	
		Reduce output records	0	298917	298917	
		Reduce shuffle bytes	0	13452240	13452240	
		Shuffled Maps	0	4	4	
		Spilled Records	839435	839435	1678870	
		Total committed heap usage (bytes)	662454272	60751872	723206144	
		Virtual memory (bytes) snapshot	6017675264	1511354368	7529029632	

1.1 Implementing Co-Occurence 20 / 20

- √ + 6 pts Correct \$\$\small\textsf{WordCo.java}\$\$
- √ + 2 pts Student comments in \$\$\small\textsf{WordCo.java}\$\$
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1.2 Checking the Output 5/5

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- √ + 1 pts Correct number of pairs \$\$\small\text{loved,you}\$\$: \$\$\small15\$\$
- √ + 1 pts Correct number of pairs \$\$\small\text{you,loved}\$\$: \$\$\small6\$\$
- √ + 1 pts Correct number of pairs \$\$\small\text{verona,julia}\$\$: \$\$\small2\$\$
 - 0.5 pts No pages selected
 - + 0 pts No credit

- (b) By using "wc -l part-r-00000" and "grep pattern part-r-00000" commands, we have:
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1.3 Communication Costs 5 / 5

- √ + 5 pts Correct communication cost: \$\$\small 1,012,561\$\$
 - **0.5 pts** Pages not selected
 - + 0 pts No credit

(d)

Example 1: Paris is the capital of France.

Example 2: Ronaldo joins Juventus.

In English, most useful information of a sentence are usually presented by the subject and the object, while they are usually separated (by verb and other things).

We can easily eye-ball that the meaningful co-occurrence we want to learn are (Paris, capital), (Paris, France) in the first example, and (Ronaldo, Juventus) in the second examples. Merely counting the co-occurrence of words directly next to each other would miss both of this pairs, meanwhile, collecting some meaningless pairs such as (Paris, is) and (is, the).

(e)

When k is the size of the vocabulary, the communication costs are $\frac{k^2-k}{2}$ when using pairs and k – 1 when using stripes. The memories needed in reduce() fuction are 2 ids + 1 count * m for pairs and 1 id + (k – 1 ids and counts) * m when using stripes. (m is the total number of users)

We can see that the communication cost for pairs are significantly higher than stripes' as k gets larger since it's a quadratic verses linear function. On the other hand, pairs requires much less memory, especially when m gets big because of the difference between the coefficients before m.

1.4 The Drawbacks 10 / 10

- + 5 pts Partially Correct
- 1 pts Pages not selected
- + **0 pts** No credit

 \checkmark + 10 pts Correct drawback: it fails to model the complete pattern of linguistic semantics, ie. the context window might be too small compared to tri-gram or n-gram.

(d)

Example 1: Paris is the capital of France.

Example 2: Ronaldo joins Juventus.

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We can see that the communication cost for pairs are significantly higher than stripes' as k gets larger since it's a quadratic verses linear function. On the other hand, pairs requires much less memory, especially when m gets big because of the difference between the coefficients before m.

1.5 Stripes 10 / 10

- √ + 5 pts Correct communication cost: \$\$k\$\$
 - + 3 pts Partially correct communication cost
- √ + 5 pts Correct explanation of effect on memory usage
 - + 3 pts Partially correct explanation of effect on memory usage
 - + 0 pts No Credit
 - 1 pts Page not selected

(a)

$$\text{Cosine similarity} = \mathsf{C}(\mathsf{x},\mathsf{y}) = \cos(r_x,r_y) = \frac{\sum_{S \in S_{xy}} r_{xs} r_{ys}}{\sqrt{\sum_{S \in S_{xy}} r_{xs}^2} \sqrt{\sum_{S \in S_{xy}} r_{ys}^2}}$$

If we normalize vectors by subtracting the vector means, i.e., substituting $r_{\chi s}$ with $(r_{\chi s} - \overline{r_{\chi}})$ and substituting r_{ys} with $(r_{ys} - \overline{r_{y}})$, we get the Pearson correlation:

$$\text{Pearson correlation} = \text{P(x,y)} = \frac{\sum_{S \in S_{\mathcal{X}\mathcal{Y}}} (r_{xS} - \overline{r_x}) (r_{yS} - \overline{r_y})}{\sqrt{\sum_{S \in S_{\mathcal{X}\mathcal{Y}}} (r_{xS} - \overline{r_x})^2} \sqrt{\sum_{S \in S_{\mathcal{X}\mathcal{Y}}} (r_{yS} - \overline{r_y})^2}}$$

(b)

- Pearson correlation removes bias because of normalization (subtracting means).
- Computing Pearson correlation has more complex processes (computing the mean and subtract it) so the implementation is harder; also, we have to store all the vectors in order to compute the mean, requiring more memory.

(c)

- Easy to implement.
- Only tells similarity of two users' watch lists. Does not tell anything about the ratings.
- Applying a threshold. Divide the data into high ratings (>3) and low ratings (<3). We maybe want to ignore ratings lower than 3.

2.1 Pearson Correlation 5 / 10

- + 10 pts totally correct with proof and provide math equation
- √ + 5 pts not efficient proof with math equation
 - + 2 pts partially correct
 - + 0 pts no credit
 - + 0 pts Grade by YQ

(a)

$$\text{Cosine similarity} = \mathsf{C}(\mathsf{x},\mathsf{y}) = \cos(r_x,r_y) = \frac{\sum_{S \in S_{xy}} r_{xs} r_{ys}}{\sqrt{\sum_{S \in S_{xy}} r_{xs}^2} \sqrt{\sum_{S \in S_{xy}} r_{ys}^2}}$$

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- Applying a threshold. Divide the data into high ratings (>3) and low ratings (<3). We maybe want to ignore ratings lower than 3.

2.2 Quality vs. Feasibility 5 / 5

- √ + 2.5 pts benefit Correct
- √ + 2.5 pts Disadvantage Correct
 - + 0 pts No credict
 - + 0 pts grade by YQ

(a)

$$\text{Cosine similarity} = \mathsf{C}(\mathsf{x},\mathsf{y}) = \cos(r_x,r_y) = \frac{\sum_{S \in S_{xy}} r_{xs} r_{ys}}{\sqrt{\sum_{S \in S_{xy}} r_{xs}^2} \sqrt{\sum_{S \in S_{xy}} r_{ys}^2}}$$

If we normalize vectors by subtracting the vector means, i.e., substituting $r_{\chi s}$ with $(r_{\chi s} - \overline{r_{\chi}})$ and substituting r_{ys} with $(r_{ys} - \overline{r_{y}})$, we get the Pearson correlation:

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- Pearson correlation removes bias because of normalization (subtracting means).
- Computing Pearson correlation has more complex processes (computing the mean and subtract it) so the implementation is harder; also, we have to store all the vectors in order to compute the mean, requiring more memory.

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- Easy to implement.
- Only tells similarity of two users' watch lists. Does not tell anything about the ratings.
- Applying a threshold. Divide the data into high ratings (>3) and low ratings (<3). We maybe want to ignore ratings lower than 3.

2.3 Jaccard Similarity 5 / 5

- √ + 0 pts Graded by GD
- √ + 5 pts Correct
 - + 4 pts Mostly correct
 - + 2.5 pts Partially correct

(a)

- When having more users than items, it saves computation since computing similarities between users would be expensive.
- Does not have to rebuild everything when users' list changes.

(b)

	User1	User2	User3
Movie1	1		1
Movie2	3	2	2
Movie3	2	3	
Movie4			
Movie5		5	

$$\cos(\text{movie1, movie2}) = \frac{1*3+1*2}{\sqrt{1^2+1^2}\sqrt{3^2+2^2}} = 5/\sqrt{2*13} = 0.98$$

$$\cos(\text{movie1, movie3}) = \frac{1*2}{\sqrt{1^2}\sqrt{2^2}} = 2/\sqrt{4} = 1$$

$$\cos(\text{movie1, movie4}) = 0$$

$$\cos(\text{movie1, movie5}) = 0$$

$$\cos(\text{movie2, movie3}) = \frac{3*2+2*3}{\sqrt{3^2+2^2}\sqrt{2^2+3^2}} = 12/\sqrt{13*13} = 0.923$$

$$\cos(\text{movie2, movie4}) = 0$$

$$\cos(\text{movie2, movie5}) = \frac{2*5}{\sqrt{2^2}\sqrt{5^2}} = 10/\sqrt{4*25} = 1$$

$$\cos(\text{movie3, movie4}) = 0$$

$$\cos(\text{movie3, movie5}) = \frac{3*5}{\sqrt{3^2}\sqrt{5^2}} = 1$$

$$\cos(\text{movie4, movie5}) = 0$$

3.1 Benefits **5** / **5**

 $\sqrt{+2.5}$ pts Correct benefit (1/2). Benefits of the dual approach include: being more efficient to compute if there are significantly more users than items, reducing the bias of user comparison since classifications for items tend to be more well-defined leading to more accurate predictions, finding similar items is easier than finding similar people

- + 1.5 pts Partially correct benefit (1/2)
- + 0 pts Incorrect benefit (1/2)
- √ + 2.5 pts Correct benefit (2/2)
 - + 1.5 pts Partially correct benefit (2/2)
 - + 0 pts Incorrect benefit (2/2)
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- √ + 0 pts Graded by CS

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$$\cos(\text{movie3, movie5}) = \frac{3*5}{\sqrt{3^2}\sqrt{5^2}} = 1$$

$$\cos(\text{movie4, movie5}) = 0$$

3.2 Implementing your Program 3 / 25

- + 5 pts Correct first mapper output:
- \$\$\small\textsf{(user-id, (movie-id, rating))}\$\$
 - + 3 pts Partially correct first mapper output
 - + 5 pts Correct first reducer input:
- \$\$\small\textsf{(user-id, [(movie-id, rating), (movie-id, rating), \ldots])}\$\$
 - + 3 pts Partially correct first reducer input
 - + **5 pts** Correct first reducer output:
- $\$ \small\textsf{(movie-id, movie-id), (} \mathbf{r_1, r_2, r_1 r_2, r_1^2, r_2^2}\textsf{)}\$\$
 - + 3 pts Partially correct first reducer output
 - + 5 pts Correct second reducer input:
- $\$ \small\textsf(((movie-id, movie-id), [()\mathbf{r_1, r_2, r_1 r_2, r_1^2, r_2^2)\textsf(), \ldots])}\$\$
 - + 3 pts Partially correct second reducer input
 - + 5 pts Correct second reducer output:
- \$\$\small\textsf{((movie-id, movie-id), cosine_similarity)}\$\$
- √ + 3 pts Partially correct second reducer output
 - 2.5 pts Pages not selected
 - + 0 pts No credit
- √ + 0 pts graded by CS
 - You do not show any of the inputs or outputs for the MR jobs.