

# PROCESSAMENTO DIGITAL DE SINAIS

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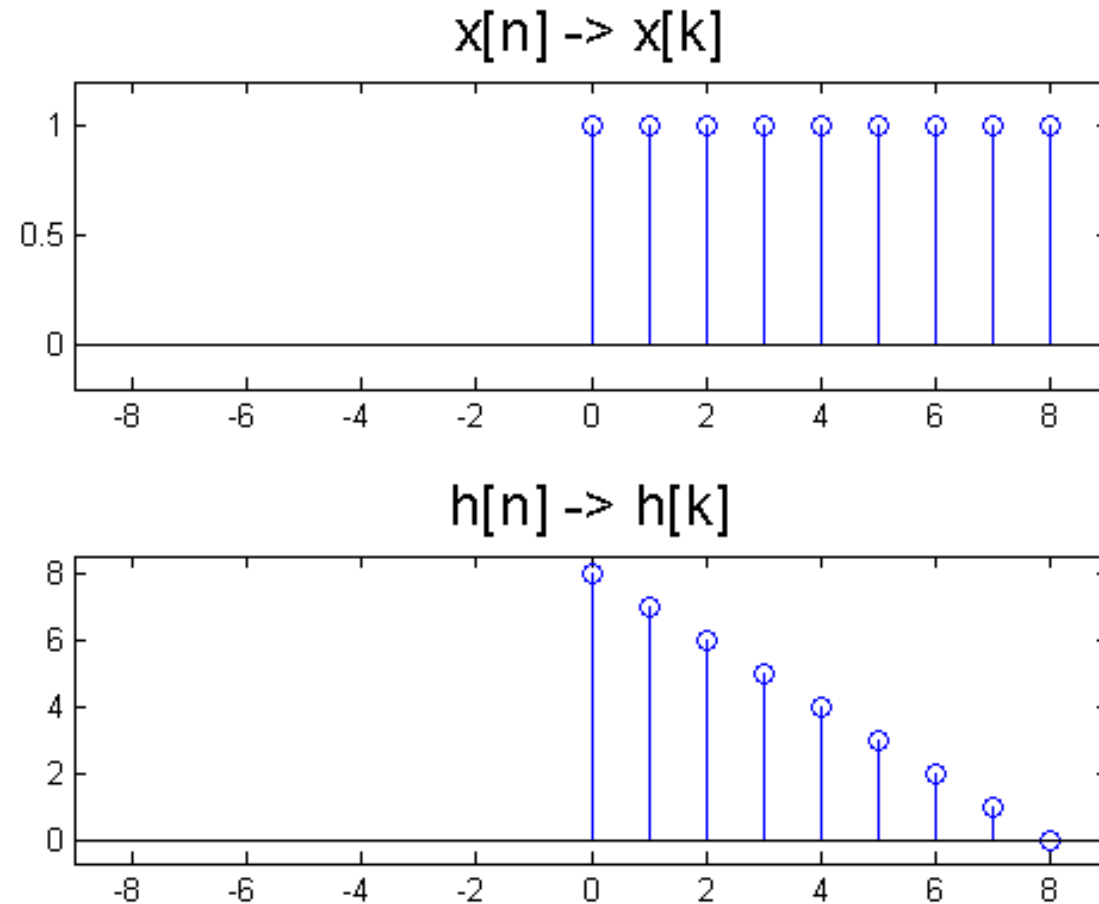
Turma EC  
2018

# Aula 05

## Convolução (Cont.) e exercícios

# Convolução na prática

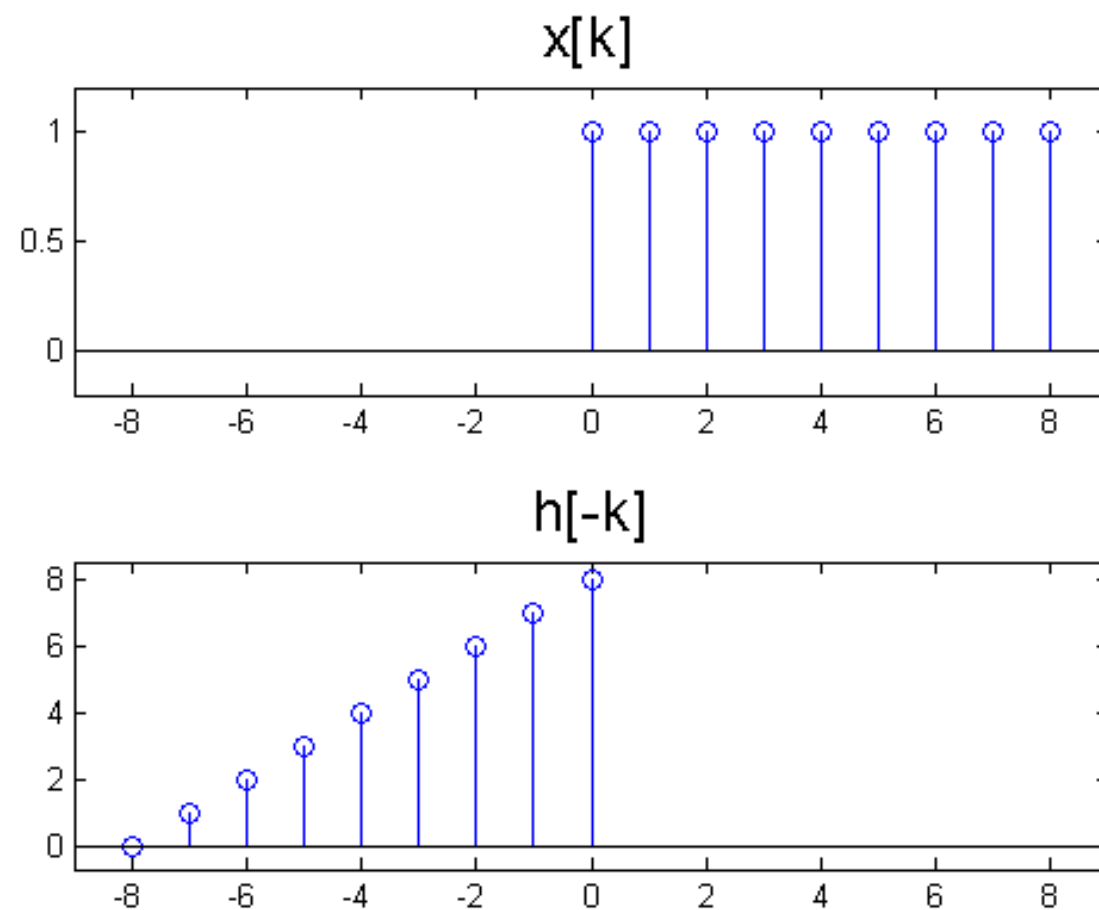
$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$



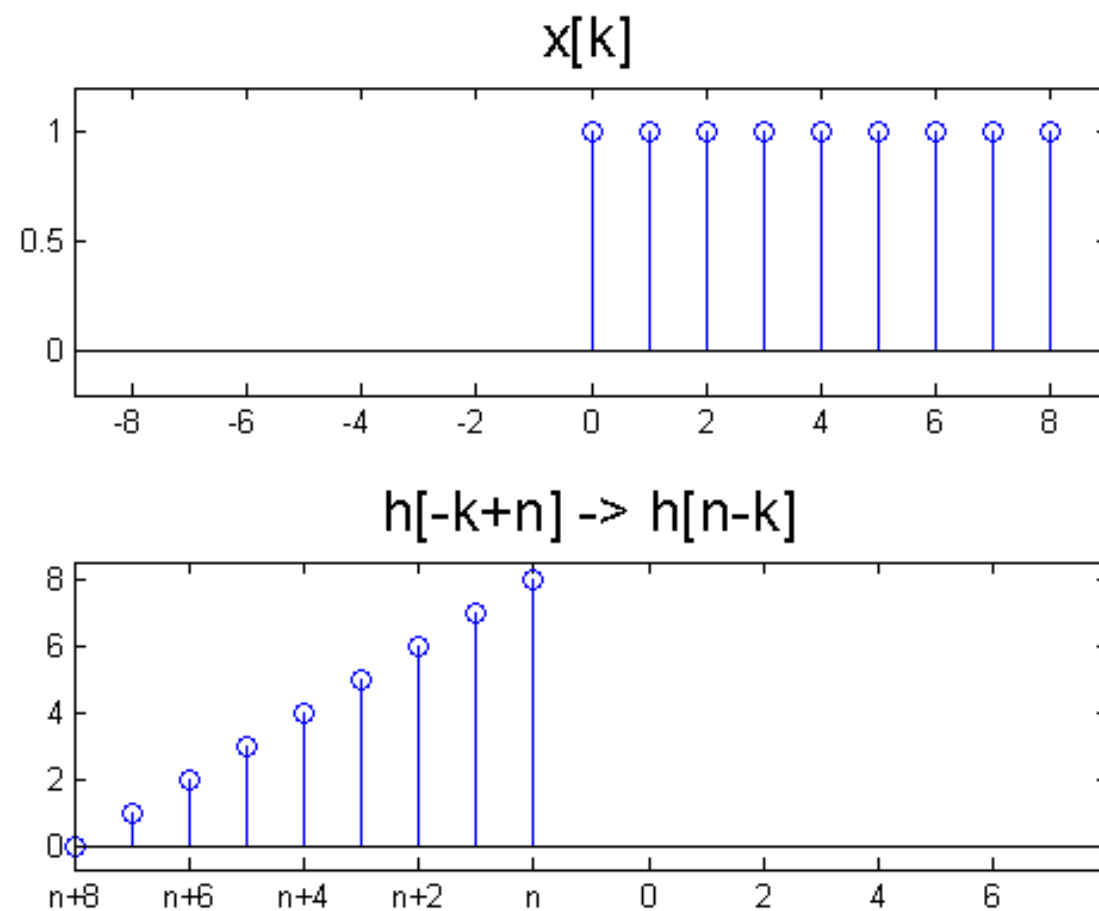
$$x[n] = u[n]$$

$$h[n] = \begin{cases} 8 - n, & n \geq 0 \\ 0, & n < 0 \end{cases}$$

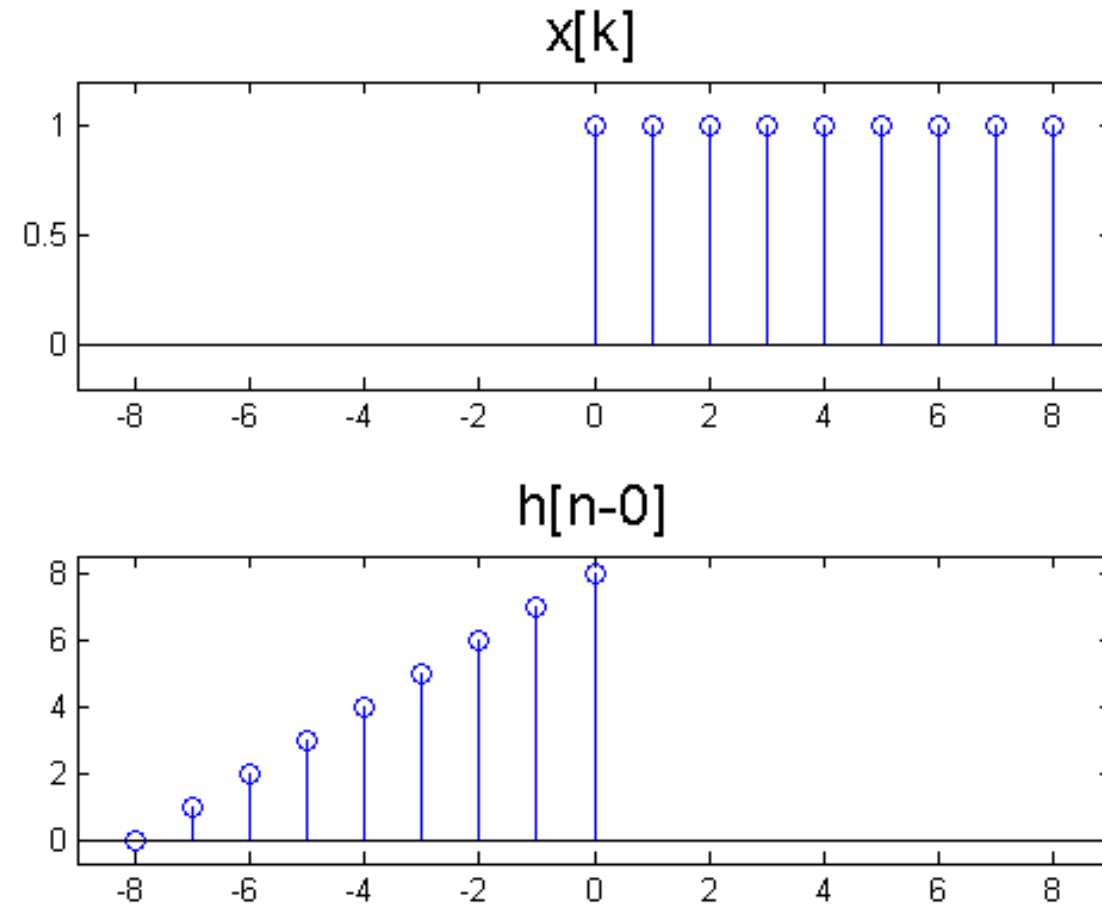
# Convolução na prática



# Convolução na prática



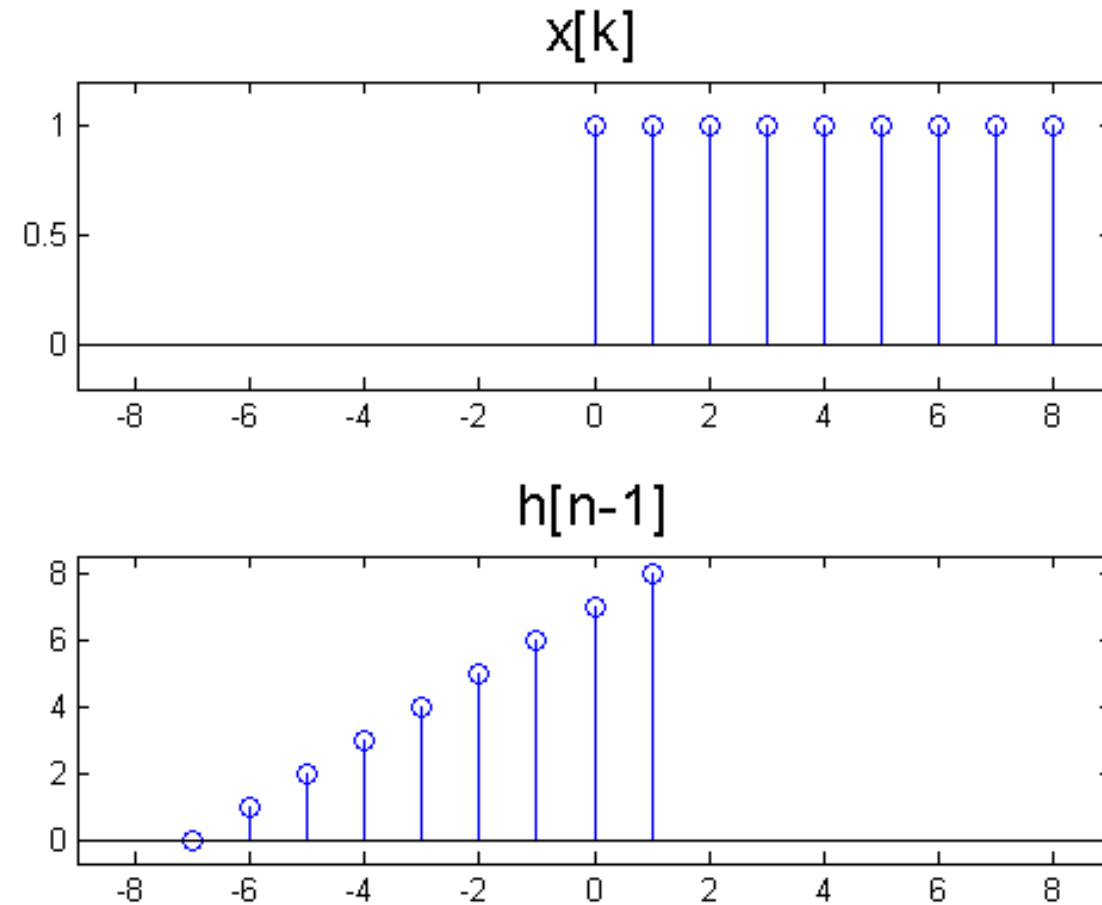
# Convolução na prática



$$y[0] = x[0] \times h[0]$$

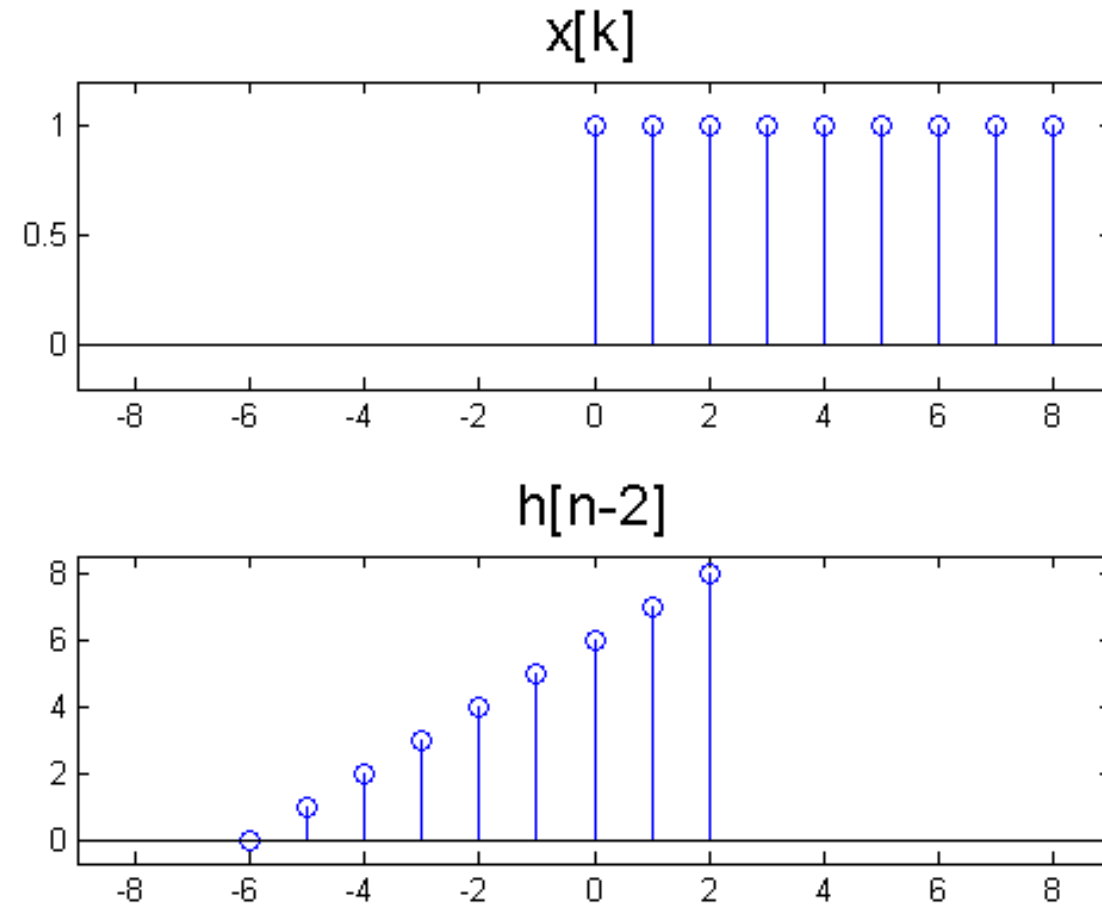
$$y[0] = 1 \times 8 = 8$$

# Convolução na prática



$$\begin{aligned} y[1] &= x[0] \times h[1] + \\ &= x[1] \times h[0] \\ &= 1 \times 7 + 1 \times 8 \\ &= 15 \end{aligned}$$

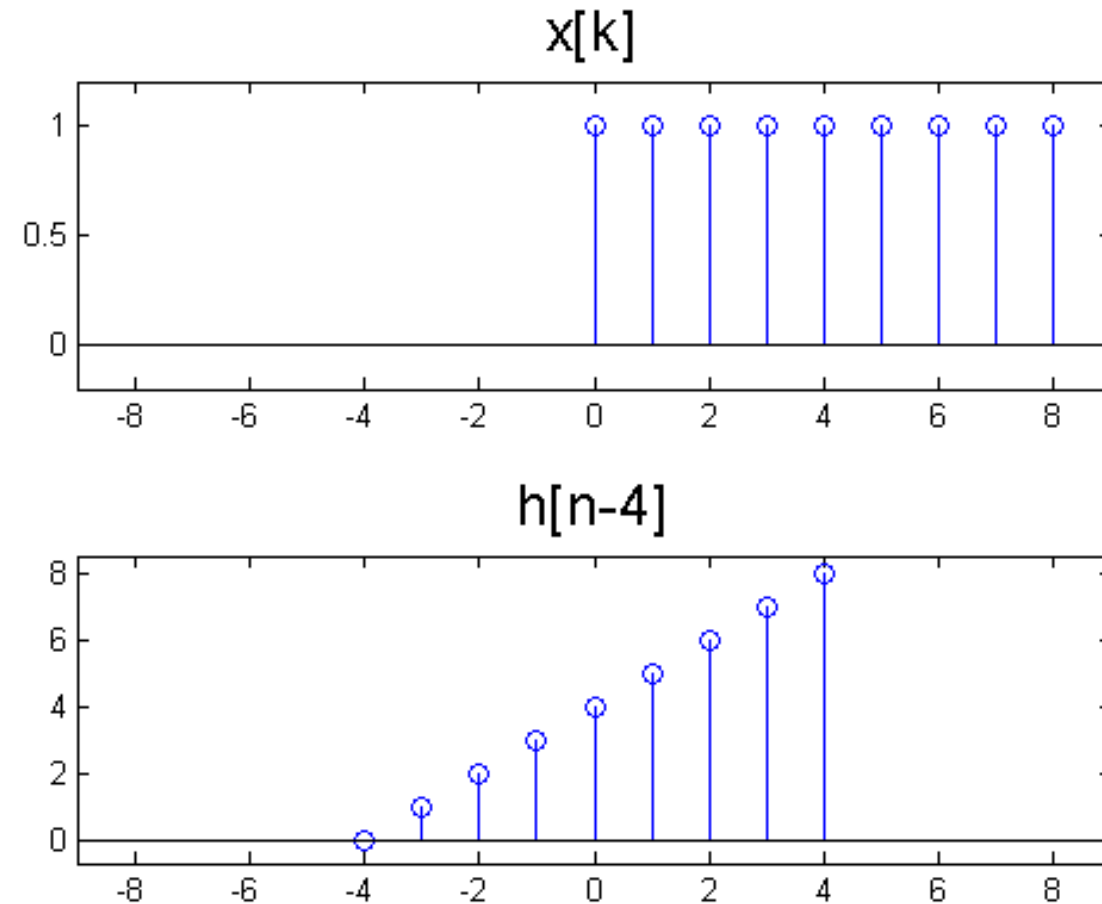
# Convolução na prática



$$\begin{aligned}y[2] &= x[0] \times h[2] + \\&= x[1] \times h[1] + \\&= x[2] \times h[0] \\&= 6 + 7 + 8 \\&= 21\end{aligned}$$

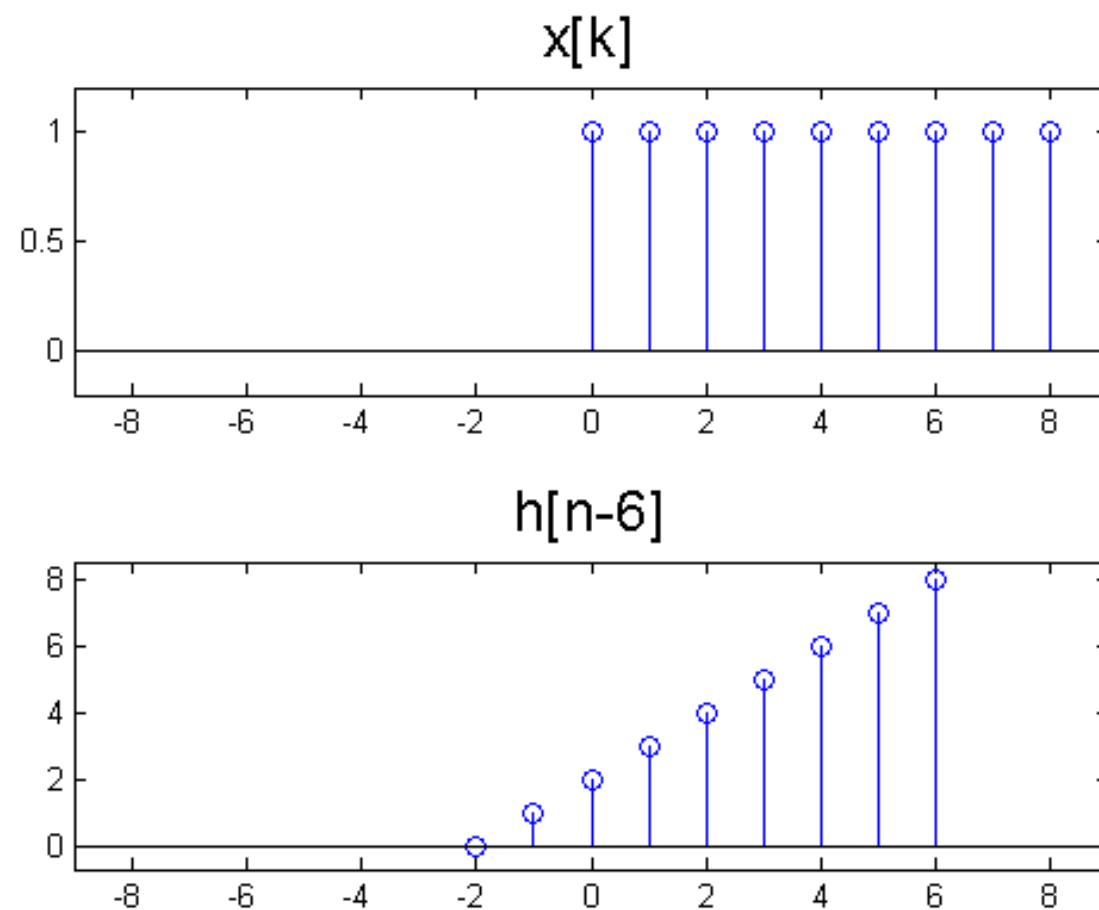


# Convolução na prática

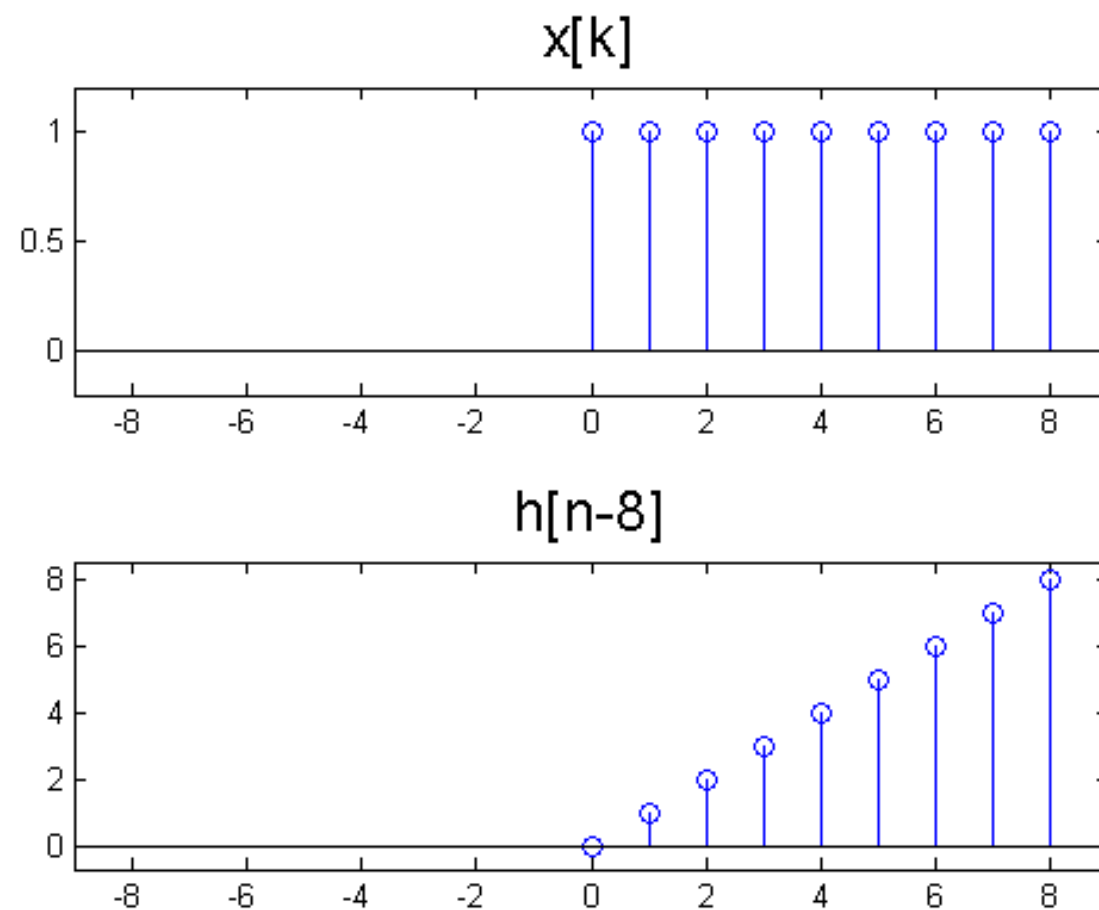


$$\begin{aligned} y[4] &= x[0] \times h[4] + \\ &= x[1] \times h[3] + \\ &= x[2] \times h[2] + \\ &= x[3] \times h[1] + \\ &= x[4] \times h[0] \\ &= 4 + 5 + 6 + 7 \\ &\quad + 8 \\ &= 30 \end{aligned}$$

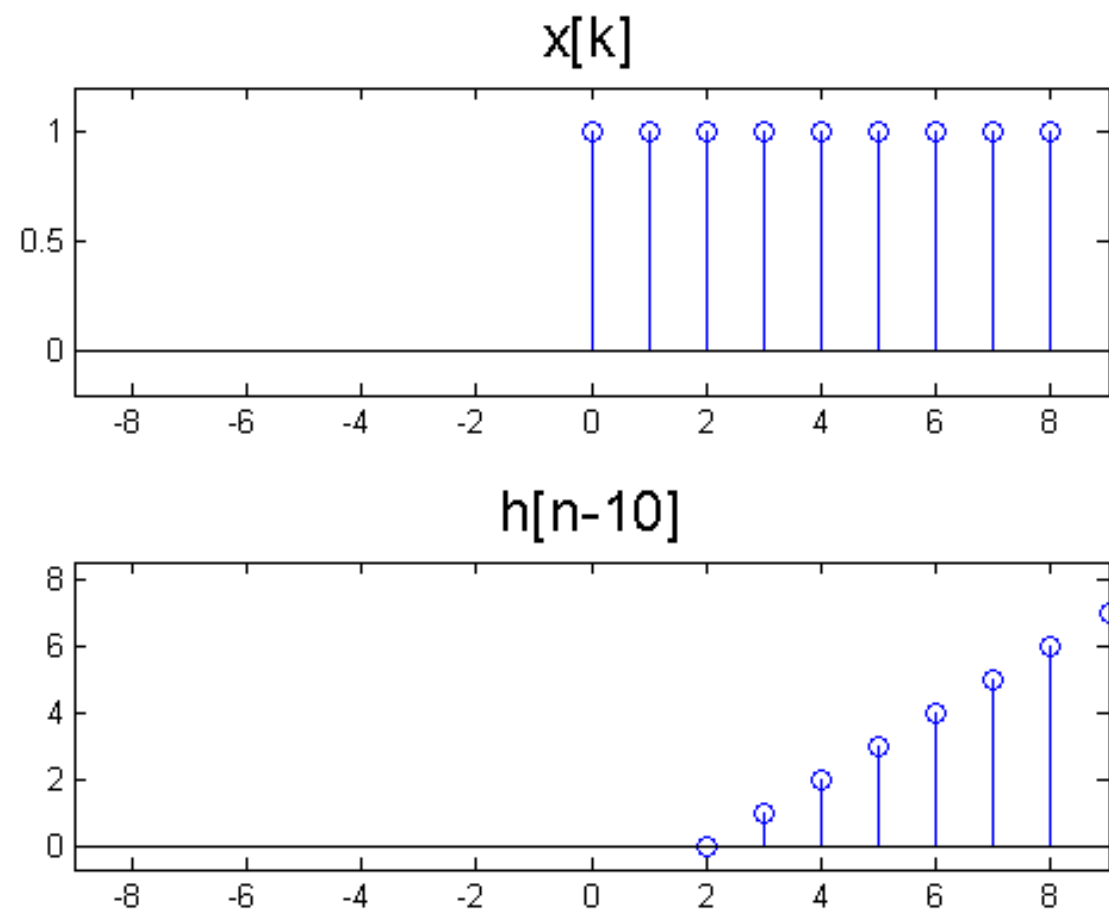
# Convolução na prática



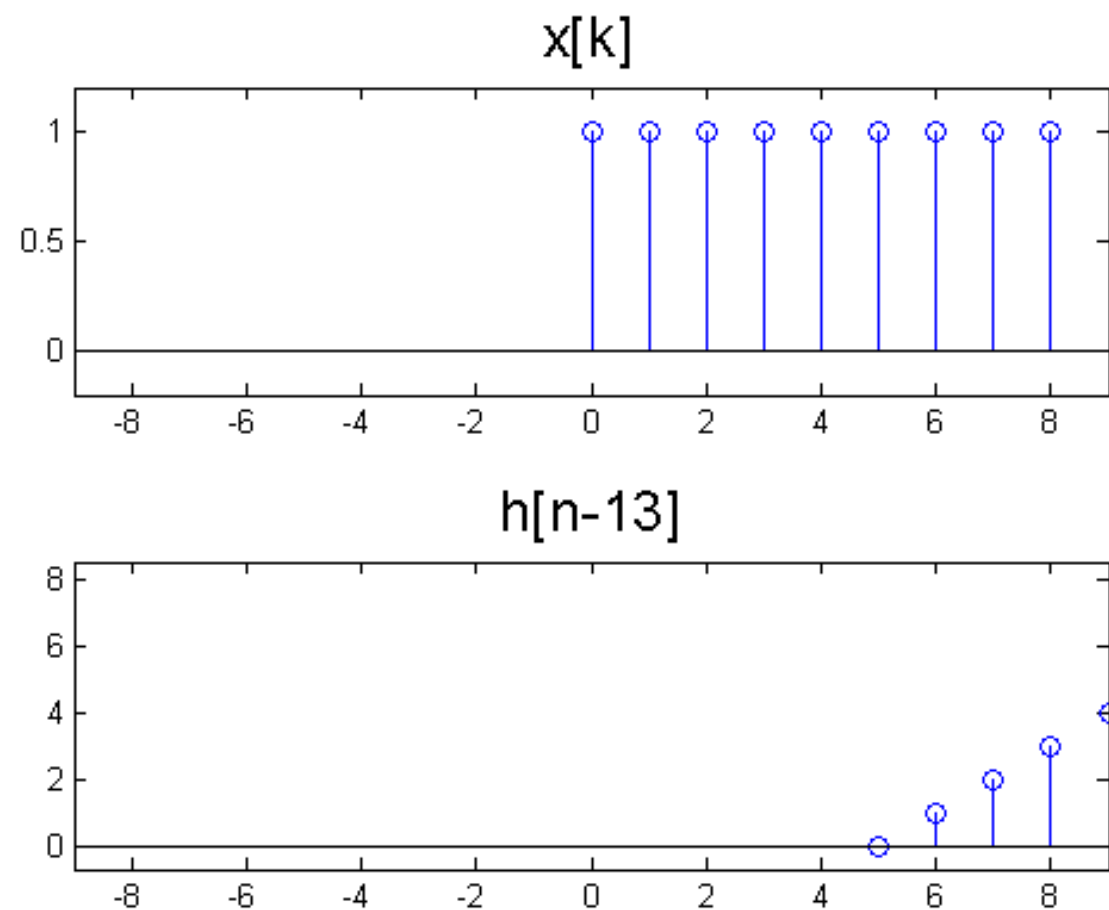
# Convolução na prática



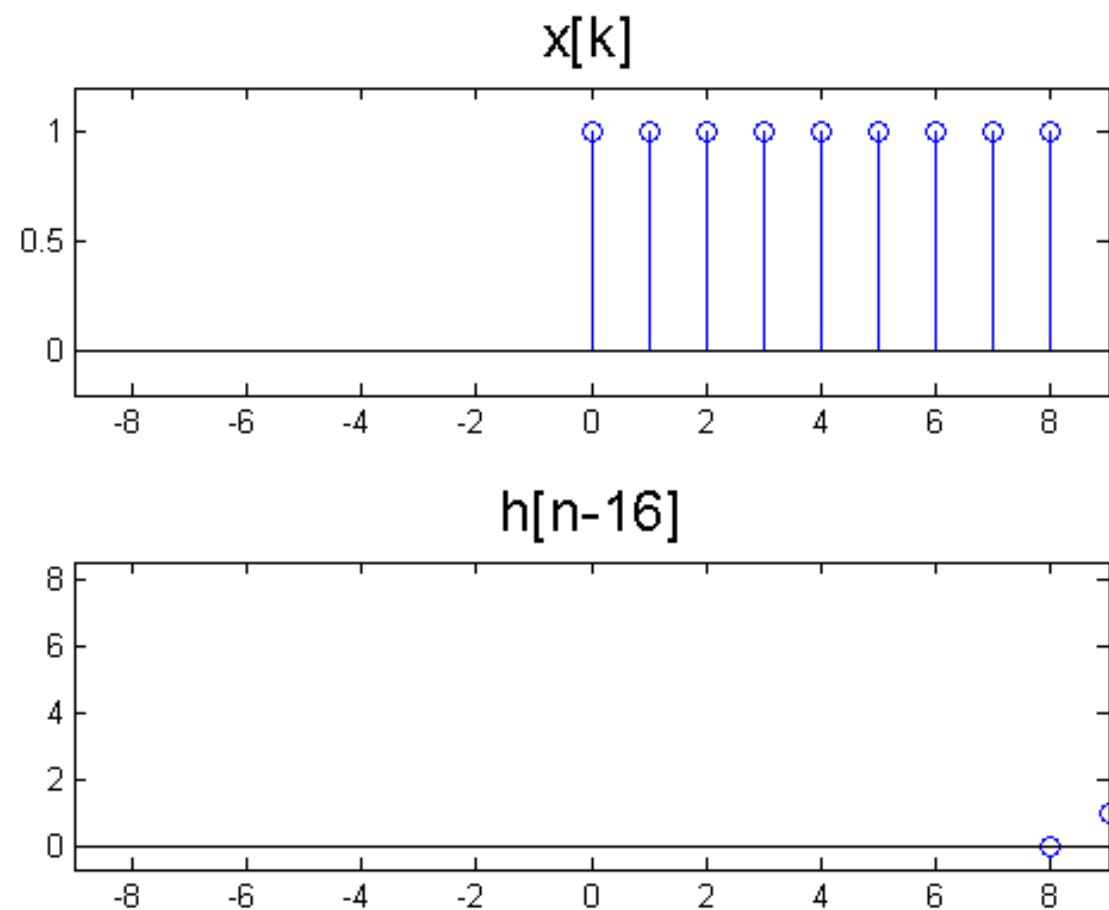
# Convolução na prática



# Convolução na prática

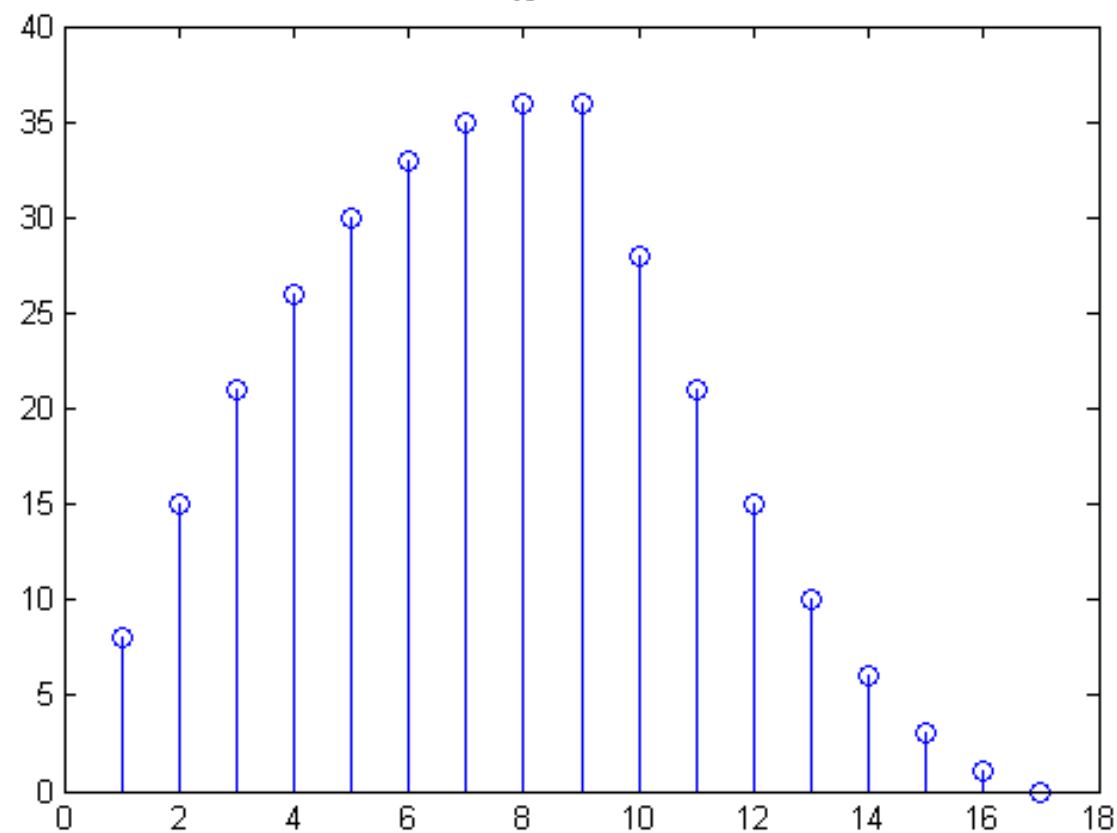


# Convolução na prática



# Convolução na prática

$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$



# Exercício

- A resposta ao impulso de um sistema LIT é:

$$h[n] = u[n] - u[n - 5]$$

- Ao se aplicar a esse sistema o sinal de entrada:

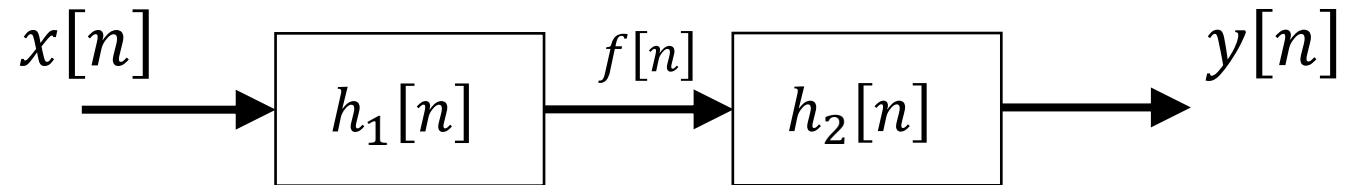
$$x[n] = n; 0 \leq n \leq 5$$

- Calcule a saída  $y[n]$  do sistema



# Exercício

- Um determinado sistema é formado por dois subsistemas. Cada um possui sua própria resposta ao impulso ( $h_1[n]$  e  $h_2[n]$ )



- Passar o sinal de entrada pelos dois subsistemas é o mesmo que convolui-lo com a convolução das duas respostas ao impulso, ou seja:

$$y[n] = \sum_{k=-\infty}^{\infty} x[k] [h_1[n-k] * h_2[n-k]]$$

- Sendo  $h_1[n] = -2\delta[n] + \delta[n-1] + 2\delta[n-2]$  e  $h_2[n] = n/2, 0 \leq n \leq 4$ , encontre a resposta ao impulso do sistema completo e convolua o sinal  $x[n] = u[n] - u[n-3]$