

CST 370 – Spring A 2020 Homework 2

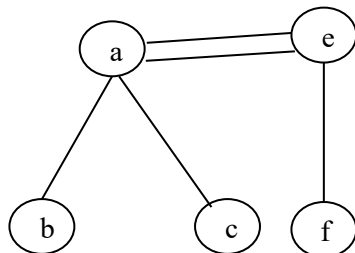
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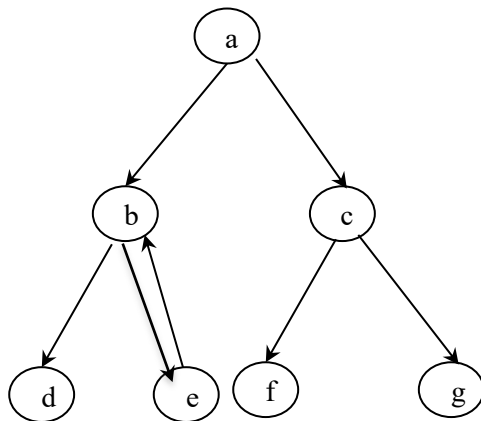
How to turn in?

- Write your answer to the questions 1 to 7, and submit it on the iLearn. You can submit the file in PDF format. Don't forget to write your name and class ID number at the beginning of the file.
- For Questions 8 and 9, you should submit your C++ source files on the iLearn.
- Thus, you have to submit three files (one PDF file and two C++ source file) on the iLearn.
- Note that the due date is 11:55(PM). This is the iLearn's timestamp, not your submission time. Since there could be a long delay between your computer and iLearn, you should **submit early**.

1. (5 points) (a) Based on our textbook's definition, is this a graph? (True/False) Explain to support your answer.



(b) Based on our textbook's definition, is this a graph? (True/False) Explain to support your answer

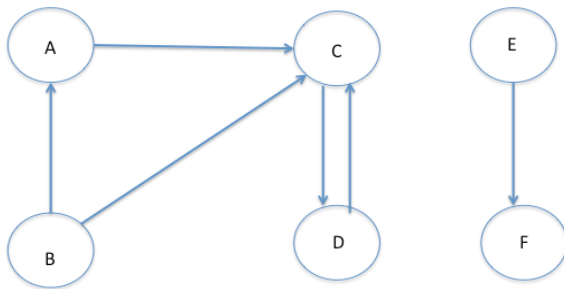


2. (10 points) Assume that you should search a number in a list of n numbers. How can you take advantage of the fact that **the list is known to be sorted**? Give separate answers for the following two cases.

(a) A list represented in an array.

(b) A list represented in a linked list.

3. (5 points) Represent the following graph in the adjacency list as you learned in the class. Note that there are **six vertices** (= A, B, C, D, E, and F) in the graph.



4. (5 points) Assume a binary tree with six vertices such as v_1 , v_2 , v_3 , v_4 , v_5 , and v_6 . Determine the maximum number of edges possible in the tree.

5. (5 points) (a) If your program takes $n \cdot \log n$ time and your classmate's program takes n^2 time, whose program is faster? Pick one between "You" and "Your Classmate".

(b) If your program takes $\log n$ time and your classmate's program takes *constant* time, whose program is faster? Pick one between "You" and "Your Classmate".

6. (10 points) Consider the following algorithm.

Algorithm *Compute* ($A[0..n-1]$)

1. $\text{num1} \leftarrow A[0]$;

2. $\text{num2} \leftarrow A[0]$

3. $i \leftarrow 1$

```

4. while i < n do
5.   if A[i] < num1
6.     num1 ← A[i];
7.   if A[i] > num2
8.     num2 ← A[i];
9.   i ← i + 1
10. return (num2 – num1);

```

- (a) Present the basic operation of the algorithm. When you present the basic operation, you should indicate the line number of the basic operation clearly.
- (b) Present the time complexity category of the algorithm among the eight most popular time complexity categories we covered in the lecture.

7. (10 points) Consider the following algorithm

```

1. Algorithm Mystery(n)
2. // Input: A nonnegative integer n
3. S ← 0
4. for i ← 1 to n do
5.   k ← i * i
6.   S ← S + k
7. return S

```

- (a) What does this algorithm compute?
- (b) What is its basic operation?
- (c) Present the time complexity category of the algorithm among the eight most popular time complexity categories we covered in the lecture.

8. (25 points) Write a C++ program called **sieve.cpp** that implements the **sieve of Eratosthenes** algorithm in our textbook (page 6 ~ 7). The following video will help your understanding of the algorithm:

<https://youtu.be/klcIklsWzrY>

For the assignment, you can assume that the user always enters a positive integer which is bigger than 1. For the program, you have to use a **dynamic memory** to create array(s) to store data. For details on the dynamic memory, read <http://www.cplusplus.com/doc/tutorial/dynamic/>

For the assignment, you **have to write your program based on the pseudocode in our textbook**. If you use other algorithm or library, you will get penalized.

Grading guide and test cases for the sieve.cpp:

- Missing head comment elements (= Title, Abstract, ID, Name, and Date).
- Compilation failed → It will be very serious.
- Your program should use the dynamic memory for array(s).
- Test case 1: Input number 2 → 2
- Test case 2: Input number 10 → 2, 3, 5, 7

- Test case 3: Input number 25 → 2, 3, 5, 7, 11, 13, 17, 19, 23
- Test case 4: Input number 101 → 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 101

9. (25 points) Write a C++ program “palindrome.cpp” that reads a string of characters from user and determines if the string is a palindrome or not. For the program, you should store each character of the string in an array (use **dynamic memory** to create array(s)) and follow the algorithm described in the lecture.

Palindrome is a string that reads the same from both the beginning and the end. Here are sample test cases:

- (1) Input string 1: racecar
Output: Yes, it's a palindrome
- (2) Input string 2: abcdefghijihgfedcba
Output: Yes, it's a palindrome
- (3) Input string 3: CSUMB
Output: No, it's not a palindrome