

1. Derive the Equation for $\nabla_b J(w, b)$.

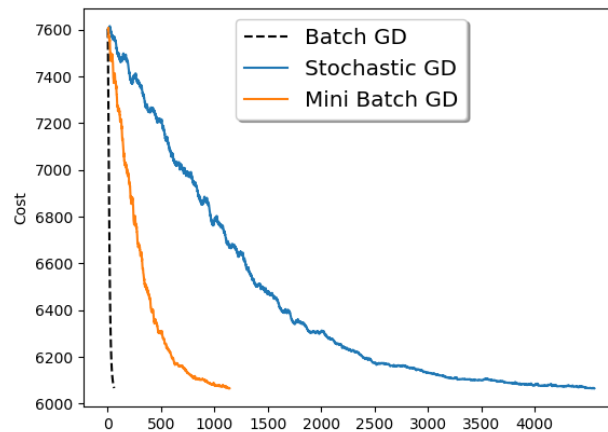
Solution:

$$\nabla_b J(w, b) = c \sum_{i=1}^m \frac{\partial L(x^{(i)}, y^{(i)})}{\partial b};$$

$$\text{here } \frac{\partial L(x^{(i)}, y^{(i)})}{\partial b} = \begin{cases} 0 & ; \text{if } y^{(i)}(X^{(i)}w + b) \geq 1 \\ -y^{(i)} & ; \text{otherwise} \end{cases}$$

2. Plot of $J_k(w, b)$ vs. the number of iterations (k).

Solution:



3. Convergence times in seconds.

Solution:

Plot=True	Plot=False
BGD convergence time: 0.028690814971923828	BGD convergence time: 0.02623438835144043
SGD convergence time: 0.8405246734619141	SGD convergence time: 0.4165914058685303
MBGD convergence time: 0.3373892307281494	MBGD convergence time: 0.18897056579589844

In both of the above cases, final cost = 6065 (approx.)

4. Source code is attached in zip file.