

# Homework 5

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## Questions

1. In the following, we have five data points and three cluster centers:

```
p1<- c(0,0,6,2,5)
p2<- c(0,6,6,2,1)
p3<- c(2,4,6,0,3)
p4<- c(1,3,7,0,6)
p5<- c(3,3,4,0,0)
c1<- c(0,0,1,1,1)
c2<- c(0,1,1,1,0)
c3<- c(1,1,1,0,0)
kable(rbind(p1, p2, p3, p4, p5), caption = "Points")
```

Table 1: Points

p1	0	0	6	2	5
p2	0	6	6	2	1
p3	2	4	6	0	3
p4	1	3	7	0	6
p5	3	3	4	0	0

```
kable(rbind(c1, c2, c3), caption = "Clusters")
```

Table 2: Clusters

c1	0	0	1	1	1
c2	0	1	1	1	0
c3	1	1	1	0	0

- a. Please for each data point find the closest cluster center, based on Euclidean distance.

```
# Cluster 1
sqrt(sum((p1-c1)^2))
```

```
## [1] 6.480741
```

```
# Cluster 2
sqrt(sum((p1-c2)^2))
```

```
## [1] 7.211103
```

```
# Cluster 3
sqrt(sum((p1-c3)^2))
```

```
## [1] 7.483315
```

```
# Result: Point 1 will be grouped with Cluster 1
```

```
# Cluster 1
sqrt(sum((p2-c1)^2))
```

```
## [1] 7.874008
```

```
# Cluster 2
sqrt(sum((p2-c2)^2))
```

```
## [1] 7.211103
```

```
# Cluster 3
sqrt(sum((p2-c3)^2))
```

```
## [1] 7.483315
```

```
# Result: Point 2 will be grouped with Cluster 2
```

```
# Cluster 1
sqrt(sum((p3-c1)^2))
```

```
## [1] 7.071068
```

```
# Cluster 2
sqrt(sum((p3-c2)^2))
```

```
## [1] 6.928203
```

```
# Cluster 3
sqrt(sum((p3-c3)^2))
```

```
## [1] 6.63325
```

```
# Result: Point 3 will be grouped with Cluster 3
```

```
# Cluster 1
sqrt(sum((p4-c1)^2))
```

```
## [1] 8.485281
```

```
# Cluster 2
sqrt(sum((p4-c2)^2))
```

```
## [1] 8.831761
```

```
# Cluster 3
sqrt(sum((p4-c3)^2))
```

```
## [1] 8.717798
```

```
# Result: Point 4 will be grouped with Cluster 1
```

```
# Cluster 1
sqrt(sum((p5-c1)^2))
```

```
## [1] 5.385165
```

```
# Cluster 2
sqrt(sum((p5-c2)^2))
```

```
## [1] 4.795832
```

```
# Cluster 3
sqrt(sum((p5-c3)^2))
```

```
## [1] 4.123106
```

```
# Result: Point 5 will be grouped with Cluster 3
```

b. Please for each cluster center find the associated points, based on the above results.

```
Q1<- data.frame(point = c(1,2,3,4,5), "grouped with cluster" = c(1,2,3,1,3))
kable(Q1)
```

point	grouped.with.cluster
1	1
2	2
3	3
4	1
5	3

c. Please for each cluster compute the new center, based on the above results.

```

# Cluster 1 -> Includes point 1 and point 4
newc1<- (c1+p1+p4)/3

# Cluster 2 -> Includes point 2
newc2<- (c2+p2)/2

# Cluster 3 -> Includes point 3 and point 5
newc3<- (c3+p3+p5)/3

kable(data.frame(cluster = c(1,2,3), coordinates = unname(rbind(newc1, newc2, newc3))))

```

cluster	coordinates.1	coordinates.2	coordinates.3	coordinates.4	coordinates.5
1	0.3333333	1.000000	4.666667	1.0	4.0
2	0.0000000	3.500000	3.500000	1.5	0.5
3	2.0000000	2.666667	3.666667	0.0	1.0