



Softmax Classifier

Lecture 06

Softmax function

Logistic Classifier

$$WX = \hat{Y}$$



$$y \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix}$$

SOFTMAX

$$S(yi) = \frac{e^{yi}}{\sum_i e^{yi}}$$

$p = 0.7$ **A**

$p = 0.2$ **B**

$p = 0.1$ **C**

1.0



PROBABILITIES

```
tf.matmul(X,W)+b
```



$$WX = \hat{Y}$$



$$y \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix}$$

$$\hat{Y}$$

logits

SOFTMAX

$$S(yi) = \frac{e^{yi}}{\sum_i e^{yi}}$$

$p = 0.7$

$p = 0.2$

$p = 0.1$

PROBABILITIES

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

Cost function: cross entropy

Cost (Loss)

$$L = \frac{1}{N} \sum_i D(S(WX_i + b), L_i)$$

TRAINING SET

$$D(S, L) = - \sum_i L_i \log(S_i)$$

hypothesis

Cross entropy cost/loss

reduce_sum(, axis=1) axis=1 -> row에서 합계를 계산, axis=0 -> column에서 합계를 계산

```
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
```

```
optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
```

```
import tensorflow as tf
x_data = [[1, 2, 1, 1], [2, 1, 3, 2], [3, 1, 3, 4], [4, 1, 5, 5], [1, 7, 5, 5], [1, 2, 5, 6], [1, 6, 6, 6], [1, 7, 7, 7]]
y_data = [[0, 0, 1], [0, 0, 1], [0, 0, 1], [0, 1, 0], [0, 1, 0], [0, 1, 0], [1, 0, 0], [1, 0, 0]] # 0,1,2
```

```
X = tf.placeholder("float", [None, 4]) # row : N , column : 4
Y = tf.placeholder("float", [None, 3]) # row : N , column : 3
nb_classes = 3 # column of Y
```

```
W = tf.Variable(tf.random_normal([4, nb_classes]), name='weight') # row : 4 , column : 3
b = tf.Variable(tf.random_normal([nb_classes]), name='bias')
```

```
# tf.nn.softmax computes softmax activations
# softmax = exp(logits) / reduce_sum(exp(logits), dim)
hypothesis = tf.nn.softmax(tf.matmul(X, W) + b)
```

```
# Cross entropy cost/loss (reduce_sum( , axis=1 ) axis=1 -> row에서 합계를 계산, axis=0 -> column에서 합계를 계산)
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
```

```
# optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1)
# train = optimizer.minimize(cost) -> 실행 : sess.run(train)으로 실행해야 함
optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
```

```
# Launch graph
with tf.Session() as sess:
    sess.run(tf.global_variables_initializer())
    for i in range(len(x_data)):
        print(i+1, "번째 x_data", x_data[i], "=> y_data", y_data[i], end="")
        if (y_data[i] == [1, 0, 0]):
            print(" : 0")
        elif (y_data[i] == [0, 1, 0]):
            print(" : 1")
        elif (y_data[i] == [0, 0, 1]):
            print(" : 2")
```

$$D(S, L) = - \sum_i L_i \log(S_i)$$

nb_classes 'ONE-HOT'
ENCODING

1.0
0.0
0.0

1 번째 x_data [1, 2, 1, 1] ==> y_data [0, 0, 1] : 2
 2 번째 x_data [2, 1, 3, 2] ==> y_data [0, 0, 1] : 2
 3 번째 x_data [3, 1, 3, 4] ==> y_data [0, 0, 1] : 2
 4 번째 x_data [4, 1, 5, 5] ==> y_data [0, 1, 0] : 1
 5 번째 x_data [1, 7, 5, 5] ==> y_data [0, 1, 0] : 1
 6 번째 x_data [1, 2, 5, 6] ==> y_data [0, 1, 0] : 1
 7 번째 x_data [1, 6, 6, 6] ==> y_data [1, 0, 0] : 0
 8 번째 x_data [1, 7, 7, 7] ==> y_data [1, 0, 0] : 0

```
for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data}) # 실행 : sess.run(optimizer) 으로 실행해야 함
    if step % 200 == 0:
        cost_v, W_v = sess.run([cost,W],feed_dict={X: x_data, Y: y_data})
        print('='*20, step, "번째 Learning", '='*20)
        print("cost : ", cost_v, "\nW : ", W_v)
```

Weight → row : 4 , column : 3



```
===== 0 번째 Learning =====
cost : 3.6451883
W : [[ 0.7168987 -0.23286213  0.28869355]
      [ 1.4674631  1.4823829  1.052482 ]
      [-1.6186061  0.01691242 -0.8614841 ]
      [-1.0679966 -0.4912663  0.04156154]]
===== 200 번째 Learning =====
cost : 0.596512
W : [[-1.0872966  0.28811795  1.5719084 ]
      [ 1.3888952  1.0571648  1.5562694 ]
      [-0.49595264 -0.51861405 -1.4486113 ]
      [-0.44033748 -0.11886172 -0.95850164]]
===== 400 번째 Learning =====
cost : 0.48940927
W : [[-1.6811438  0.43864465  2.0152295 ]
      [ 1.2551967  1.0893495  1.6577837 ]
      [ 0.06578756 -0.7553408 -1.7736238 ]
      [-0.6009978  0.14388406 -1.0605853 ]]
.
.
.
```

```
.
.
.
===== 1800 번째 Learning =====
cost : 0.1746932
W : [[-3.7331817  0.9934499  3.5124629 ]
      [ 0.81080514  1.1602981  2.0312307 ]
      [ 2.6173372 -1.5376157 -3.542897 ]
      [-1.6726953  0.9069222 -0.7519227 ]]
===== 2000 번째 Learning =====
cost : 0.16201103
W : [[-3.9105399  1.0405984  3.6426697]
      [ 0.7697886  1.1618105  2.070735 ]
      [ 2.857559 -1.6031579 -3.7175748]
      [-1.7902993  0.9852507 -0.7126456]]
```

```
# Testing & One-hot encoding
# argmax (a, 0)에서 0의 의미는 같은 열에서 max value 인덱스를 출력 (인덱스는 0 부터 시작)
# argmax (a, 1)에서 1의 의미는 같은 행에서 max value 인덱스를 출력 (인덱스는 0 부터 시작)
print("\n● Testing & One-hot encoding & argmax")

a = sess.run(hypothesis, feed_dict={X: [[1, 11, 7, 9]]})
print("Test data X : [1, 11, 7, 9] --> ", end = "")
print("hypothesis :",a, "-->", sess.run(tf.argmax(a, 1)))
print('='*100)

b = sess.run(hypothesis, feed_dict={X: [[1, 3, 4, 3]]})
print("Test data X : 1, 3, 4, 3] --> ", end = "")
print("hypothesis :",b, "-->", sess.run(tf.argmax(b, 1)))
print('='*100)

c = sess.run(hypothesis, feed_dict={X: [[1, 1, 0, 1]]})
print("Test data X : [1, 1, 0, 1] --> ", end = "")
print("hypothesis :",c, "-->", sess.run(tf.argmax(c, 1)))
print('='*100)

all = sess.run(hypothesis, feed_dict={ X: [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]})
print("Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]] ")
print("hypothesis \n",all, "-->", sess.run(tf.argmax(all, 1)))
print('='*100)
```



● Testing & One-hot encoding & argmax

Test data X : [1, 11, 7, 9] --> hypothesis : [[8.581670e-03 9.914078e-01 1.050219e-05]] --> [1]

=====

Test data X : 1, 3, 4, 3] --> hypothesis : [[0.8252531 0.15725392 0.01749295]] --> [0]

=====

Test data X : [1, 1, 0, 1] --> hypothesis : [[2.0768354e-08 3.9369191e-04 9.9960631e-01]] --> [2]

=====

Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]

hypothesis

[[8.5816700e-03 9.9140781e-01 1.0502190e-05]

[8.2525313e-01 1.5725392e-01 1.7492952e-02]

[2.0768352e-08 3.9369191e-04 9.9960631e-01]] --> [1 0 2]

=====

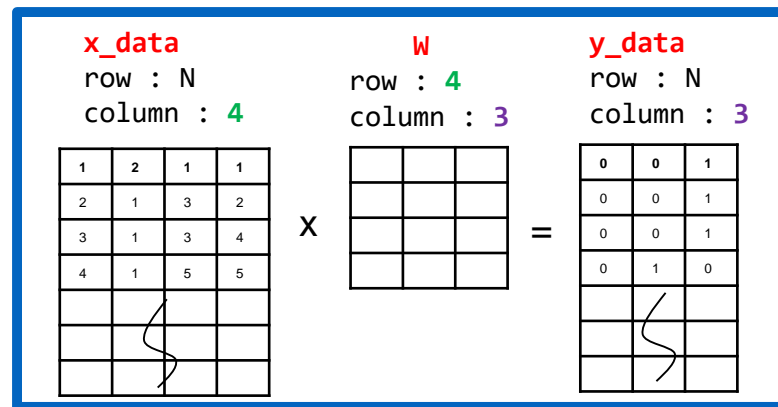
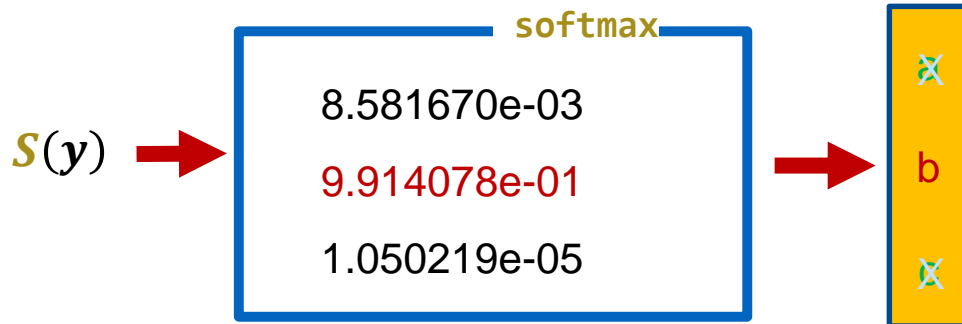
Test & one-hot encoding

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

```
a = sess.run(hypothesis, feed_dict={X: [[1, 11, 7, 9]]})
print("Test data X : [1, 11, 7, 9] --> ", end = "")
print("hypothesis :", a, "-->", sess.run(tf.argmax(a, 1)))
print('='*100)
```



```
Test data X : [1, 11, 7, 9] --> hypothesis : [[8.581670e-03 9.914078e-01 1.050219e-05]] --> [1]
```



Test & one-hot encoding

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

```
all = sess.run(hypothesis, feed_dict={ X: [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]})  
print("Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]] ")  
print("hypothesis \n",all, "-->", sess.run(tf.argmax(all, 1)))  
print('='*100)
```



```
Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]
```

```
hypothesis
```

```
[[8.5816700e-03 9.9140781e-01 1.0502190e-05]
```

```
[8.2525313e-01 1.5725392e-01 1.7492952e-02]
```


































```
[2.0768352e-08 3.9369191e-04 9.9960631e-01]] --> [1 0 2]
```

```
=====
```

Fancy softmax Classifier

- `one_hot`
- `reshape`
- `cross_entropy`

Animal classification

Birds	Insect	Fishes	Amphibians	Reptiles	Mammals
					
					
					
					
					
					
					

x_data

1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3
1	0	0	1	0	0	1	1	1	1	0	0	4	0	0	1	0
1	0	0	1	0	0	1	1	1	1	0	0	4	1	0	1	0
1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0
1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0
1	0	0	1	0	0	0	1	1	1	0	0	4	1	1	1	0
0	0	1	0	0	1	0	1	1	0	0	1	0	1	1	0	3
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3
1	0	0	1	0	0	0	1	1	1	0	0	4	0	1	0	0
1	0	0	1	0	0	1	1	1	1	0	0	4	1	0	1	0
0	1	1	0	1	0	0	0	1	1	0	0	2	1	1	0	1
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3
0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	6
0	0	1	0	0	1	1	0	0	0	0	0	4	0	0	0	6
0	0	1	0	0	1	1	0	0	0	0	0	6	0	0	0	6
0	1	1	0	1	0	1	0	1	1	0	0	2	1	0	0	1
1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0

0~6

Predicting animal type based on various features

```
xy = np.loadtxt('g:\\data-04-zoo.csv', delimiter=',', dtype=np.float32)
```

```
x_data = xy[:, 0:-1]
```

```
y_data = xy[:, [-1]]
```

tf.one_hot and reshape

x_data														y_data			
1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	0
1	0	0	1	0	0	1	1	1	1	0	0	4	0	0	1	0	0
1	0	0	1	0	0	1	1	1	1	0	0	4	1	0	1	0	0
1	0	0	1	0	0	0	1	1	1	1	0	4	1	0	1	0	0
1	0	0	1	0	0	0	1	1	1	1	0	4	1	1	1	0	0
0	0	1	0	0	1	0	1	1	0	0	1	0	1	1	0	3	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	0
1	0	0	1	0	0	0	1	1	1	1	0	4	0	1	0	0	0
1	0	0	1	0	0	1	1	1	1	1	0	4	1	0	1	0	0
0	1	1	0	1	0	0	0	1	1	1	0	2	1	1	0	1	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	0
0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	6	0
0	0	1	0	0	1	1	0	0	0	0	0	4	0	0	0	6	0
0	0	1	0	0	1	1	0	0	0	0	0	6	0	0	0	6	0
0	1	1	0	1	0	1	0	1	1	0	0	2	1	0	0	1	0
1	0	0	1	0	0	0	1	1	1	1	0	4	1	0	1	0	0

tf.one_hot :

If the input indices is rank **N**,
the output will have rank **N+1**.

ex) input : `[[0][3]]`

→ output : `[[[1000000]][[0001000]]]`

`nb_classes = 7`

`Y = tf.placeholder(tf.int32, [None, 1])` # None row, 1 column (0 ~ 6) -> shape=(?, 1)

`Y_one_hot = tf.one_hot(Y, nb_classes)` # Y는 0부터 시작함, one hot shape=(?, 1, 7)

`Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes])` # shape=(?, 7)

tf.one_hot and reshape

x_data

y_data

0~6

nb_classes = 7

Y = tf.placeholder(tf.int32, [None, 1]) # 0~6 사이의 값을 넣기 위해 shape=(?, 1) 설정

Y_one_hot = tf.one_hot(Y, nb_classes) # one hot shape=(?, 1, 7)
 0~6 7

0 3 Y_one_hot
 [[1000000] [0001000]]



Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes]) # shape=(?, 7)
 7

[[1000000] [0001000]]

Y_one_hot	Y
1000000	0
0100000	1
0010000	2
0001000	3
0000100	4
0000010	5
0000001	6

1	0
0	3
1	0
1	0
1	0
1	0
0	3
0	3
0	0
1	0
0	1
0	3
0	6
0	6
0	1
1	0

tf.one_hot and reshape

```
import numpy as np
x = np.arange(12)
print(x)

[ 0  1  2  3  4  5  6  7  8  9 10 11]

x = x.reshape(3, 4)
x.shape

(3, 4)

print(x)

[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

```
x.reshape(-1, 1)
array([[0],
 [ 1],
 [ 2],
 [ 3],
 [ 4],
 [ 5],
 [ 6],
 [ 7],
 [ 8],
 [ 9],
[10],
[11]])
```

```
x.reshape(-1, 2)
array([[ 0,  1],
 [ 2,  3],
 [ 4,  5],
 [ 6,  7],
 [ 8,  9],
[10, 11]])
```

```
x.reshape(-1, 3)
array([[ 0,  1,  2],
 [ 3,  4,  5],
 [ 6,  7,  8],
 [ 9, 10, 11]])
```

softmax_cross_entropy_with_logits

SCORE →

```
logit = tf.matmul(X, W) + b  
hypothesis = tf.nn.softmax(logit)
```

1

Cross entropy cost/loss

```
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
```

one-hot

2

Cross entropy cost/loss

```
cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logit,  
                                                  labels=Y_one_hot)
```

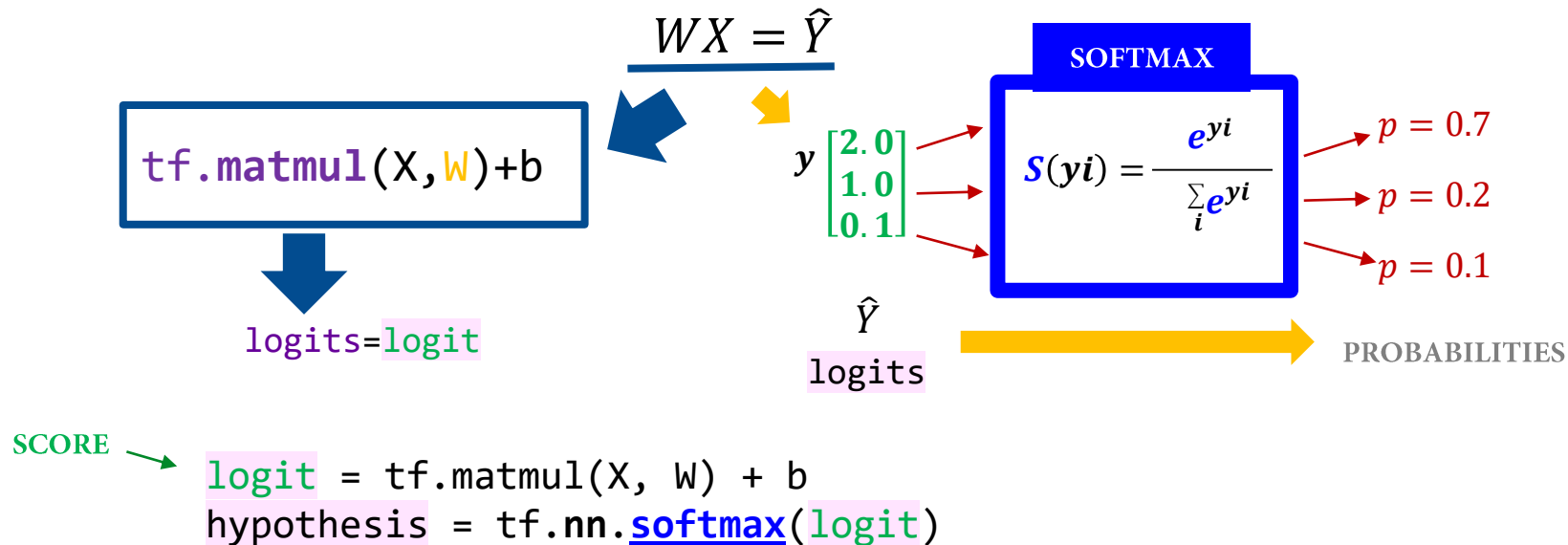
```
cost = tf.reduce_mean(cost_i)
```

Y의 label

=

softmax_cross_entropy_with_logits

hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)




```

import tensorflow as tf
import numpy as np
# Predicting animal type based on various features
xy = np.loadtxt('g:\\data-04-zoo.csv', delimiter=',', dtype=np.float32) # column : 17
x_data = xy[:, 0:-1] # column : 16
y_data = xy[:, [-1]] # column : 1

nb_classes = 7 # Y의 종류가 총 7개로 구성되어 있음

X = tf.placeholder(tf.float32, [None, 16]) # row : None , column : 16
Y = tf.placeholder(tf.int32, [None, 1]) # row : None , column : 1 ( 0, 1, 2, 3, 4, 5, 6 (총 7개 종류로 구성))

Y_one_hot = tf.one_hot(Y, nb_classes) # one hot
Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes]) # ex) 1000000... structure

W = tf.Variable(tf.random_normal([16, nb_classes]), name='weight') # row : 16 , column : 7
b = tf.Variable(tf.random_normal([nb_classes]), name='bias') # column : 7

# tf.nn.softmax computes softmax activations
# softmax = exp(logits) / reduce_sum(exp(logits), dim)
logit = tf.matmul(X, W) + b
hypothesis = tf.nn.softmax(logit)

# Cross entropy cost/Loss
cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logit, labels=Y_one_hot)
cost = tf.reduce_mean(cost_i)

optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)

# tf.argmax(A , flag) : matrix A에서 flag가 0이면 column 기준, 1이면 row 기준으로 큰 값의 index를 반환함 (index는 0부터 시작..)
prediction = tf.argmax(hypothesis, 1) # flag가 1이므로 row 기준으로 큰 값의 index를 반환함
correct_prediction = tf.equal(prediction, tf.argmax(Y_one_hot, 1)) # flag가 1이므로 row 기준으로 큰 값의 index를 반환함
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))

```

tf.argmax
큰 값이 있는 곳의 **index**를 반환함

```

# Launch graph
with tf.Session() as sess:
    sess.run(tf.global_variables_initializer())

# Learning
for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data})
    if step % 100 == 0:
        loss, acc = sess.run([cost, accuracy], feed_dict={X: x_data, Y: y_data})
        print("Step: {:5}\tCost: {:.3f}\tAccuracy: {:.2%}".format(step, loss, acc) )

# Let's see if we can predict
pred = sess.run(prediction, feed_dict={X: x_data})
line = len(x_data)
i = 0
print ("\n", "="*30, line, "개 Data analysis ", "="*20)
for p, y in zip(pred, y_data.flatten()): # y_data.flatten() 다차원 배열을 1차원 배열로 변형시킴
    i = i+1
    print(i, "번째 : Is the prediction equal to the true value? => [{}] : Prediction: {} True Y: {}".format(p == int(y), p, int(y)))

# Testing & One-hot encoding
test_x = [[0,0,1,0,0,1,0,1,1,0,0,1,0,1,0,0]]
print("\n• Testing & One-hot encoding & argmax")
print("Test data X :", test_x )
print("prediction :", sess.run(prediction, feed_dict={X: test_x}))

```

Learning

```
for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data})
    if step % 100 == 0:
        loss, acc = sess.run([cost, accuracy], feed_dict={X: x_data, Y: y_data})
        print("Step: {:5}\tCost: {:.3f}\tAccuracy: {:.2%}".format(step, loss, acc ) )
```



Step: 0	Cost: 4.624	Accuracy: 9.90%
Step: 100	Cost: 0.680	Accuracy: 78.22%
Step: 200	Cost: 0.433	Accuracy: 85.15%
Step: 300	Cost: 0.313	Accuracy: 87.13%
Step: 400	Cost: 0.237	Accuracy: 91.09%
Step: 500	Cost: 0.187	Accuracy: 97.03%
Step: 600	Cost: 0.153	Accuracy: 99.01%
Step: 700	Cost: 0.129	Accuracy: 100.00%
Step: 800	Cost: 0.112	Accuracy: 100.00%
Step: 900	Cost: 0.099	Accuracy: 100.00%
Step: 1000	Cost: 0.089	Accuracy: 100.00%
Step: 1100	Cost: 0.080	Accuracy: 100.00%
Step: 1200	Cost: 0.074	Accuracy: 100.00%
Step: 1300	Cost: 0.068	Accuracy: 100.00%
Step: 1400	Cost: 0.063	Accuracy: 100.00%
Step: 1500	Cost: 0.059	Accuracy: 100.00%
Step: 1600	Cost: 0.055	Accuracy: 100.00%
Step: 1700	Cost: 0.052	Accuracy: 100.00%
Step: 1800	Cost: 0.050	Accuracy: 100.00%
Step: 1900	Cost: 0.047	Accuracy: 100.00%
Step: 2000	Cost: 0.045	Accuracy: 100.00%

Let's see if we can predict

```
pred = sess.run(prediction, feed_dict={X: x_data})
```

```
line = len(x_data)
```

```
i = 0
```

```
print ("\n", "="*30, line, "개 Data analysis ", "="*20)
```

```
for p, y in zip(pred, y_data.flatten()): # y_data.flatten() 다차원 배열을 1차원 배열로 변형시킴
```

```
i = i+1
```

```
print(i, "번째 : Is the prediction equal to the true value? => [{}]: Prediction: {} True Y: {}".format(p == int(y), p, int(y)))
```



===== 101 개 Data analysis =====

1 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

2 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

3 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3

4 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

5 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

6 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

7 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

8 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3

9 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3

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97 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

98 번째 : Is the prediction equal to the true value? => [True] : Prediction: 5 True Y: 5

99 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0

100 번째 : Is the prediction equal to the true value? => [True] : Prediction: 6 True Y: 6

101 번째 : Is the prediction equal to the true value? => [True] : Prediction: 1 True Y: 1

```
test_x = [[0,0,1,0,0,1,0,1,1,0,0,1,0,1,0,0]]  
print("\n● Testing & One-hot encoding & argmax")  
print("Test data X :", test_x )  
print("prediction :", sess.run(prediction, feed_dict={X: test_x}))
```



- Testing & One-hot encoding & argmax

Test data X : [[0, 0, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0]]

prediction : [3]