

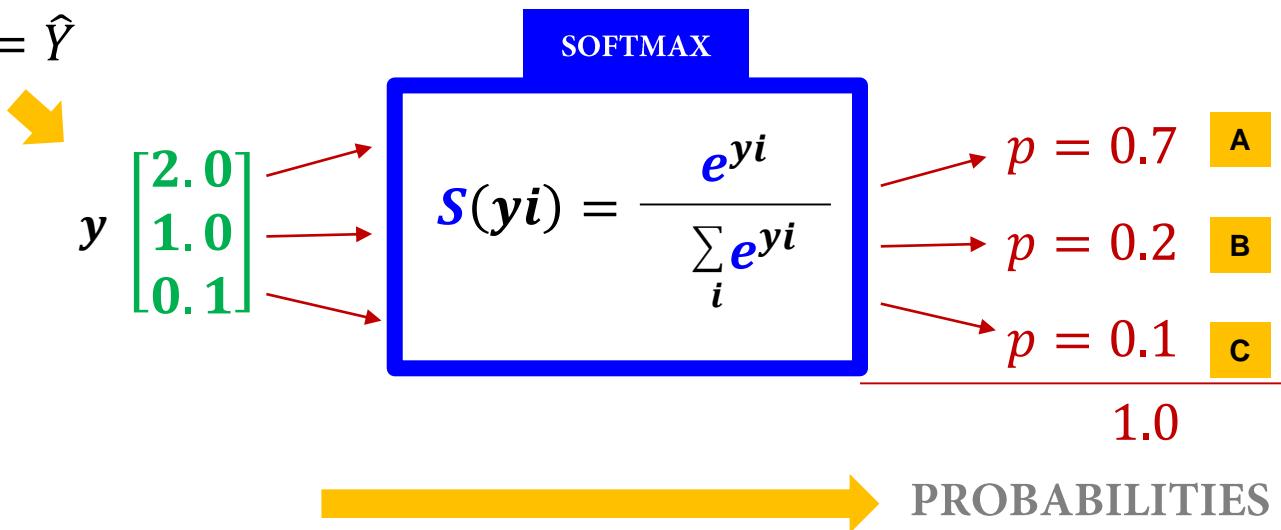
Softmax Classifier

Lecture 06

Softmax function

Logistic Classifier

$$WX = \hat{Y}$$



```
tf.matmul(X,W)+b
```

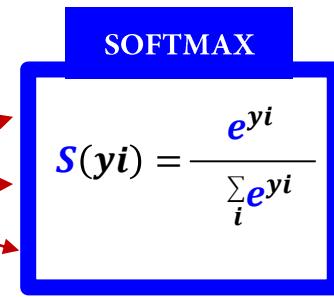


$$WX = \hat{Y}$$



$$y \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix}$$

$$\hat{Y} \text{ logits}$$



$$\begin{aligned} p &= 0.7 \\ p &= 0.2 \\ p &= 0.1 \end{aligned}$$

PROBABILITIES

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

Cost function: cross entropy

Cost (Loss)

$$L = \frac{1}{N} \sum_i D(S(WX_i + b), L_i)$$

TRAINING SET

$$D(S, L) = - \sum_i L_i \log(S_i)$$

hypothesis

```
# Cross entropy cost/loss
# reduce_sum( , axis=1 ) axis=1 -> row에서 합계를 계산, axis=0 -> column에서 합계를 계산
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
```

```
optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
```

```

import tensorflow as tf
x_data = [[1, 2, 1, 1], [2, 1, 3, 2], [3, 1, 3, 4], [4, 1, 5, 5], [1, 7, 5, 5], [1, 2, 5, 6], [1, 6, 6, 6], [1, 7, 7, 7]]
y_data = [[0, 0, 1], [0, 0, 1], [0, 0, 1], [0, 1, 0], [0, 1, 0], [0, 1, 0], [1, 0, 0], [1, 0, 0]] # 0,1,2

```

2 2 2 1 1 1 0 0

```

X = tf.placeholder("float", [None, 4]) # row : N , column : 4
Y = tf.placeholder("float", [None, 3]) # row : N , column : 3
nb_classes = 3 # column of Y

W = tf.Variable(tf.random_normal([4, nb_classes]), name='weight') # row : 4 , column : 3
b = tf.Variable(tf.random_normal([nb_classes]), name='bias')

# tf.nn.softmax computes softmax activations
# softmax = exp(logits) / reduce_sum(exp(logits), dim)
hypothesis = tf.nn.softmax(tf.matmul(X, W) + b)

```

```

# Cross entropy cost/Loss (reduce_mean( , axis=1 ) axis=1 -> row에서 합계를 계산, axis=0 -> column에서 합계를 계산)
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))

```

```

# optimizer = tf.train.GradientDescentOptimizer(Learning_rate=0.1)
# train = optimizer.minimize(cost) -> 실행 : sess.run(train)으로 실행해야 함
optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)

```

```

# Launch graph
with tf.Session() as sess:
    sess.run(tf.global_variables_initializer())
    for i in range(len(x_data)):
        print(i+1, "번째 x_data", x_data[i], "==> y_data", y_data[i], end="")
        if (y_data[i] == [1, 0, 0]):
            print(" : 0")
        elif (y_data[i] == [0, 1, 0]):
            print(" : 1")
        elif (y_data[i] == [0, 0, 1]):
            print(" : 2")

```

ex06_1.ipynb

(1/3)

nb_classes
'ONE-HOT'
ENCODING

1.0
0.0
0.0

$$D(S, L) = -\sum_i L_i \log(S_i)$$



1 번째 x_data [1, 2, 1, 1] ==> y_data [0, 0, 1] : 2
 2 번째 x_data [2, 1, 3, 2] ==> y_data [0, 0, 1] : 2
 3 번째 x_data [3, 1, 3, 4] ==> y_data [0, 0, 1] : 2
 4 번째 x_data [4, 1, 5, 5] ==> y_data [0, 1, 0] : 1
 5 번째 x_data [1, 7, 5, 5] ==> y_data [0, 1, 0] : 1
 6 번째 x_data [1, 2, 5, 6] ==> y_data [0, 1, 0] : 1
 7 번째 x_data [1, 6, 6, 6] ==> y_data [1, 0, 0] : 0
 8 번째 x_data [1, 7, 7, 7] ==> y_data [1, 0, 0] : 0

```

for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data}) # 실행 : sess.run(optimizer) 으로 실행해야 함
    if step % 200 == 0:
        cost_v, W_v = sess.run([cost,W],feed_dict={X: x_data, Y: y_data})
        print('*20, step, "번째 Learning", '*20)
        print("cost : ", cost_v, "\nW : ", W_v)

```



Weight → row : 4 , column : 3

```

===== 0 번째 Learning =====
cost : 3.6451883
W: [[ 0.7168987 -0.23286213  0.28869355]
 [ 1.4674631  1.4823829  1.052482 ]
 [-1.6186061  0.01691242 -0.8614841 ]
 [-1.0679966 -0.4912663  0.04156154]]
===== 200 번째 Learning =====
cost : 0.596512
W: [[-1.0872966  0.28811795  1.5719084 ]
 [ 1.3888952  1.0571648  1.5562694 ]
 [-0.49595264 -0.51861405 -1.4486113 ]
 [-0.44033748 -0.11886172 -0.95850164]]
===== 400 번째 Learning =====
cost : 0.48940927
W: [[-1.6811438  0.43864465  2.0152295 ]
 [ 1.2551967  1.0893495  1.6577837 ]
 [ 0.06578756 -0.7553408 -1.7736238 ]
 [-0.6009978  0.14388406 -1.0605853 ]]
.
.
```

```

.
.
.
===== 1800 번째 Learning =====
cost : 0.1746932
W: [[-3.7331817  0.9934499  3.5124629 ]
 [ 0.81080514  1.1602981  2.0312307 ]
 [ 2.6173372 -1.5376157 -3.542897 ]
 [-1.6726953  0.9069222 -0.7519227 ]]
===== 2000 번째 Learning =====
cost : 0.16201103
W: [[-3.9105399  1.0405984  3.6426697]
 [ 0.7697886  1.1618105  2.070735 ]
 [ 2.857559 -1.6031579 -3.7175748]
 [-1.7902993  0.9852507 -0.7126456]]
```

```
# Testing & One-hot encoding
# argmax (a, 0) 에서 0의 의미는 같은 열에서 max value 인덱스를 출력 (인덱스는 0 부터 시작)
# argmax (a, 1) 에서 1의 의미는 같은 행에서 max value 인덱스를 출력 (인덱스는 0 부터 시작)
print("\n• Testing & One-hot encoding & argmax")

a = sess.run(hypothesis, feed_dict={X: [[1, 11, 7, 9]]})
print("Test data X : [1, 11, 7, 9] --> ", end = "")
print("hypothesis :", a, "-->", sess.run(tf.argmax(a, 1)))
print('=*100)

b = sess.run(hypothesis, feed_dict={X: [[1, 3, 4, 3]]})
print("Test data X : 1, 3, 4, 3] --> ", end = "")
print("hypothesis :", b, "-->", sess.run(tf.argmax(b, 1)))
print('=*100)

c = sess.run(hypothesis, feed_dict={X: [[1, 1, 0, 1]]})
print("Test data X : [1, 1, 0, 1] --> ", end = "")
print("hypothesis :", c, "-->", sess.run(tf.argmax(c, 1)))
print('=*100)

all = sess.run(hypothesis, feed_dict={ X: [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]})
print("Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]] ")
print("hypothesis \n", all, "-->", sess.run(tf.argmax(all, 1)))
print('=*100)
```



```
• Testing & One-hot encoding & argmax
Test data X : [1, 11, 7, 9] --> hypothesis : [[8.581670e-03 9.914078e-01 1.050219e-05]] --> [1]
=====
Test data X : 1, 3, 4, 3] --> hypothesis : [[0.8252531 0.15725392 0.01749295]] --> [0]
=====
Test data X : [1, 1, 0, 1] --> hypothesis : [[2.0768354e-08 3.9369191e-04 9.9960631e-01]] --> [2]
=====
Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]
hypothesis
[[8.581670e-03 9.9140781e-01 1.0502190e-05]
[8.2525313e-01 0.15725392e-01 0.017492952e-02]
[2.0768352e-08 3.9369191e-04 9.9960631e-01]] --> [1 0 2]
```

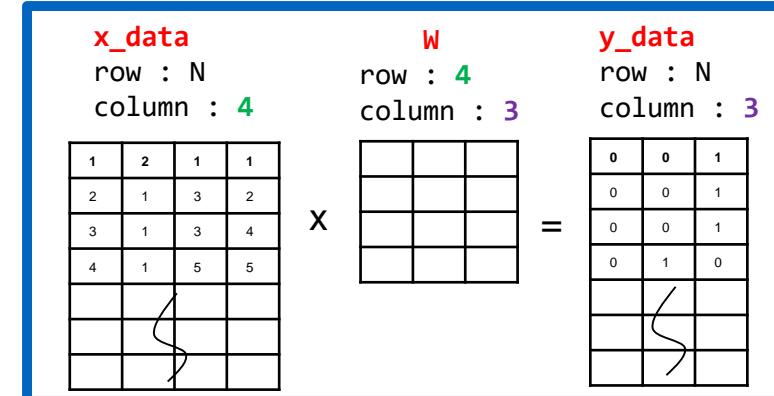
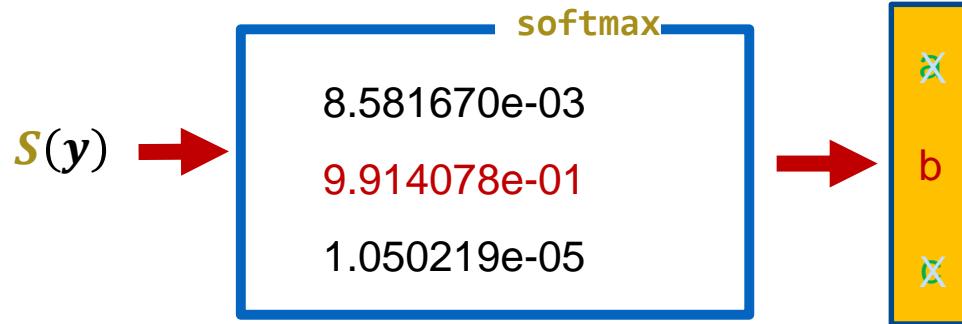
Test & one-hot encoding

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

```
a = sess.run(hypothesis, feed_dict={X: [[1, 11, 7, 9]]})
print("Test data X : [1, 11, 7, 9] --> ", end = "")
print("hypothesis :", a, "-->", sess.run(tf.argmax(a, 1)))
print('*'*100)
```



```
Test data X : [1, 11, 7, 9] --> hypothesis : [[8.581670e-03 9.914078e-01 1.050219e-05]] --> [1]
=====
```



Test & one-hot encoding

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```

```
all = sess.run(hypothesis, feed_dict={ X: [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]})
print("Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]] ")
print("hypothesis \n",all, "-->", sess.run(tf.argmax(all, 1)))
print('='*100)
```

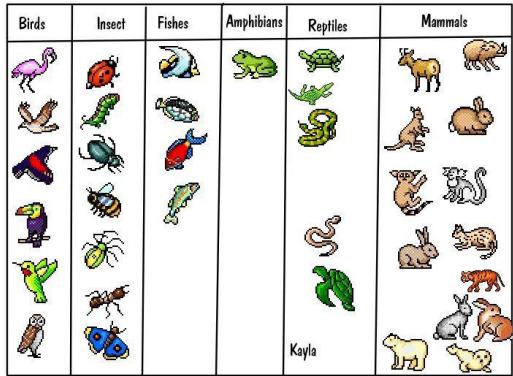


```
Test data X : [[1, 11, 7, 9], [1, 3, 4, 3], [1, 1, 0, 1]]
hypothesis
[[8.5816700e-03 9.9140781e-01 1.0502190e-05]
[8.2525313e-01 1.5725392e-01 1.7492952e-02]
[2.0768352e-08 3.9369191e-04 9.9960631e-01]] --> [1 0 2]
=====
```

Fancy softmax Classifier

- one_hot
- reshape
- cross_entropy

Animal classification



tf.one_hot and reshape

	x_data															y_data 0~6	
1	0	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	0
1	0	0	0	1	0	0	1	1	1	0	0	4	0	0	1	0	
1	0	0	0	1	0	0	1	1	1	0	0	4	1	0	1	0	
1	0	0	0	1	0	0	1	1	1	0	0	4	1	0	1	0	
1	0	0	0	1	0	0	1	1	1	0	0	4	1	1	1	0	
0	0	1	0	0	1	0	1	1	0	0	1	0	1	1	0	3	
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	
1	0	0	0	1	0	0	1	1	1	0	0	4	0	1	0	0	
1	0	0	0	1	0	0	1	1	1	0	0	4	1	0	1	0	
0	1	1	0	1	0	0	0	1	1	0	0	2	1	1	0	1	
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	3	
0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	6	
0	0	1	0	0	1	1	0	0	0	0	0	4	0	0	0	6	
0	0	1	0	0	1	1	0	0	0	0	0	6	0	0	0	6	
0	1	1	0	1	0	1	0	1	1	0	0	2	1	0	0	1	
1	0	0	0	1	0	0	1	1	1	0	0	4	1	0	1	0	

`tf.one_hot :`

If the input indices is rank N,
the output will have rank N+1.

`ex) input : [[0][3]]`

`→ output : [[[1000000]] [[0001000]]]`

`nb_classes = 7`

`Y = tf.placeholder(tf.int32, [None, 1]) # None row, 1 column (0 ~ 6) -> shape=(?, 1)`

`Y_one_hot = tf.one_hot(Y, nb_classes) # Y는 0부터 시작함, one hot shape=(?, 1, 7)`

`Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes]) # shape=(?, 7)`

tf.one_hot and reshape

x_data

1	0	0	1	0	0	0	1	1	1	0	0	4	1	0	1	0
0	0	1	0	0	1	1	1	1	0	0	1	0	1	0	1	0

nb_classes = 7

```
Y = tf.placeholder(tf.int32, [None, 1]) # 0~6 사이의 값을 넣기 위해 shape=(?, 1) 설정
Y_one_hot = tf.one_hot(Y, nb_classes) # one hot shape=(?, 1, 7)
```

0~6 7

0

3

Y_one_hot

[[[1000000] [0001000]]]



y_data

0~6

1	0	0	3	0	0	0	1	0	1	0	0	1	0	1	0	1	0
0	1	0	0	1	0	0	0	1	0	0	1	0	1	0	0	1	0
1	1	0	0	0	1	0	0	0	1	0	0	1	0	0	1	0	1
0	0	1	0	0	0	1	0	0	0	1	0	0	1	0	0	0	1
0	0	0	3	0	0	0	0	1	0	0	1	0	0	1	0	0	1
0	0	0	6	0	0	0	0	0	1	0	0	1	0	0	1	0	0
0	0	0	6	0	0	0	0	0	0	1	0	0	1	0	0	1	0
0	0	0	1	0	0	0	0	0	0	0	1	0	0	1	0	0	1
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Y_one_hot	Y
1000000	0
0100000	1
0010000	2
0001000	3
0000100	4
0000010	5
0000001	6

Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes]) # shape=(?, 7)

7

[[1000000] [0001000]]]

tf.one_hot and reshape

```
import numpy as np  
x = np.arange(12)  
print(x)
```

```
x = x.reshape(3, 4)  
x.shape
```

```
(3, 4)
```

```
print(x)
```

```
[[ 0  1  2  3]  
 [ 4  5  6  7]  
 [ 8  9 10 11]]
```

```
x.reshape(-1, 1)  
array([[0],  
[ 1],  
[ 2],  
[ 3],  
[ 4],  
[ 5],  
[ 6],  
[ 7],  
[ 8],  
[ 9],  
[10],  
[11]])
```

```
x.reshape(-1, 2)  
array([[ 0,  1],  
[ 2,  3],  
[ 4,  5],  
[ 6,  7],  
[ 8,  9],  
[10, 11]])
```

```
x.reshape(-1, 3)  
array([[ 0,  1,  2],  
[ 3,  4,  5],  
[ 6,  7,  8],  
[ 9, 10, 11]])
```

softmax_cross_entropy_with_logits

SCORE

```
logit = tf.matmul(X, W) + b
hypothesis = tf.nn.softmax(logit)
```

1

```
# Cross entropy cost/loss
cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
```

2

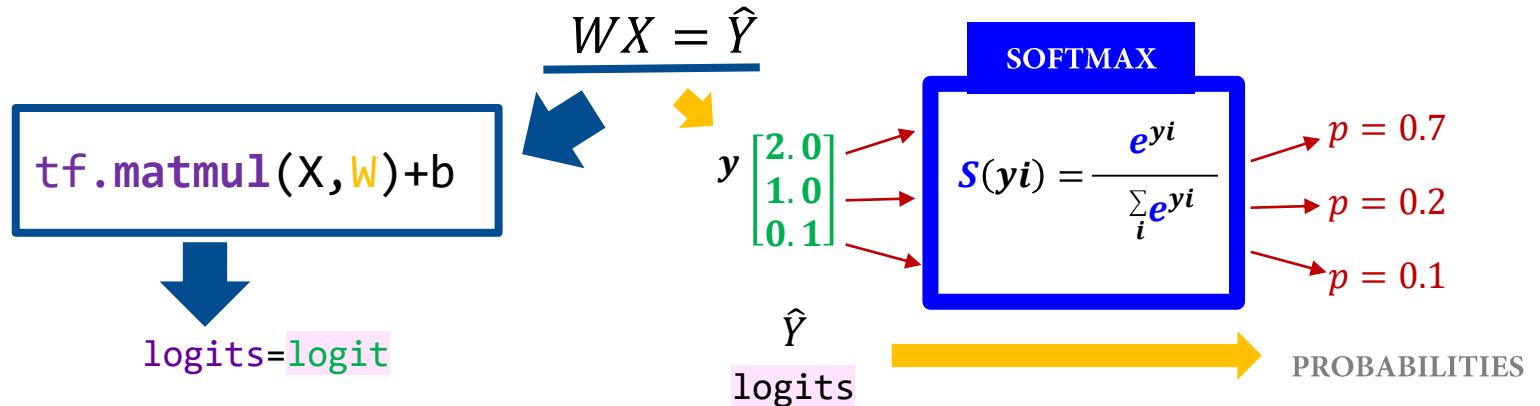
```
# Cross entropy cost/loss
cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logit,
                                                labels=Y_one_hot)
cost = tf.reduce_mean(cost_i)
```

one-hot

Y의 label

softmax_cross_entropy_with_logits

```
hypothesis = tf.nn.softmax(tf.matmul(X,W)+b)
```



SCORE

```
logit = tf.matmul(X, W) + b
hypothesis = tf.nn.softmax(logit)
```

```

import tensorflow as tf
import numpy as np
# Predicting animal type based on various features
xy = np.loadtxt('g:\data-04-zoo.csv', delimiter=',', dtype=np.float32) # column : 17
x_data = xy[:, :-1] # column : 16
y_data = xy[:, [-1]] # column : 1

nb_classes = 7 # Y의 종류가 총 7개로 구성되어 있음

X = tf.placeholder(tf.float32, [None, 16]) # row : None , column : 16
Y = tf.placeholder(tf.int32, [None, 1]) # row : None , column : 1 ( 0, 1, 2, 3, 4, 5, 6 (총 7개 종류로 구성))

Y_one_hot = tf.one_hot(Y, nb_classes) # one hot
Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes]) # ex) 1000000... structure

```

```

W = tf.Variable(tf.random_normal([16, nb_classes]), name='weight') # row : 16 , column : 7
b = tf.Variable(tf.random_normal([nb_classes]), name='bias') # column : 7

```

```

# tf.nn.softmax computes softmax activations
# softmax = exp(Logits) / reduce_sum(exp(Logits), dim)
logit = tf.matmul(X, W) + b
hypothesis = tf.nn.softmax(logit)

```

```

# Cross entropy cost/loss
cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logit, labels=Y_one_hot)
cost = tf.reduce_mean(cost_i)

```

```
optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
```

tf.argmax(A , flag) : matrix A에서 flag가 0이면 column 기준, 1이면 row 기준으로 큰 값의 index를 반환함 (index는 0부터 시작..)

prediction = tf.argmax(hypothesis, 1) # flag가 1이므로 row 기준으로 큰 값의 index를 반환함

correct_prediction = tf.equal(prediction, tf.argmax(Y_one_hot, 1)) # flag가 1이므로 row 기준으로 큰 값의 index를 반환함

accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))

tf.argmax
큰 값이 있는 곳의 index를 반환함

```

# Launch graph
with tf.Session() as sess:
    sess.run(tf.global_variables_initializer())

# Learning
for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data})
    if step % 100 == 0:
        loss, acc = sess.run([cost, accuracy], feed_dict={X: x_data, Y: y_data})
        print("Step: {:5}\tCost: {:.3f}\tAccuracy: {:.2%}".format(step, loss, acc))

# Let's see if we can predict
pred = sess.run(prediction, feed_dict={X: x_data})
line = len(x_data)
i = 0
print ("\n","="*30, line, "¶ Data analysis ", "="*20)
for p, y in zip(pred, y_data.flatten()): # y_data.flatten() 다차원 배열을 1차원 배열로 변형시킴
    i = i+1
    print(i, "번째 : Is the prediction equal to the true value? => [{}] : Prediction: {} True Y: {}".format(p == int(y), p, int(y)))

# Testing & One-hot encoding
test_x = [[0,0,1,0,0,1,0,1,1,0,0,1,0,1,0,0]]
print("\n¶ Testing & One-hot encoding & argmax")
print("Test data X :", test_x )
print("prediction :", sess.run(prediction, feed_dict={X: test_x}))

```

```
# Learning
for step in range(2001):
    sess.run(optimizer, feed_dict={X: x_data, Y: y_data})
    if step % 100 == 0:
        loss, acc = sess.run([cost, accuracy], feed_dict={X: x_data, Y: y_data})
        print("Step: {:5}\tCost: {:.3f}\tAccuracy: {:.2%}".format(step, loss, acc))
```



Step: 0	Cost: 4.624	Accuracy: 9.90%
Step: 100	Cost: 0.680	Accuracy: 78.22%
Step: 200	Cost: 0.433	Accuracy: 85.15%
Step: 300	Cost: 0.313	Accuracy: 87.13%
Step: 400	Cost: 0.237	Accuracy: 91.09%
Step: 500	Cost: 0.187	Accuracy: 97.03%
Step: 600	Cost: 0.153	Accuracy: 99.01%
Step: 700	Cost: 0.129	Accuracy: 100.00%
Step: 800	Cost: 0.112	Accuracy: 100.00%
Step: 900	Cost: 0.099	Accuracy: 100.00%
Step: 1000	Cost: 0.089	Accuracy: 100.00%
Step: 1100	Cost: 0.080	Accuracy: 100.00%
Step: 1200	Cost: 0.074	Accuracy: 100.00%
Step: 1300	Cost: 0.068	Accuracy: 100.00%
Step: 1400	Cost: 0.063	Accuracy: 100.00%
Step: 1500	Cost: 0.059	Accuracy: 100.00%
Step: 1600	Cost: 0.055	Accuracy: 100.00%
Step: 1700	Cost: 0.052	Accuracy: 100.00%
Step: 1800	Cost: 0.050	Accuracy: 100.00%
Step: 1900	Cost: 0.047	Accuracy: 100.00%
Step: 2000	Cost: 0.045	Accuracy: 100.00%

```
# Let's see if we can predict
pred = sess.run(prediction, feed_dict={X: x_data})
line = len(x_data)
i = 0
print ("\n", "*30, line, "|| Data analysis ", "*20)
for p, y in zip(pred, y_data.flatten()): # y_data.flatten() 다차원 배열을 1차원 배열로 변형시킴
    i = i+1
    print(i, "번째 : Is the prediction equal to the true value? => [{}] : Prediction: {} True Y: {}".format(p == int(y), p, int(y)))
```



```
=====
1 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
2 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
3 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3
4 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
5 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
6 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
7 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
8 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3
9 번째 : Is the prediction equal to the true value? => [True] : Prediction: 3 True Y: 3
.
.
.
97 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
98 번째 : Is the prediction equal to the true value? => [True] : Prediction: 5 True Y: 5
99 번째 : Is the prediction equal to the true value? => [True] : Prediction: 0 True Y: 0
100 번째 : Is the prediction equal to the true value? => [True] : Prediction: 6 True Y: 6
101 번째 : Is the prediction equal to the true value? => [True] : Prediction: 1 True Y: 1
```

```
test_x = [[0,0,1,0,0,1,0,1,1,0,0,1,0,1,0,0]]  
print("\n• Testing & One-hot encoding & argmax")  
print("Test data X :", test_x )  
print("prediction :", sess.run(prediction, feed_dict={X: test_x}))
```



- Testing & One-hot encoding & argmax

Test data X : [[0, 0, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0]]
prediction : [3]