TensorFlow Basics

Lecture 01

TensorFlow ™ Install Develop API r1.0 Deploy Extend Resources Versions Search GitHub

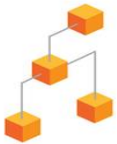
An open-source software library
for Machine Intelligence

GET STARTED

TensorFlow 1.0 has arrived!

We're excited to announce the release of TensorFlow 1.0! Check out the migration guide to upgrade your code with ease.

UPGRADE NOW



Dynamic graphs in TensorFlow

We've open-sourced TensorFlow Fold to make it easier than ever to work with input data with varying shapes and sizes.

LEARN MORE

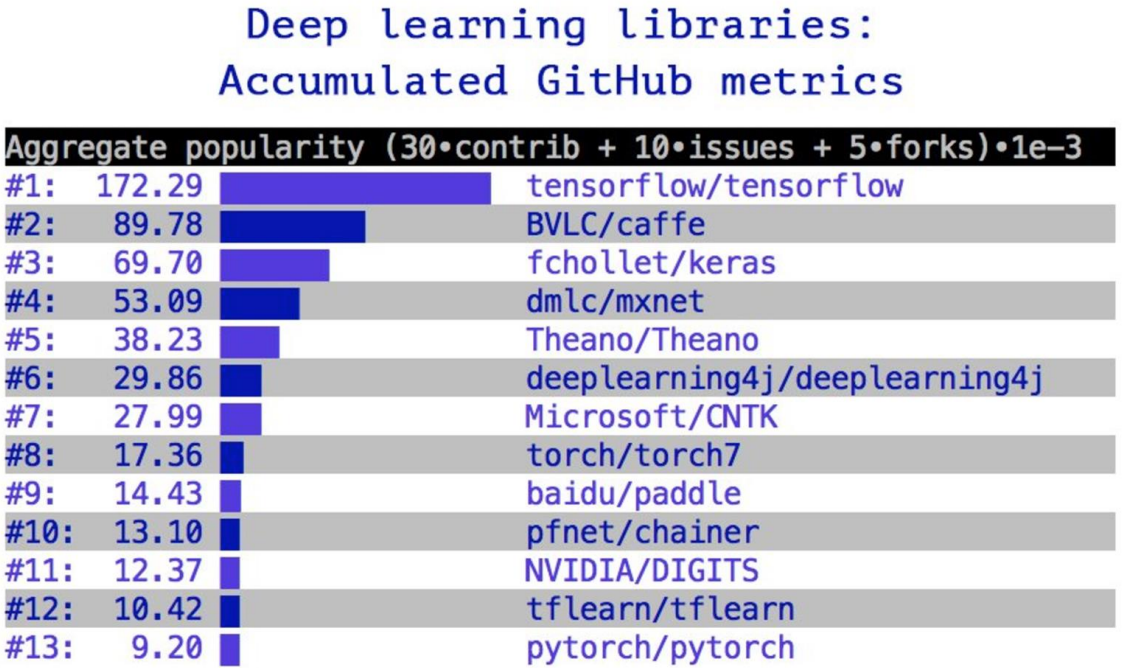
The 2017 TensorFlow Dev Summit

Thousands of people from the TensorFlow community participated in the first flagship event. Watch the keynote and talks.

WATCH VIDEOS

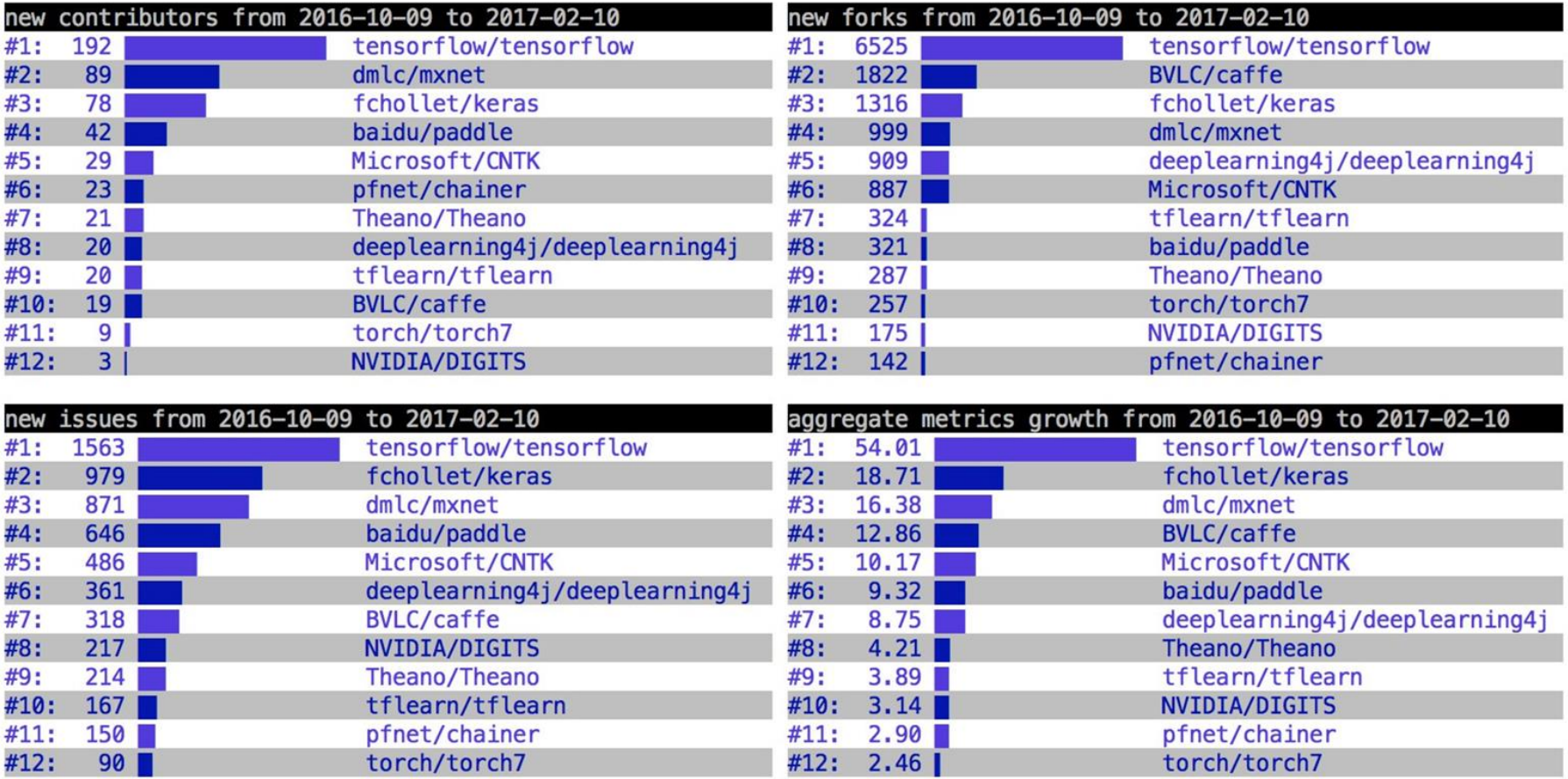
https://www.tensorflow.org

TensorFlow



https://twitter.com/fchollet/status/830499993450450944/

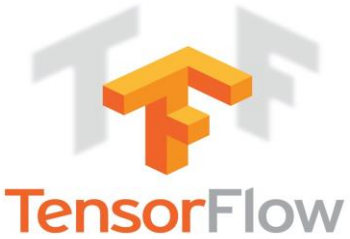
Deep learning libraries: growth over past three months



https://twitter.com/fchollet/status/830499993450450944/

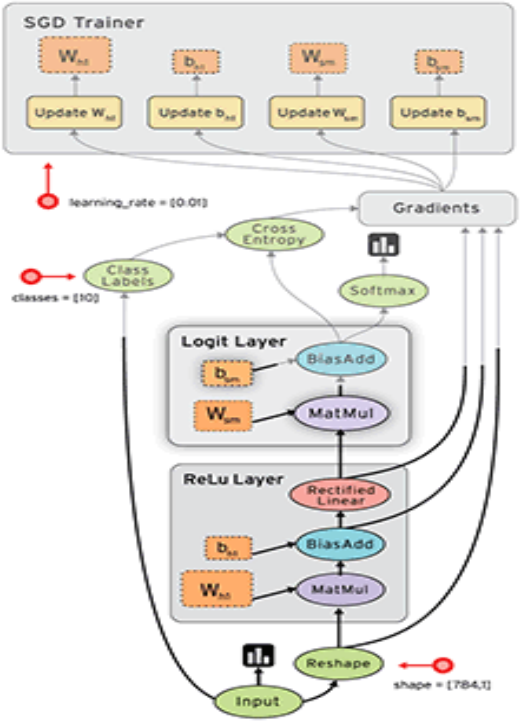
TensorFlow

- TensorFlow™ is an **open source software library** for **numerical computation** using **data flow graphs**.
- Python



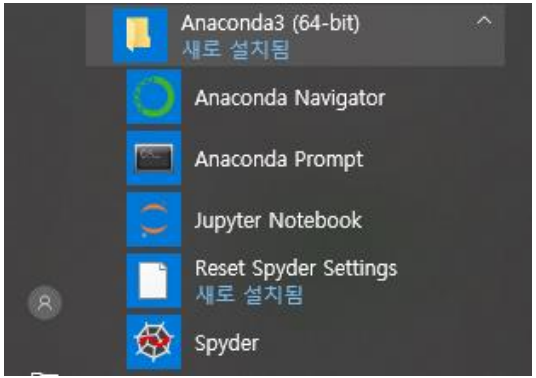
What is a Data Flow Graph?

- Nodes in the graph represent mathematical operations
- Edges represent the multidimensional data arrays (tensors) communicated between them.



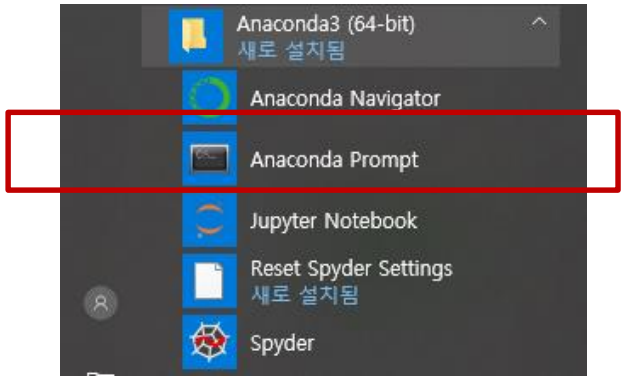
Installing Anaconda

- Installing Anaconda



https://www.anaconda.com/download/#windows

Installing TensorFlow



※ pip

파이썬 패키지를 관리하는 소프트웨어

G:\>pip install tensorflow

or

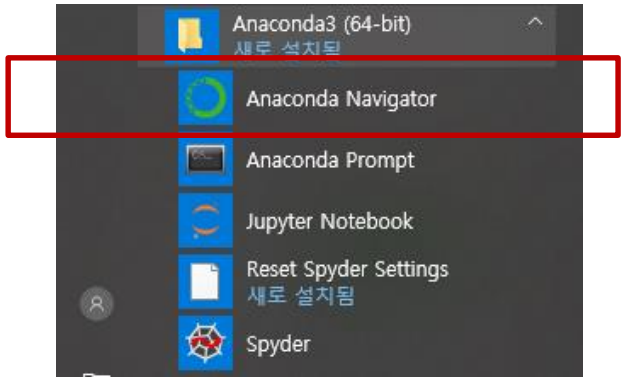
G:\>pip install --upgrade tensorflow

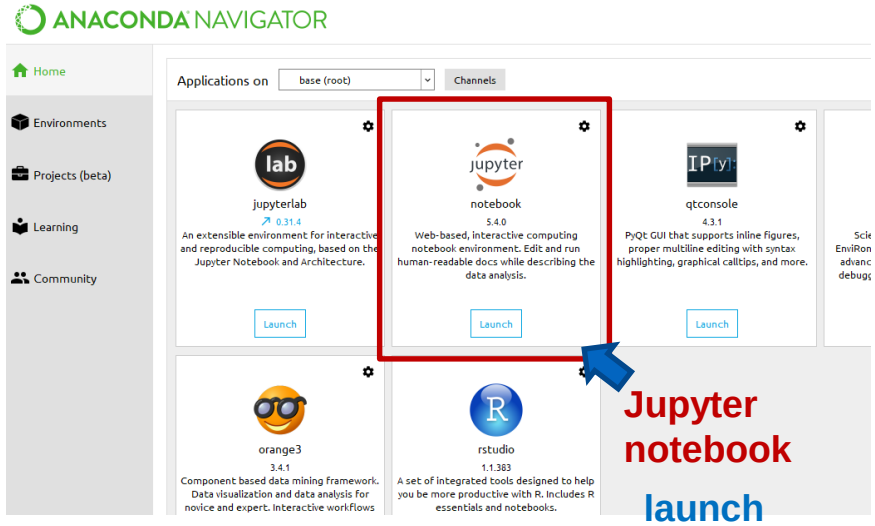
```
G:₩>ipython
Python 3.6.4 |Anaconda, Inc.| (default, Jan 16 2018, 10:22:32) [MSC v.1900 64 bit (AMD64)]
Type 'copyright', 'credits' or 'license' for more information
IPython 6.2.1 -- An enhanced Interactive Python. Type '?' for help.

In [1]:
```

Test in Anaconda Prompt

```
In [1]: import tensorflow as tf

In [2]: tf.__version__
Out[2]: '1.7.0‘
In [3]: hello = tf.constant("Hello, TensorFlow!")

In [4]: sess = tf.Session()

In [5]: print(sess.run(hello))
b'Hello, TensorFlow!'

In [6]: exit
```

Test in Anaconda Navigator





※ Jupyter notebook

머신러닝이나 데이터분석 용도로 파이썬을 사용하는 경우에 주로 사용하는 툴로써 가벼우며 코드를 실행 및 수정이 간편

Test in Anaconda Navigator

Test in Jupyter notebook

```
In [1]: import tensorflow as tf

In [2]: tf.__version__
Out[2]: '1.7.0‘
In [3]: hello = tf.constant("Hello, TensorFlow!")

In [4]: sess = tf.Session()

In [5]: print(sess.run(hello))
b'Hello, TensorFlow!'
```

shift + enter

b’String’ ‘**b**’ indicates *Bytes literals*

Test in Jupyter notebook (1/4)

```
import tensorflow as tf
3 # a rank 0 tensor; this is a scalar with shape []
3

[1. ,2., 3.] # a rank 1 tensor; this is a vector with shape [3]
[1.0, 2.0, 3.0]

[[1., 2., 3.], [4., 5., 6.]] # a rank 2 tensor; a matrix with shape [2, 3]
[[1.0, 2.0, 3.0], [4.0, 5.0, 6.0]]

[[[1., 2., 3.]], [[7., 8., 9.]]] # a rank 3 tensor with shape [2, 1, 3]
[[[1.0, 2.0, 3.0]], [[7.0, 8.0, 9.0]]]

node1 = tf.constant(3.0, tf.float32)  # 상수를 할당, 변수를 할당할 때는 tf.Variable() 사용
Node2 = tf.constant(4.0) # 상수, also tf.float32 implicitly
node3 = tf.add(node1, node2) # 연산자

print("노드 1:", node1, "노드 2:", node2)
print("노드 3: ", node3)
노드 1: Tensor("Const_18:0", shape=(), dtype=float32) 노드 2: Tensor("Const_19:0", shape=(), dtype=float32)
노드 3:  Tensor("Add_8:0", shape=(), dtype=float32)
```

Test in Jupyter notebook (2/4)

1
```
sess = tf.Session()
```
2
```
print("sess.run(node1, node2): ", sess.run([node1, node2]))
print("sess.run(node3): ", sess.run(node3))
sess.run(node1, node2):  [3.0, 4.0]
sess.run(node3):  7.0

a = tf.placeholder(tf.float32) # 플레이스홀더
b = tf.placeholder(tf.float32) # 플레이스홀더
adder_node = a + b  # + provides a shortcut for tf.add(a, b)
print(sess.run(adder_node, feed_dict={a: 3, b: 4.5}))
print(sess.run(adder_node, feed_dict={a: [1,3], b: [2, 4]}))
7.5
[3. 7.]

add_and_triple = adder_node * 3.
print(sess.run(add_and_triple, feed_dict={a: 3, b:4.5}))
22.5
```

Test in Jupyter notebook (3/4)

```
import tensorflow as tf
import numpy as np  #행렬 라이브러리 제공

a = tf.constant([1,2,3])
b = tf.constant([[10, 20, 30], [100, 200, 300]])
c = tf.add(a,b)

print(c) # 만약 Session 을 열고 run 하지 않고 c를 프린트 한다면...
with tf.Session() as sess:
    print (sess.run(c))
```

1

2

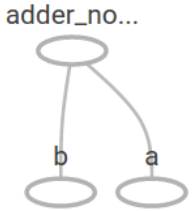
```
Tensor("Add_4:0", shape=(2, 3), dtype=int32)

[[ 11  22  33]
 [101 202 303]]
```

Test in Jupyter notebook (4/4)

```
import tensorflow as tf
import numpy as np

t = tf.zeros([3,])
with tf.Session() as sess:
    print (sess.run(t),"\n")

# tf.random_normal   정규분포 난수로 텐서 생성
# tf.random_uniform  균등분포 난수로 텐서 생성

t1 = tf.random_normal([1] ) #shape, mean, standard deviation
t2 = tf.random_normal([2,2])
t3 = tf.random_uniform([1], -3, 3) #shape, mean, standard deviation
t4 = tf.random_uniform([2,2], -4, 3)

with tf.Session() as sess:
    print ("t1 : ", sess.run(t1))
    print ("t2 : ", sess.run(t2), "\n")
    print ("t3 : ", sess.run(t3))
    print ("t4 : ", sess.run(t4))
```

```
[0. 0. 0.]

t1 :  [-1.5805651]
t2 :  [[0.5062811  1.9646689 ]
 [0.31635258 0.5122979 ]]

t3 :  [2.7569304]
t4 :  [[-1.891392   1.7238994]
 [ 2.0100794  1.1356215]]
```

Computational Graph



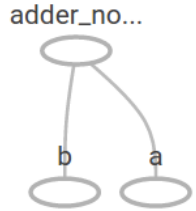
import tensorflow as tf

In [4]:
```
node1 = tf.constant(3.0, tf.float32)
node2 = tf.constant(4.0) # also tf.float32 implicitly
node3 = tf.add(node1, node2)
```

In [5]:
```
print("node1:", node1, "node2:", node2)
print("node3: ", node3)
```

```
node1: Tensor("Const_1:0", shape=(), dtype=float32) node2: Tensor("Const_2:0", shape=(), dtyp
e=float32)
node3:  Tensor("Add:0", shape=(), dtype=float32)
```

Computational Graph



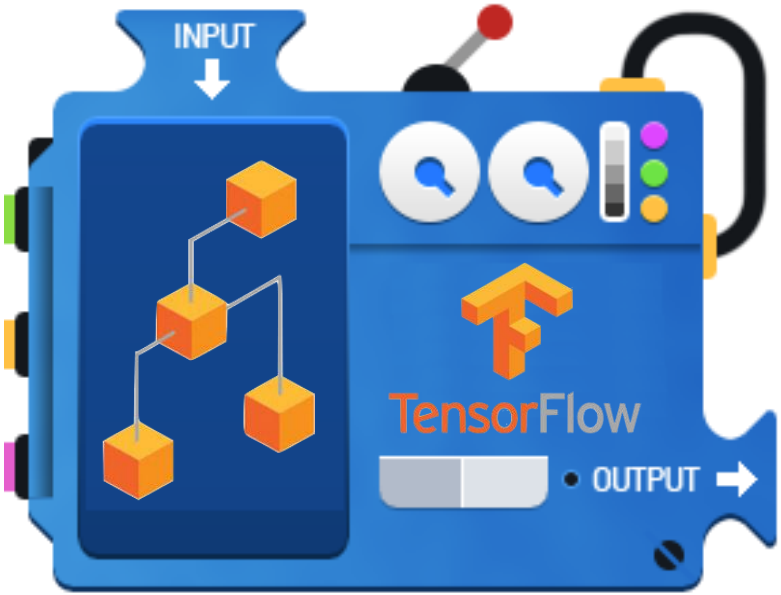

```
In [6]: sess = tf.Session()
        print("sess.run(node1, node2): ", sess.run([node1, node2]))
        print("sess.run(node3): ", sess.run(node3))

        sess.run(node1, node2):  [3.0, 4.0]
        sess.run(node3):  7.0

        sess.close()
```

```
with tf.Session() as sess:
    .
    .
    .
```

TensorFlow Mechanics

2 feed data and run graph (operation)
sess.run (op)

1 Build graph using
TensorFlow operations



3 update variables
in the graph
(and return values)

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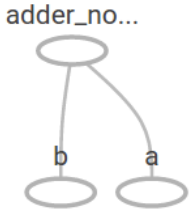
Computational Graph



1 Build graph (tensors) using TensorFlow operations

```
In [4]: node1 = tf.constant(3.0, tf.float32)
        node2 = tf.constant(4.0) # also tf.float32 implicitly
        node3 = tf.add(node1, node2)
```

2 feed data and run graph (operation)
sess.run (op)

3 update variables in the graph
(and return values)

```
In [6]: sess = tf.Session()
        print("sess.run(node1, node2): ", sess.run([node1, node2]))
        print("sess.run(node3): ", sess.run(node3))
```

```
sess.run(node1, node2):  [3.0, 4.0]
sess.run(node3):  7.0
```

Placeholder

In [7]:
```
a = tf.placeholder(tf.float32)
b = tf.placeholder(tf.float32)
adder_node = a + b  # + provides a shortcut for tf.add(a, b)

print(sess.run(adder_node, feed_dict={a: 3, b: 4.5}))
print(sess.run(adder_node, feed_dict={a: [1,3], b: [2, 4]}))
```

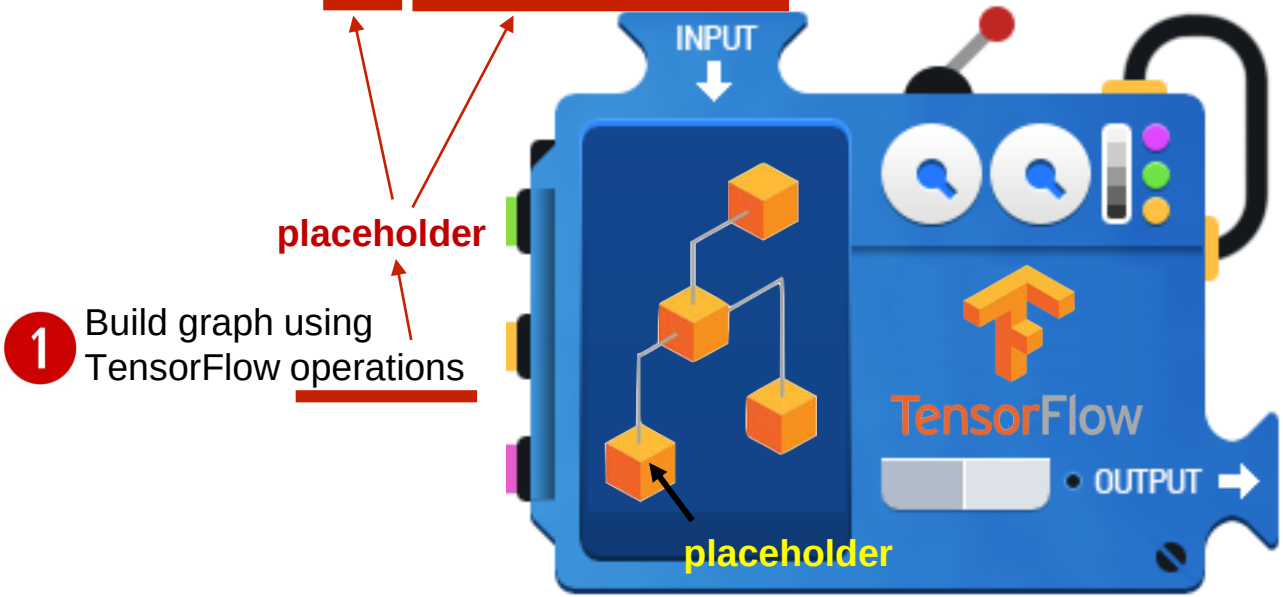
```
7.5
[ 3.  7.]
```

In [8]:
```
add_and_triple = adder_node * 3.
print(sess.run(add_and_triple, feed_dict={a: 3, b:4.5}))
```

```
22.5
```

TensorFlow Mechanics

2 feed data and run graph (operation)
sess.run (op, feed_dict={x: x_data})



Everything is **Tensor**

Tensors

In [3]:
```
3 # a rank 0 tensor; this is a scalar with shape []
[1. ,2., 3.] # a rank 1 tensor; this is a vector with shape [3]
[[1., 2., 3.], [4., 5., 6.]] # a rank 2 tensor; a matrix with shape [2, 3]
[[[1., 2., 3.]], [[7., 8., 9.]]] # a rank 3 tensor with shape [2, 1, 3]
```

Out[3]:
```
[[[1.0, 2.0, 3.0]], [[7.0, 8.0, 9.0]]]
```

```
t = tf.Constant([1., 2., 3.])
```

Tensor Ranks

```
t = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

Rank	Math entity	Python example
0	Scalar (magnitude only)	`s = 483`
1	Vector (magnitude and direction)	`v = [1.1, 2.2, 3.3]`
2	Matrix (table of numbers)	`m = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]`
3	3-Tensor (cube of numbers)	`t = [[[2], [4], [6]], [[8], [10], [12]], [[14], [16], [18]]]`
n	n-Tensor (you get the idea)	`....`

Tensor Ranks


```
import tensorflow as tf
c0 = tf.constant(10) # rank 0
c1 = tf.constant([10]) # rank 0
c2 = tf.constant([1,2])  # rank 1
c3 = tf.constant([1,2,3])  # rank 1
c4 = tf.constant([[1,2,3],[4,5,6]])  # rank 2
c5 = tf.constant([[1,2,3],[4,5,6],[7,8,9]])  # rank 2
c6 = tf.constant([[[2],[4]],[[8],[10]],[[12],[14]],[[18],[20]]])  # rank 3
c7 = tf.constant([[[2],[4],[6]],[[8],[10],[12]],[[14],[16],[18]]])  # rank 3

with tf.Session() as sess:
    print("c0 value : ",sess.run((c0)), ",\t c0 rank : ",sess.run(tf.rank(c0)))

    print('='*50)
    print("c1 value : ",sess.run((c1)), ",\t c1 rank : ",sess.run(tf.rank(c1)))

    print('='*50)
    print("c2 value : ",sess.run((c2)), ",\t c2 rank : ",sess.run(tf.rank(c2)))

    print('='*50)
    print("c3 value : ",sess.run((c3)), ",\t c3 rank : ",sess.run(tf.rank(c3)))

    print('='*50)
    print("c4 value : ")
    print(sess.run((c4)), ",\t c4 rank : ",sess.run(tf.rank(c4)))

    print('='*50)
    print("c5 value : ")
    print(sess.run((c5)), ",\t c5 rank : ",sess.run(tf.rank(c5)))

    print('='*50)
    print("c6 value : ")
    print(sess.run((c6)), ",\t c6 rank : ",sess.run(tf.rank(c6)))

    print('='*50)
    print("c7 value : ")
    print(sess.run((c7)), ",\t c7 rank : ",sess.run(tf.rank(c7)))
```

```
c0 value :  10 ,            c0 rank :  0
==================================================
c1 value :  [10] ,          c1 rank :  1
==================================================
c2 value :  [1 2] ,         c2 rank :  1
==================================================
c3 value :  [1 2 3] ,       c3 rank :  1
==================================================
c4 value :
[[1 2 3]
 [4 5 6]] ,                 c4 rank :  2
==================================================
c5 value :
[[1 2 3]
 [4 5 6]
 [7 8 9]] ,                 c5 rank :  2
==================================================
c6 value :
[[[ 2]
  [ 4]]

 [[ 8]
  [10]]

 [[12]
  [14]]

 [[18]
  [20]]] ,                  c6 rank :  3
==================================================
c7 value :
[[[ 2]
  [ 4]
  [ 6]]

 [[ 8]
  [10]
  [12]]

 [[14]
  [16]
  [18]]] ,                  c7 rank :  3
```

Tensor Shapes

```
t = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

Shapes ?
[3,3]

Rank	Shape	Dimension number	Example
0	[]	0-D	A 0-D tensor. A scalar.
1	[D0]	1-D	A 1-D tensor with shape [5].
2	[D0, D1]	2-D	A 2-D tensor with shape [3, 4].
3	[D0, D1, D2]	3-D	A 3-D tensor with shape [1, 4, 3].
n	[D0, D1, ... Dn-1]	n-D	A tensor with shape [D0, D1, ... Dn-1].

Tensor Shapes


```
import tensorflow as tf
c0 = tf.constant(10) # rank 0
c1 = tf.constant([10]) # rank 0
c2 = tf.constant([1,2]) # rank 1
c3 = tf.constant([1,2,3]) # rank 1
c4 = tf.constant([[1,2,3],[4,5,6]]) # rank 2
c5 = tf.constant([[1,2,3],[4,5,6],[7,8,9]]) # rank 2
c6 = tf.constant([[[2],[4]],[[8],[10]],[[12],[14]],[[18],[20]]]) # rank 3
c7 = tf.constant([[[2],[4],[6]],[[8],[10],[12]],[[14],[16],[18]]]) # rank 3

with tf.Session() as sess:
    print("c0 value : ",sess.run((c0)), ",\t c0 shape : ",sess.run(tf.shape(c0)))

    print('='*50)
    print("c1 value : ",sess.run((c1)), ",\t c1 shape : ",sess.run(tf.shape(c1)))

    print('='*50)
    print("c2 value : ",sess.run((c2)), ",\t c2 shape : ",sess.run(tf.shape(c2)))

    print('='*50)
    print("c3 value : ",sess.run((c3)), ",\t c3 shape : ",sess.run(tf.shape(c3)))

    print('='*50)
    print("c4 value : ")
    print(sess.run((c4)), ",\t c4 shape : ",sess.run(tf.shape(c4)))

    print('='*50)
    print("c5 value : ")
    print(sess.run((c5)), ",\t c5 shape : ",sess.run(tf.shape(c5)))

    print('='*50)
    print("c6 value : ")
    print(sess.run((c6)), ",\t c6 shape : ",sess.run(tf.shape(c6)))

    print('='*50)
    print("c7 value : ")
    print(sess.run((c7)), ",\t c7 shape : ",sess.run(tf.shape(c7)))
```

```
c0 value :  10 ,            c0 shape :  []
==================================================
c1 value :  [10] ,          c1 shape :  [1]
==================================================
c2 value :  [1 2] ,         c2 shape :  [2]
==================================================
c3 value :  [1 2 3] ,       c3 shape :  [3]
==================================================
c4 value :
[[1 2 3]
 [4 5 6]] ,                 c4 shape :  [2 3]
==================================================
c5 value :
[[1 2 3]
 [4 5 6]
 [7 8 9]] ,                 c5 shape :  [3 3]
==================================================
c6 value :
[[[ 2]
  [ 4]]

 [[ 8]
  [10]]

 [[12]
  [14]]

 [[18]
  [20]]] ,                  c6 shape :  [4 2 1]
==================================================
c7 value :
[[[ 2]
  [ 4]
  [ 6]]

 [[ 8]
  [10]
  [12]]

 [[14]
  [16]
  [18]]] ,                  c7 shape :  [3 3 1]
```

Tensor Size

```
t = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

Size ?

[9]

Tensor Size


```
import tensorflow as tf
c0 = tf.constant(10) # rank 0
c1 = tf.constant([10]) # rank 0
c2 = tf.constant([1,2]) # rank 1
c3 = tf.constant([1,2,3]) # rank 1
c4 = tf.constant([[1,2,3],[4,5,6]]) # rank 2
c5 = tf.constant([[1,2,3],[4,5,6],[7,8,9]]) # rank 2
c6 = tf.constant([[[2],[4]],[[8],[10]],[[12],[14]],[[18],[20]]]) # rank 3
c7 = tf.constant([[[2],[4],[6]],[[8],[10],[12]],[[14],[16],[18]]]) # rank 3

with tf.Session() as sess:
    print("c0 value : ",sess.run((c0)), ",\t c0 size : ",sess.run(tf.size(c0)))

    print('='*50)
    print("c1 value : ",sess.run((c1)), ",\t c1 size : ",sess.run(tf.size(c1)))

    print('='*50)
    print("c2 value : ",sess.run((c2)), ",\t c2 size : ",sess.run(tf.size(c2)))

    print('='*50)
    print("c3 value : ",sess.run((c3)), ",\t c3 size : ",sess.run(tf.size(c3)))

    print('='*50)
    print("c4 value : ")
    print(sess.run((c4)), ",\t c4 size : ",sess.run(tf.size(c4)))

    print('='*50)
    print("c5 value : ")
    print(sess.run((c5)), ",\t c5 size : ",sess.run(tf.size(c5)))

    print('='*50)
    print("c6 value : ")
    print(sess.run((c6)), ",\t c6 size : ",sess.run(tf.size(c6)))

    print('='*50)
    print("c7 value : ")
    print(sess.run((c7)), ",\t c7 size : ",sess.run(tf.size(c7)))
```

```
c0 value :  10 ,          c0 size :  1
==================================================
c1 value :  [10] ,        c1 size :  1
==================================================
c2 value :  [1 2] ,       c2 size :  2
==================================================
c3 value :  [1 2 3] ,     c3 size :  3
==================================================
c4 value :
[[1 2 3]
 [4 5 6]] ,               c4 size :  6
==================================================
c5 value :
[[1 2 3]
 [4 5 6]
 [7 8 9]] ,               c5 size :  9
==================================================
c6 value :
[[[ 2]
  [ 4]]

 [[ 8]
  [10]]

 [[12]
  [14]]

 [[18]
  [20]]] ,                 c6 size :  8
==================================================
c7 value :
[[[ 2]
  [ 4]
  [ 6]]

 [[ 8]
  [10]
  [12]]

 [[14]
  [16]
  [18]]] ,                 c7 size :  9
```

Tensor Types

```
t = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

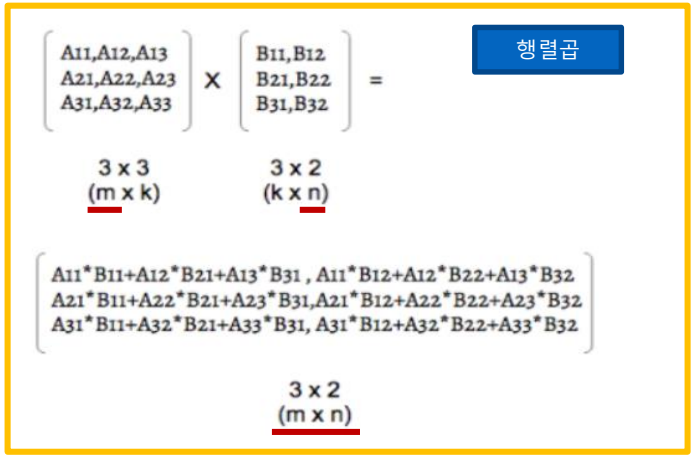
Data type	Python type	Description
DT_FLOAT	tf.float32	32 bits floating point.
DT_DOUBLE	tf.float64	64 bits floating point.
DT_INT8	tf.int8	8 bits signed integer.
DT_INT16	tf.int16	16 bits signed integer.
DT_INT32	tf.int32	32 bits signed integer.
DT_INT64	tf.int64	64 bits signed integer.

...

tf.matmul

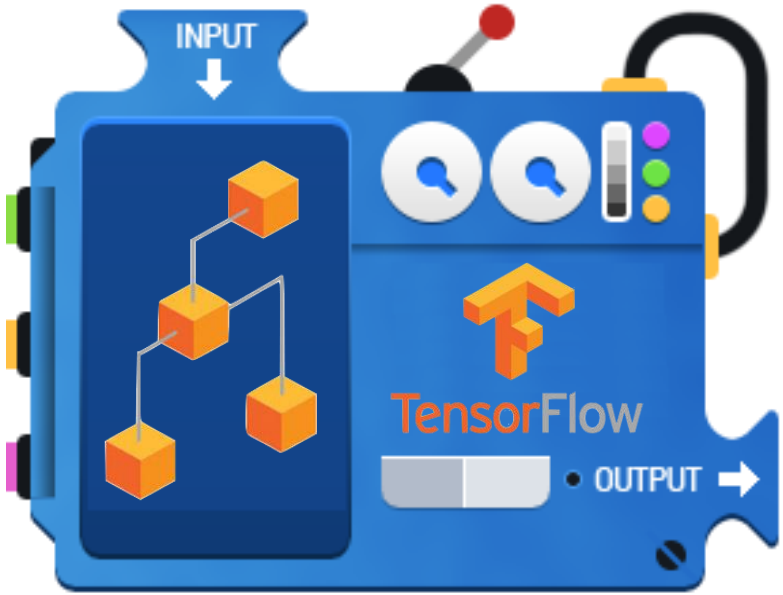
```
import tensorflow as tf
x = tf.constant([[1,2,3],[4,5,6]])
w = tf.constant([[2,3],[5,6],[50,60]])
b = tf.constant([100,200])
expr1 = tf.matmul(x, w)
expr2 = tf.matmul(x, w) + b

with tf.Session() as sess:
    print("\n x : \n",sess.run((x)))
    print("\n w : \n",sess.run((w)))
    print("\n b : \n",sess.run((b)))
    print("\n expr1 : \n",sess.run((expr1)))
    print("\n expr2 : \n",sess.run((expr2)))
```

```
x :
[[1 2 3]
[4 5 6]]

w :
[[ 2  3]
[ 5  6]
[50 60]]

b :
[100 200]

expr1 :
[[162 195]
[333 402]]

expr2 :
[[262 395]
[433 602]]
```



TensorFlow Mechanics

2 feed data and run graph (operation)
sess.run (op, feed_dict={x: x_data})



1 Build graph using
TensorFlow operations

3 update variables
in the graph
(and return values)

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TensorFlow Basic (summary)

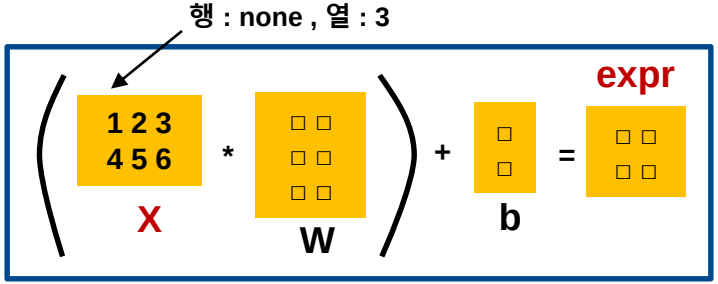
```
# 텐서플로우의 기본적인 구성을 익힙니다.
import tensorflow as tf

# tf.constant 상수를 의미합니다.
hello = tf.constant('Hello, TensorFlow!')
print(hello)

a = tf.constant(10)
b = tf.constant(32)
c = tf.add(a, b) # a + b 로도 쓸 수 있음
print(c)

# 위에서 변수와 수식들을 정의했지만, 실행이 정의한 시점에서 실행되는 것은 아닙니다.
# 다음처럼 Session 객체와 run 메소드를 사용할 때 계산이 됩니다.
# 따라서 모델을 구성하는 것과, 실행하는 것을 분리하여 프로그램을 깔끔하게 작성할 수 있습니다.
# 그래프를 실행할 세션을 구성합니다.
sess =
# sess.run: 설정한 텐서 그래프(변수나 수식 등등)를 실행합니다.
print( (hello))
print( ([a, b, c]))

# 세션을 닫습니다.
sess.close()
```

```
Tensor("Const:0", shape=(), dtype=string)
Tensor("Add:0", shape=(), dtype=int32)
b'Hello, TensorFlow!'
[10, 32, 42]
```

Placeholder & Variable (summary 1/2)

```
# 플레이스홀더와 변수의 개념을 익혀봅니다
import tensorflow as tf

# tf.placeholder: 계산을 실행할 때 입력값을 받는 변수로 사용합니다.
# None 은 크기가 정해지지 않았음을 의미합니다.
X = tf.[redacted](tf.float32, [None, 3]) # None 행 3 열 플레이스홀더 할당
print(X)

# X 플레이스홀더에 넣을 값 입니다.
# 플레이스홀더에서 설정한 것 처럼, 두번째 차원의 요소의 갯수는 3개 입니다.
x_data = [[1, 2, 3], [4, 5, 6]] # 2행3 열구조

# tf.Variable: 그래프를 계산하면서 최적화 할 변수들입니다.
# tf.random_normal: 각 변수들의 초기값을 정규분포 랜덤 값으로 초기화합니다.
W = tf.[redacted](tf.random_normal([3, 2])) # 3행 2열 변수 할당
b = tf.[redacted](tf.random_normal([2, 1])) # 2행 1열 변수 할당

# 입력값과 변수들을 계산할 수식을 작성합니다.
# tf.matmul 처럼 mat* 로 되어 있는 함수로 행렬 계산을 수행합니다.
expr = tf.matmul([redacted], [redacted]) + b # 2행2 열 구조
```

```
Tensor("Placeholder:0", shape=(?, 3), dtype=float32)
=== x_data ===
[[1, 2, 3], [4, 5, 6]]
=== W ===
[[-0.597651   -0.6604751 ]
 [-2.2989275  -0.787894  ]
 [-0.21801808 -1.0365014 ]]
=== b ===
[[ 0.02285073]
 [-0.8386975 ]]
=== expr ===
[[ -5.8267097  -5.3229165]
 [-16.032047  -13.639076 ]]
```



Placeholder & Variable (summary 2/2)

```
# 그래프를 실행할 세션을 구성합니다.
sess = [redacted]

# 위에서 설정한 Variable 들의 값들을 초기화 하기 위해
# 처음에 tf.global_variables_initializer 를 한 번 실행해야 합니다.
[redacted](tf.global_variables_initializer())

print("=== x_data ===")
print(x_data)
print("=== W ===")
print([redacted](W))
print("=== b ===")
print([redacted](b))
print("=== expr ===")

# expr 수식에는 X 라는 입력값이 필요합니다.
# 따라서 expr 실행시에는 이 변수에 대한 실제 입력값을 다음처럼 넣어줘야합니다.
print([redacted](expr, feed_dict={X: [redacted]}))
sess.close()
```

```
Tensor("Placeholder:0", shape=(?, 3), dtype=float32)
=== x_data ===
[[1, 2, 3], [4, 5, 6]]
=== W ===
[[-0.597651   -0.6604751 ]
 [-2.2989275  -0.787894  ]
 [-0.21801808 -1.0365014 ]]
=== b ===
[[ 0.02285073]
 [-0.8386975 ]]
=== expr ===
[[ -5.8267097  -5.3229165]
 [-16.032047  -13.639076 ]]
```

expr = tf.matmul(X, W) + b # 2행2열구조