



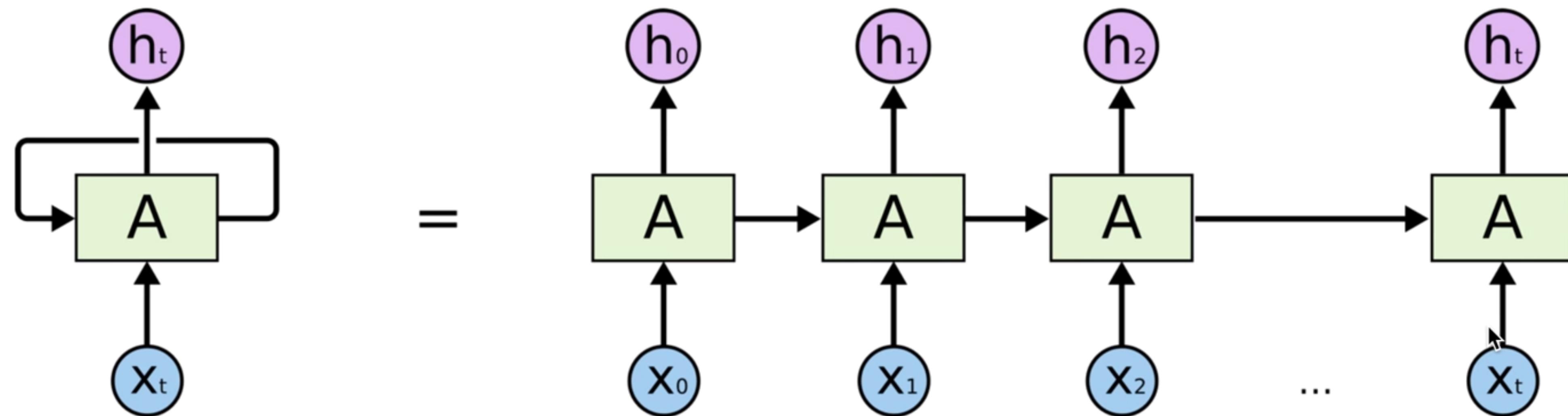
Lecture 12

# Recurrent Neural Network (RNN)

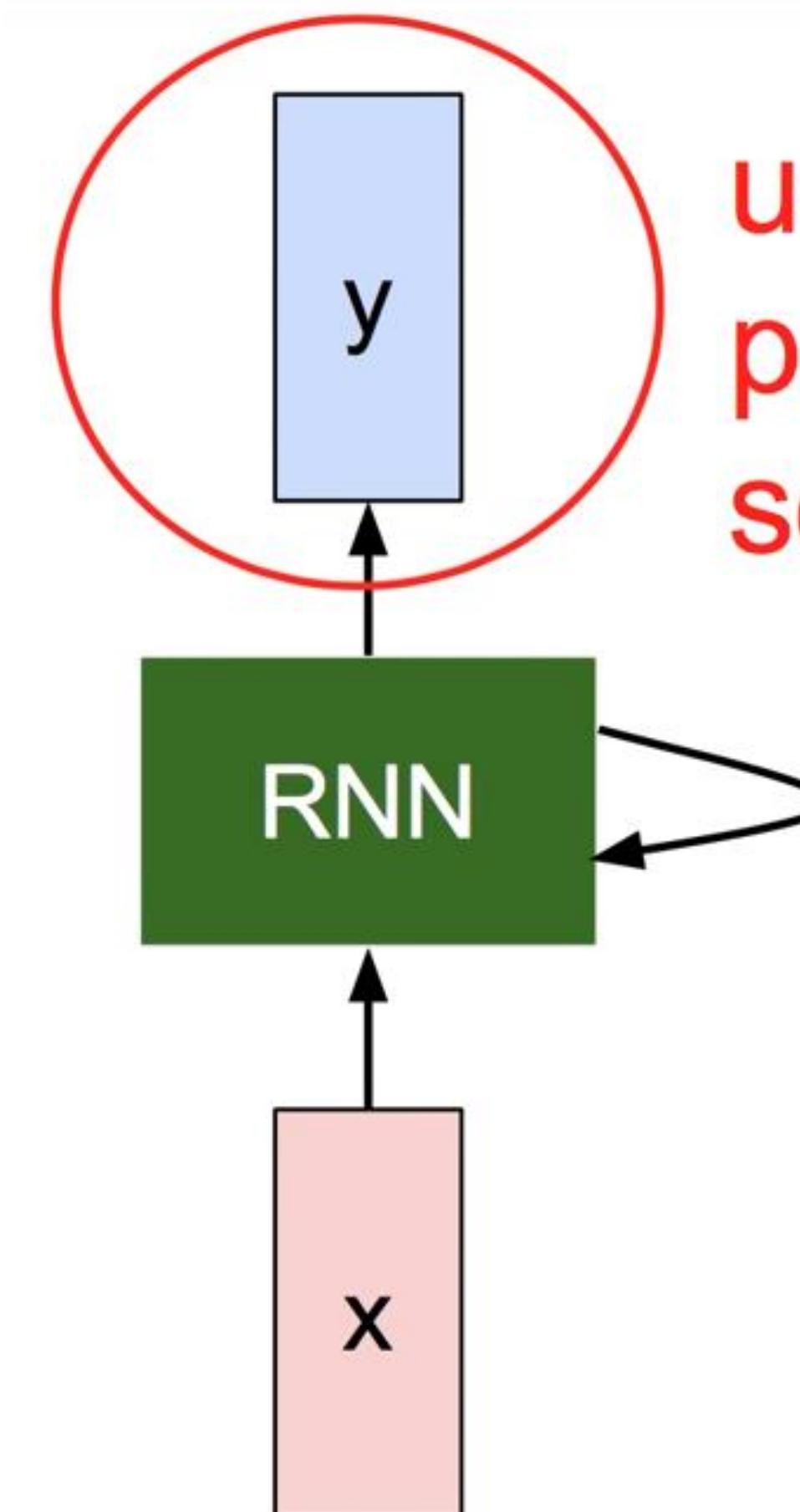
# Sequence data

- We don't understand one word only
- We understand based on the previous words
- NN/CNN cannot do this

# Sequence data



# Recurrent Neural Network



usually want to  
predict a vector at  
some time steps

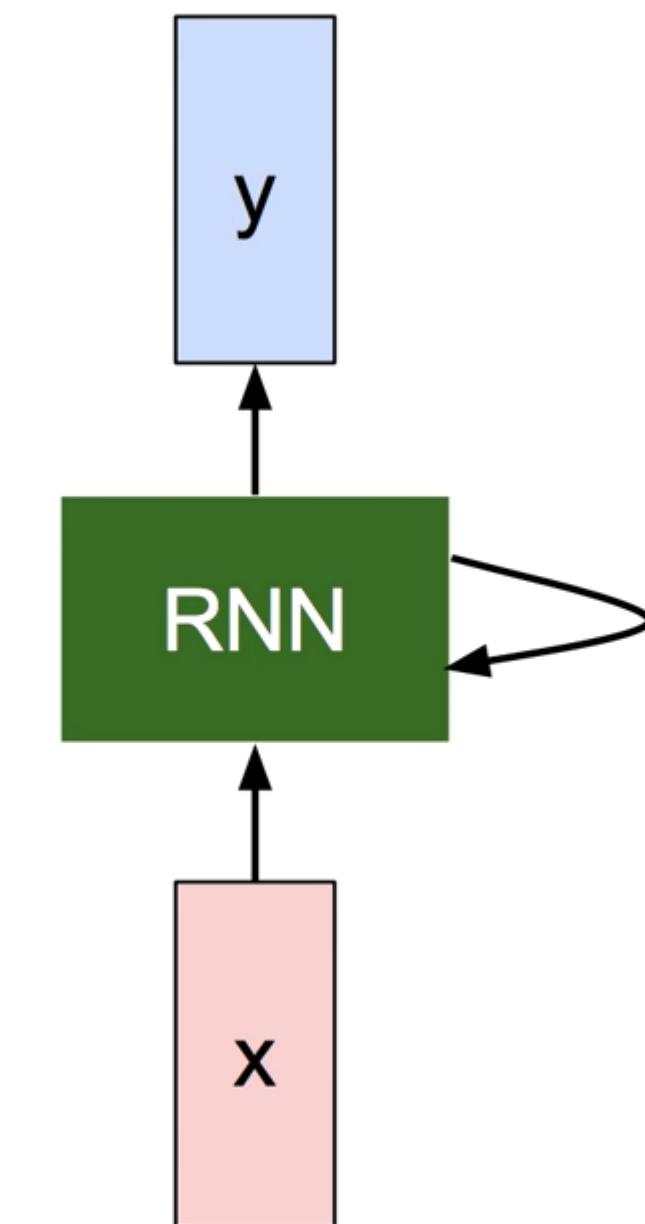
# Recurrent Neural Network

- We can process a sequence of vectors  $x$  by applying a recurrence formula at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$

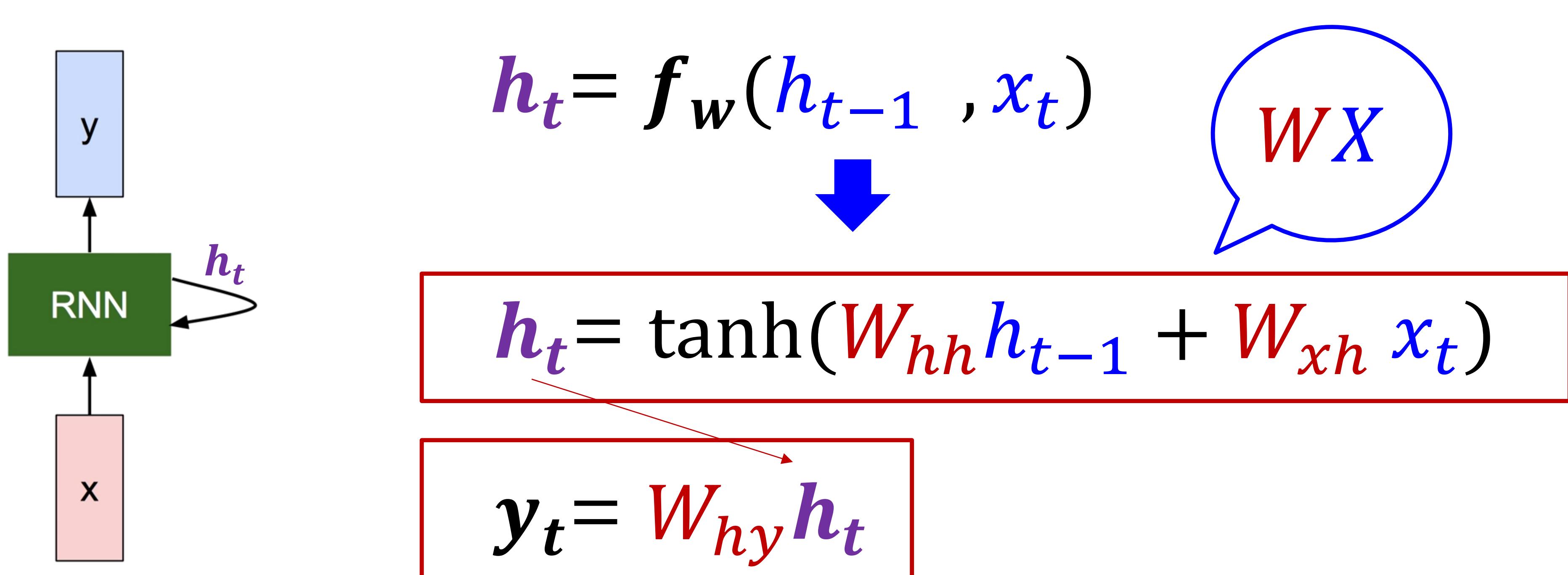
new state      /      old state      input vector at  
 some function      |      some time step

with parameters W



# (Vanilla) Recurrent Neural Network

- The state consists of a single “**hidden**” vector  $\mathbf{h}$ :

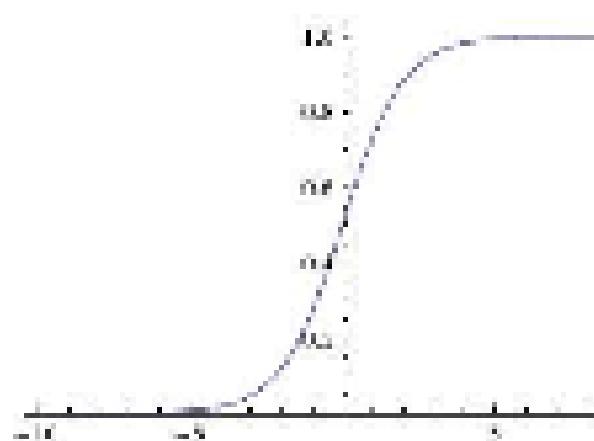


# Activation Functions

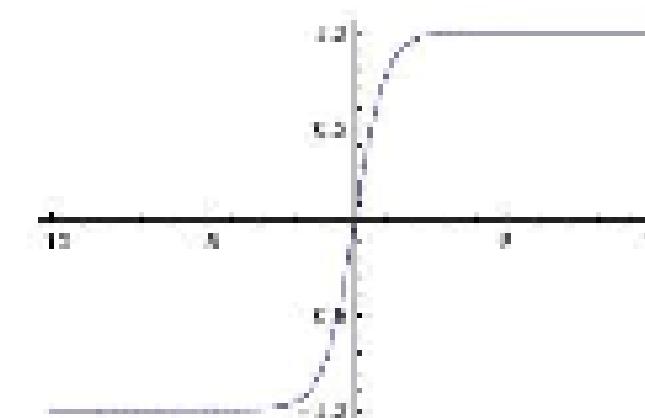
## Activation Functions

### Sigmoid

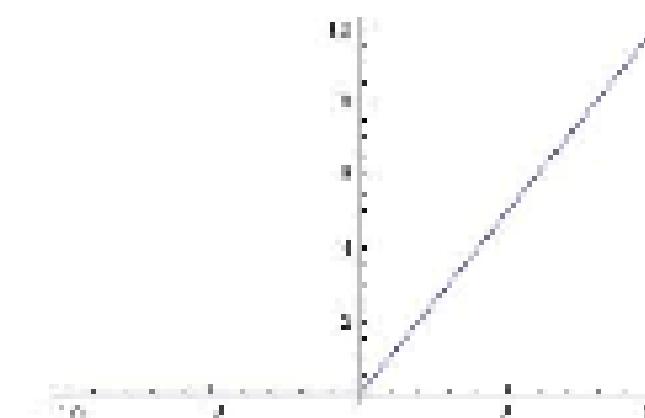
$$\sigma(x) = 1/(1 + e^{-x})$$



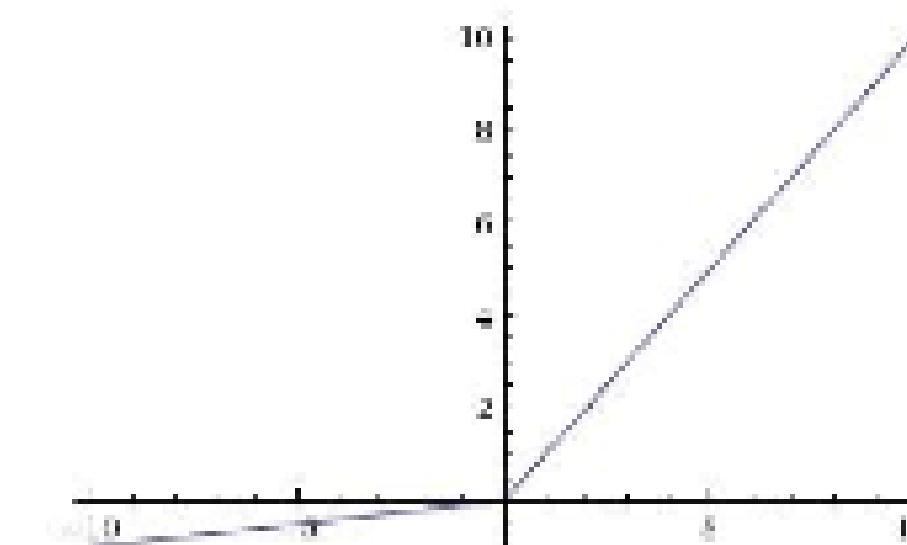
### tanh tanh(x)



### ReLU max(0,x)



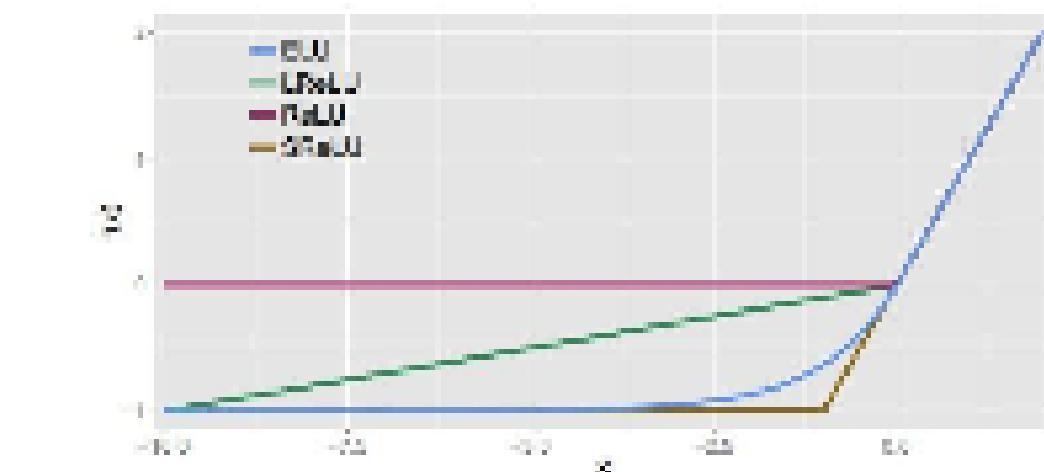
### Leaky ReLU max(0.1x, x)



### Maxout $\max(w_1^T x + b_1, w_2^T x + b_2)$

### ELU

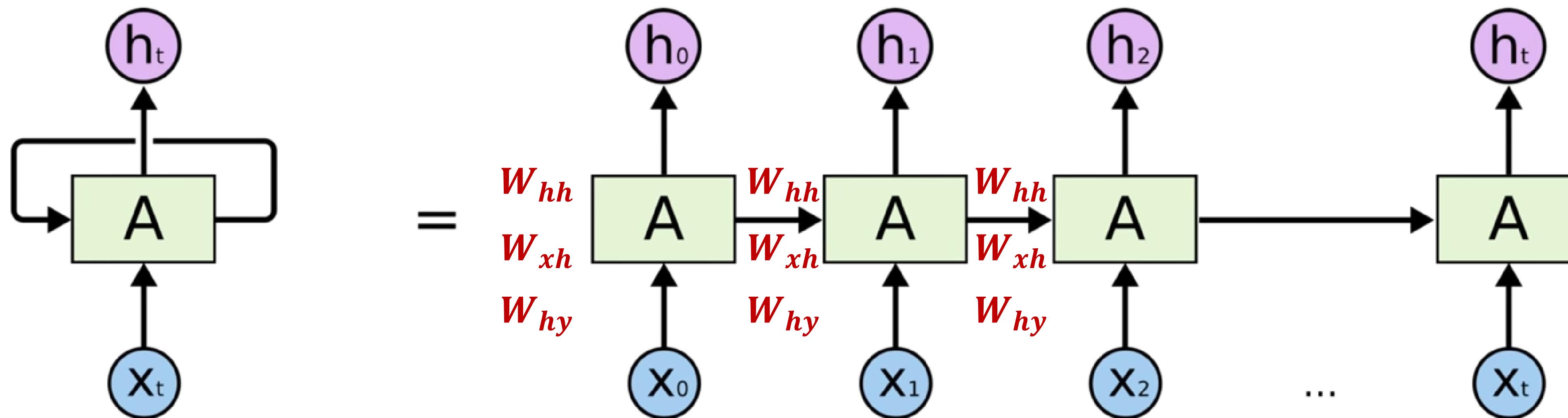
$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) - 1) & \text{if } x \leq 0 \end{cases}$$



# (Vanilla) Recurrent Neural Network

- Notice : **the same function and the same set of parameters**  
are used at every time step.

$W_{hh}$   
 $W_{xh}$   
 $W_{hy}$



# (Vanilla) Recurrent Neural Network

- Character-level language model example

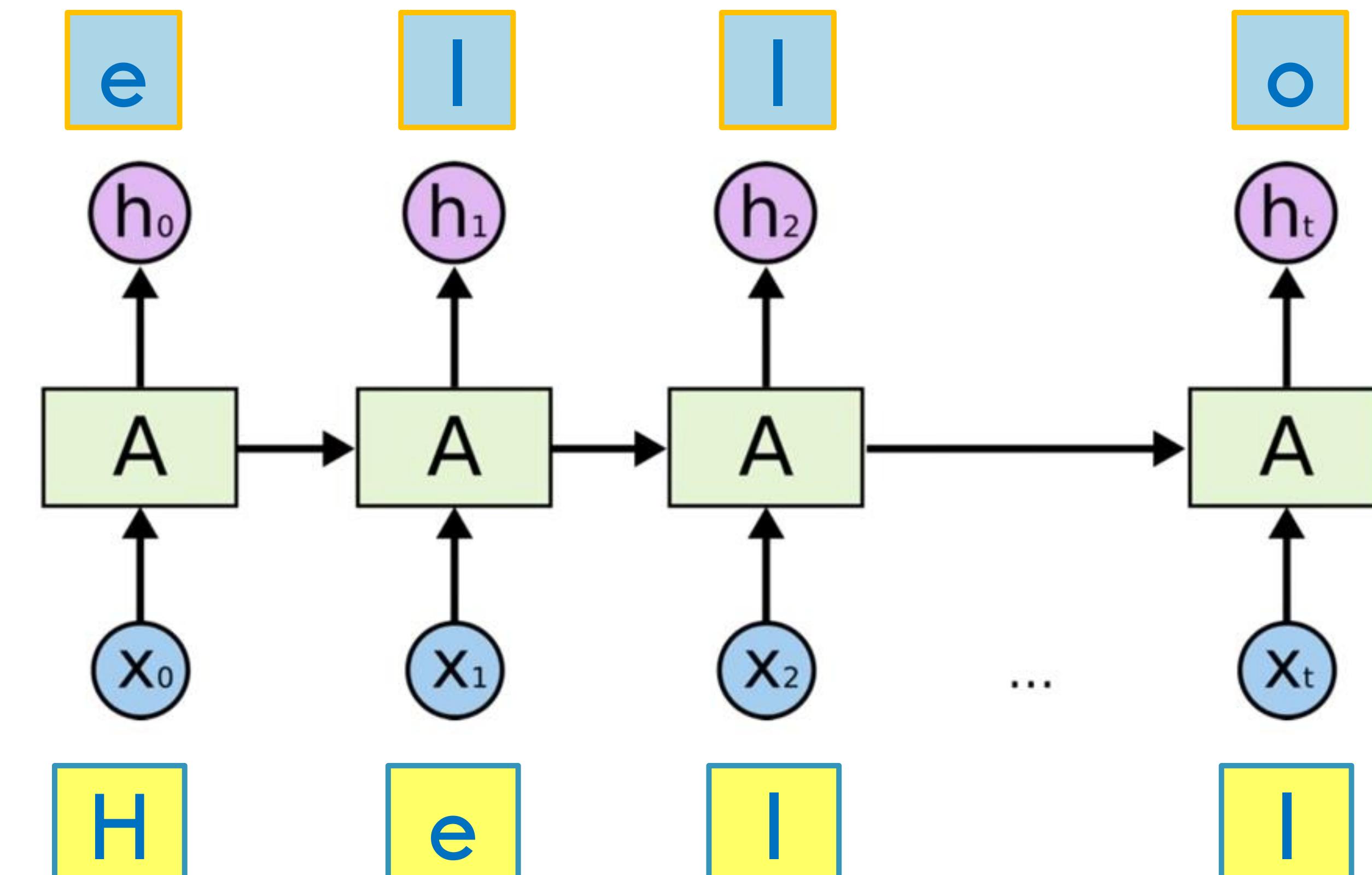
Vocabulary :

[h, e, l, o]

Example training

Sequence :

“hello”



# (Vanilla) Recurrent Neural Network

- Character-level language model example

Vocabulary :

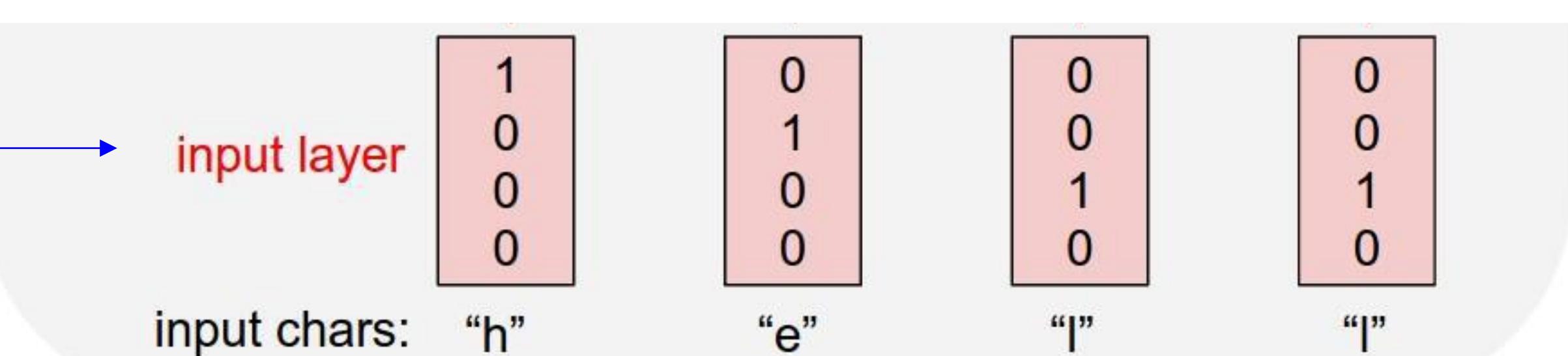
[h, e, l, o]

Example training

Sequence :

“hello”

one-hot encoding



# (Vanilla) Recurrent Neural Network

- # • Character-level language model example

# Vocabulary :

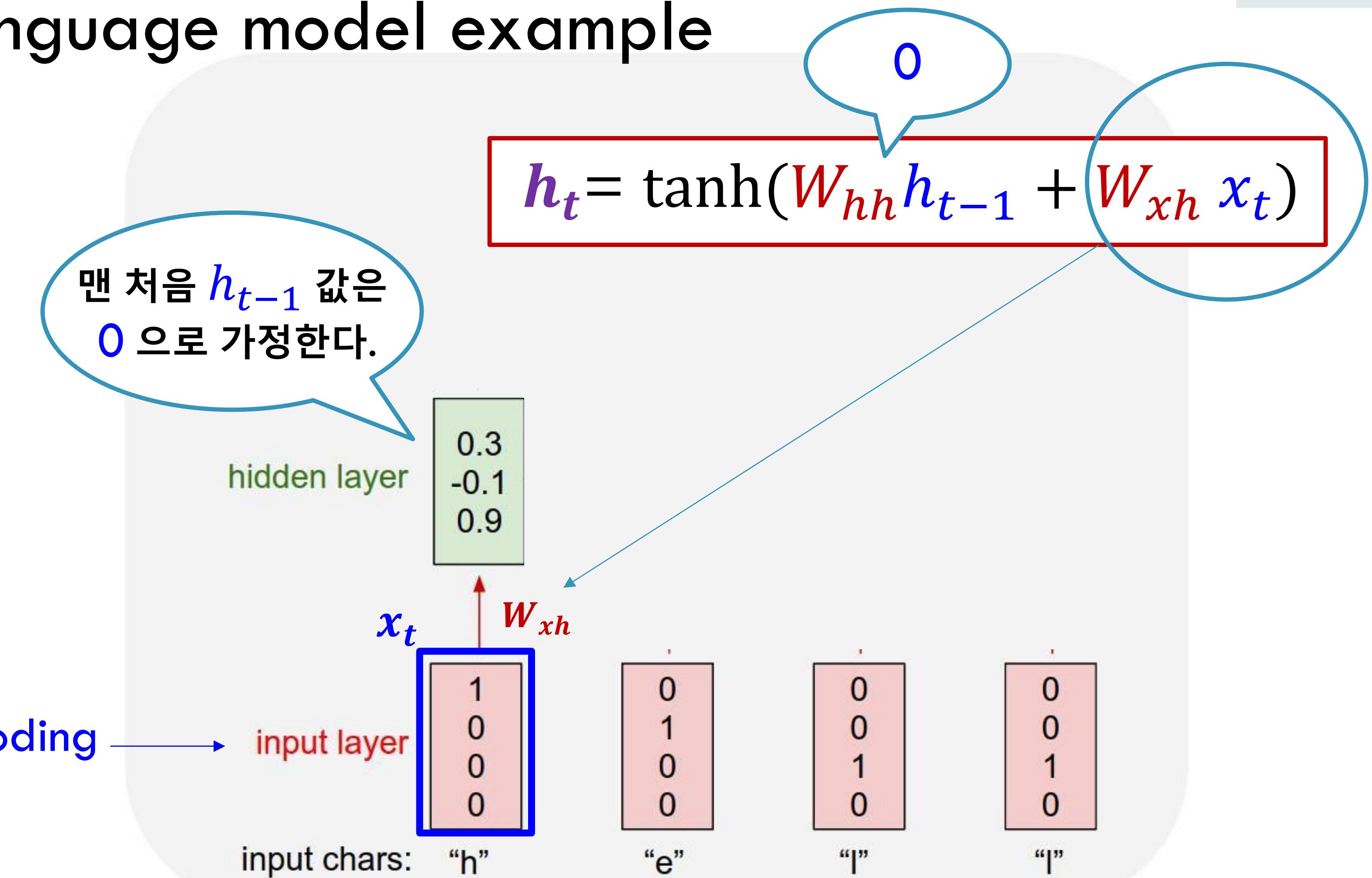
[h, e, l, o]

# Example training

# Sequence :

**“hello”**

one-hot encoding → input layer



# (Vanilla) Recurrent Neural Network

- Character-level language model example

Vocabulary :

[h, e, l, o]

Example training

Sequence :

“hello”

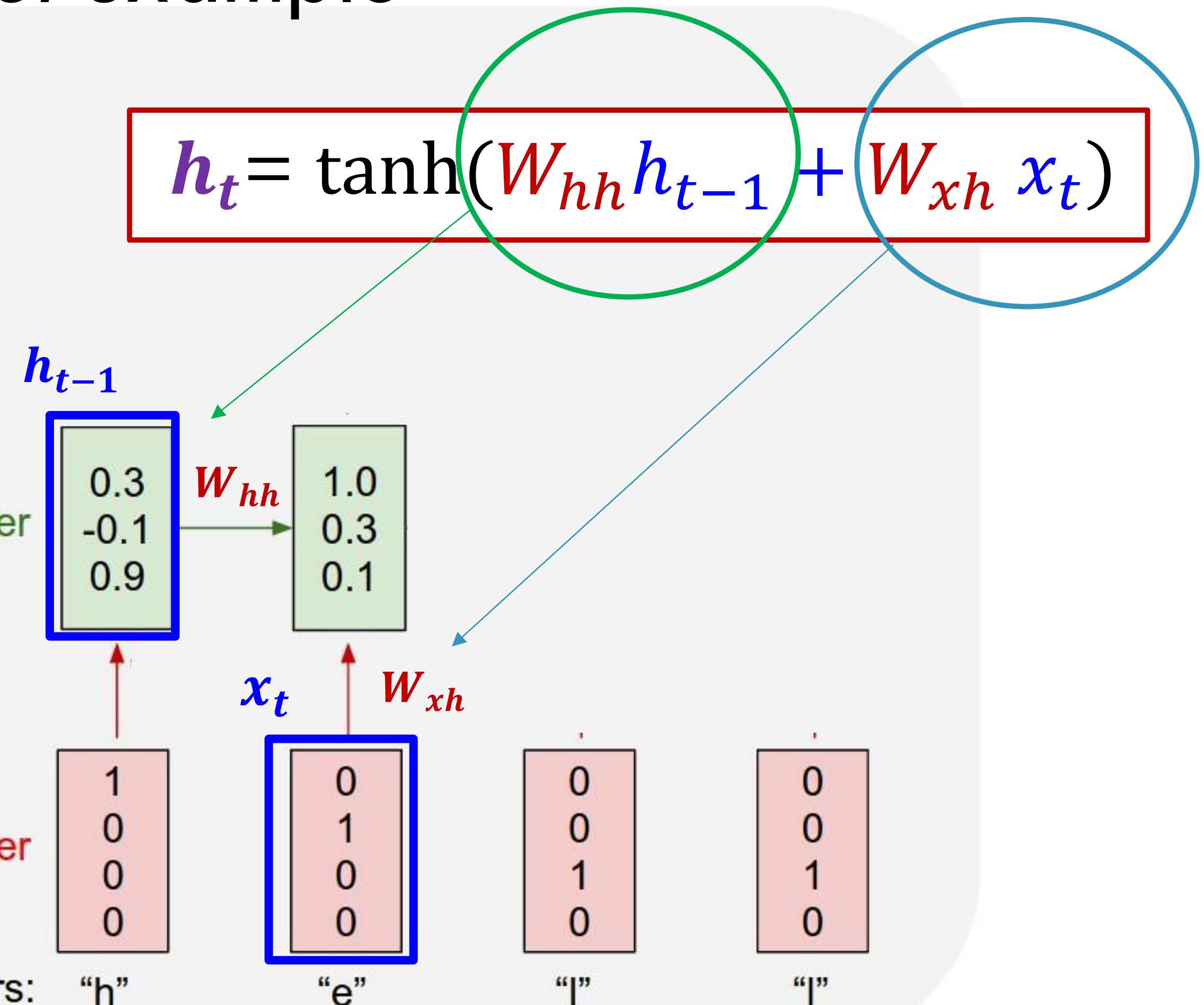
one-hot encoding → input layer

input chars: “h”

“e”

“l”

“l”



# (Vanilla) Recurrent Neural Network

- Character-level language model example

Vocabulary :

[h, e, l, o]

Example training

Sequence :

“hello”

one-hot encoding

input layer

input chars: “h”

0  
0  
0  
0

0  
1  
0  
0

0  
0  
1  
0

0  
0  
1  
0

hidden layer

0.3  
-0.1  
0.9

$h_{t-1}$

1.0  
0.3  
0.1

0.1  
-0.5  
-0.3

0  
0  
0  
0

0  
1  
0  
0

0  
0  
1  
0

0  
0  
1  
0

$W_{hh}$

$W_{xh}$

$$\mathbf{h}_t = \tanh(\mathbf{W}_{hh} \mathbf{h}_{t-1} + \mathbf{W}_{xh} \mathbf{x}_t)$$

# (Vanilla) Recurrent Neural Network

- Character-level language model example

Vocabulary :

[h, e, l, o]

Example training  
Sequence :  
“hello”

one-hot encoding → input layer

input chars: “h”

0  
1  
0  
0

0  
0  
1  
0

0  
0  
1  
0

0  
0  
1  
0

hidden layer

0.3  
-0.1  
0.9

1.0  
0.3  
0.1

0.1  
-0.5  
-0.3

-0.3  
0.9  
0.7

↑

↑

↑

0  
1  
0  
0

0  
0  
1  
0

0  
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1  
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0  
0  
1  
0

$h_{t-1}$

$x_t$

↓

$W_{hh}$

$W_{xh}$

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# (Vanilla) Recurrent Neural Network

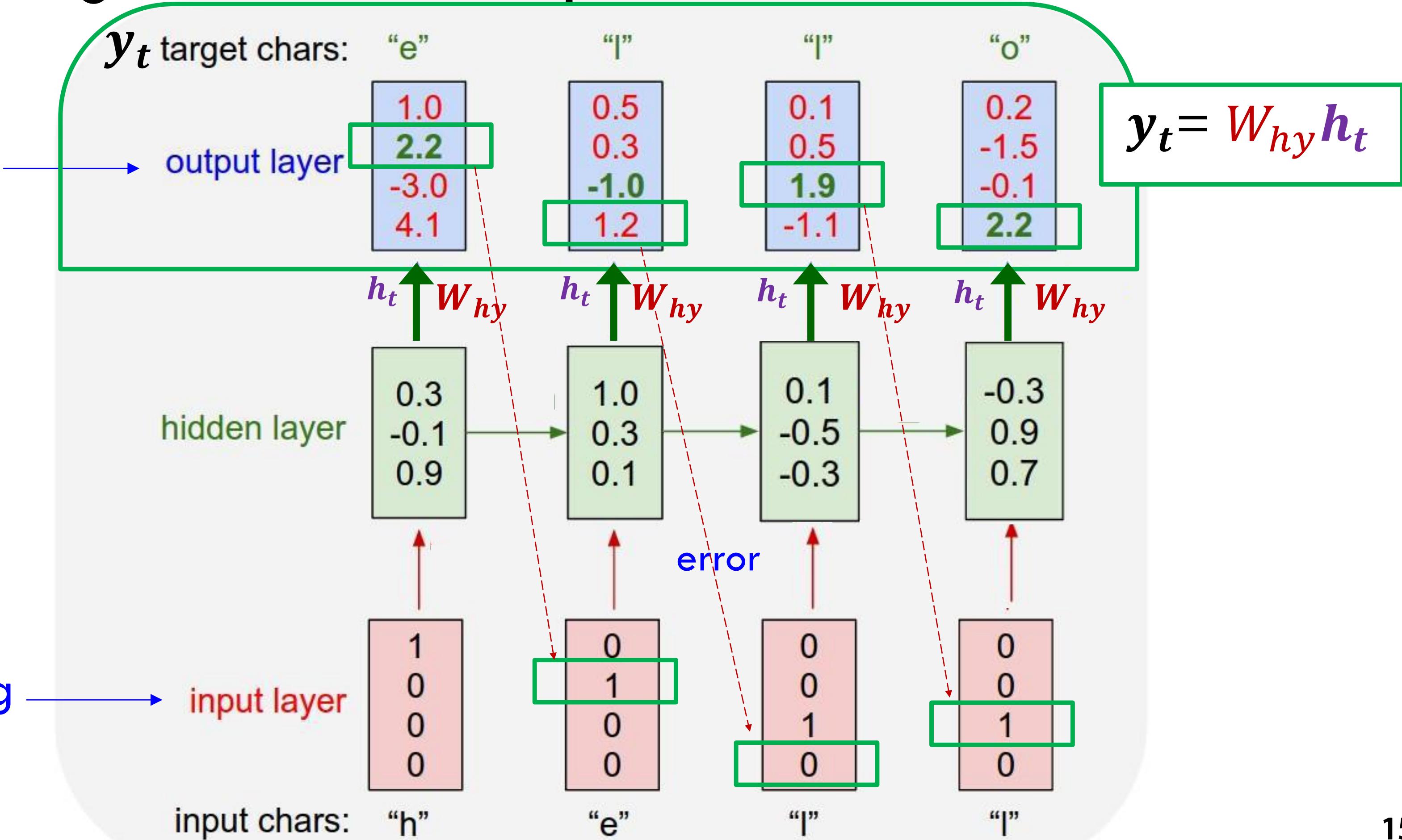
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- Character-level language model example

Vocabulary :  
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Sequence :  
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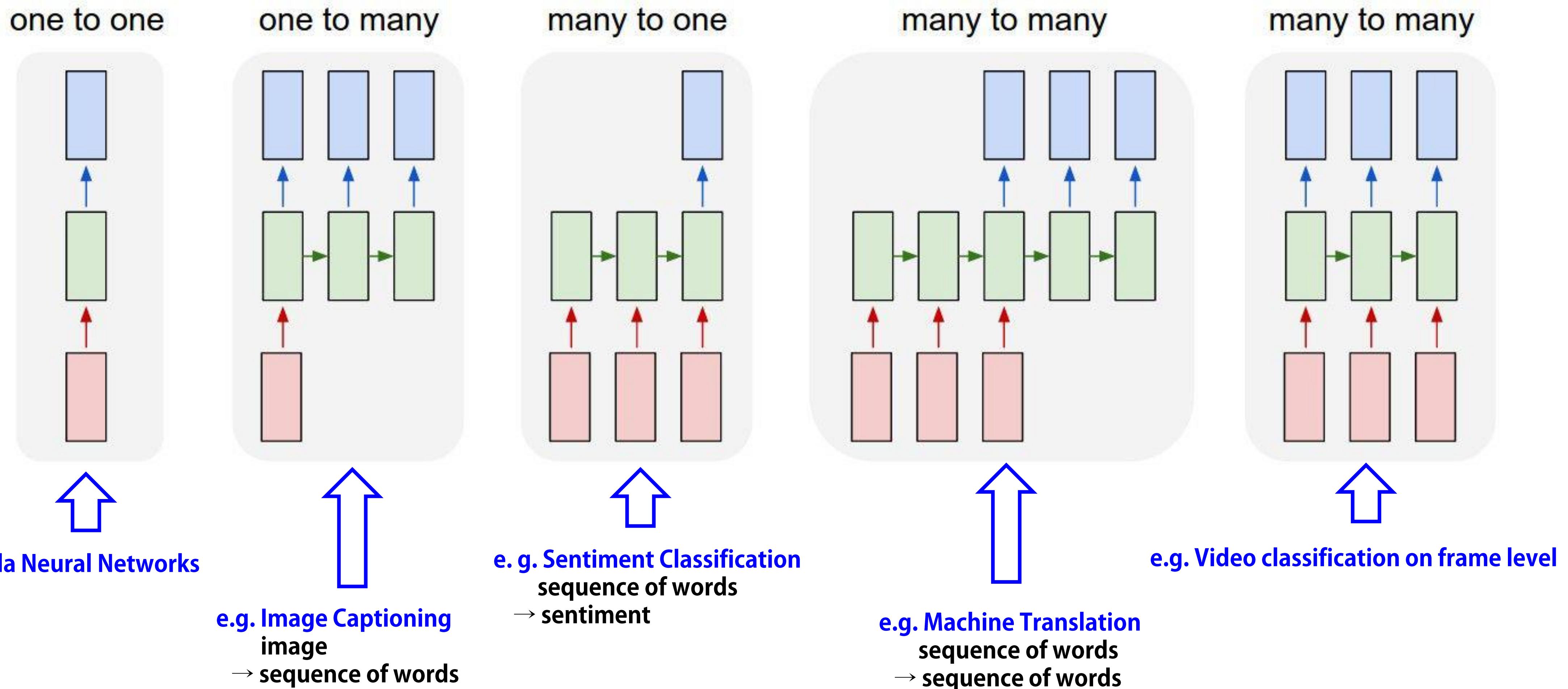
one-hot encoding



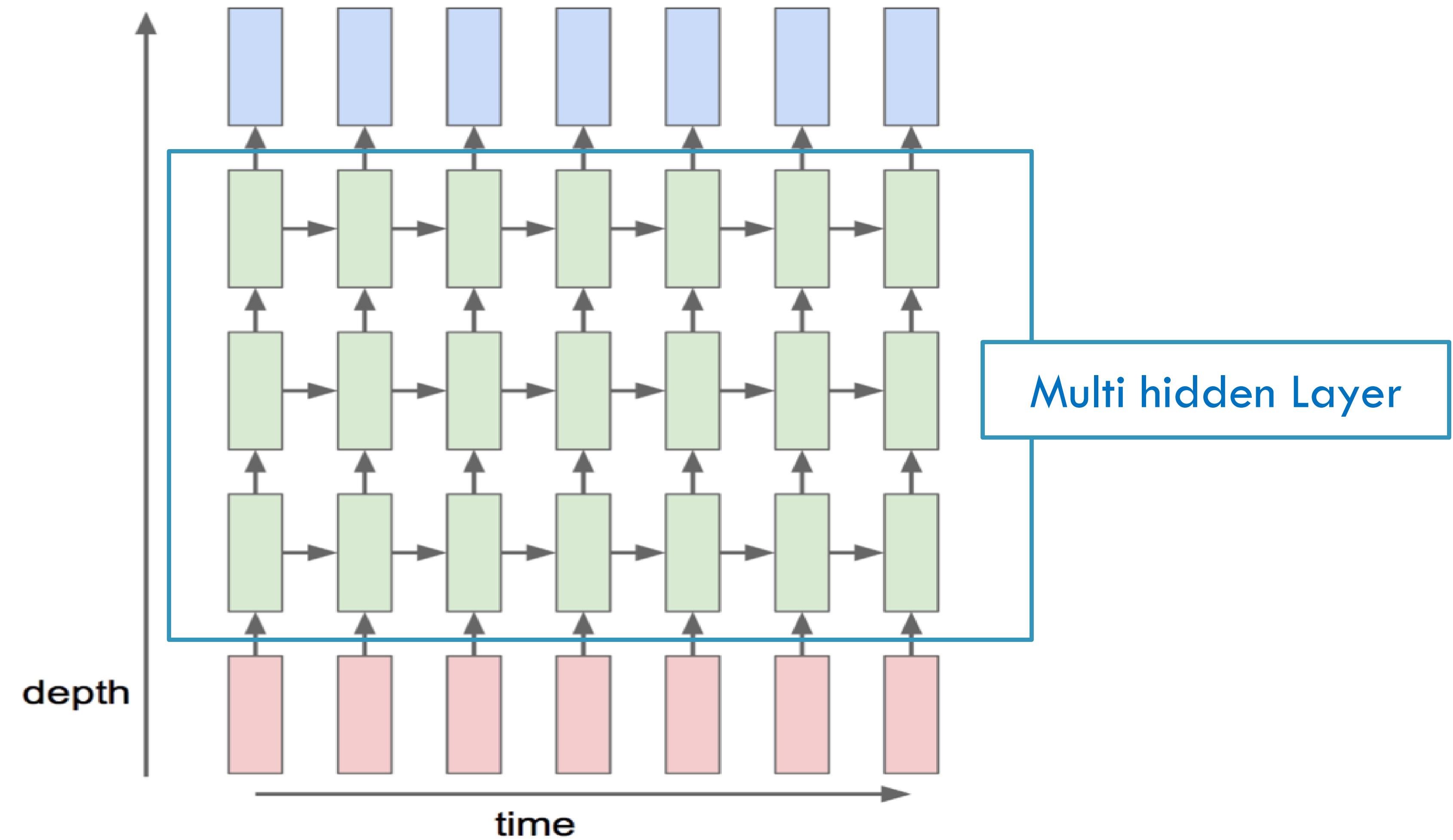
# RNN applications

- Language Modeling
- Speech Recognition
- Machine Translation
- Conversation Modeling / Question Answering
- Image / Video Captioning
- Image / Music / Dance Generation

# Recurrent Networks offer a lot of flexibility:



# Multi-Layer RNN



# Training RNNs is challenging

- Several advanced models
  - Long Short Term Memory ([LSTM](#))
  - [GRU](#) by Cho et al. 2014