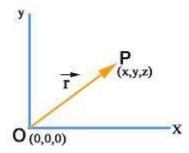
The vector form of a hyperplane is: $w^T x + w_0 = 0$

• **Vectors** can be interpreted as coordinates as well as a line segment from the origin to the coordinate.

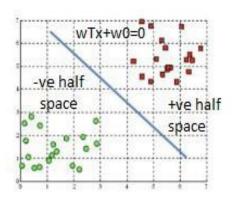
Where,
$$w=\begin{bmatrix}w_1\\w_2\\w_3\\.\\.\\.\\w_n\end{bmatrix}$$
 and, $x=\begin{bmatrix}x_1\\x_2\\x_3\\.\\.\\.\\x_n\end{bmatrix}$

For example, the below-given vector \overrightarrow{r} can be considered as coordinates of point P(x,y,z) as well as a line segment from the origin to point P(x,y,z).



 Half Spaces: In geometry, a half-space is either of the two parts into which a plane divides the three-dimensional Euclidean space.

Example: Let's assume that a hyperplane $w^T x + w_0 = 0$ is classifying the data points of two different classes in a space.



Let's say we got a point x_0 in the space.

Now, If:

$$w^Tx_0+w_0>0$$
 => The point is in the +ve halfspace
$$w^Tx_0+w_0<0$$
 => The point is in the -ve halfspace.

• The **transpose** operation changes a column vector into a row vector and vice versa. For example,

$$\text{if}\quad \vec{a}=\begin{bmatrix}a_1\\a_2\\a_3\\.\\.\\.\\a_n\end{bmatrix} \qquad \text{then,}\quad \overrightarrow{a}^T=\begin{bmatrix}a_1&a_2&a_3&.&.&.&a_n\end{bmatrix}$$

• The dot product of two vectors \overrightarrow{a} and \overrightarrow{b} is given as :

$$\overrightarrow{a}$$
. \overrightarrow{b} = $a_1b_1 + a_2b_2 + a_3b_3 + ... + a_nb_n$

Where,
$$\vec{a}=\begin{bmatrix}a_1\\a_2\\a_3\\.\\.\\.\\a_n\end{bmatrix}$$
 and $\vec{b}=[b_1\ b_2\ b_3\ .\ .\ .\ b_n]$

Also,
$$\overrightarrow{a}.\overrightarrow{b}=\overrightarrow{b}.\overrightarrow{a}$$

Geometrically, it is the product of the magnitudes of the two vectors and the cosine of the angle between them.

i.e.
$$\overrightarrow{a}.\overrightarrow{b} = |\overrightarrow{a}|.|\overrightarrow{b}|.cos(\theta)$$

where $\boldsymbol{\theta}$ is the angle between the two vectors.

If the dot product of two vectors is **zero**, then the vectors are **perpendicular** to each other.

A unit vector is a vector that has a magnitude of 1.
To convert a vector into a unit vector, we divide the vector by its magnitude.

i.e. unit vector =
$$\widehat{u} = \frac{\overrightarrow{u}}{||\overrightarrow{u}||}$$

- → We can multiply any scalar value with the unit vector to get the desired magnitude (equal to that scalar value) in the same direction.
- → All vectors with the same unit vector are parallel
- **Distance between two points** having coordinates (x_1, y_1) and (x_2, y_2) in an x-y plane is given as:

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

 Norm or Magnitude of a vector is calculated by taking the square root of dot product with itself.

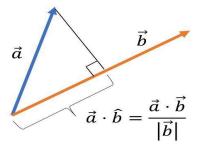
i.e.
$$||\overrightarrow{a}|| = \sqrt{\overrightarrow{a} \cdot \overrightarrow{a}}$$

It represents the **length** of a vector or **distance** of \overrightarrow{d} coordinate from the origin.

• Angle between two vectors is given as :

$$\theta = \cos^{-}\left(\frac{\overrightarrow{a}.\overrightarrow{b}}{||\overrightarrow{a}||.||\overrightarrow{b}||}\right)$$

• Projection of vector \overrightarrow{a} on $\overrightarrow{b} = \frac{\overrightarrow{a} \cdot \overrightarrow{b}}{||b||}$



• At the **point of intersection** of two lines, both lines will have the same coordinates. **Example**:

Let's say we have two lines, y = x+2 and y = 2x+1. We need to find the point of intersection of these two lines.

We assume that the lines intersect at a single point (a,b). Therefore, this point will satisfy both the line's equations.

i.e.
$$b = a+2$$
 — i) $b = 2a+1$ — ii)

Solving the above two equations, we get a = 1 and b = 3.

Therefore, the given two lines intersect at the point (1,3).