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# Convolutional Neural Networks

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Convolution, LeNet, AlexNet, VGGNet,  
GoogleNet, Resnet, Deconvolution

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Feb 1, 2017  
Aaditya Prakash

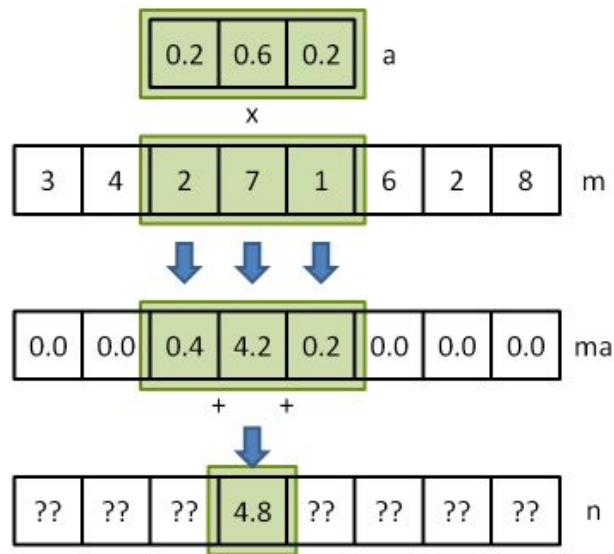
# Convolution

|                 |                 |                 |   |   |
|-----------------|-----------------|-----------------|---|---|
| 1 <sub>x1</sub> | 1 <sub>x0</sub> | 1 <sub>x1</sub> | 0 | 0 |
| 0 <sub>x0</sub> | 1 <sub>x1</sub> | 1 <sub>x0</sub> | 1 | 0 |
| 0 <sub>x1</sub> | 0 <sub>x0</sub> | 1 <sub>x1</sub> | 1 | 1 |
| 0               | 0               | 1               | 1 | 0 |
| 0               | 1               | 1               | 0 | 0 |

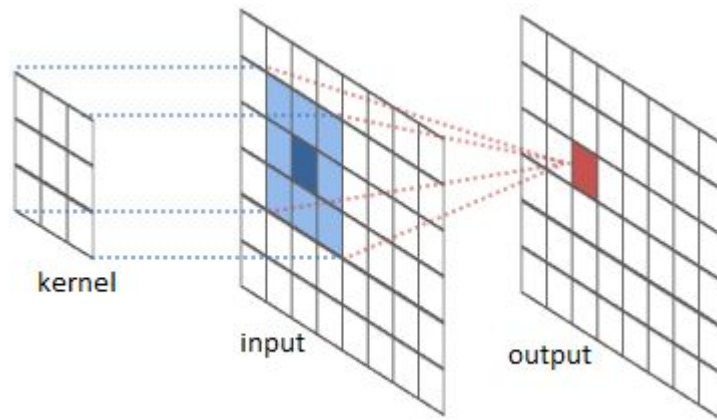
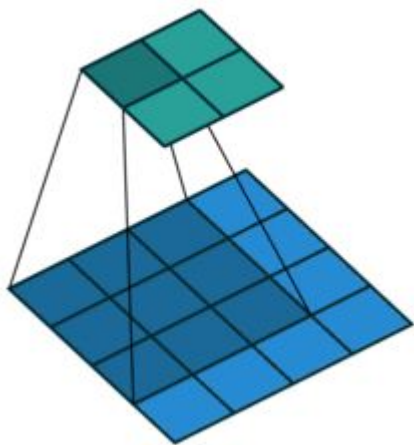
Image

|   |  |  |
|---|--|--|
| 4 |  |  |
|   |  |  |
|   |  |  |

Convolved  
Feature



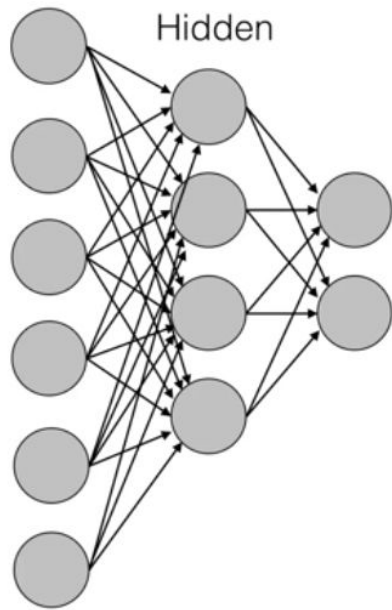
# Convolution



# Demo Convolution

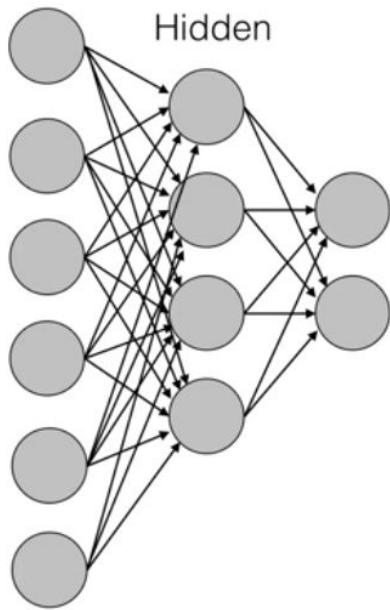
# Convolution in Neural Networks

Input

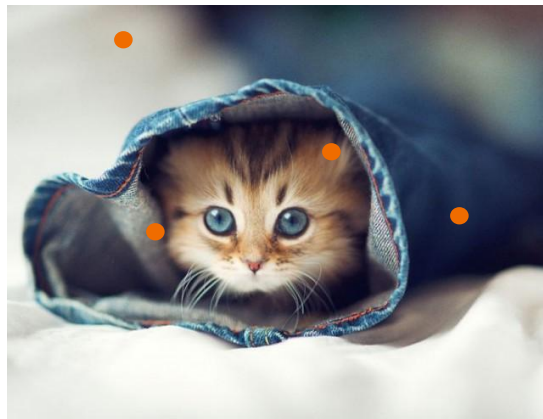
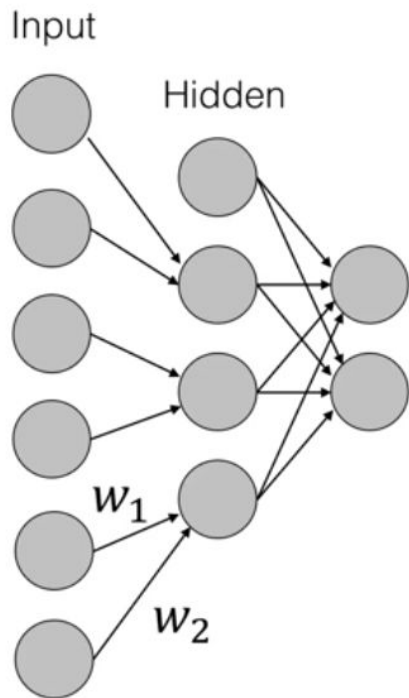


# Convolution in Neural Networks

Input

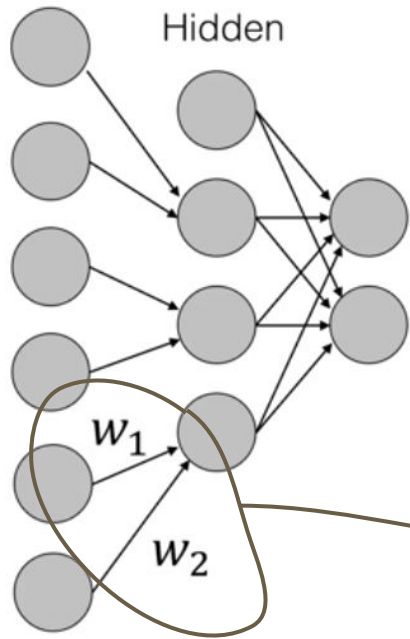


# Convolution in Neural Networks



# Convolution in Neural Networks

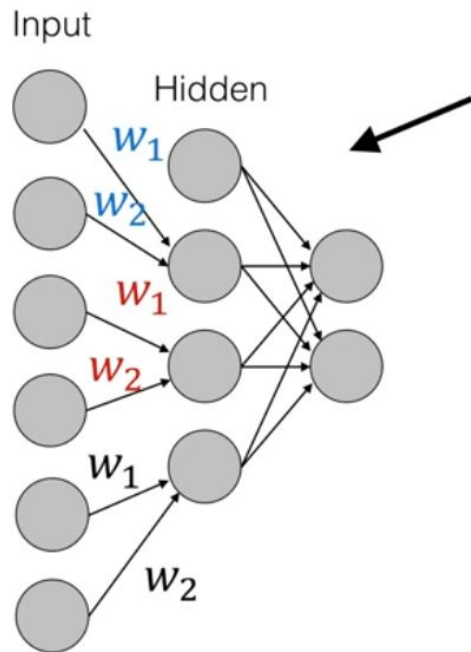
Input



$$y = w_1x_1 + w_2x_2$$



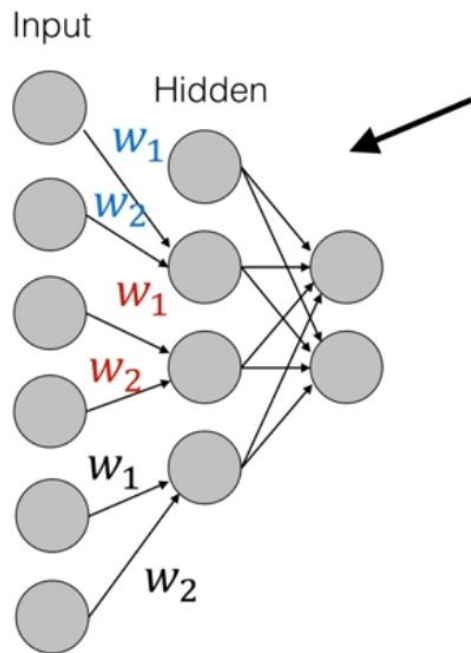
# Stride 1-D



1-d convolution with

- filters: 1
- filter size: 2
- stride: 2

# Stride 1-D

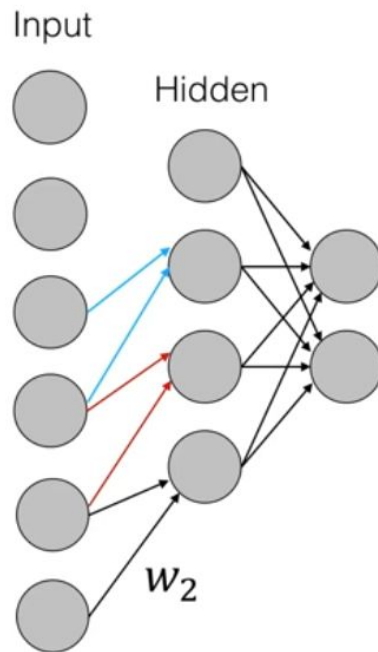


1-d convolution with

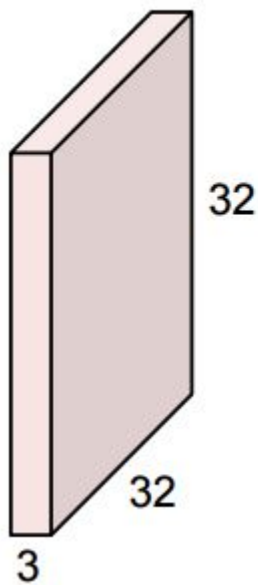
- filters: 1
- filter size: 2
- stride: 2

1-d convolution with

- filters: 1
- filter size: 2
- stride: **1**



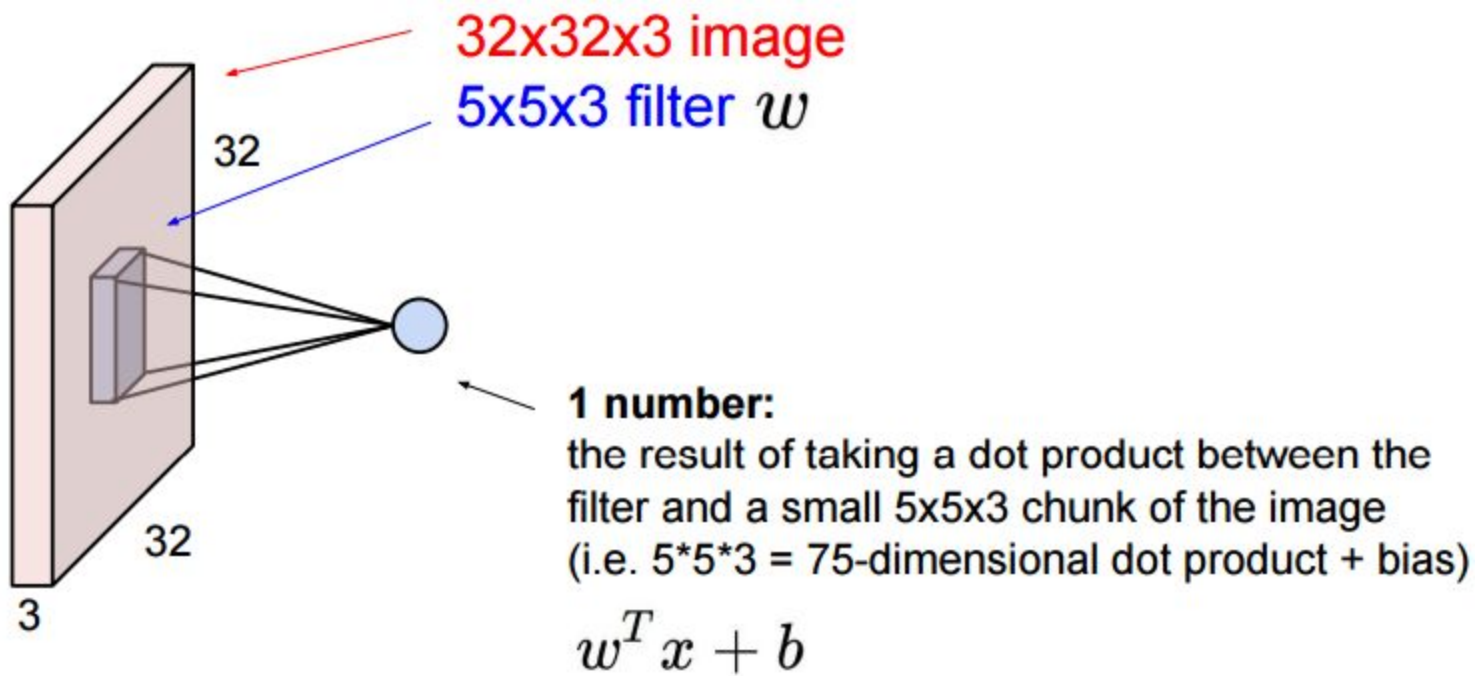
32x32x3 image

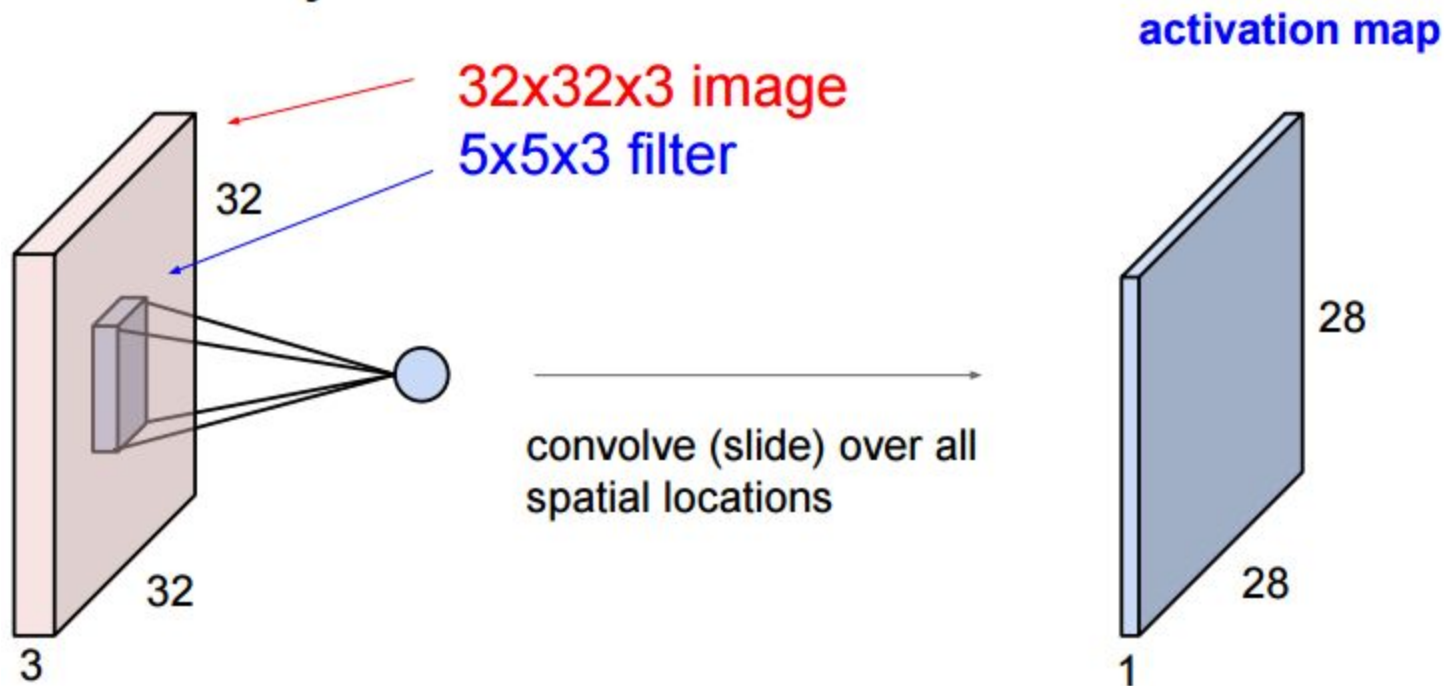


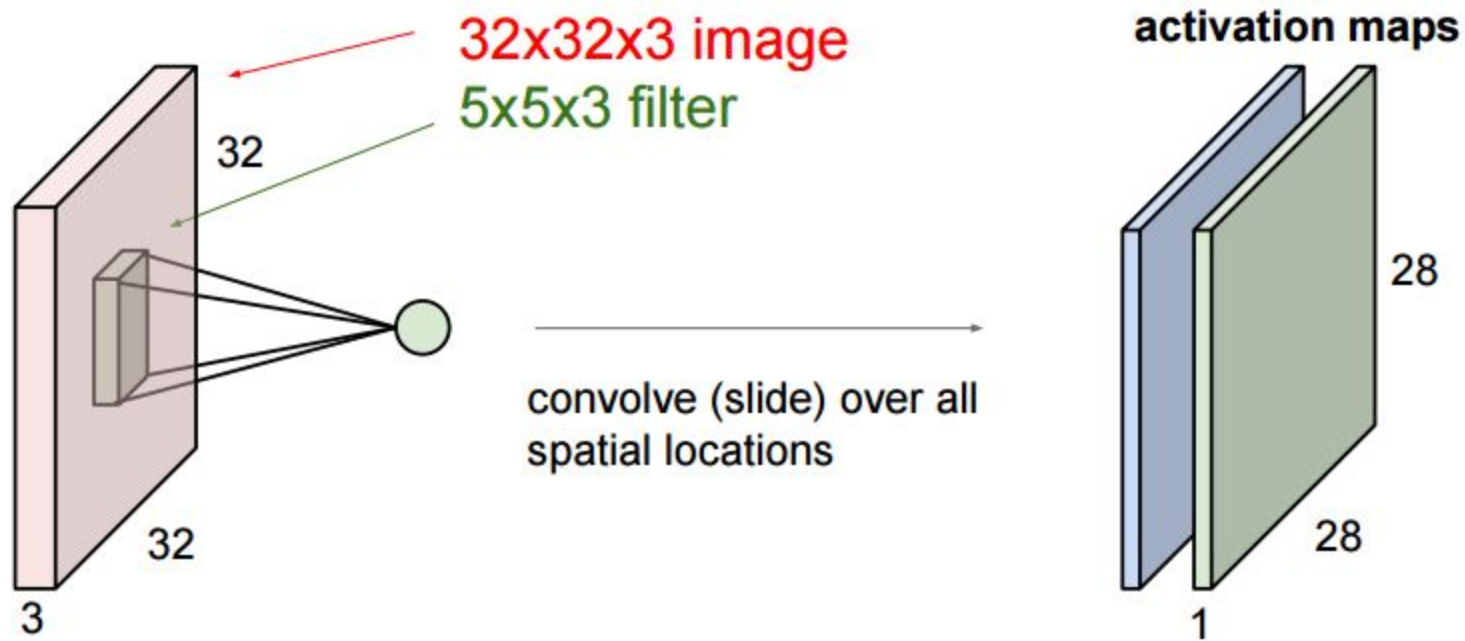
5x5x3 filter



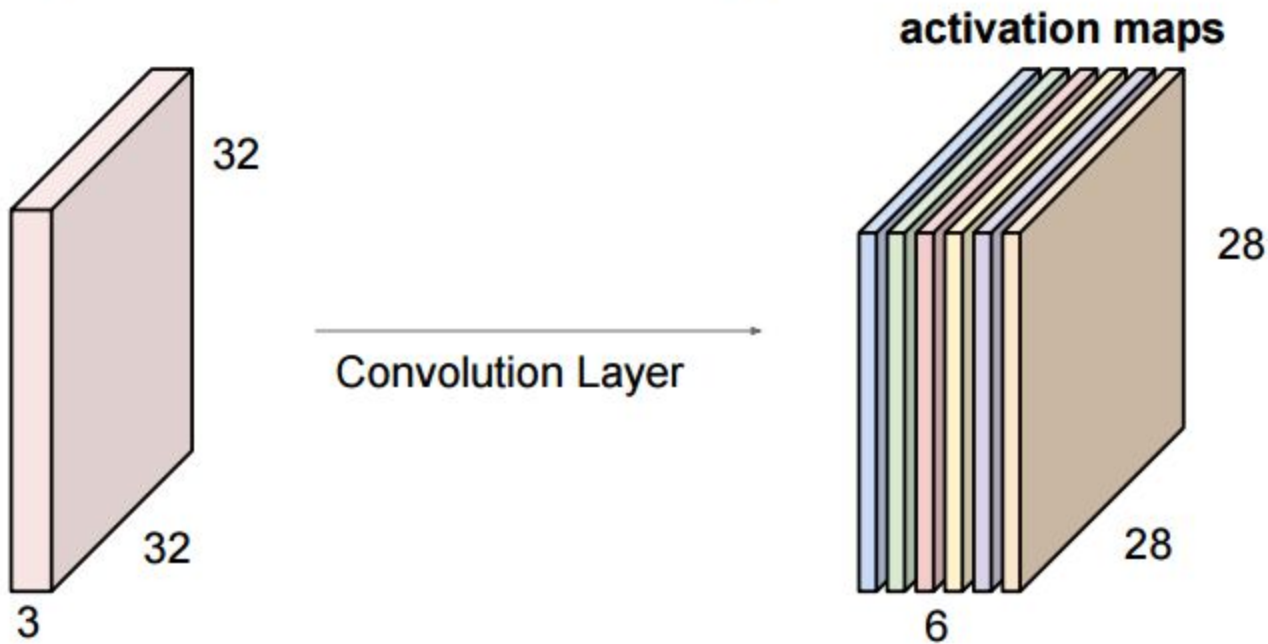
**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”



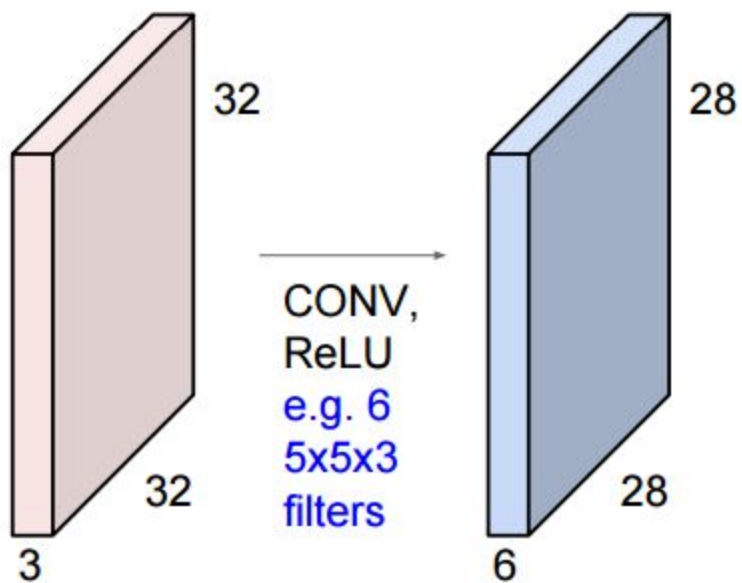




For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

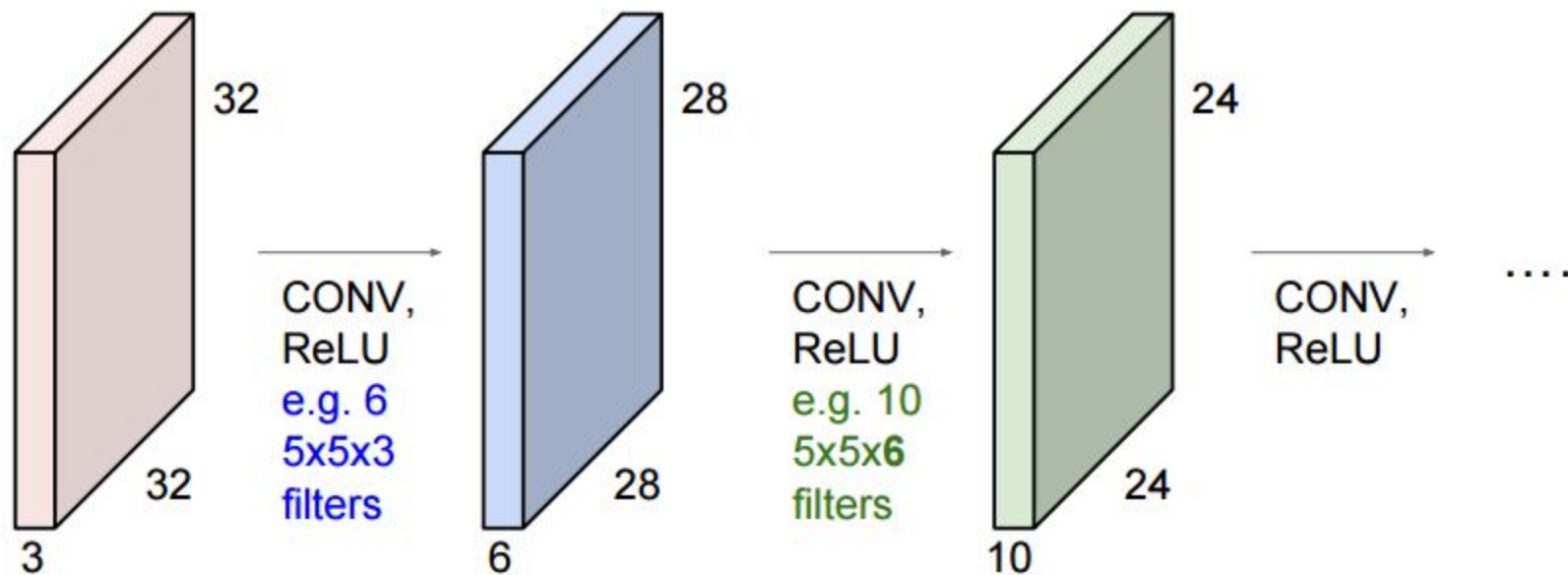


**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions

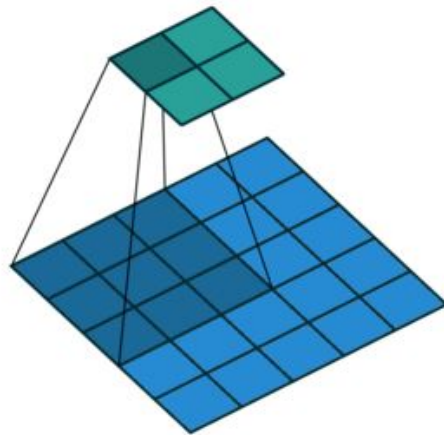
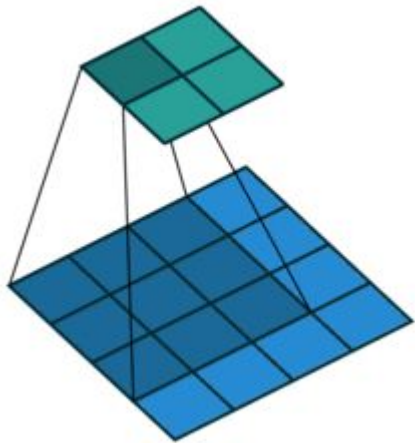




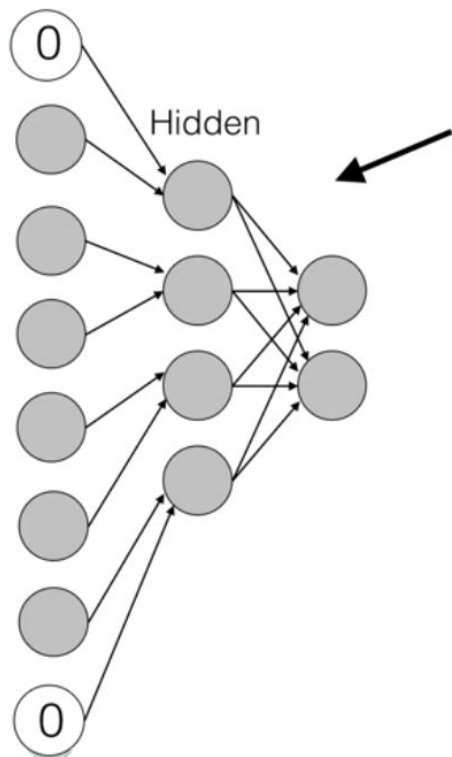
**Preview:** ConvNet is a sequence of Convolutional Layers, interspersed with activation functions



# Stride 2-D

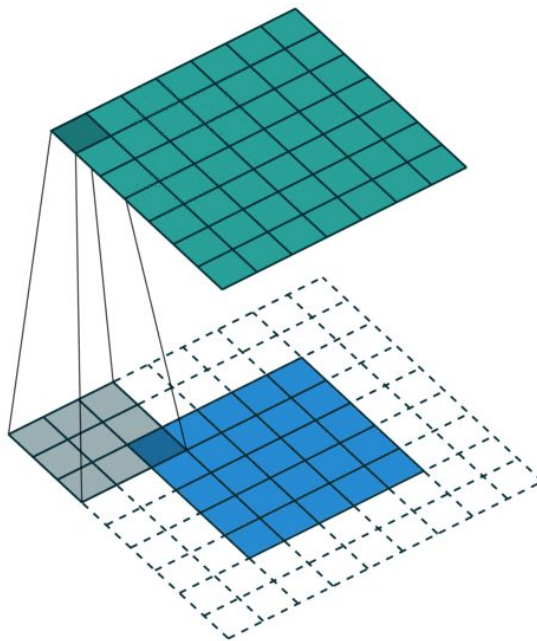


# Padding

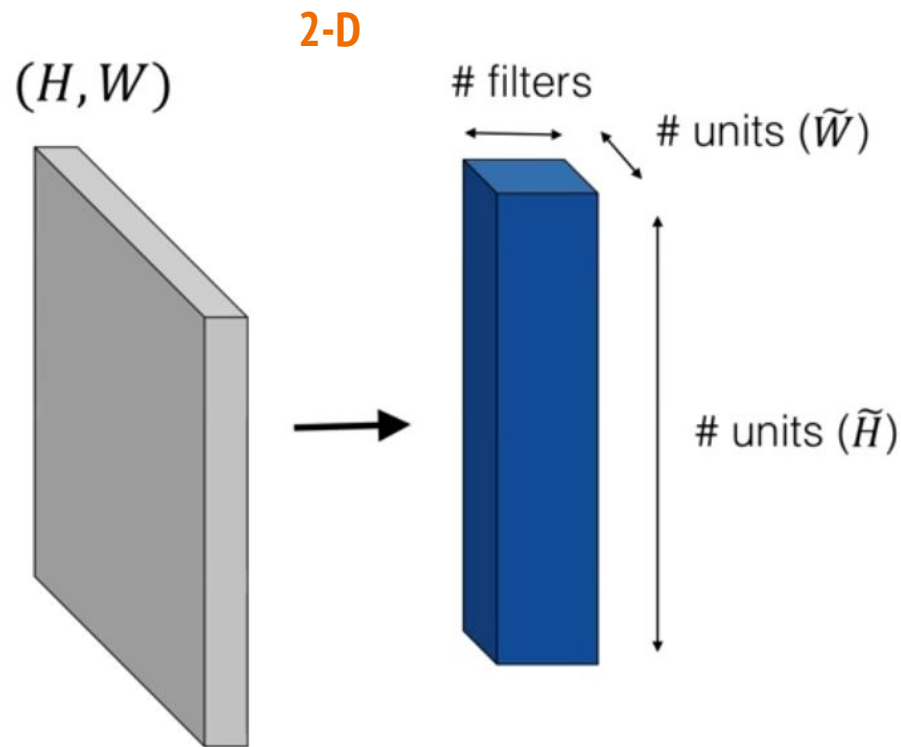
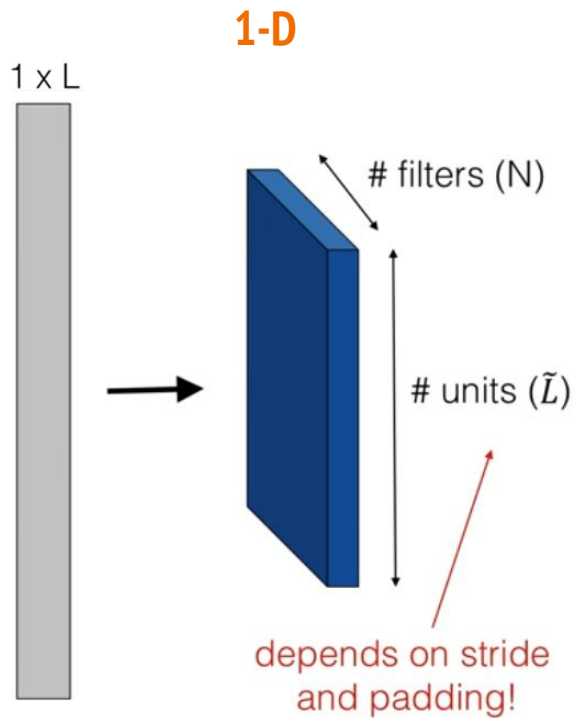


1-d convolution with

- filters: 1
- filter size: 2
- stride: 2
- padding: 1

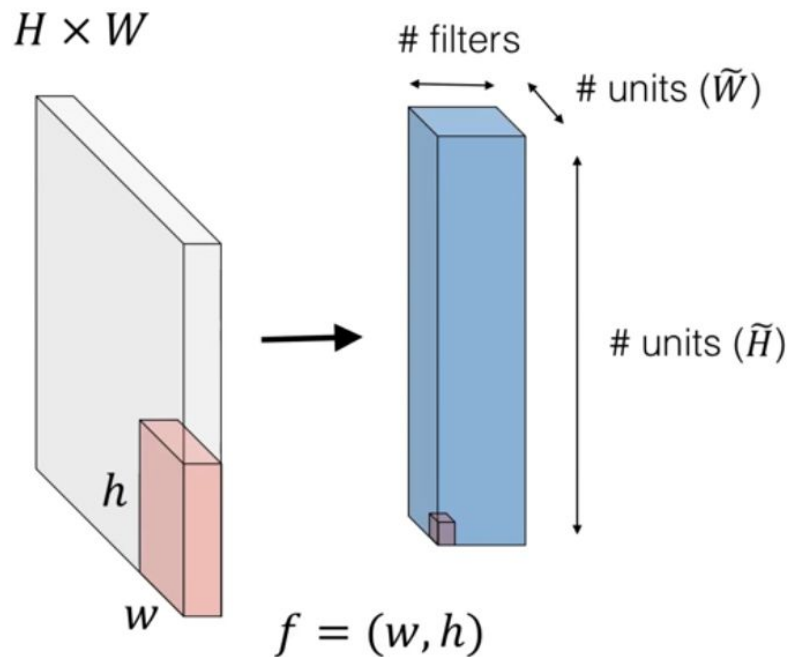


# Features / Filters



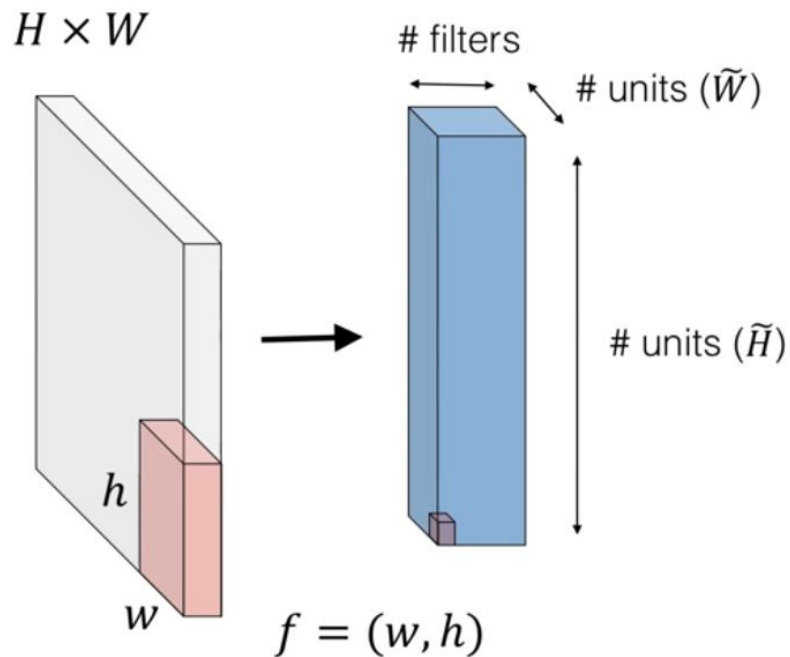
# Features / Filters

2-D

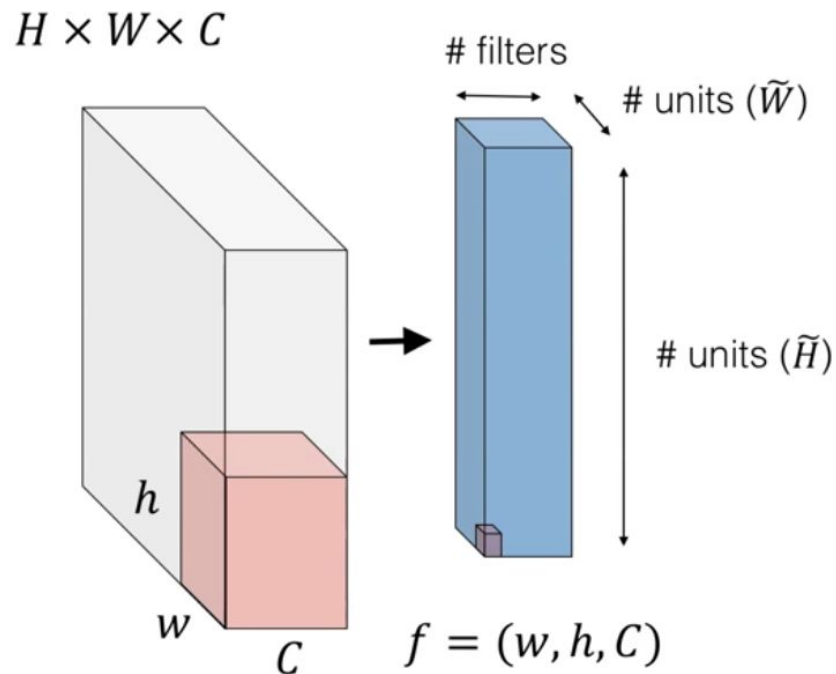


# Features / Filters

2-D

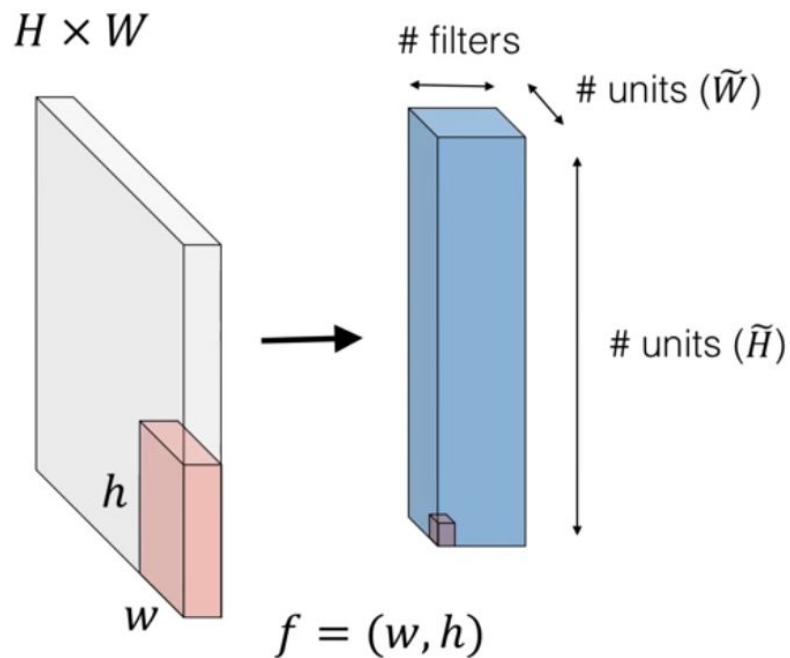


3-D

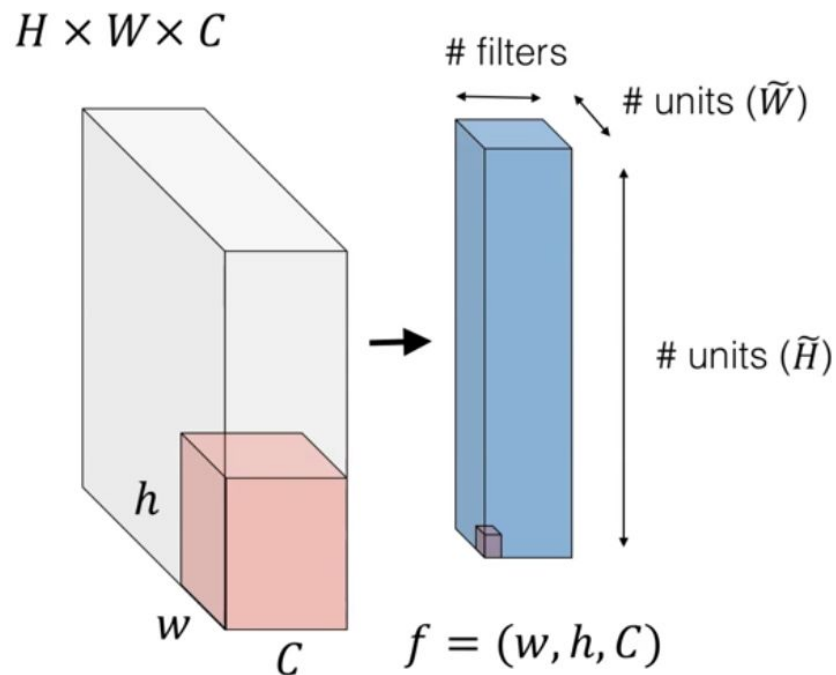


# Features / Filters

## 2-D



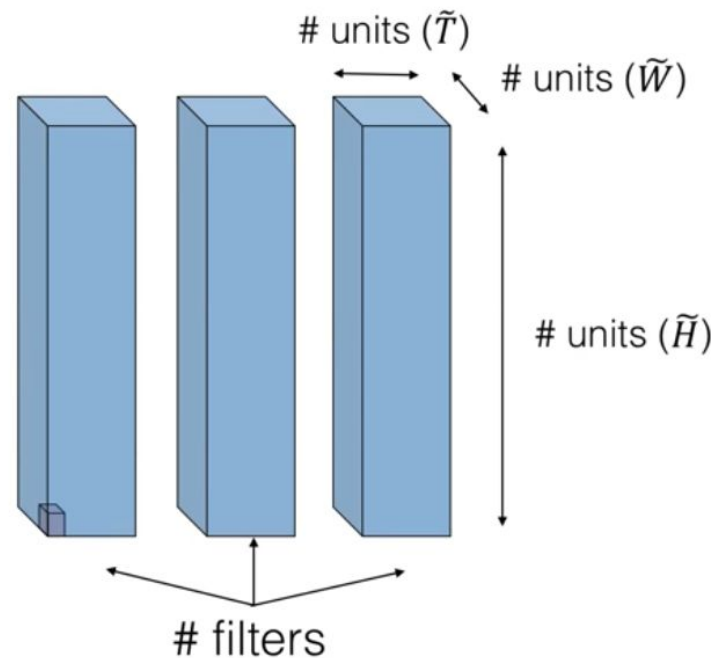
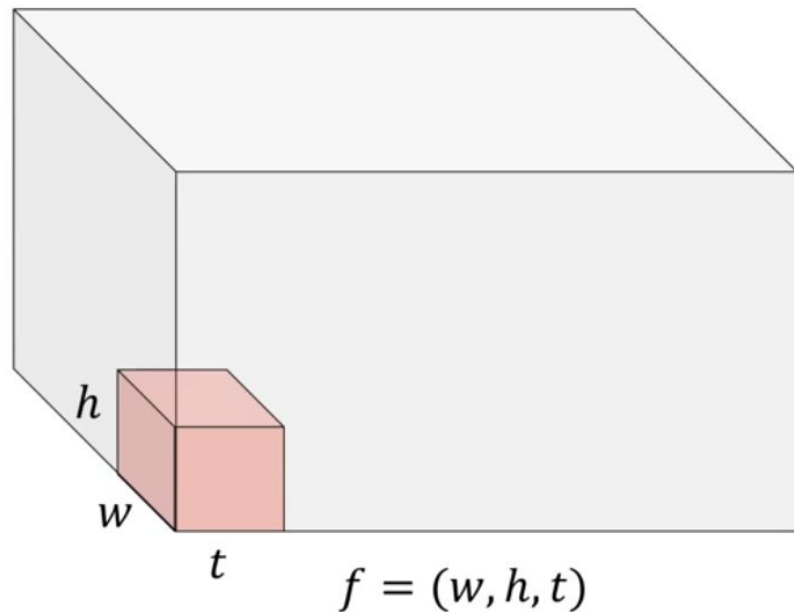
## 3-D 2-D Multichannel



# Features / Filters

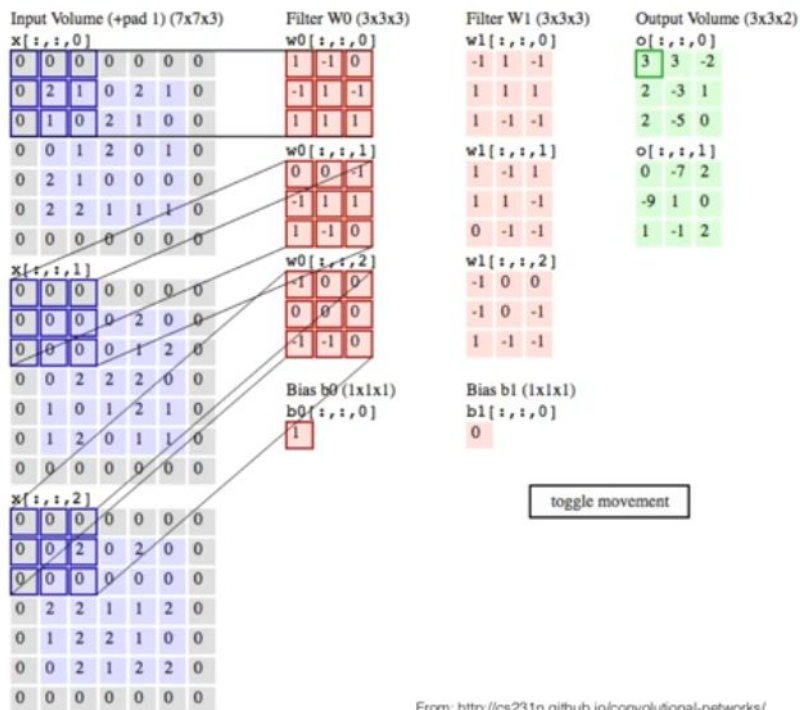
3-D

$H \times W \times T$



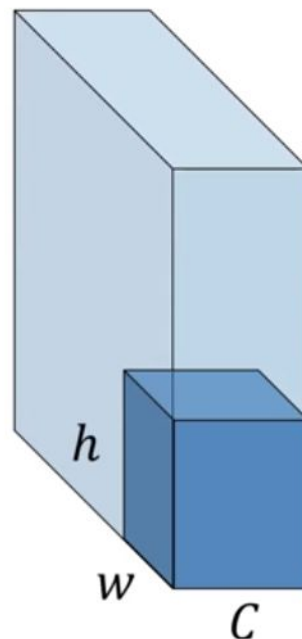


# 2-D Convolution



From: <http://cs231n.github.io/convolutional-networks/>

$H \times W \times C$



# filters

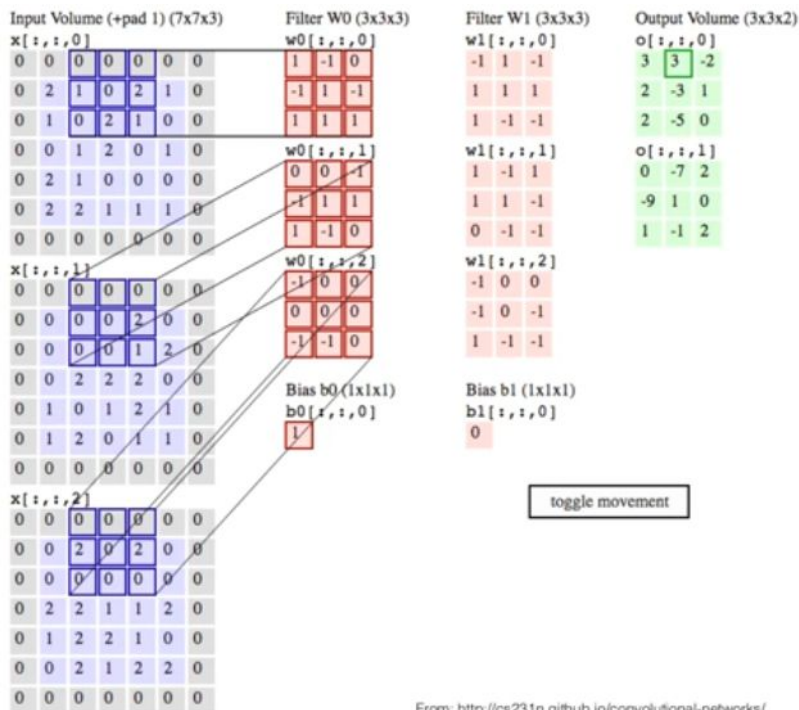
# units ( $\tilde{W}$ )



# units ( $\tilde{H}$ )

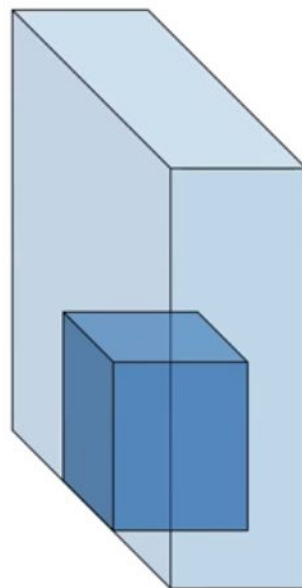
$f_1 = (w, h, C)$

# 2-D Convolution



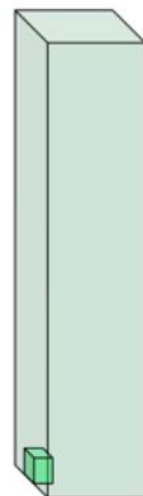
From: <http://cs231n.github.io/convolutional-networks/>

$H \times W \times C$



# filters

# units ( $\tilde{W}$ )



# units ( $\tilde{H}$ )

$$f_1 = (w, h, C)$$

# Pooling

1-D

|   |   |   |   |
|---|---|---|---|
| 0 | 1 | 4 | 9 |
| 3 | 2 | 5 | 8 |
| 1 | 2 | 3 | 1 |
| 3 | 1 | 7 | 4 |

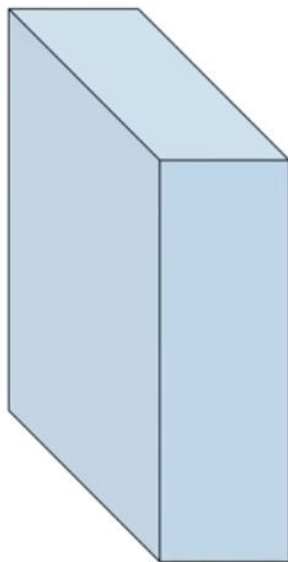


**Max pool:**  
2x2 filters  
Stride 2

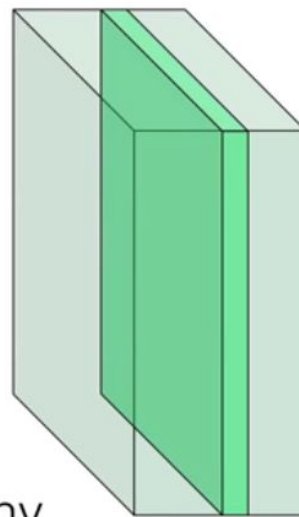
|   |   |
|---|---|
| 3 | 9 |
| 3 | 7 |

2-D

$224 \times 224 \times 3$

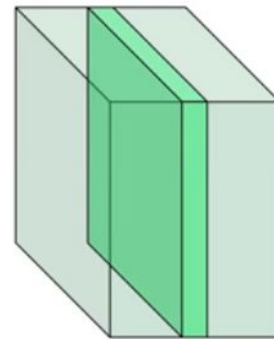


$224 \times 224 \times 64$



conv

$112 \times 112 \times 64$



pool

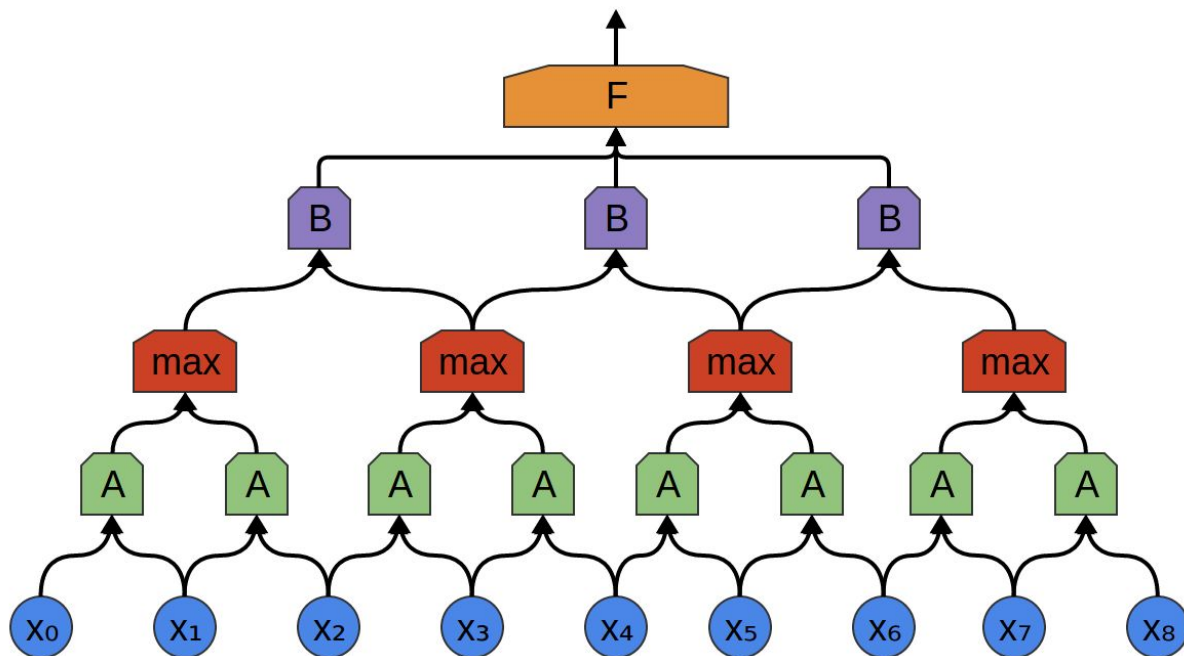
# Pooling

## Geoff Hinton on Pooling----

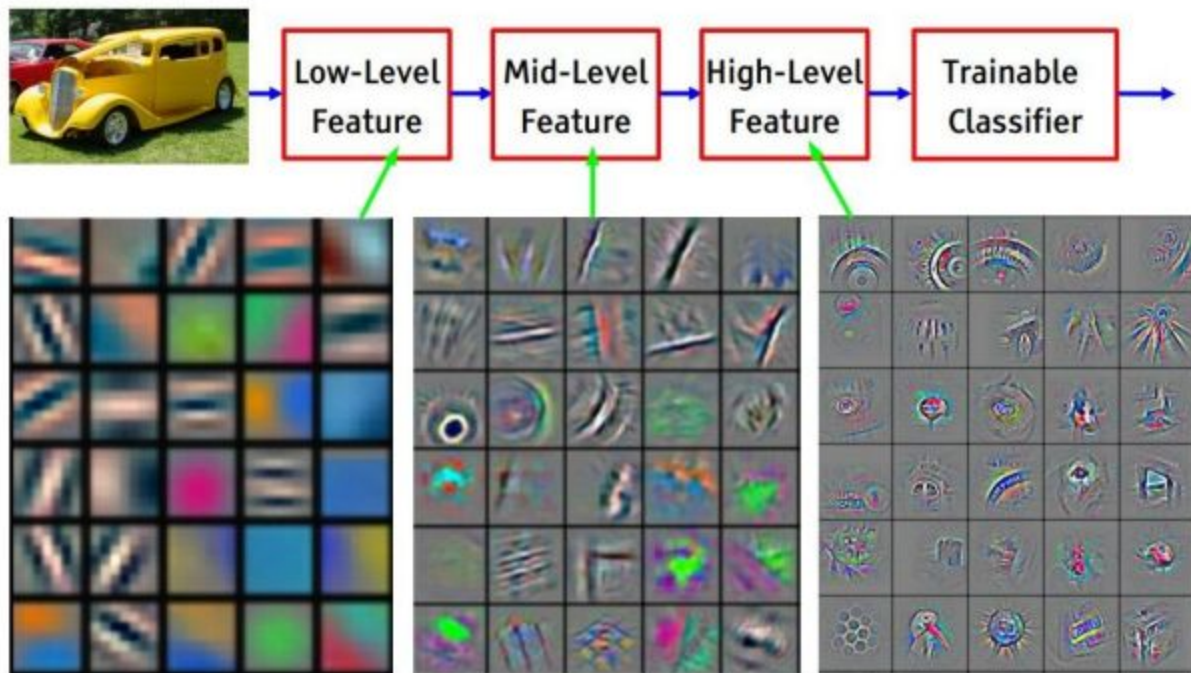
The pooling operation used in convolutional neural networks is a big mistake and the fact that it works so well is a disaster.

If the pools do not overlap, pooling loses valuable information about where things are. We need this information to detect precise relationships between the parts of an object.

# Convolutional Neural Network



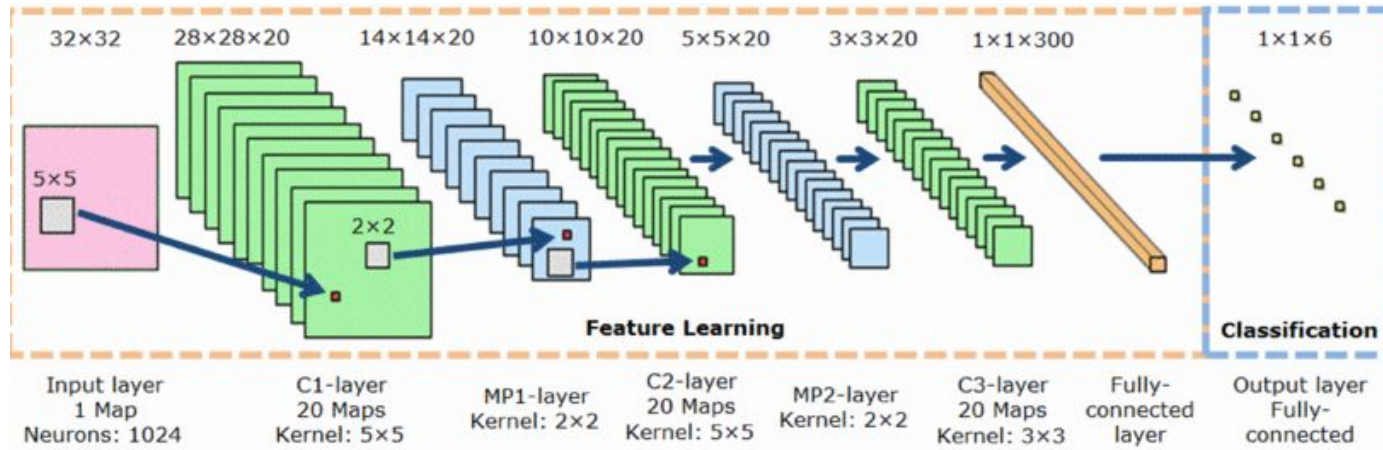
# Convolutional Neural Network



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

# Demo Embedding

# LeNet



\*Original LeNet-5 has two FCL at the end, and filter sizes are slightly different



# AlexNet (2012 Winner)

AlexNet architecture:

[227x227x3] INPUT

[55x55x96] CONV1: 96 11x11 filters at stride 4, pad 1

[27x27x96] MAX POOL1: 3x3 filters at stride 2

[27x27x96] NORM1: Normalization layer

[27x27x256] CONV2: 256 5x5 filters at stride 1, pad 1

[13x13x256] MAX POOL2: 3x3 filters at stride 2

[13x13x256] NORM2: Normalization layer

[13x13x384] CONV3: 384 3x3 filters at stride 1, pad 1

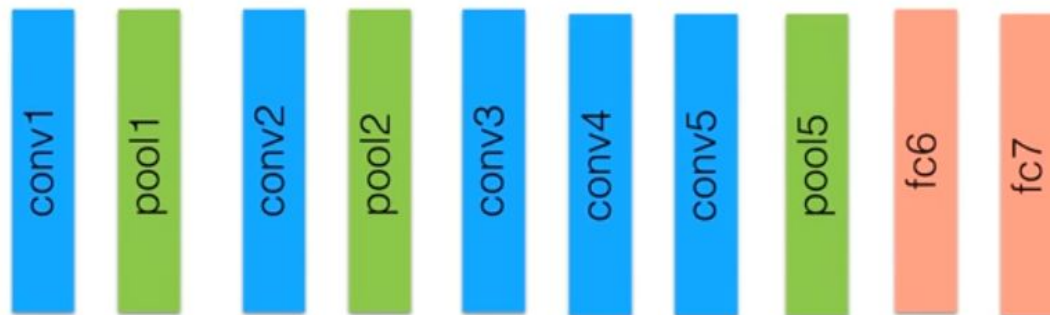
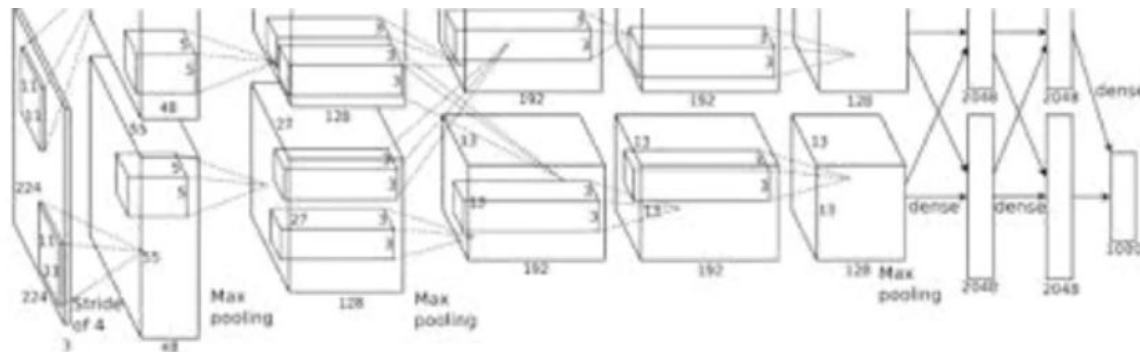
[13x13x384] CONV4: 384 3x3 filters at stride 1, pad 1

[13x13x256] CONV5: 256 3x3 filters at stride 1, pad 1

[6x6x256] MAX POOL3: 3x3 filters at stride 2 [4096]

FC6: 4096 neurons [4096] FC7: 4096 neurons [1000]

FC8: 1000 neurons (class scores)



# VGG Net

INPUT: [224x224x3] memory:  $224*224*3=150K$  params: 0 (not counting biases)

CONV3-64: [224x224x64] memory:  $224*224*64=3.2M$  params:  $(3*3*3)*64 = 1,728$

CONV3-64: [224x224x64] memory:  $224*224*64=3.2M$  params:  $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory:  $112*112*64=800K$  params: 0

CONV3-128: [112x112x128] memory:  $112*112*128=1.6M$  params:  $(3*3*64)*128 = 73,728$

CONV3-128: [112x112x128] memory:  $112*112*128=1.6M$  params:  $(3*3*128)*128 = 147,456$

POOL2: [56x56x128] memory:  $56*56*128=400K$  params: 0

CONV3-256: [56x56x256] memory:  $56*56*256=800K$  params:  $(3*3*128)*256 = 294,912$

CONV3-256: [56x56x256] memory:  $56*56*256=800K$  params:  $(3*3*256)*256 = 589,824$

CONV3-256: [56x56x256] memory:  $56*56*256=800K$  params:  $(3*3*256)*256 = 589,824$

POOL2: [28x28x256] memory:  $28*28*256=200K$  params: 0

CONV3-512: [28x28x512] memory:  $28*28*512=400K$  params:  $(3*3*256)*512 = 1,179,648$

CONV3-512: [28x28x512] memory:  $28*28*512=400K$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [28x28x512] memory:  $28*28*512=400K$  params:  $(3*3*512)*512 = 2,359,296$

POOL2: [14x14x512] memory:  $14*14*512=100K$  params: 0

CONV3-512: [14x14x512] memory:  $14*14*512=100K$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100K$  params:  $(3*3*512)*512 = 2,359,296$

CONV3-512: [14x14x512] memory:  $14*14*512=100K$  params:  $(3*3*512)*512 = 2,359,296$

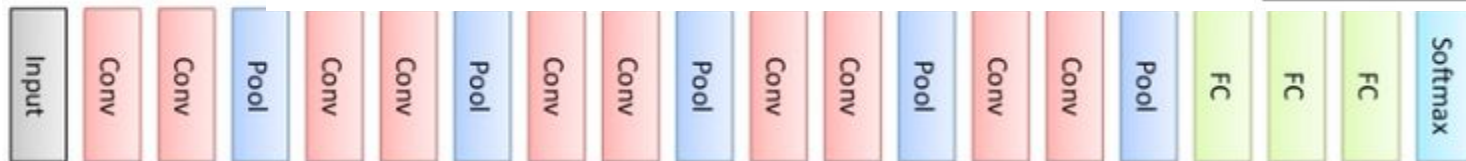
POOL2: [7x7x512] memory:  $7*7*512=25K$  params: 0

FC: [1x1x4096] memory: 4096 params:  $7*7*512*4096 = 102,760,448$

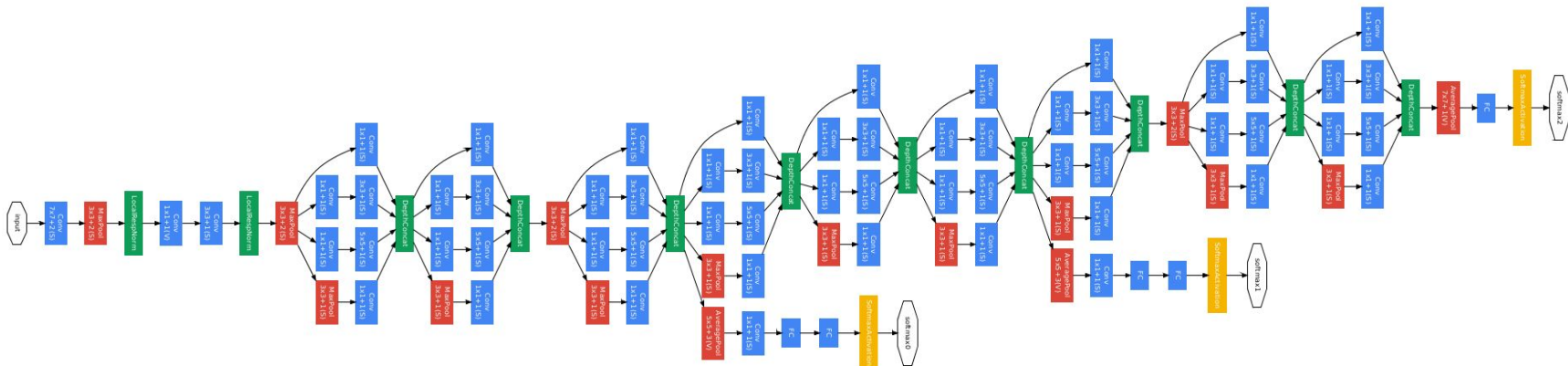
FC: [1x1x4096] memory: 4096 params:  $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params:  $4096*1000 = 4,096,000$

| ConvNet Configuration     |                  |                  |
|---------------------------|------------------|------------------|
| B                         | C                | D                |
| 13 weight layers          | 16 weight layers | 16 weight layers |
| put (224 × 224 RGB image) |                  |                  |
| conv3-64                  | conv3-64         | conv3-64         |
| conv3-64                  | conv3-64         | conv3-64         |
| maxpool                   |                  |                  |
| conv3-128                 | conv3-128        | conv3-128        |
| conv3-128                 | conv3-128        | conv3-128        |
| maxpool                   |                  |                  |
| conv3-256                 | conv3-256        | conv3-256        |
| conv3-256                 | conv3-256        | conv3-256        |
| maxpool                   |                  |                  |
| conv3-512                 | conv3-512        | conv3-512        |
| conv3-512                 | conv3-512        | conv3-512        |
| maxpool                   |                  |                  |
| conv3-512                 | conv3-512        | conv3-512        |
| conv3-512                 | conv3-512        | conv3-512        |
| maxpool                   |                  |                  |
| conv3-512                 | conv3-512        | conv3-512        |
| conv3-512                 | conv3-512        | conv3-512        |
| maxpool                   |                  |                  |
| FC-4096                   |                  |                  |
| FC-4096                   |                  |                  |
| FC-1000                   |                  |                  |
| soft-max                  |                  |                  |



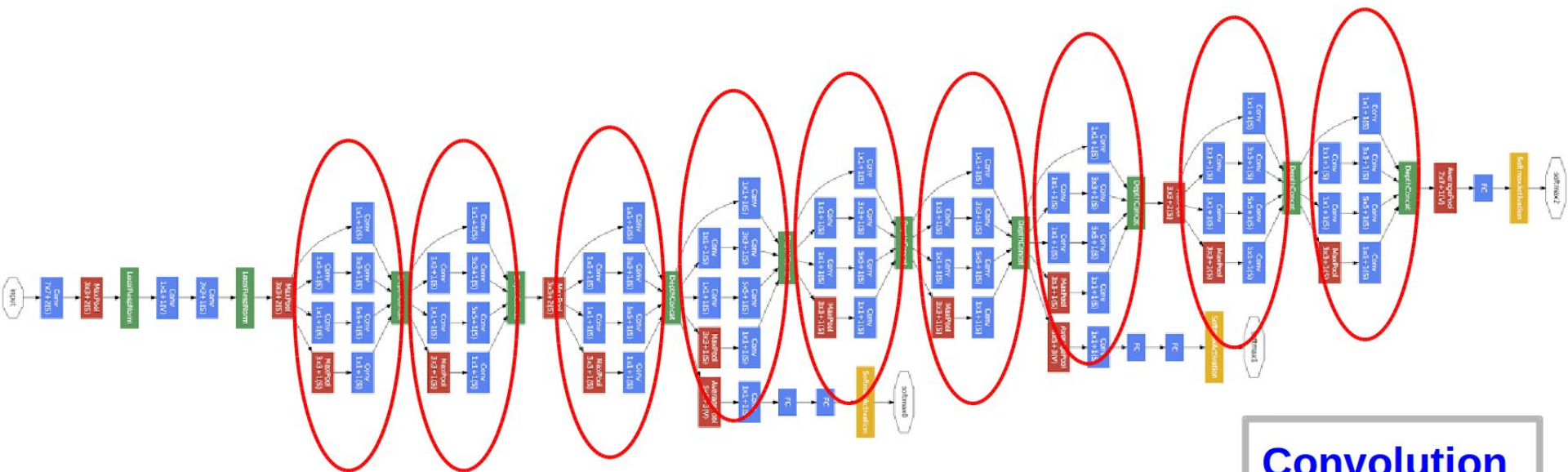
# GoogLeNet (2014 winner)



## Peasant's network vs Google's

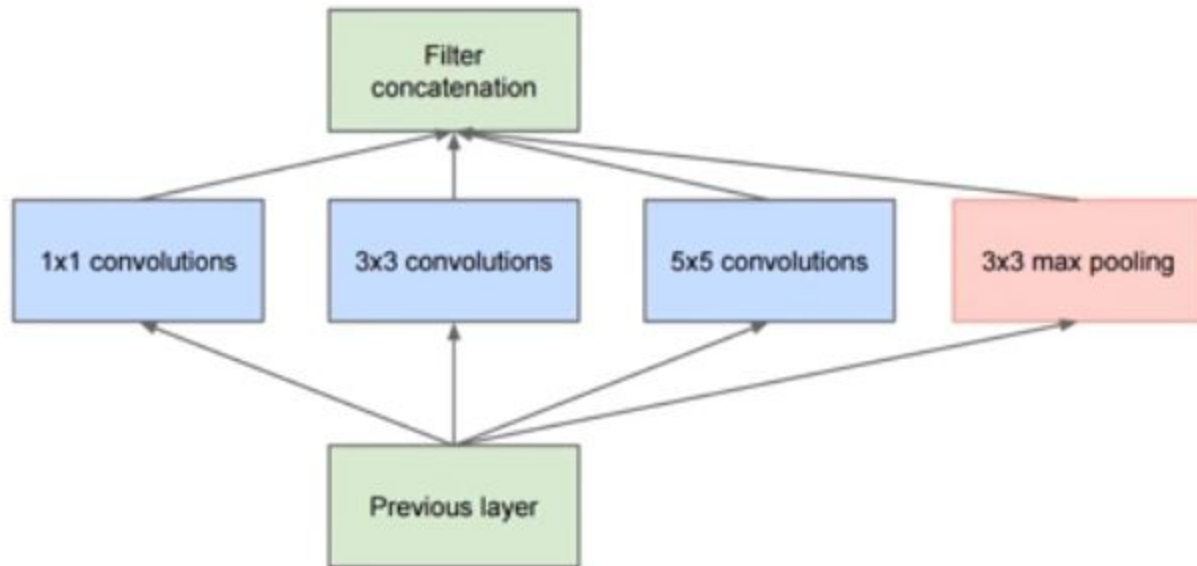


# GoogLeNet (2014 winner)

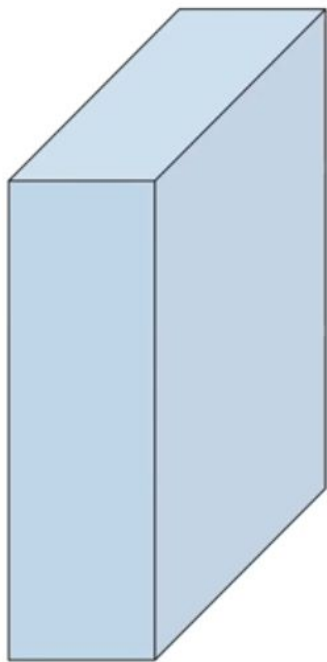


**Convolution**  
**Pooling**  
**Softmax**  
**Concat/Normalize**

# Inception



# Inception

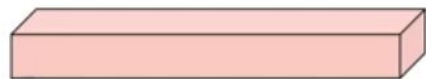


1 x 1?

3 x 3?

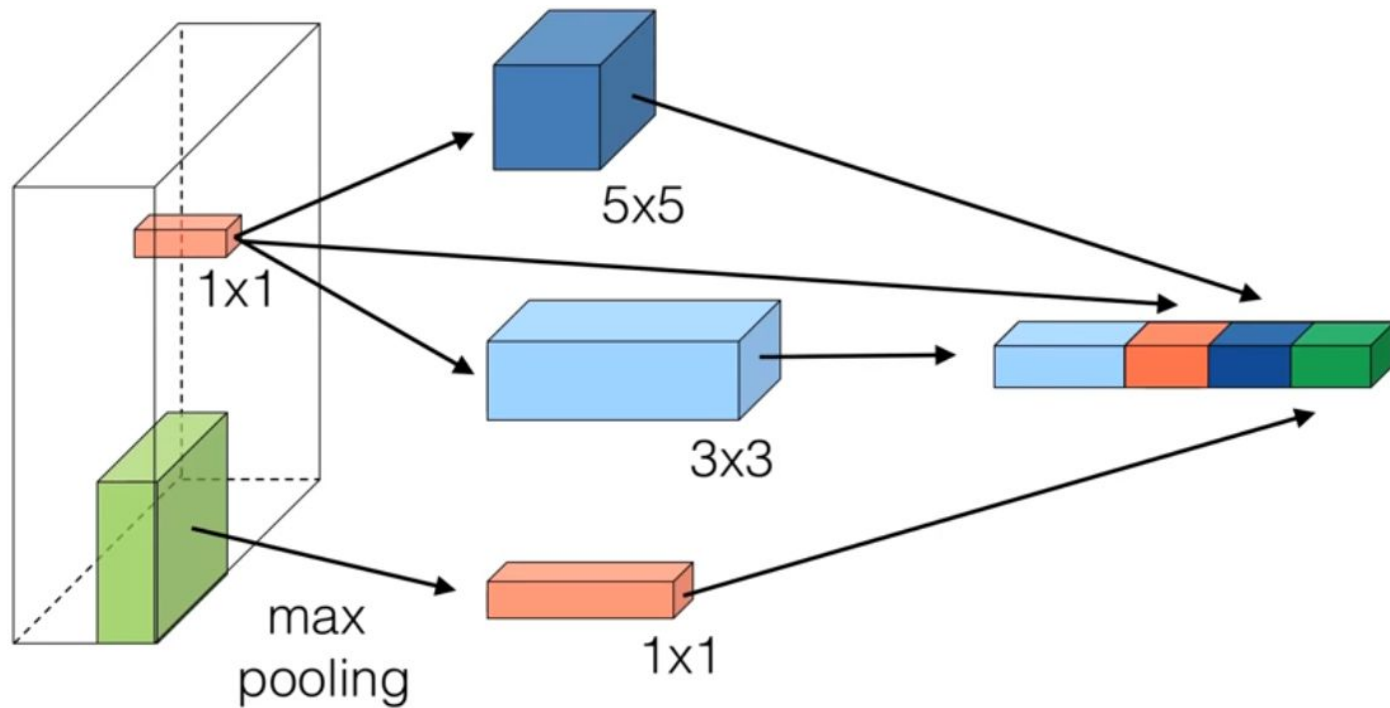
5 x 5?

Pooling?





# Inception





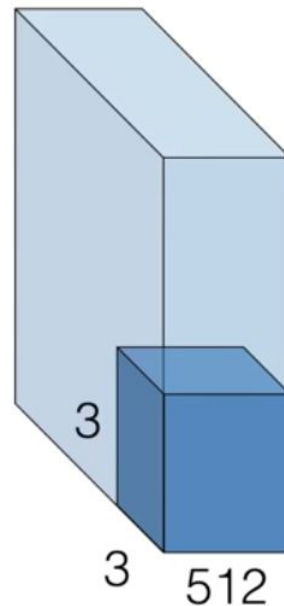
# Inception

| type           | patch size/<br>stride | output<br>size | depth | #1×1 | #3×3<br>reduce | #3×3 | #5×5<br>reduce | #5×5 | pool<br>proj | params | ops  |
|----------------|-----------------------|----------------|-------|------|----------------|------|----------------|------|--------------|--------|------|
| convolution    | 7×7/2                 | 112×112×64     | 1     |      |                |      |                |      |              | 2.7K   | 34M  |
| max pool       | 3×3/2                 | 56×56×64       | 0     |      |                |      |                |      |              |        |      |
| convolution    | 3×3/1                 | 56×56×192      | 2     |      | 64             | 192  |                |      |              | 112K   | 360M |
| max pool       | 3×3/2                 | 28×28×192      | 0     |      |                |      |                |      |              |        |      |
| inception (3a) |                       | 28×28×256      | 2     | 64   | 96             | 128  | 16             | 32   | 32           | 159K   | 128M |
| inception (3b) |                       | 28×28×480      | 2     | 128  | 128            | 192  | 32             | 96   | 64           | 380K   | 304M |
| max pool       | 3×3/2                 | 14×14×480      | 0     |      |                |      |                |      |              |        |      |
| inception (4a) |                       | 14×14×512      | 2     | 192  | 96             | 208  | 16             | 48   | 64           | 364K   | 73M  |
| inception (4b) |                       | 14×14×512      | 2     | 160  | 112            | 224  | 24             | 64   | 64           | 437K   | 88M  |
| inception (4c) |                       | 14×14×512      | 2     | 128  | 128            | 256  | 24             | 64   | 64           | 463K   | 100M |
| inception (4d) |                       | 14×14×528      | 2     | 112  | 144            | 288  | 32             | 64   | 64           | 580K   | 119M |

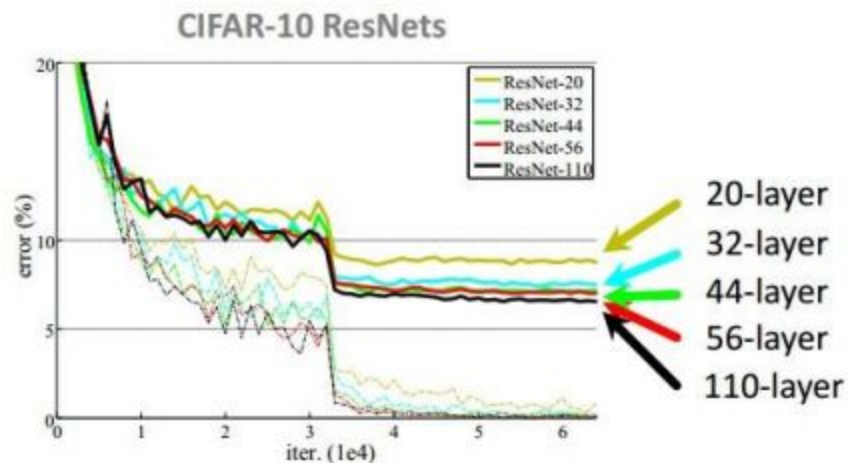
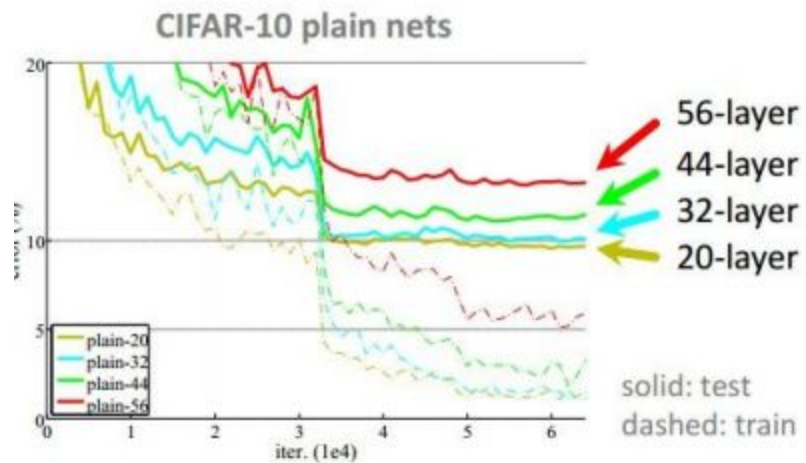
If we used (3 × 3, 512) convolution:

(3 × 3 × 512 × 512) parameters = 2.359 million parameters

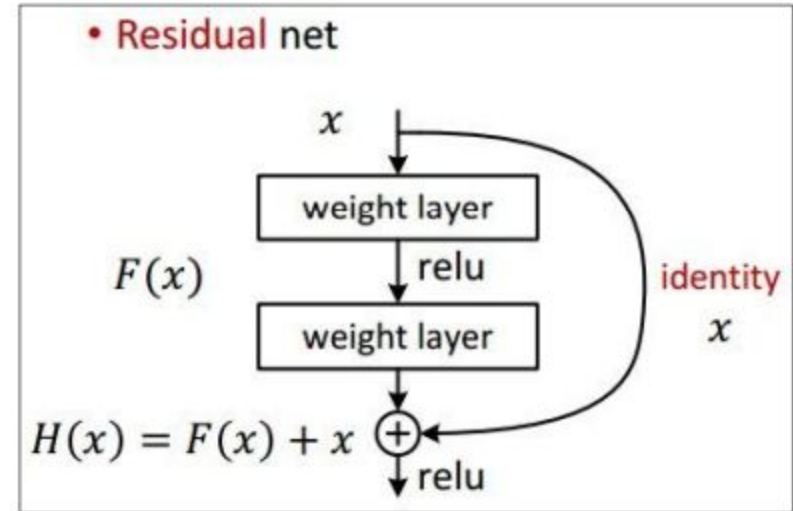
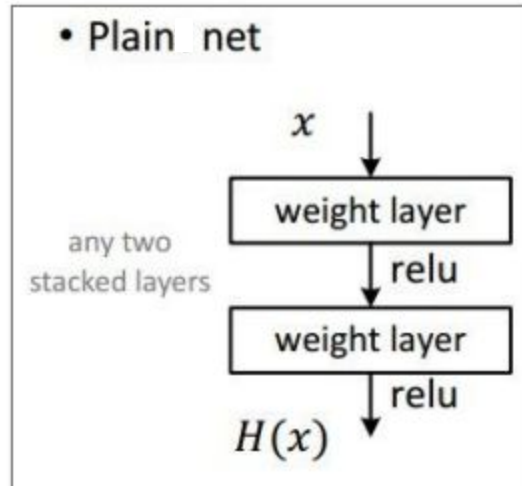
Inception module: 437K parameters



# Going Deeper

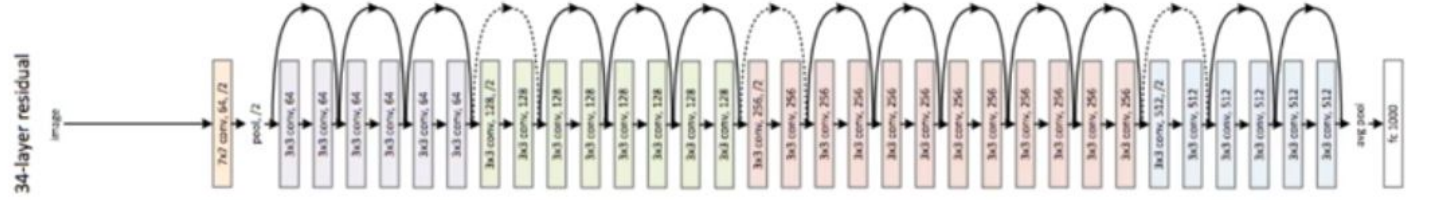


# Resnet (2015 winner)

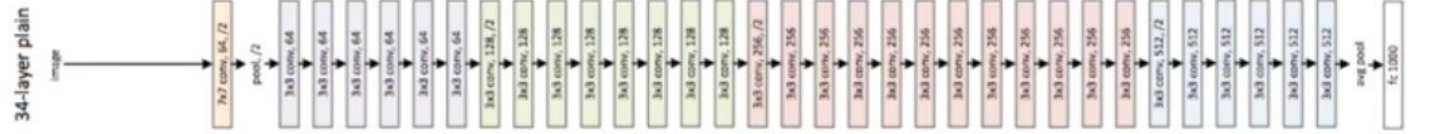


# Resnet - comparison with other nets

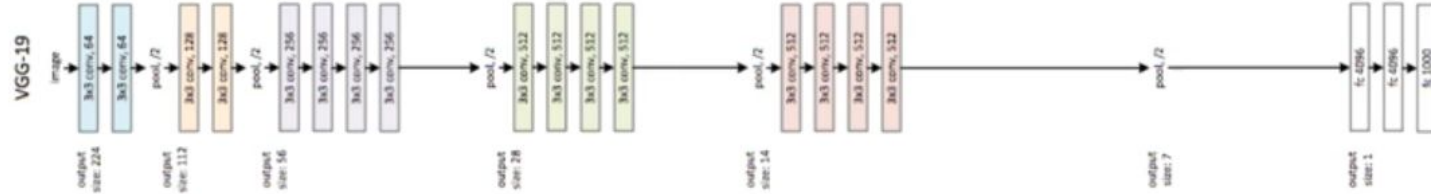
34-residual



34-plain



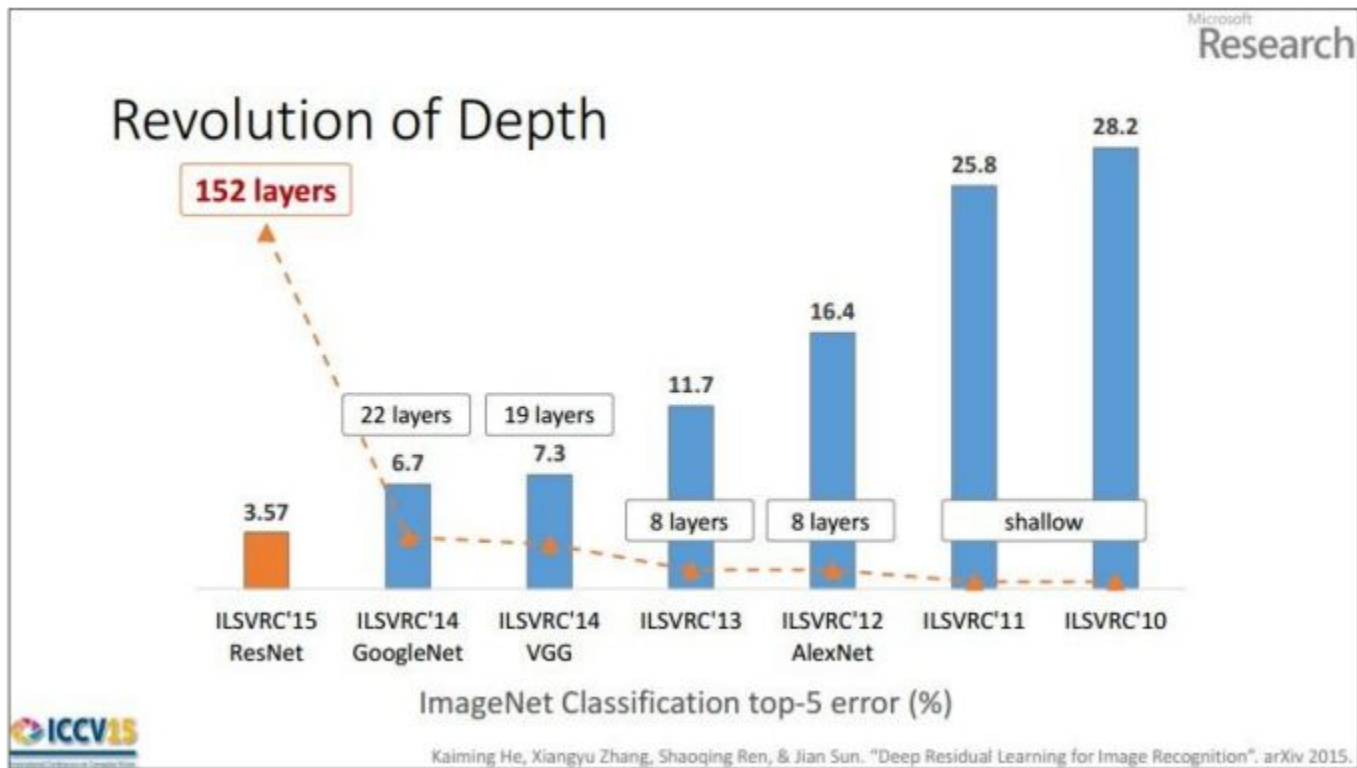
VGG



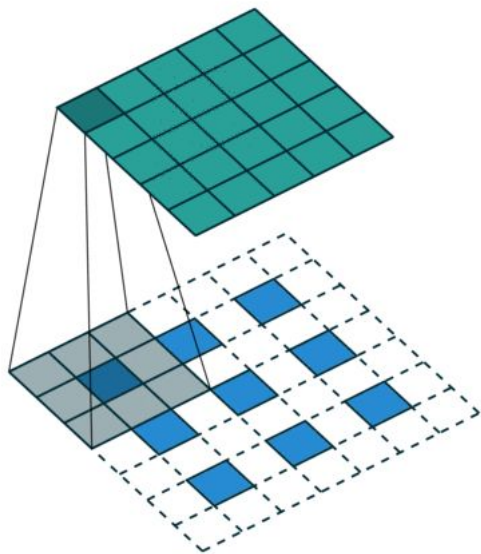
# Resnet - Number of layer comparison

| layer name | output size | 18-layer  | 34-layer  | 50-layer  | 101-layer  | 152-layer  |
|------------|-------------|---|---|---|--|--|
| conv1      | 112×112     | 7×7, 64, stride 2   |   |   |  |  |
| conv2_x    | 56×56       | 3×3 max pool, stride 2  |   |   |  |  |
|            |             | $\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 2$   | $\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 3$   | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$    | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$     | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$     |
| conv3_x    | 28×28       | $\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 4$ | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$  | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$   | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$   |
| conv4_x    | 14×14       | $\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 6$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$ |
| conv5_x    | 7×7         | $\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$  | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$  |
|            | 1×1         | average pool, 1000-d fc, softmax  |   |   |  |  |
| FLOPs      |             | $1.8 \times 10^9$   | $3.6 \times 10^9$   | $3.8 \times 10^9$   | $7.6 \times 10^9$  | $11.3 \times 10^9$   |

# Depth - The Stigma

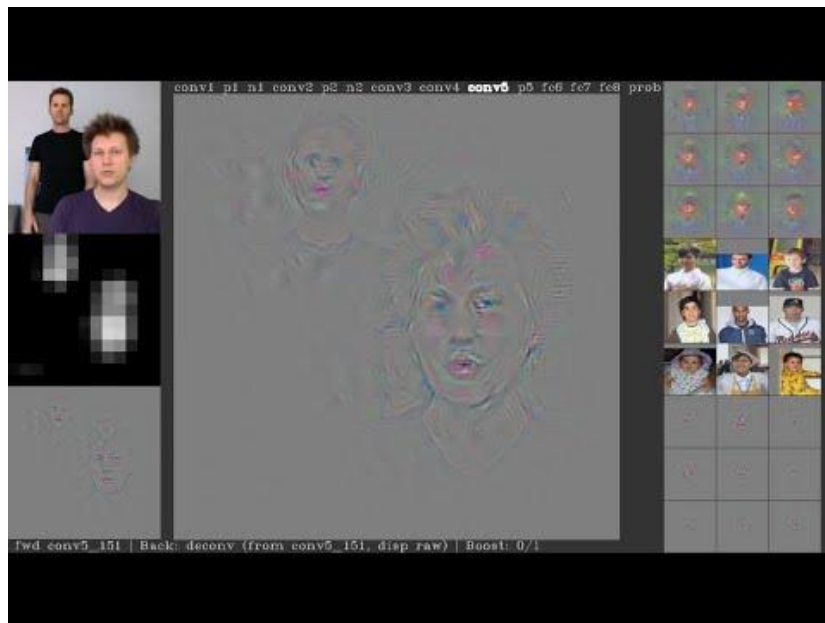


# Deconvolution / Transpose Convolution / Fractional Convolution

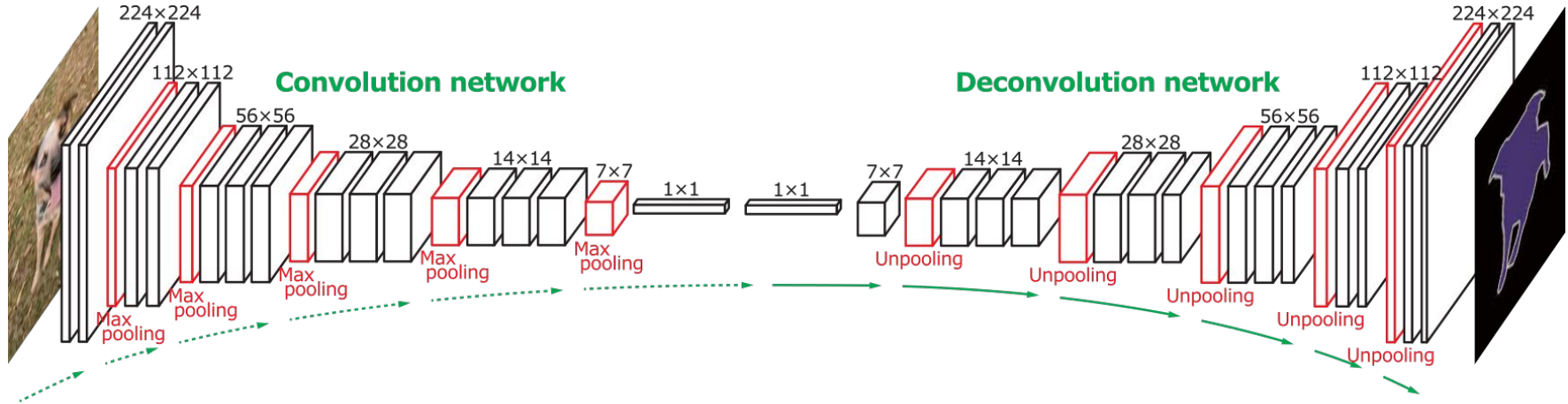


# Demo Deconv





# Semantic Segmentation



# Artistic Style Transfer

- Feed the artistic image through the VGG net and compute and save the Gram matrix  $G$ .
- Feed the photograph through the VGG net and save the feature maps  $F$ .
- Generate a white noise image. Through backpropagation, iteratively update this image until it has a feature map and a Gram matrix that are close to  $F$  and  $G$ , respectively.



# Fooling CNNs

## Adversarial Examples and Rubbish Classes

Answers -

1. Due to high dimensional dot products
2. Occurs in both linear (ReLU) & Non-linear models
3. Direction of perturbation matters not specific point
4. Also occurs in Shallow networks not just DNN
5. Regularisation doesn't prevent fooling examples
6. Adversarial training is good regularization
7. Extremely low probability (not observed in test)

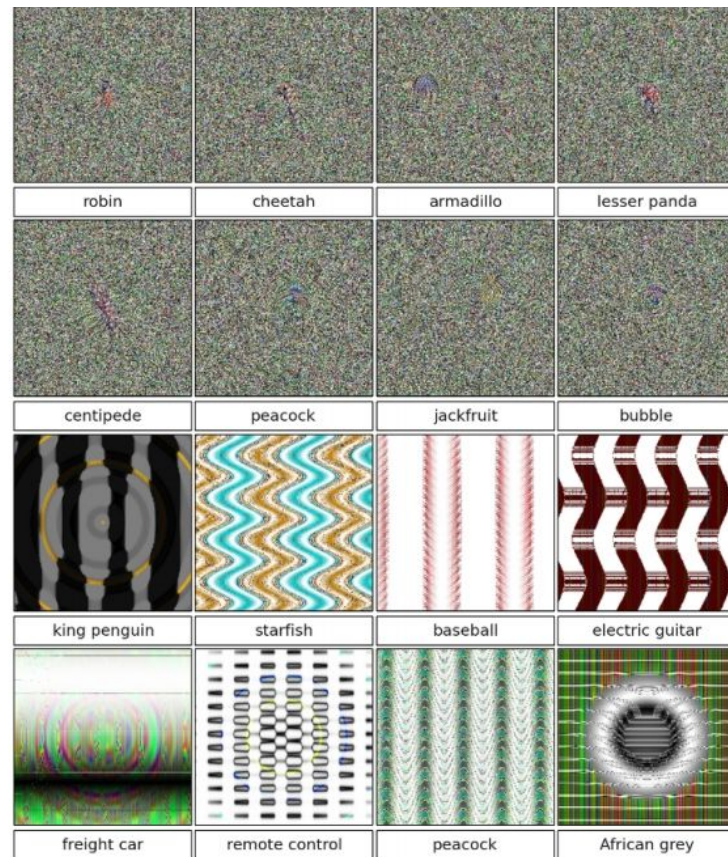


Figure 1. Evolved images that are unrecognizable to humans, but that state-of-the-art DNNs trained on ImageNet believe with  $\geq 99.6\%$  certainty to be a familiar object. This result highlights differences between how DNNs and humans recognize objects. Images are either directly (*top*) or indirectly (*bottom*) encoded.

# Summary

- ConvNets stack CONV, POOL, FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Typical architectures look like  
$$[(\text{CONV-RELU})^N - \text{POOL}]^M - (\text{FC-RELU})^K, \text{SOFTMAX}$$
where  $N$  is usually up to  $\sim 5$ ,  $M$  is large,  $0 \leq K \leq 2$ .
- but recent advances such as ResNet/GoogLeNet challenge this paradigm

## Credits

1. [CS231n](#) Convnets
2. [Chris Colah's](#) awesome blog
3. [Chris Burger](#) - Style transfer images
4. [Convolutional Neural Networks](#) - Nervana Systems
5. [DeepVis](#) - Jason Yosiniki
6. [Fooling CNNs](#) - Anh Nguyen
7. [More demos](#) - Yann LeCun

