Social network Graph Link Prediction - Facebook Challenge

In [1]:

```
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import csv
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xgboost as xgb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore, DataFrame
from pandas import read hdf
from scipy.sparse.linalg import svds, eigs
import gc
from tqdm import tqdm
```

1. Reading Data

```
In [2]:
```

```
if os.path.isfile('data/after_eda/train_pos_after_eda.csv'):
    train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter=',',create_using=nx
.DiGraph(),nodetype=int)
    print(nx.info(train_graph))
else:
    print("please run the FB_EDA.ipynb or download the files from drive")
```

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

31 1 6 01 3 1 3 6 615A \$205 615Z3 \$205 3 16 01 3

```
In [3]:
```

In [4]:

```
#one test case
print(jaccard_for_followees(273084,1505602))
```

0.0

In [5]:

```
#node 1635354 not in graph
print(jaccard_for_followees(273084,1505602))
```

0.0

In [6]:

In [7]:

```
print(jaccard_for_followers(273084,470294))
```

0

In [8]:

```
#node 1635354 not in graph
print(jaccard_for_followees(669354,1635354))

0
```

2.2 Cosine distance

```
\begin{equation} CosineDistance = \frac{|X\cap Y|}{|X|\cdot|Y|} \end{equation}
```

```
In [9]:
```

In [11]:

```
print(cosine_for_followees(273084,1635354))
```

0

In [12]:

In [13]:

```
print(cosine_for_followers(2,470294))
```

0.02886751345948129

In [14]:

```
print(cosine_for_followers(669354,1635354))
```

0

3. Ranking Measures

https://networkx.github.io/documentation/networkx-

1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are

currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

```
In [15]:
```

```
if not os.path.isfile('data/fea_sample/page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
else:
    pr = pickle.load(open('data/fea_sample/page_rank.p','rb'))
```

In [16]:

```
print('min',pr[min(pr, key=pr.get)])
print('max',pr[max(pr, key=pr.get)])
print('mean',float(sum(pr.values())) / len(pr))

min 1.6556497245737814e-07
max 2.7098251341935827e-05
mean 5.615699699389075e-07
```

In [17]:

```
#for imputing to nodes which are not there in Train data
mean_pr = float(sum(pr.values())) / len(pr)
print(mean_pr)
```

5.615699699389075e-07

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

In [18]:

```
#if has direct edge then deleting that edge and calculating shortest path
def compute_shortest_path_length(a,b):
    p=-1
    try:
        if train_graph.has_edge(a,b):
            train_graph.remove_edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
            train_graph.add_edge(a,b)
    else:
        p= nx.shortest_path_length(train_graph,source=a,target=b)
    return p
    except:
        return -1
```

In [19]:

```
#testing
compute shortest path length(77697. 826021)
```

```
Out[19]:

10

In [20]:

#testing
compute_shortest_path_length(669354,1635354)

Out[20]:
-1
```

4.2 Checking for same community

In [21]:

```
#getting weekly connected edges from graph
wcc=list(nx.weakly_connected_components(train_graph))
def belongs to same wcc(a,b):
   index = []
   if train_graph.has_edge(b,a):
       return 1
   if train_graph.has_edge(a,b):
           for i in wcc:
                if a in i:
                    index= i
                   break
            if (b in index):
                train graph.remove edge(a,b)
                if compute shortest path length(a,b) ==-1:
                   train_graph.add_edge(a,b)
                    return 0
                    train graph.add edge(a,b)
                    return 1
            else:
                return 0
   else:
            for i in wcc:
               if a in i:
                   index= i
                   break
            if(b in index):
               return 1
            else:
               return 0
```

```
In [22]:
```

0

```
belongs_to_same_wcc(861, 1659750)

Out[22]:
0

In [23]:
belongs_to_same_wcc(669354,1635354)

Out[23]:
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices. \$\$A(x,y)=\sum_{u in $N(x) \sim N(y) \frac{1}{\log(|N(u)|)}$

```
In [24]:
```

```
#adar index
def calc adar in(a,b):
   sum=0
   try:
       n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors(b))))
       if len(n)!=0:
           for i in n:
               sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
       else:
           return 0
   except:
       return 0
```

In [25]:

```
calc adar in(1,189226)
Out[25]:
0
In [26]:
calc adar in (669354, 1635354)
Out[26]:
```

4.4 Is persion was following back:

```
In [27]:
```

0

```
def follows_back(a,b):
   if train_graph.has_edge(b,a):
       return 1
   else:
       return 0
```

```
In [28]:
follows_back(1,189226)
Out[28]:
```

```
In [29]:
```

```
follows back(669354,1635354)
```

```
Out[29]:
```

0

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/ Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is \$\$x_i = \alpha \sum_{ij} A_{ij} x_j + \beta (x_i) + \beta (x_i

where A is the adjacency matrix of the graph G with eigenvalues \$\$\lambda\$\$.

The parameter $\$ controls the initial centrality and $\$ and $\$ frac{1}{\lambda_{max}}.\$\$

```
In [30]:
```

```
if not os.path.isfile('data/fea_sample/katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('data/fea_sample/katz.p','wb'))
else:
    katz = pickle.load(open('data/fea_sample/katz.p','rb'))
```

In [31]:

```
print('min', katz[min(katz, key=katz.get)])
print('max', katz[max(katz, key=katz.get)])
print('mean', float(sum(katz.values())) / len(katz))
```

min 0.0007313532484065916 max 0.003394554981699122 mean 0.0007483800935562018

In [32]:

```
mean_katz = float(sum(katz.values())) / len(katz)
print(mean_katz)
```

0.0007483800935562018

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm

In [33]:

```
if not os.path.isfile('data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
else:
    hits = pickle.load(open('data/fea_sample/hits.p','rb'))
```

In [34]:

```
print('min',hits[0][min(hits[0], key=hits[0].get)])
print('max',hits[0][max(hits[0], key=hits[0].get)])
print('mean',float(sum(hits[0].values())) / len(hits[0]))
```

```
min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
```

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
In [35]:
```

```
import random
if os.path.isfile('data/after_eda/train_after_eda.csv'):
    filename = "data/after_eda/train_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 15100030
    # n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n_train = 15100028
    s = 100000 #desired sample size
    skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
    #https://stackoverflow.com/a/22259008/4084039
```

In [36]:

```
if os.path.isfile('data/after_eda/train_after_eda.csv'):
    filename = "data/after_eda/test_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 3775008
    # n_test = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n_test = 3775006
    s = 50000 #desired sample size
    skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
    #https://stackoverflow.com/a/22259008/4084039
```

In [37]:

```
print("Number of rows in the train data file:", n_train)
print("Number of rows we are going to elimiate in train data are",len(skip_train))
print("Number of rows in the test data file:", n_test)
print("Number of rows we are going to elimiate in test data are",len(skip_test))
```

```
Number of rows in the train data file: 15100028
Number of rows we are going to elimiate in train data are 15000028
Number of rows in the test data file: 3775006
Number of rows we are going to elimiate in test data are 3725006
```

In [38]:

```
df_final_train = pd.read_csv('data/after_eda/train_after_eda.csv', skiprows=skip_train, names=['source_node', 'destination_node'])
df_final_train['indicator_link'] = pd.read_csv('data/train_y.csv', skiprows=skip_train, names=['indicator_link'])
print("Our train matrix size ",df_final_train.shape)
df_final_train.head(2)
```

Our train matrix size (100002, 3)

Out[38]:

source_node destination_node indicator_link

0	273084	1505602	1
1	623878	481358	1

In [39]:

```
df_final_test = pd.read_csv('data/after_eda/test_after_eda.csv', skiprows=skip_test, names=['source_nod
e', 'destination_node'])
df_final_test['indicator_link'] = pd.read_csv('data/test_y.csv', skiprows=skip_test, names=['indicator_link'])
```

```
print("Our test matrix size ", df_final_test.shape)
df_final_test.head(2)
```

Our test matrix size (50002, 3)

Out[39]:

	source_node	destination_node	indicator_link
0	848424	784690	1
1	1430179	1505513	1

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard_followers
- 2. jaccard_followees
- 3. cosine followers
- 4. cosine followees
- 5. num_followers_s
- 6. num_followees_s
- 7. num_followers_d
- 8. num_followees_d
- 9. inter_followers
- 10. inter followees

In [40]:

```
if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
    #mapping jaccrd followers to train and test data
   df final train['jaccard followers'] = df final train.apply(lambda row:
                                            jaccard for followers(row['source node'], row['destination n
ode']),axis=1)
   df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                            jaccard_for_followers(row['source_node'],row['destination_n
ode']),axis=1)
    #mapping jaccrd followees to train and test data
   df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                            jaccard for followees(row['source node'], row['destination n
ode']),axis=1)
   df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                            jaccard for followees(row['source node'], row['destination n
ode']),axis=1)
        #mapping jaccrd followers to train and test data
   df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
                                           cosine for followers(row['source node'], row['destination no
de']),axis=1)
   df final test['cosine followers'] = df final test.apply(lambda row:
                                           cosine for followers(row['source node'], row['destination no
de']),axis=1)
    #mapping jaccrd followees to train and test data
   df final train['cosine followees'] = df final train.apply(lambda row:
                                           cosine_for_followees(row['source_node'], row['destination_no
de']),axis=1)
   df final test['cosine followees'] = df final test.apply(lambda row:
                                            cosine for followees (row['source node'], row['destination no
de']),axis=1)
```

In [41]:

```
def compute_features_stage1(df_final):
    #calculating no of followers followees for source and destination
```

```
#calculating intersection of followers and followees for source and destination
   num followers s=[]
   num followees s=[]
   num followers d=[]
   num followees d=[]
   inter followers=[]
   inter_followees=[]
   for i, row in df final.iterrows():
            s1=set(train graph.predecessors(row['source node']))
            s2=set(train graph.successors(row['source node']))
           s1 = set()
           s2 = set()
            d1=set(train graph.predecessors(row['destination node']))
           d2=set(train_graph.successors(row['destination_node']))
       except:
           d1 = set()
           d2 = set()
       num followers s.append(len(s1))
       num followees s.append(len(s2))
       num followers d.append(len(d1))
       num followees d.append(len(d2))
       inter followers.append(len(s1.intersection(d1)))
        inter followees.append(len(s2.intersection(d2)))
   return num followers s, num followers d, num followees s, num followees d, inter followers, inter f
ollowees
```

In [42]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stagel.h5'):
    df_final_train['num_followers_s'],    df_final_train['num_followers_d'],    \
        df_final_train['num_followes_s'],    df_final_train['num_followees_d'],    \
        df_final_train['inter_followers'],    df_final_train['inter_followees']= compute_features_stagel(df_final_train)

    df_final_test['num_followers_s'],    df_final_test['num_followers_d'],    \
        df_final_test['num_followees_s'],    df_final_test['num_followees_d'],    \
        df_final_test['inter_followers'],    df_final_test['inter_followees']= compute_features_stagel(df_final_test)

    hdf = HDFStore('data/fea_sample/storage_sample_stagel.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()

else:

    df_final_train = read_hdf('data/fea_sample/storage_sample_stagel.h5', 'train_df',mode='r')
    df_final_test = read_hdf('data/fea_sample/storage_sample_stagel.h5', 'test_df',mode='r')
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

In [43]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage2.h5'):
    #mapping adar index on train
    df_final_train['adar_index'] = df_final_train.apply(lambda row: calc_adar_in(row['source_node'], row
['destination_node']),axis=1)
    #mapping adar index on test
    df_final_test['adar_index'] = df_final_test.apply(lambda row: calc_adar_in(row['source_node'], row['destination_node']),axis=1)
```

```
#mapping followback or not on train
    df final train['follows back'] = df final train.apply(lambda row: follows back(row['source node'],r
ow['destination node']),axis=1)
    #mapping followback or not on test
    df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node'], row
['destination node']),axis=1)
    #mapping same component of wcc or not on train
    df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source node
'],row['destination node']),axis=1)
    ##mapping same component of wcc or not on train
    df_final_test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_wcc(row['source_node']
,row['destination_node']),axis=1)
    #mapping shortest path on train
    df final train['shortest path'] = df final train.apply(lambda row: compute shortest path length(row
['source node'], row['destination node']), axis=1)
    #mapping shortest path on test
    df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['
source node'],row['destination node']),axis=1)
    hdf = HDFStore('data/fea sample/storage sample stage2.h5')
   hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
   hdf.close()
else:
   df_final_train = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'train_df',mode='r')
df_final_test = read_hdf('data/fea_sample/storage_sample_stage2.h5', 'test_df',mode='r')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - weight of outgoing edges
 - · weight of incoming edges + weight of outgoing edges
 - weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities_s of source
- 9. authorities s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other.

| Credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

In [44]:

```
#weight for source and destination of each link
Weight in = {}
Weight out = {}
for i in tqdm(train_graph.nodes()):
   s1=set(train graph.predecessors(i))
    w in = 1.0/(np.sqrt(1+len(s1)))
   Weight in[i]=w in
    s2=set(train graph.successors(i))
    w \text{ out} = 1.0/(np.sqrt(1+len(s2)))
    Weight out[i]=w out
#for imputing with mean
mean weight in = np.mean(list(Weight in.values()))
mean weight out = np.mean(list(Weight out.values()))
100%|
                                                                          | 1780722/1780722 [00:10<00:00
, 171448.06it/s]
```

In [45]:

```
if not os.path.isfile('data/fea_sample/storage_sample_stage3.h5'):
    #mapping to pandas train
   df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x, mean
   df final train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out.get(x,mean_wei
ght out))
    #mapping to pandas test
   df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x, mean we
ight in))
   df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x, mean weigh
t out))
    #some features engineerings on the in and out weights
   df final train['weight f1'] = df final train.weight in + df final train.weight out
   df final train['weight f2'] = df final train.weight in * df final train.weight out
   df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_out)
   df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
    #some features engineerings on the in and out weights
   df final test['weight f1'] = df final test.weight in + df final test.weight out
   df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
   df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
   df final test['weight f4'] = (1*df final test.weight in + 2*df final test.weight out)
```

In [46]:

```
#Hits algorithm score for source and destination in Train and test
    #if anything not there in train graph then adding 0
   df final train['hubs s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x,0))
   df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].get(x,0))
   df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].get(x,0))
   df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
    #Hits algorithm score for source and destination in Train and Test
    #if anything not there in train graph then adding 0
   df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x,0))
   df_final_train['authorities_d'] = df_final_train.destination_node.apply(lambda x: hits[1].get(x,0))
   df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hits[1].get(x,0))
   df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
   hdf = HDFStore('data/fea sample/storage sample stage3.h5')
   hdf.put('train_df',df_final_train, format='table', data_columns=True)
   hdf.put('test df', df final test, format='table', data columns=True)
   hdf.close()
else:
   df final train = read hdf('data/fea sample/storage sample stage3.h5', 'train df',mode='r')
   df final test = read hdf('data/fea sample/storage sample stage3.h5', 'test df', mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [47]:
```

```
def svd(x, S):
    try:
        z = sadj_dict[x]
        return S[z]
    except:
        return [0,0,0,0,0,0]
```

In [48]:

```
#for svd features to get feature vector creating a dict node val and inedx in svd vector
sadj_col = sorted(train_graph.nodes())
sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
```

In [49]:

```
Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype()
```

In [50]:

```
U, s, V = svds(Adj, k = 6)
print('Adjacency matrix Shape', Adj.shape)
print('U Shape', U.shape)
print('V Shape', V.shape)
print('S Shape', s.shape)
```

```
Adjacency matrix Shape (1780722, 1780722)
U Shape (1780722, 6)
V Shape (6, 1780722)
s Shape (6,)
```

```
In [51]:
```

```
if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
   df final train[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
   df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
   df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] = \
   df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6']] = \
   df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
   df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
   df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','svd_v_d_6']] = \
   df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   hdf = HDFStore('data/fea sample/storage sample stage4.h5')
   hdf.put('train df', df final train, format='table', data columns=True)
   hdf.put('test df',df final test, format='table', data columns=True)
   hdf.close()
else:
   df_final_train = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'train_df',mode='r')
df_final_test = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'test_df',mode='r')
```

In [52]:

```
df_final_train.head()
```

Out[52]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_follow
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	1722634	647399	1	0	0.181818	0.129099	0.323381	
2	404772	797880	1	0	0.000000	0.000000	0.000000	
3	542646	1740462	1	0	0.150000	0.100000	0.267261	
4	355711	1610892	1	0	0.000000	0.166667	0.000000	

5 rows × 55 columns

Preferential Attachment

Preferential Attachment for Followers

```
In [53]:
```

```
df_final_train['pref_attach_followers'] = df_final_train['num_followers_s']*df_final_train['num_followers_d']
df_final_test['pref_attach_followers'] = df_final_test['num_followers_s']*df_final_test['num_followers_d']
```

Preferential Attachment for Followees

```
In [54]:
```

```
df_final_train['pref_attach_followees'] = df_final_train['num_followees_s']*df_final_train['num_followe
es_d']
df_final_test['pref_attach_followees'] = df_final_test['num_followees_s']*df_final_test['num_followees_
d']
```

In [55]:

```
df_final_train.head()
```

Out[55]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_follow
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	1722634	647399	1	0	0.181818	0.129099	0.323381	
2	404772	797880	1	0	0.000000	0.000000	0.000000	
3	542646	1740462	1	0	0.150000	0.100000	0.267261	
4	355711	1610892	1	0	0.000000	0.166667	0.000000	

5 rows × 57 columns

<u>•</u>

SVD Dot

In [56]:

```
df_final_train.columns
```

Out[56]:

```
'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
                'svd u s 6', 'svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6', 'svd v s 1', 'svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6', 'svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6',
                 'pref attach followers', 'pref attach followees'],
             dtype='object')
In [105]:
 np.array(df_final_train[['svd_u_s_1','svd_u_s_2','svd_u_s_3','svd_u_s_4','svd_u_s_5','svd_u_s_6','svd_v
 s 1','svd v s 2','svd v s 3','svd v s 4','svd v s 5','svd v s 6']].iloc[0])
Out[105]:
array([ 1.66610323e-13, -4.61331746e-13, 1.04294289e-05, -6.67739537e-13, 2.45094202e-13, 3.58476106e-12, 7.21538336e-13, -3.92567036e-13,
                  1.98351273e-06, -1.54493783e-13, 8.10791709e-13, 1.71960986e-14])
In [59]:
 # For train data
 svd u dot = []
 svd_v_dot = []
 for i in tqdm(range(df_final_train.shape[0])):
          svd_u_s = np.array(df_final_train[['svd_u_s_1','svd_u_s_2','svd_u_s_3','svd_u_s_4','svd_u_s_5','svd
  u s 6']].iloc[i])
         svd u d = np.array(df final train[['svd u d 1','svd u d 2','svd u d 3','svd u d 4','svd u d 5','svd
 u d 6']].iloc[i])
         svd_v_s = np.array(df_final_train[['svd_v_s_1','svd_v_s_2','svd_v_s_3','svd_v_s_4','svd_v_s_5','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_s_1','svd_v_
 v_s_6']].iloc[i])
         svd v d = np.array(df final train[['svd v d 1','svd v d 2','svd v d 3','svd v d 4','svd v d 5','svd
 v d 6']].iloc[i])
         svd u dot.append(np.dot(svd u s,svd u d))
         svd_v_dot.append(np.dot(svd_v_s,svd_v_d))
100%|
                                                                                                                                                                                     | 100002/100002 [19:43<0
0:00, 84.47it/s]
In [60]:
 # Display 10 svd dot result
 svd u dot[:10]
Out[60]:
 [1.114845931448517e-11,
  5.761354022548962e-15,
  5.358055824814669e-10,
  1.10040447667311e-13,
  1.0540897473296215e-26,
  3.468728067753433e-17,
  -4.395561304757491e-37,
  2.043881626993719e-31.
  5.5917045488693284e-11,
  2.0060822359760653e-21]
In [61]:
 df final train['svd u dot'] = svd u dot
df final train['svd v dot'] = svd v dot
In [62]:
 # For test data
 # For train data
 svd u dot = []
 svd v dot = []
 for i in tadm(range(df final test.shape[0])):
```

```
svd_u_s = np.array(df_final_test[['svd_u_s_1','svd_u_s_2','svd_u_s_3','svd_u_s_4','svd_u_s_5','svd_u_s_6']
 u s 6']].iloc[i])
               svd u d = np.array(df_final_test[['svd_u d_1','svd_u d_2','svd_u d_3','svd_u d_4','svd_u d_5','svd_u d
 u d_6']].iloc[i])
               svd_v_s = np.array(df_final_test[['svd_v_s_1','svd_v_s_2','svd_v_s_3','svd_v_s_4','svd_v_s_5','svd_
 v_s_6']].iloc[i])
               svd_v_d = np.array(df_final_test[['svd_v_d_1','svd_v_d_2','svd_v_d_3','svd_v_d_4','svd_v_d_5','svd_v_d_1','svd_v_d_5','svd_v_d_5','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d_1','svd_v_d
 v d 6']].iloc[i])
               svd_u_dot.append(np.dot(svd_u_s,svd_u_d))
               svd v dot.append(np.dot(svd v s, svd v d))
 100%|
                                                                                                                                                                                                                                                                                                                   50002/50002 [06:55<00
 :00, 117.63it/s]
 In [63]:
 # Display 10 svd dot result
 svd_u_dot[:10]
Out[63]:
 [8.425153204050581e-20,
    5.383702120627523e-22,
    1.4819489830456183e-24,
    3.166962644606494e-24,
    1.694850962113967e-24,
    1.8640736443171697e-22,
    -9.764790469912655e-30,
    2.1034794852486508e-22,
    1.6170789335395426e-34,
    1.8430211061835498e-17]
 In [64]:
 df final test['svd u dot'] = svd u dot
 df final test['svd v dot'] = svd v dot
 In [65]:
 df final train.head()
Out[65]:
            source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followers num_followers
   0
                           273084
                                                                             1505602
                                                                                                                                          1
                                                                                                                                                                                                                                   0.000000
                                                                                                                                                                                                                                                                                       0.000000
                                                                                                                                                                                                                                                                                                                                            0.000000
   1
                        1722634
                                                                               647399
                                                                                                                                                                                                 0
                                                                                                                                                                                                                                  0.181818
                                                                                                                                                                                                                                                                                       0.129099
                                                                                                                                                                                                                                                                                                                                            0.323381
  2
                           404772
                                                                               797880
                                                                                                                                                                                                                                   0.000000
                                                                                                                                                                                                                                                                                       0.000000
                                                                                                                                                                                                                                                                                                                                            0.000000
   3
                           542646
                                                                            1740462
                                                                                                                                          1
                                                                                                                                                                                                 0
                                                                                                                                                                                                                                  0.150000
                                                                                                                                                                                                                                                                                       0.100000
                                                                                                                                                                                                                                                                                                                                            0.267261
                           355711
                                                                            1610892
                                                                                                                                                                                                 n
                                                                                                                                                                                                                                  0.000000
                                                                                                                                                                                                                                                                                       0.166667
                                                                                                                                                                                                                                                                                                                                            0.000000
                                                                                                                                          1
 5 rows × 59 columns
 In [66]:
 hdf = HDFStore('data/fea sample/storage sample stage5.h5')
 hdf.put('train_df',df_final_train, format='table', data_columns=True)
```

```
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
```

In [0]:

```
# prepared and stored the data from machine learning models
# pelase check the FB_Models.ipynb
```