

MA202

ASSIGNMENT 8

NAME:

ARCHIT AGRAWAL

ROLL NO. :

202051213

SECTION:

2

Exercise 1

Consider that you are given a function $f(x) = \frac{\sin(\lambda x)}{x}$ whose integration is to be found from $x = -10$ to $x = 10$. Write a program that numerically evaluates such an integral using Trapezoidal Rule, Simpson's 1/3 Rule and Simpson's 3/8 Rule. Find the integral for the values of $\lambda = 0.01, 0.1, 1, 10, 100$, using each of these methods, and comment upon the results obtained.

Exercise 2

Repeat the same exercise as above for $g(x) = \exp(\sin(\lambda x))$, for which the integration limits are $x = 0$ to $x = 5\pi$.

Exercise 1

Code

The values of λ is changed repeatedly.

```
Lower=-10 ;
upper =10 ;
n= 100;

%Trapezoidal Rule, Simpson's One third Rule and Simpson's Three Eighth Rule
by multiple application
h = (upper-lower)/n;
xVec = lower :h:upper;
xVec(n+1) = upper +h;
xVec(n+2) = xVec(n+1)+h;
xVec(n+3) = xVec(n+2)+h ;

fVec = myFunInt(xVec);
%applying correction for sinx/x = 1 as x tends to 0
fVec(51) =1;

interval_trap = zeros(n,1);
interval_onethird = zeros(n,1);
interval_threeeighth = zeros(n,1);
for i = 1:n
    interval_trap(i)=(h/2)*(fVec(i)+fVec(i+1));
    interval_onethird(i)=(h/3)*(fVec(i)+4*fVec(i+1)+fVec(i+2));
    interval_threeeighth(i)=(3*h/8)*(fVec(i)+3*fVec(i+1)+3*fVec(i+2)+fVec(i+3));
end
```

```
fprintf('The integration is ')\nI_trap1 = sum(interval_trap)\nI_onethird = sum(interval_onethird)\nI_threeeight = sum(interval_threeeighth)
```

```
function fval = myFunInt(x)\n    a = [0.01,0.1,1,10,100];\n\n    ain= 0.01\n    %ain= 0.1\n    %ain= 01\n    %ain= 10\n    %ain= 100\n\n    fval = sin(ain*x)./x;\n\nend
```

Output

```
ain = 0.0100\nThe integration is\nI_trap1 = 0.3979\nI_onethird = 0.7958\nI_threeeight = 1.1937
```

```
ain = 0.1000\nThe integration is\nI_trap1 = 2.0721\nI_onethird = 4.1440\nI_threeeight = 6.2153
```

```
ain = 1
The integration is
I_trap1 = 3.3148
I_onethird = 6.6248
I_threeeight = 9.9232
```

```
ain = 10
The integration is
I_trap1 = 1.3455
I_onethird = 2.7126
I_threeeight = 4.0652
```

```
ain = 100
The integration is
I_trap1 = 2.1733
I_onethird = 4.3471
I_threeeight = 6.5225
```

Exercise 2

Code

The values of ain is changed repeatedly.

```
lower = 0;
upper = 5*pi;
n = 100;

%Trapezoidal Rule, Simpson's One third Rule and Simpson's Three Eighth Rule
by multiple application
h = (upper-lower)/n;
xVec = lower : h : upper;
xVec(n+1) = upper + h;
xVec(n+2) = xVec(n+1) + h;
xVec(n+3) = xVec(n+2) + h;
```

```
fVec = myFunInt(xVec);  
%applying correction for  $\sin x/x = 1$  as  $x$  tends to 0  
interval_trap = zeros(n,1);  
interval_onethird = zeros(n,1);  
interval_threeeighth = zeros(n,1);  
for i = 1:n  
    interval_trap(i)=(h/2)*(fVec(i)+fVec(i+1));  
    interval_onethird(i)=(h/3)*(fVec(i)+4*fVec(i+1)+fVec(i+2));  
  
interval_threeeighth(i)=(3*h/8)*(fVec(i)+3*fVec(i+1)+3*fVec(i+2)+fVec(i+3));  
end  
fprintf('The integration is ')  
I_trap1 = sum(interval_trap)  
I_onethird = sum(interval_onethird)  
I_threeeight = sum(interval_threeeighth)
```

```
function fval = myFunInt(x)  
    a = [0.01,0.1,1,10,100];  
  
    ain= 0.01  
    %ain= 0.1  
    %ain= 01  
    %ain= 10  
    %ain= 100  
    fval = exp(sin(ain*x));  
  
end
```

Output

```
ain = 0.0100  
The integration is  
I_trap1 = 17.0062  
I_onethird = 34.0392  
I_threeeight = 51.0992
```

```
ain = 0.1000  
The integration is  
I_trap1 = 31.0436  
I_onethird = 62.3561  
I_threeeight = 93.9342
```

ain = 1

The integration is

I_trap1 = 22.1031

I_onethird = 44.1683

I_threeeight = 66.1384

ain = 10

The integration is

I_trap1 = 20.1083

I_onethird = 40.3065

I_threeeight = 60.1863

ain = 100

The integration is

I_trap1 = 15.7080

I_onethird = 31.4159

I_threeeight = 47.1239
