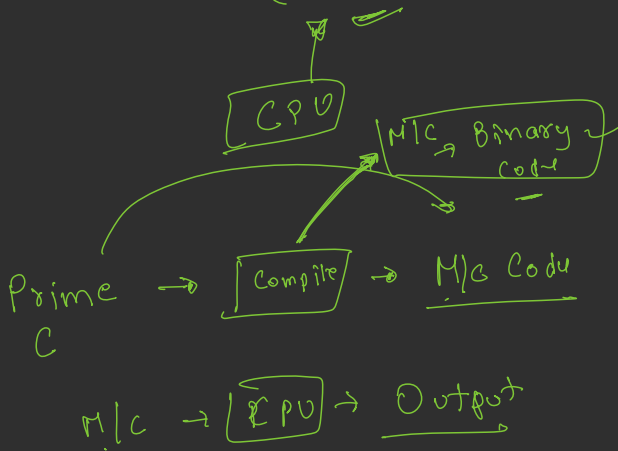
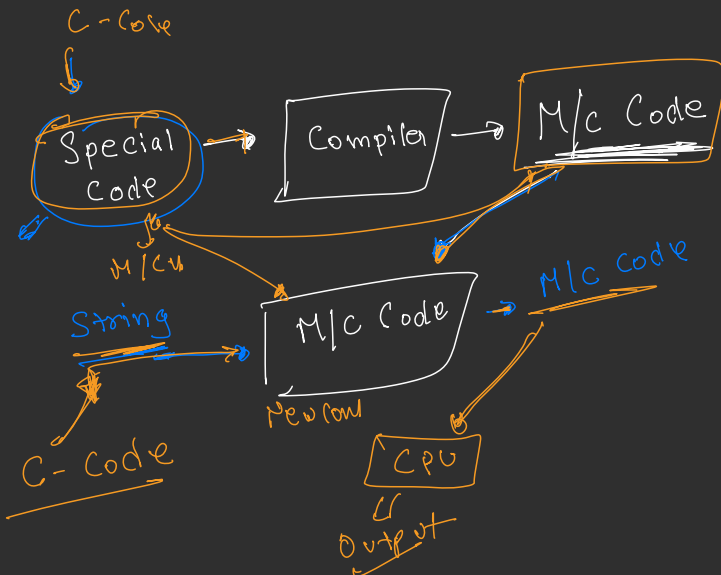
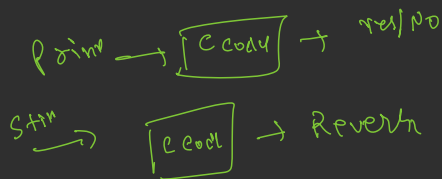
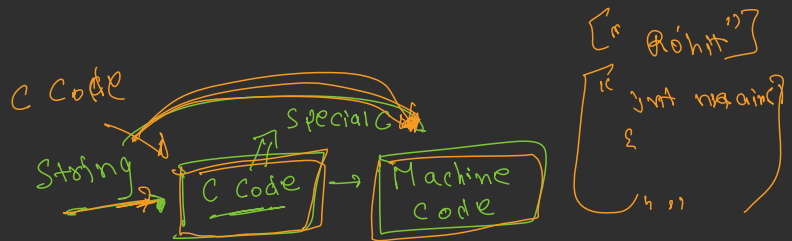
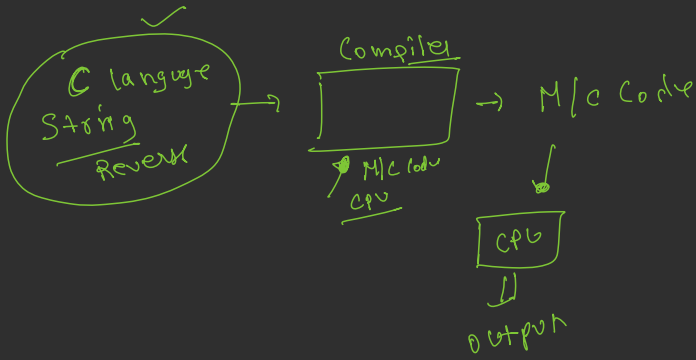
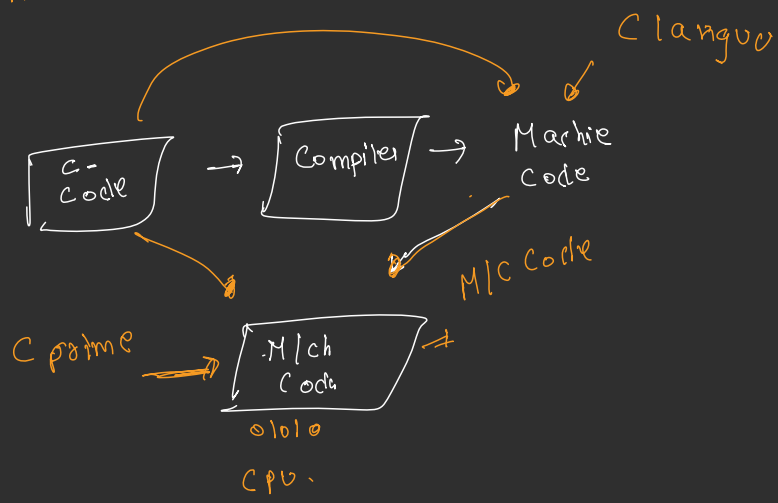
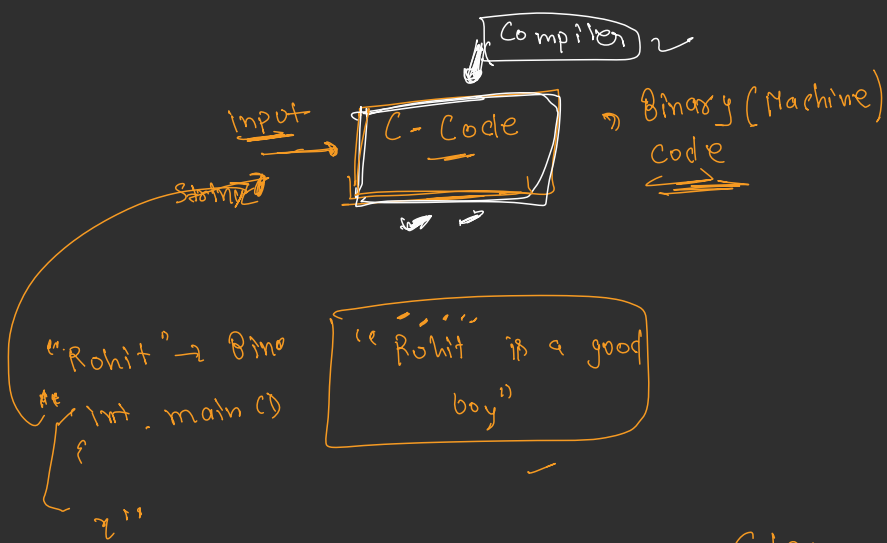


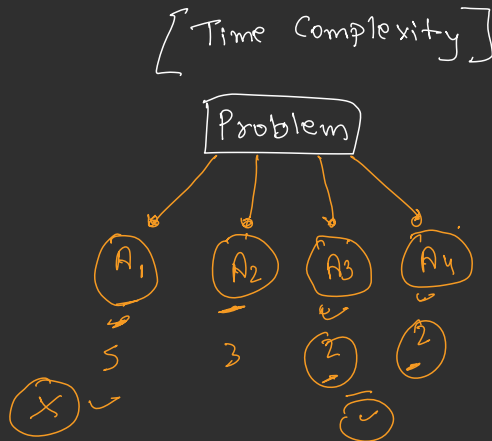
[ Binary language → Machine Code ]

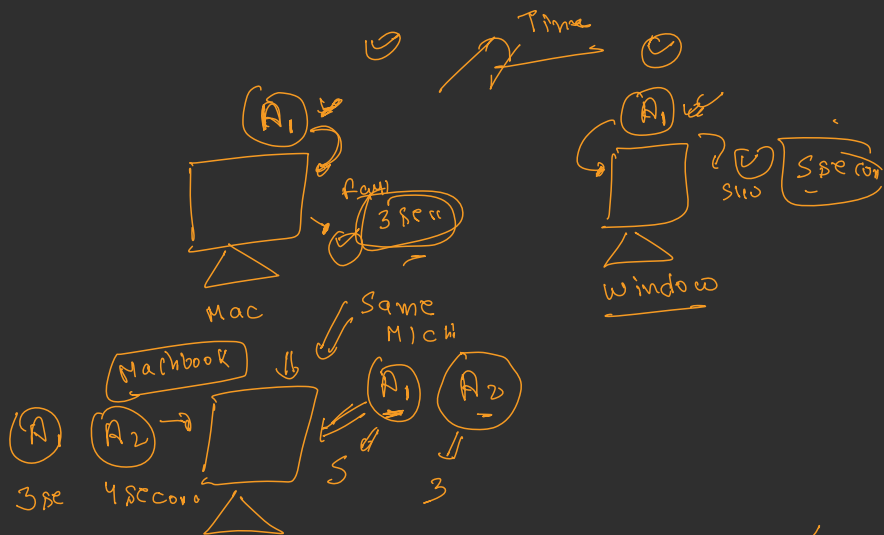
Compiler ⇒ Machine Code  
(0101010)







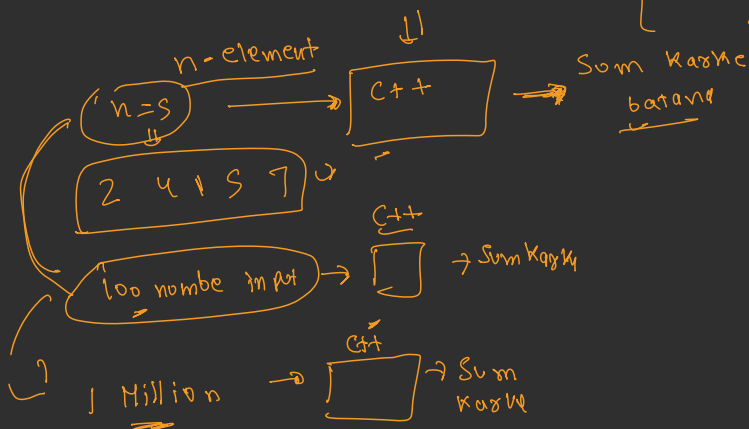




```

int arr[n]
int sum = 0
for (i = 0; i < n; i++)
    sum += arr[i];

```



Sum of n-number

```

int arr[n] = {1, 2, 3, 4, 5}
int sum = 0;
for (int i = 0; i < n; i++)
    sum += arr[i];
cout << sum;

```

n = 4

Operation:

- 1 + 1 + 1 + 1 = 4 ⇒ 3 + 1
- 1 + 1 + 1 = 3
- 1 + 1 + 1 = 3
- 1 + 1 + 1 = 3
- 1 = 1

Total operation: 14 operations

19 open

1 + 1 + 1 + 1 = 4

1 + 1 + 1 = 3

1 + 1 + 1 = 3

1 + 1 + 1 = 3

1 + 1 + 1 = 3

17 open

Input → Time Complexity → Output

n = 5 ⇒ 5 seconds

n = 100 ⇒ 100 μs

n = 1M ⇒ 1 Millisecond

Time Complexity

$3n + 4$

Number of operation

- n ⇒ 18 operation
- h ⇒ 19 operation
- 6 = n ⇒ 22 operation
- 7 = n ⇒ 25 operation

```

for (i=0; i<n; i=i+2)
{
    cout << "Hello"
}

```

Time Complexity  
 $\Rightarrow \underline{n}$

$\boxed{n}$   $\rightarrow$  better  
 $\boxed{n^2}$   $\rightarrow$  worse  
 Time Complexity =  $3n + 4$   $\rightarrow$  number 34 ✓ Betty  
 Time complexity =  $2n^2 + 6$   $\rightarrow$  206 ✓  
 ✓

for (i=0; i<n; i++)  
 {  
 }  
 n bol sakta

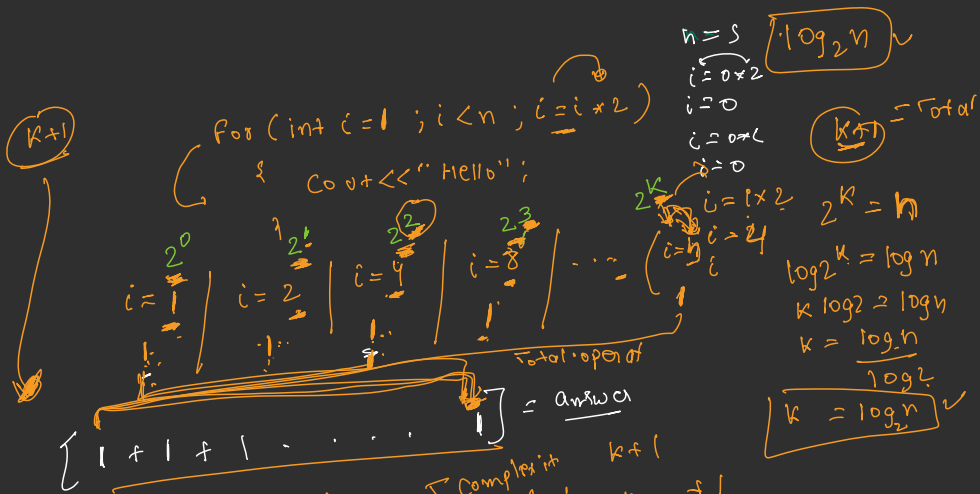












$2^k = n$   
 $\log_2 k = \log n$   
 $k \log_2 2 = \log n$

$k = \frac{\log n}{\log 2}$

$k = \log_2 n$

$k = \log_2 n$

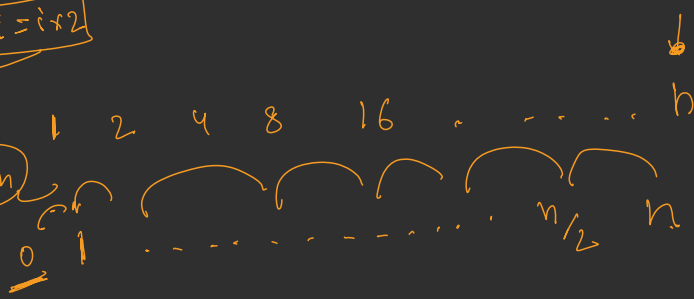
$\text{For (} i = 1 ; i < n ; i++)$   
 $\{ \text{cout} << "Hello"$

$1 + 1 + 1 + \dots + 1 = n$



$$i = i \times 2$$

$\log_2 n$



$\log_2 n$

```

for (i=0 ; i < n ; i++)
{
    for (j=0 ; j < n ; j++)
    {
        for (k=0 ; k < n ; k++)
        {
            cout << "Hello";
        }
    }
}

```

```

for (i=1 ; i < n ; i++)
{
    for (j=0 ; j <= i ; j++)
    {
        cout << "Hello";
    }
}

```

$i=1$   
 $j=0+0$   
 $1+0k$   
 $1$

$i=2$   
 $j=0+0+3$   
 $4+0k$   
 $4$

$i=3$   
 $j=0+0+8$   
 $9+0k$   
 $9$

$i=4$   
 $j=0+0+15$   
 $16$

$i=n-1$   
 $(n-1)^2$

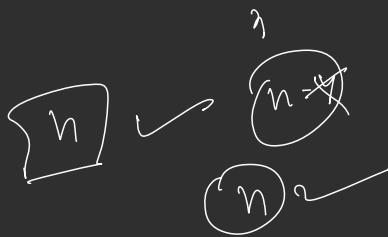
$1^2 + 2^2 + 3^2 + 4^2 + \dots + (n-1)^2$

$$\boxed{\frac{n(n+1)(2n+1)}{6}} \Rightarrow \underline{\underline{n^3}}$$

$$\frac{(n-1)(n)(2n-1)}{6}$$

$$\frac{\cancel{x}^3 + \cancel{x}^2 + \cancel{x}^2 + \cancel{x}}{\cancel{x}}$$

for ( $i=1$  ;  $i < n-1$ ) {



$$\left[ 1^2 + 2^2 + 3^2 + \dots + (n-1)^2 \right]$$

$$\left[ \frac{n(n+1)(2n+1)}{6} \right] \checkmark$$

$$\left[ \frac{(n-1)n(2n-1)}{6} \right]$$

$$\frac{\cancel{2}n^3 + \cancel{6}n^2 + \cancel{8}n + \cancel{4}}{\cancel{6}}$$

$$\left( \frac{n^3}{3} \right) \checkmark$$







Worst	Average	Best
$n$	$n/2 = \frac{n}{2}$	1

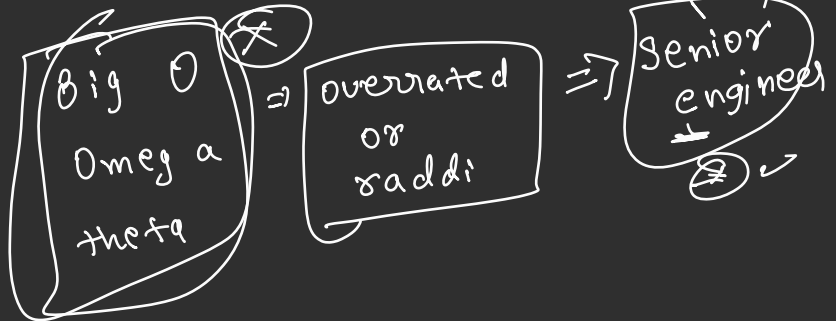
int arr[] = {10, 20, 17, 9, 8, 11}  
 element = 9

(n) ✓

```

for (i = 0; i < n; i++)
{
  if (arr[i] == element)
  {
    cout << "yes"
    return 0;
  }
}
cout << "No";

```



$O(n^4)$

method

Time Comp =  $n^2$

no. of operatio.  $O(n^2)$

$O(n^5)$   
T. Com = n

Omega

Big O

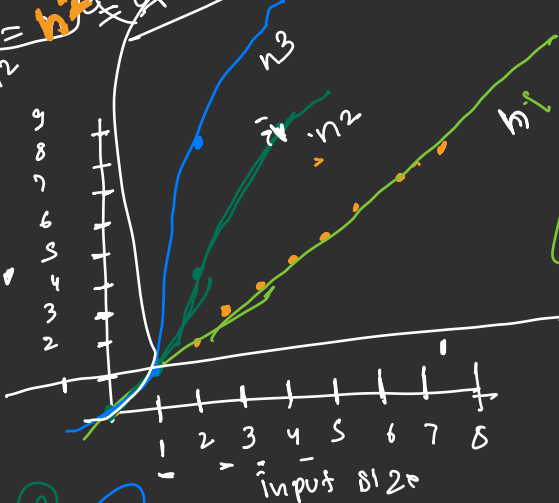
upper bound

$O(n^3)$   
 $\frac{O(n^3)}{n^2}$   
 $\frac{O(n^3)}{n^2}$

$\Omega(1)$

$\Omega(n)$

no. of operatio



no. of op.  
for (i=0; i<n; i++)  
{  
  count++  
}

$f(n) \geq n$

for (i=0; i<n^2; i++)  
{  
  count++  
}

$n=2$

$f(n) = \frac{n^2}{n}$

$\frac{n^3}{n}$

$f(n) = 1$

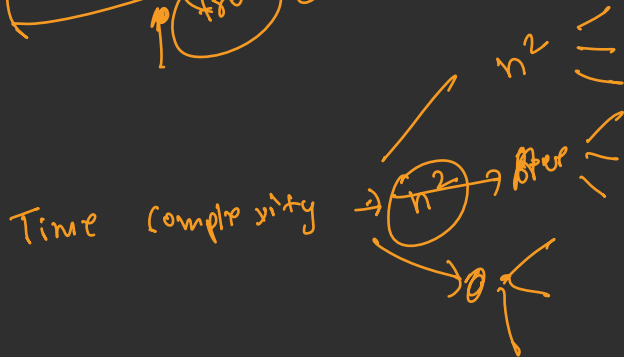
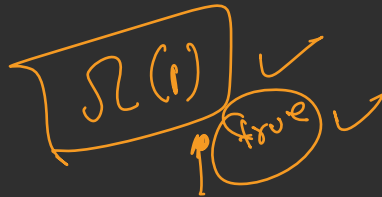
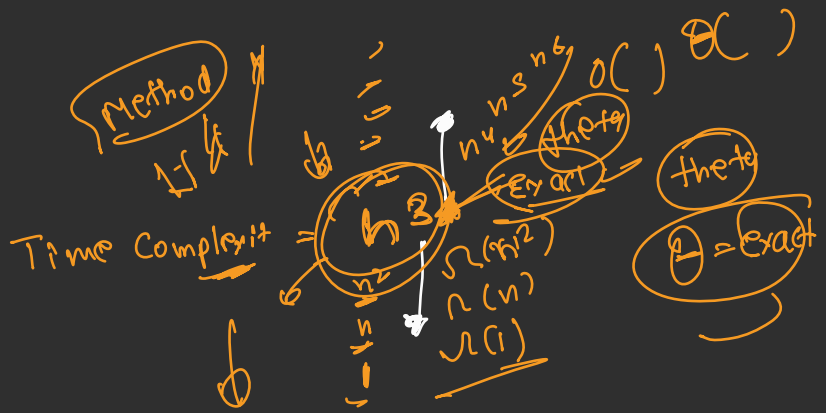
Big O  $\Rightarrow$  Upper Bound

$\downarrow$

Algorithm

$\downarrow$

Equal, ya merge  
kechhe





$$+ \underbrace{O(2^n)}_{\text{time}} \cdot \frac{99\%}{\text{time}}$$

$$\Omega(1) = \underbrace{(100\% \cdot \text{time})}_{\text{time}}$$

OC.

Conclusion



Auxiliary Space

Space Complexity:

$O(1)$

```
[ for(int i=0; i<n; i++)  
  cout<<i'.  
  ]
```



reverse the array:

int arr[n] = {1, 2, 3, 4, 5};

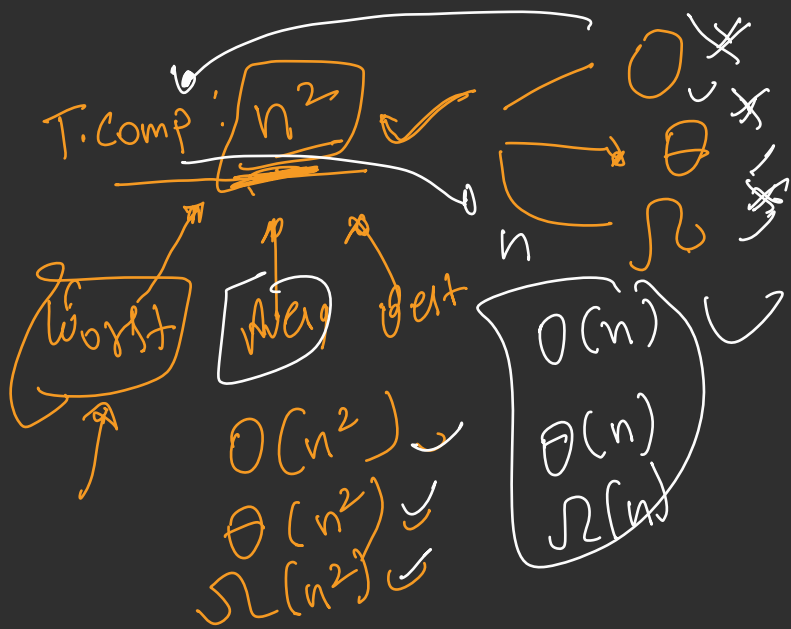
int newArr[n];  
int j = n-1;

for (int i = 0; i < n; i++)  
{  
 newArr[j] = arr[i];  
 j--;

}  
return newArr;

input  $O(n)$   
 ~~$n$~~   $O(n)$   
 $O(n)$





$O(n^4)$   $O(n^3)$   $O(n^2)$

Upper bound

Time complexity

$n^2$   
 $\Omega(n)$

Upper bound

$\Theta$

Lower bound

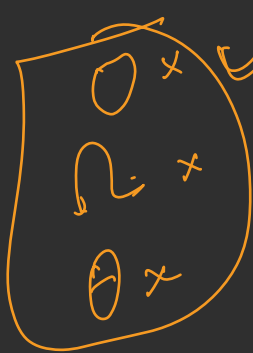
Worst case

Best

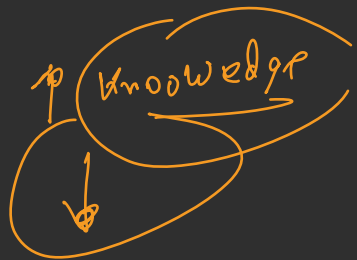
Average

Worst case

Interview w



$O(n^2)$



Dijkstra → Professor (PhD)

Course - End  
||

Data Structure

[ Sorting  $\rightarrow$  ascending order ]

[ 10, 1, 3, 9, 5 ]

problem  
1 3 5 9 10

10-9

[10, 1, 9, 3, 5]

ascending  
order

Selection  
sort (1st)

✓ 2-9

1, 10, 9, 3, 5

1, 2, 3, 9, 10, 5

1, 2, 3, 5, 10, 9

1, 2, 3, 5, 9, 10



worst case  $\Rightarrow n^2 \Rightarrow$   
 $\begin{matrix} - O(n^2) \\ \rightarrow \Theta(n^2) \\ \rightarrow \Omega(n^2) \end{matrix}$

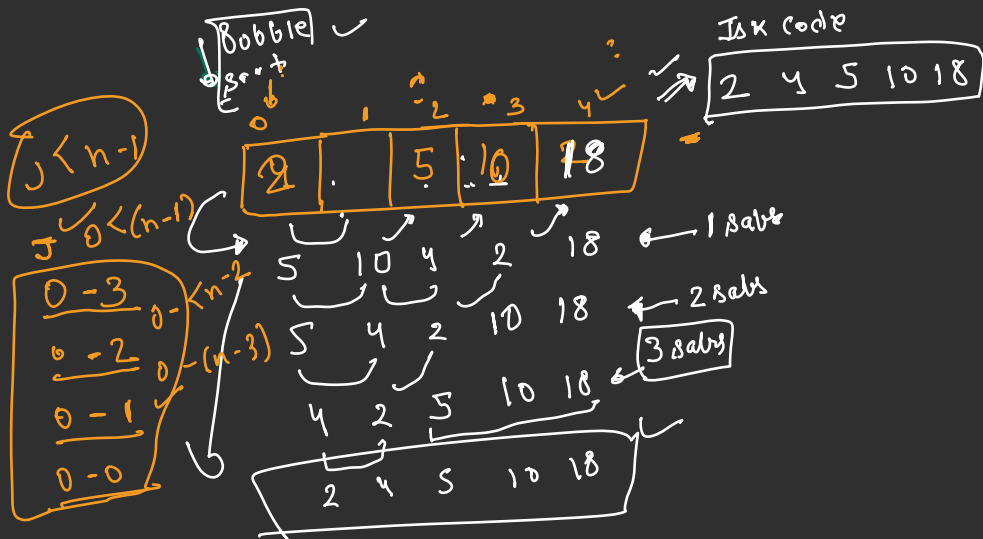
Best case  $\Rightarrow -$

int a=10, b=20  
int c=b  
b=a  
a=c  
c=20 swap  
b=10  
a=20  
a=20, b=10

void swap(a, b) {  
}

[1, 2, 3, 4, 5]

~~Algorithm~~

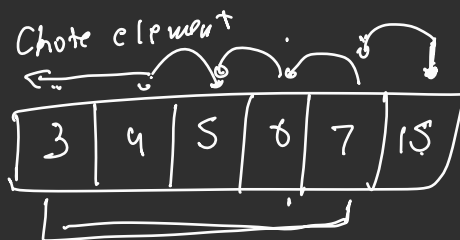
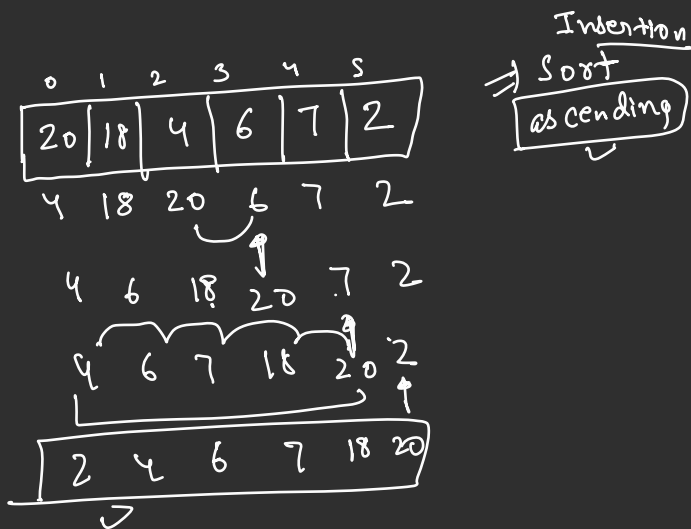


1	2	3	4	5
---	---	---	---	---

Average

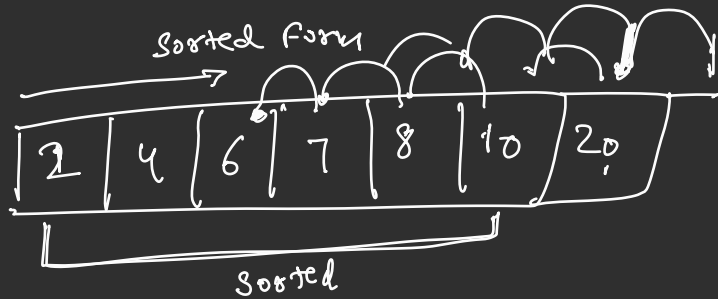
Case =  $\frac{n^2}{2}$

$\frac{n + n^2}{2} = \frac{n^2}{2}$



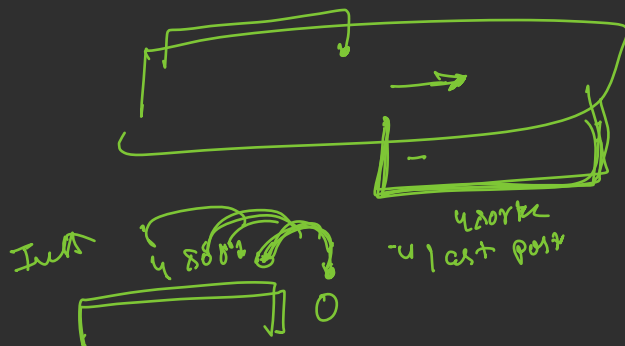
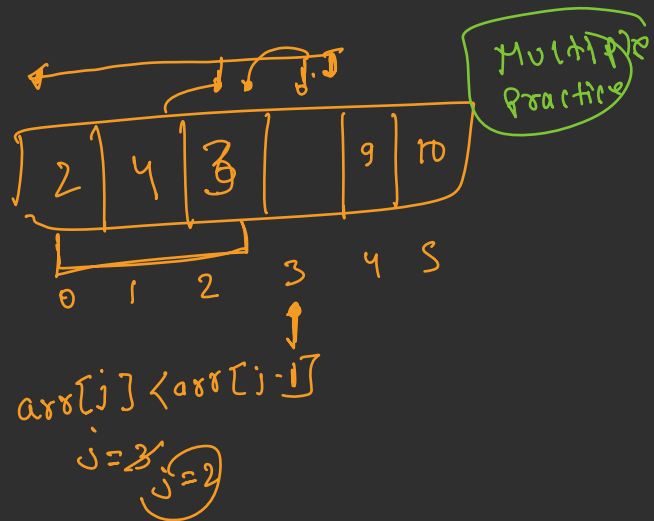
0	1	2	3	4
1	2	3	4	5

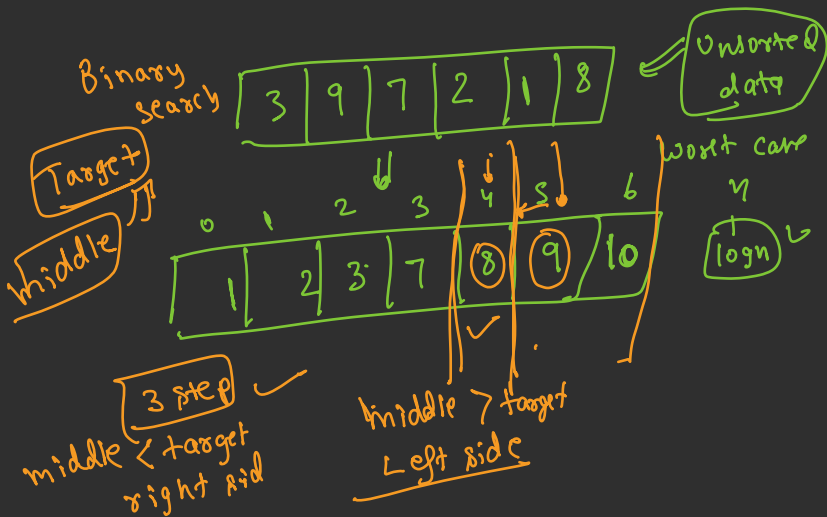
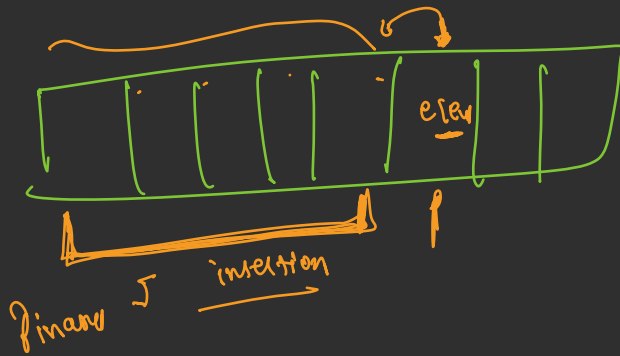
$j--$

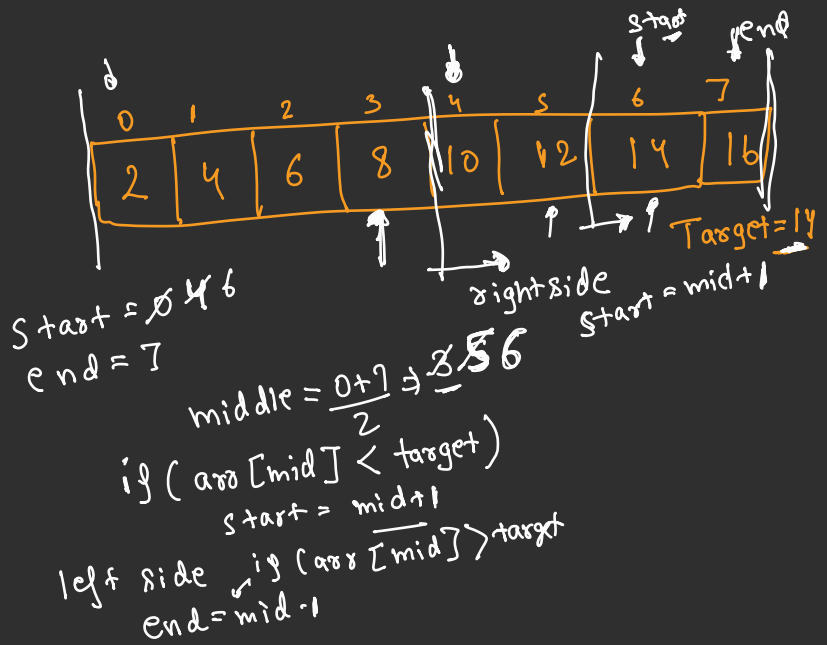
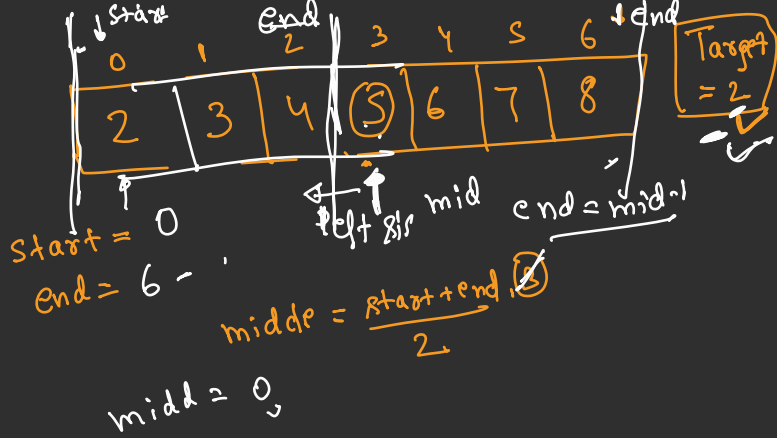


0	1	2	3	4	5
5	10	20	3	18	9

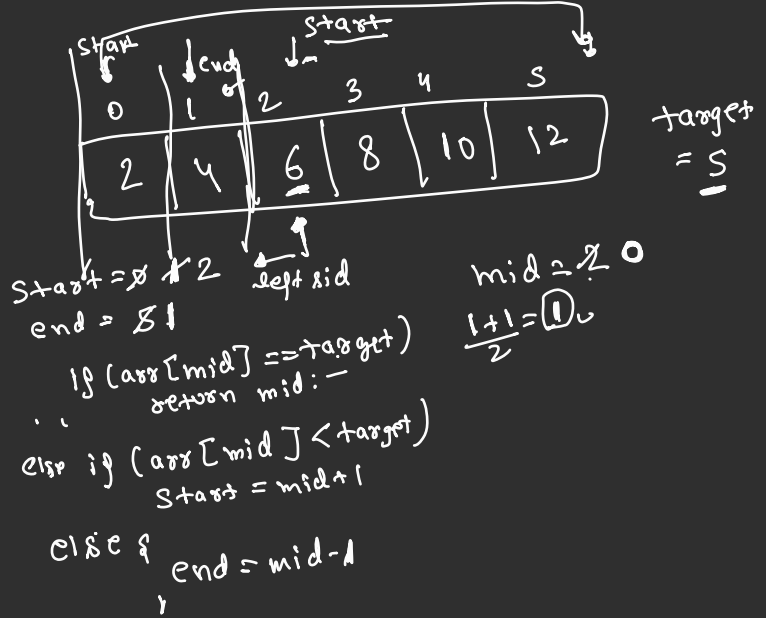
$j = 3$  ;  $j > 0$  ;  $j--$   
 if ( $arr[j] < arr[j-1]$ )  
 { swap ( $arr[j], arr[j-1]$ ) }  
 } else  
 break;



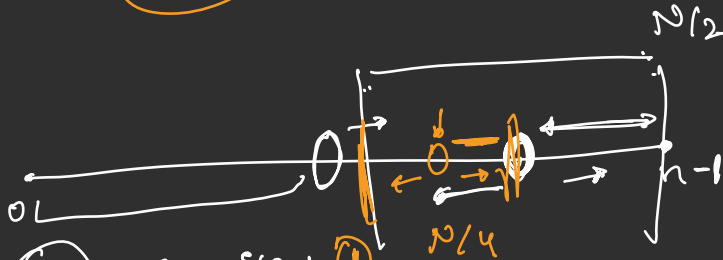








$\log_2 n$   
worst



$n/2 \Rightarrow$  cases element 1

$n/4 \Rightarrow$  cases remove 1

$n/8 =$

$\vdots$

